

# Constraining Quantum Gravity - in theory and in the lab

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**Timo Weigand, Corfu Summer Institute Workshop on Quantum Gravity, September 11, 2025**



## **How to find constraints on quantum gravity?**

1) **Idea** guided by theoretical consistency starting with certain **assumptions**

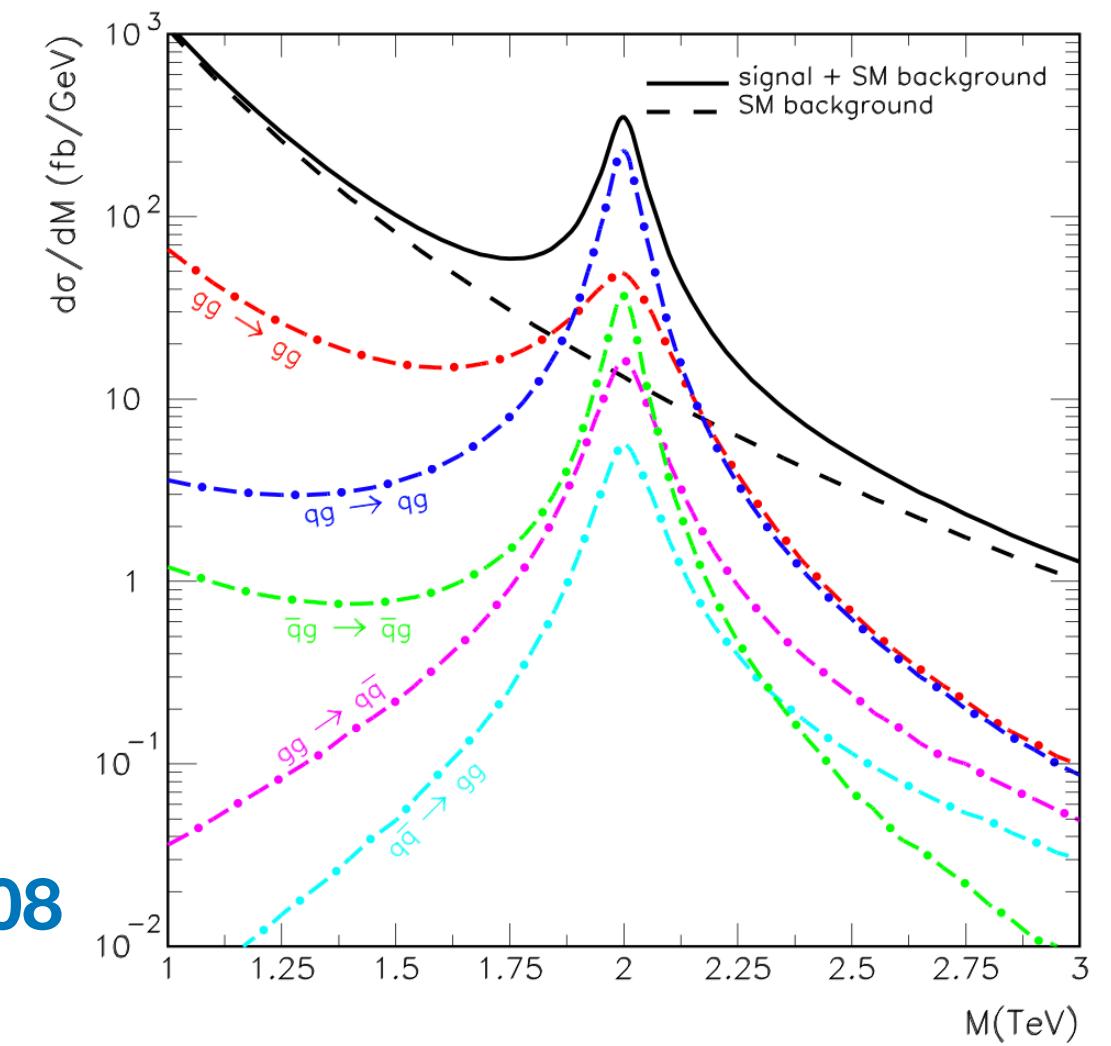
- Successful example: **String Theory**
- **Swampland Program**: attempts to relax assumptions on UV

2) **Laboratory** to test / rule out the idea

- **Theoretical laboratory** (mathematics....)
- Universe (**cosmological observations**) or actual **experiment**

*difficult: 4d Planck scale high....*

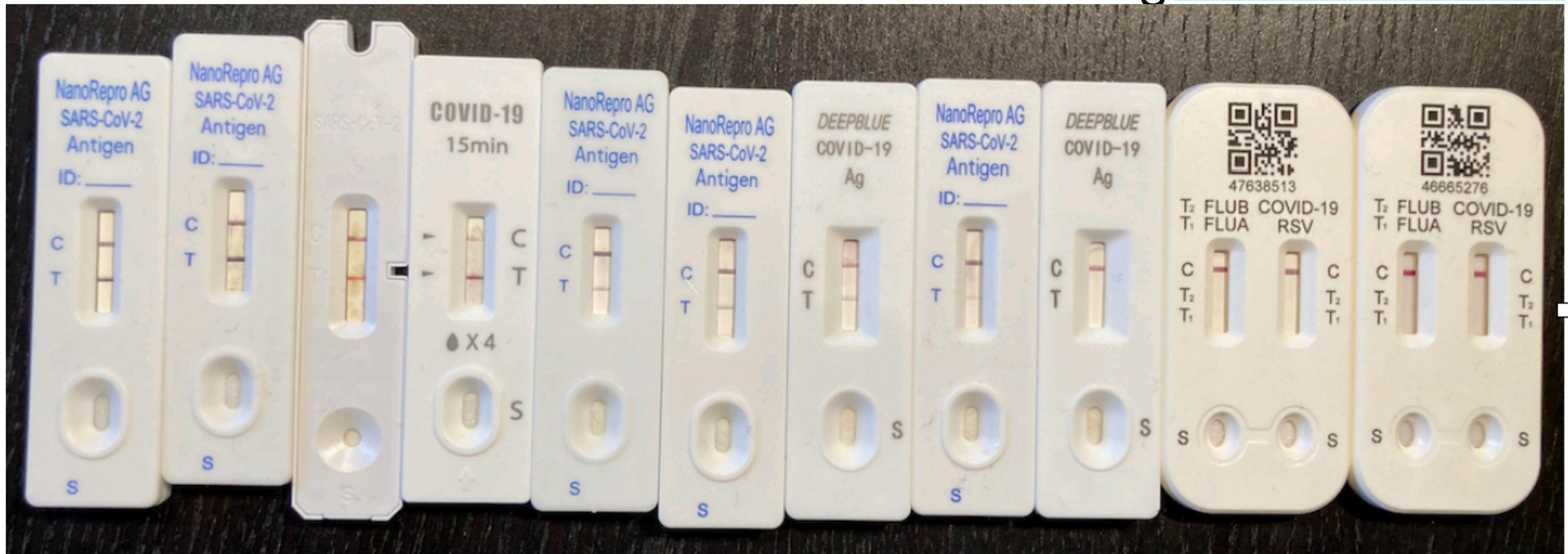
However:  
[Anchordoqui, ...,  
Lüst, Stieberger, ..., Taylor] '08



## Run 1

UP-  
GRADE

## Run 2



- 1) We are playing the long game: patience!
- 2) A negative result can also be a good result.  
<sub>3</sub>

## *This talk*

### Idea 1:

**Distance Conjecture** [Ooguri, Vafa'05]

**Emergent String Conjecture** [Lee,Lerche,TW'19]

**Laboratory 1:** Geometry of stable degenerations

**Evidence that ESC realised in Type IIB string theory on CY 3-folds at infinite distance in the complex structure**

[Friedrich, Monne, TW, Wiesner'25] [Monne, TW, Wiesner'25]

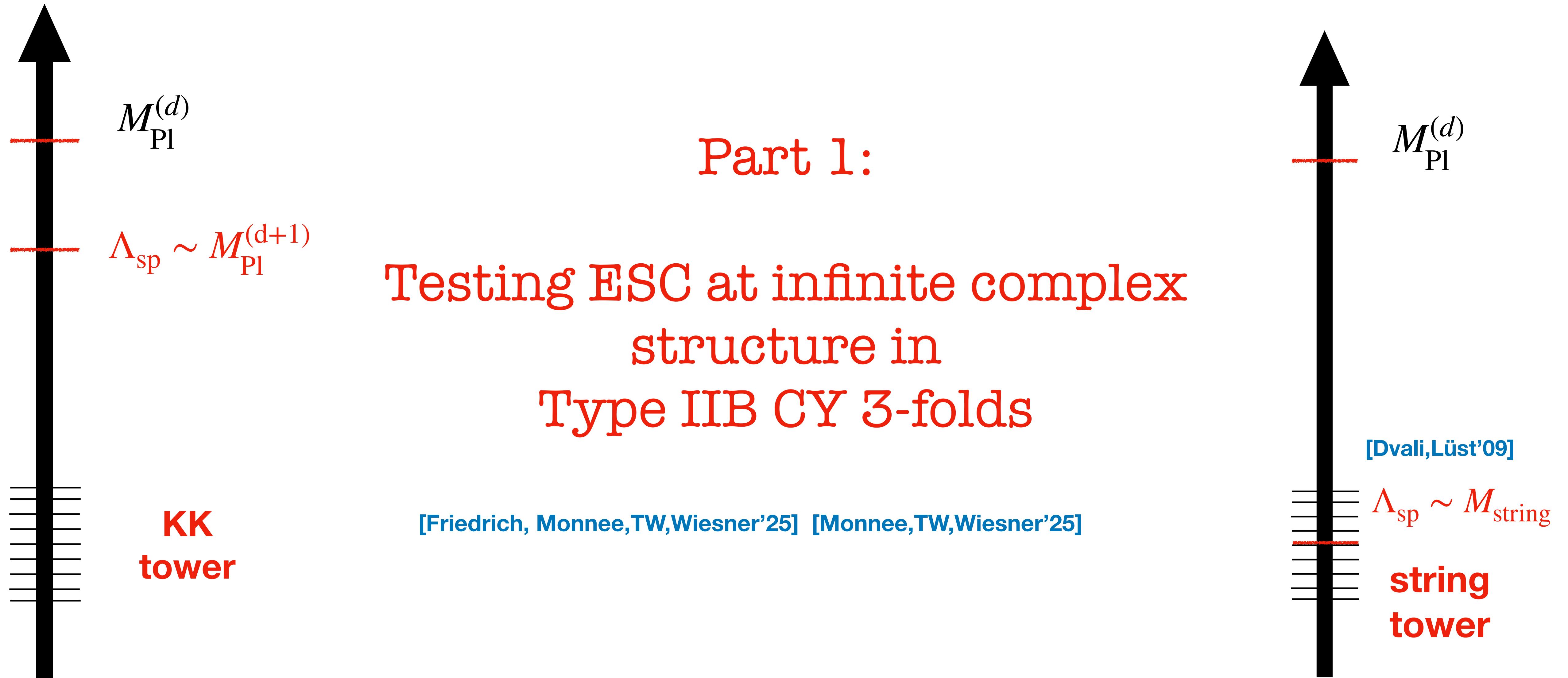
### Idea 2:

**Perturbative heterotic string**

**Laboratory 2:** Universe or axion experiments

**Finding an axion-like particle with a coupling-to-mass ratio far above the QCD line would rule out perturbative heterotic string theory.**

[Agrawal, Nee, Reig'22, '24] [Reig, TW'25]

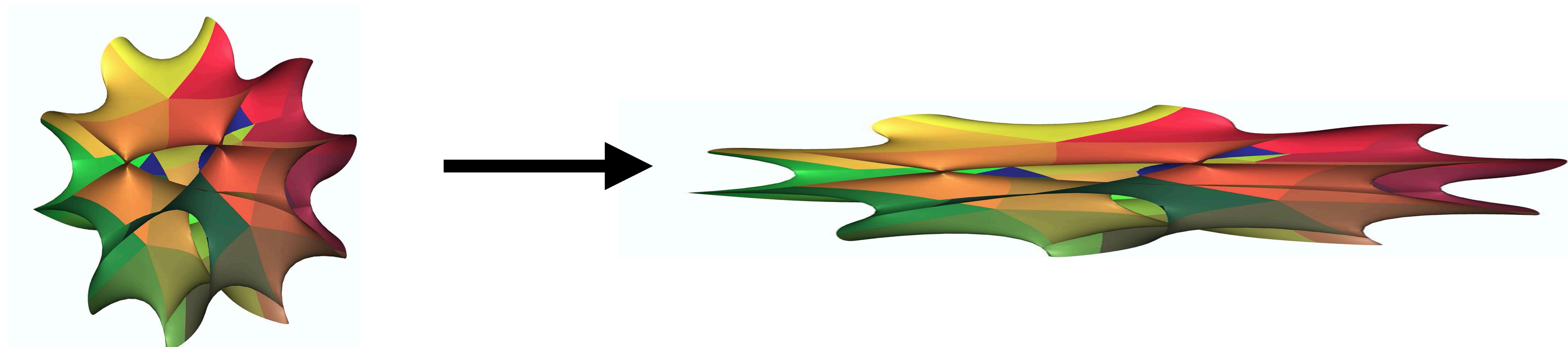


# The setup

Consider Type IIB string theory on CY 3-fold  $V$ .

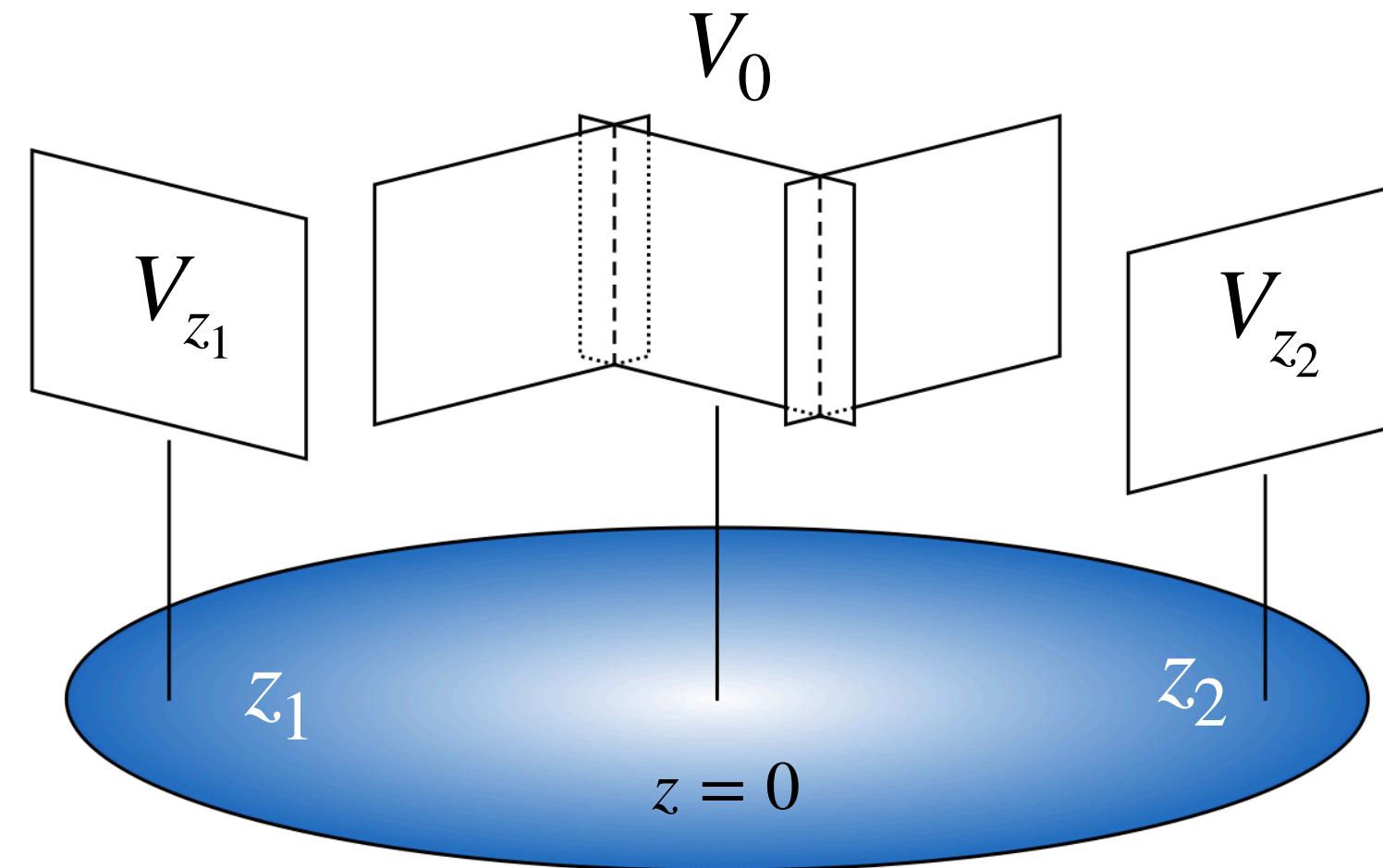
**Infinite distance limit in complex structure moduli** at fixed Kähler moduli:

⇒ highly anisotropic space with **large and small 3-cycles**



# Semi-stable degenerations

CY3  $\xrightarrow[\text{degeneration}]{\text{semi-stable}}$  **normally crossing components** [Mumford 1972]



$$V \rightarrow V_0 = V_1 \cup V_2 \cup \dots \cup V_n$$

**Example:**

$$P = x_1^{12} + x_2^{12} + x_3^6 + x_4^6 + x_5^2 - u_1^{-1}x_1x_2x_3x_4x_5 - u_2^{-1}x_1^6x_2^6 = 0 \quad \xrightarrow{u_2 \rightarrow 0} \quad V_0 = V_1 \cup V_2$$

$$V_1 = \{x_1^6 = 0\}, \quad V_2 = \{x_2^6 = 0\}$$

# The II, III, IV of infinite distance

CY3

semi-stable  
degeneration

**normally crossing components**

$$V_{i_1} \cap V_{i_2} \cap \dots \cap V_{i_n} = V_{i_1 i_2 \dots i_n}$$

**Primary type of degeneration:**

**Highest complex codimension  $d$  of intersection loci:**

[Mumford 1972]

type II:

$V_{ij} \neq 0$ : double surfaces    but  $V_{ijk} = 0$

$d = 1$

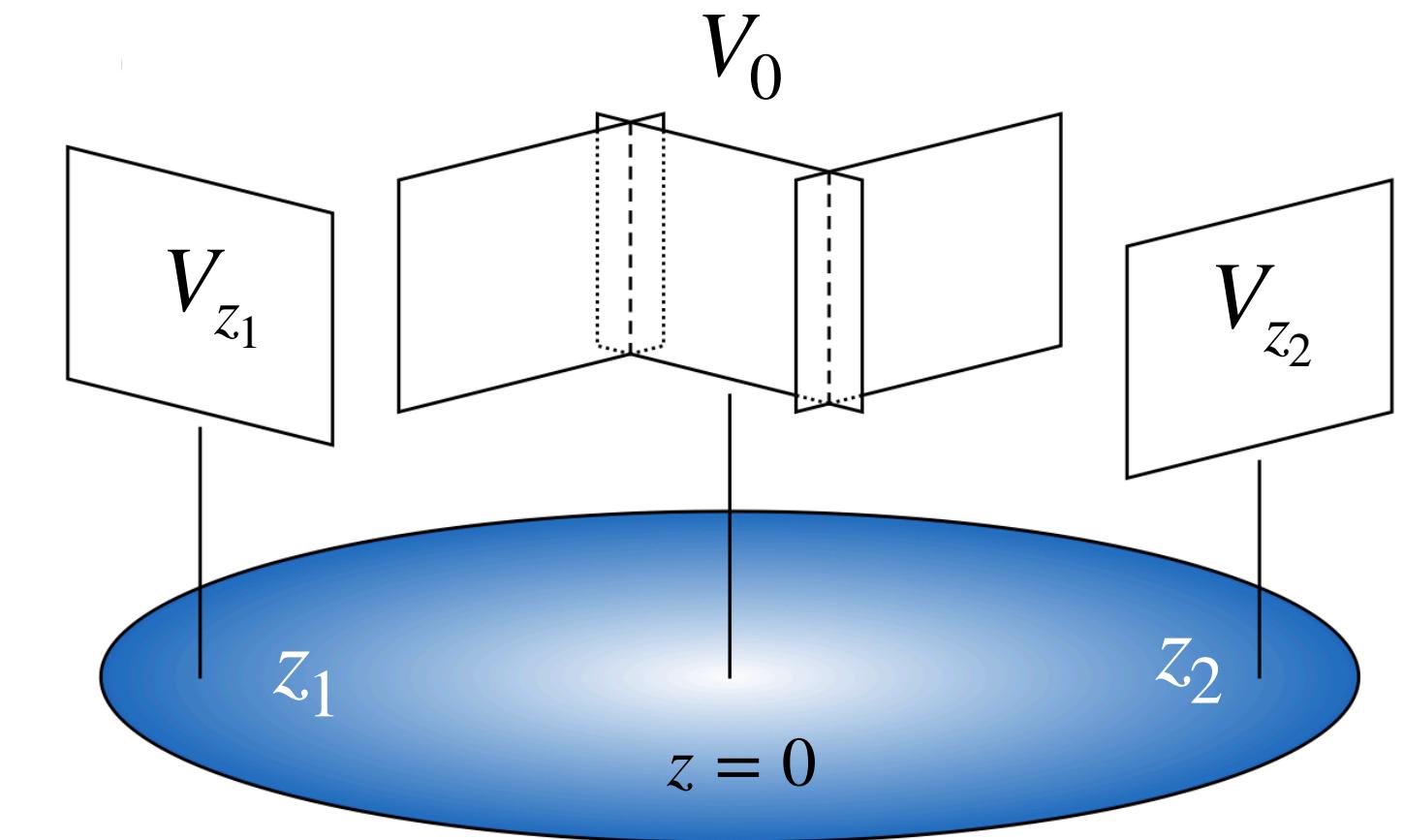
type III:

$V_{ij} \neq 0$ : double surfaces,  $V_{ijk} \neq 0$  : triple curves,    but  $V_{ijkl} = 0$                $d = 2$

type IV:

$V_{ij} \neq 0$ ,        $V_{ijk} \neq 0$ ,        $V_{ijkl} \neq 0$  (point)

$d = 3$



# Vanishing 3-cycles

# Primary type of degeneration:

# Codimension $d$ of highest-dim intersection locus:

type II:  $V_{ij} \neq 0$ : double surfaces but  $V_{ijk} = 0$   $d = 1$

type III:  $V_{ij} \neq 0$ : double surfaces,  $V_{ijk} \neq 0$ : triple curves, but  $V_{ijkl} = 0$   $d = 2$

$$\text{type IV: } \quad V_{ij} \neq 0, \quad V_{ijk} \neq 0, \quad V_{ijkl} \neq 0 \text{ (point)} \quad d = 3$$

# Vanishing 3-cycles:

## fibration

$$T^d \hookrightarrow \Gamma \rightarrow B_{3-d} \leftarrow \dots$$

**real (3-d) cycle on  
(3-d) complex dim.  
intersection locus**

# Vanishing 3-cycles

Vanishing  
3-cycles:

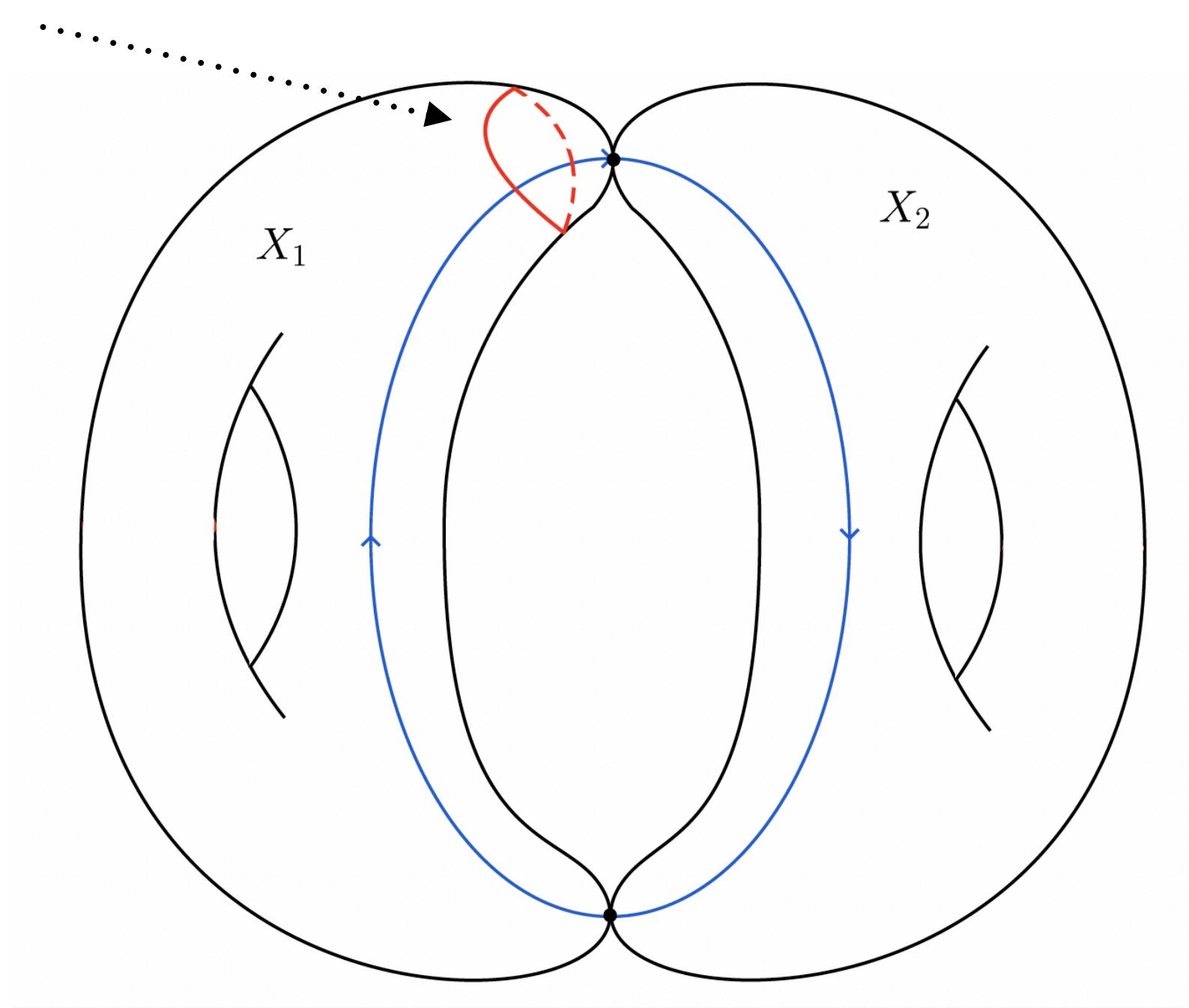
fibration

$$T^d \hookrightarrow \Gamma \rightarrow B_{3-d}$$

real (3-d) cycle on  
(3-d) intersection  
locus

$\Gamma = \text{vanishing } S^1$

Toy example:  
Degeneration of  $T^2$



# Vanishing 3-cycles in type II, III, IV

**Vanishing  
3-cycles:**

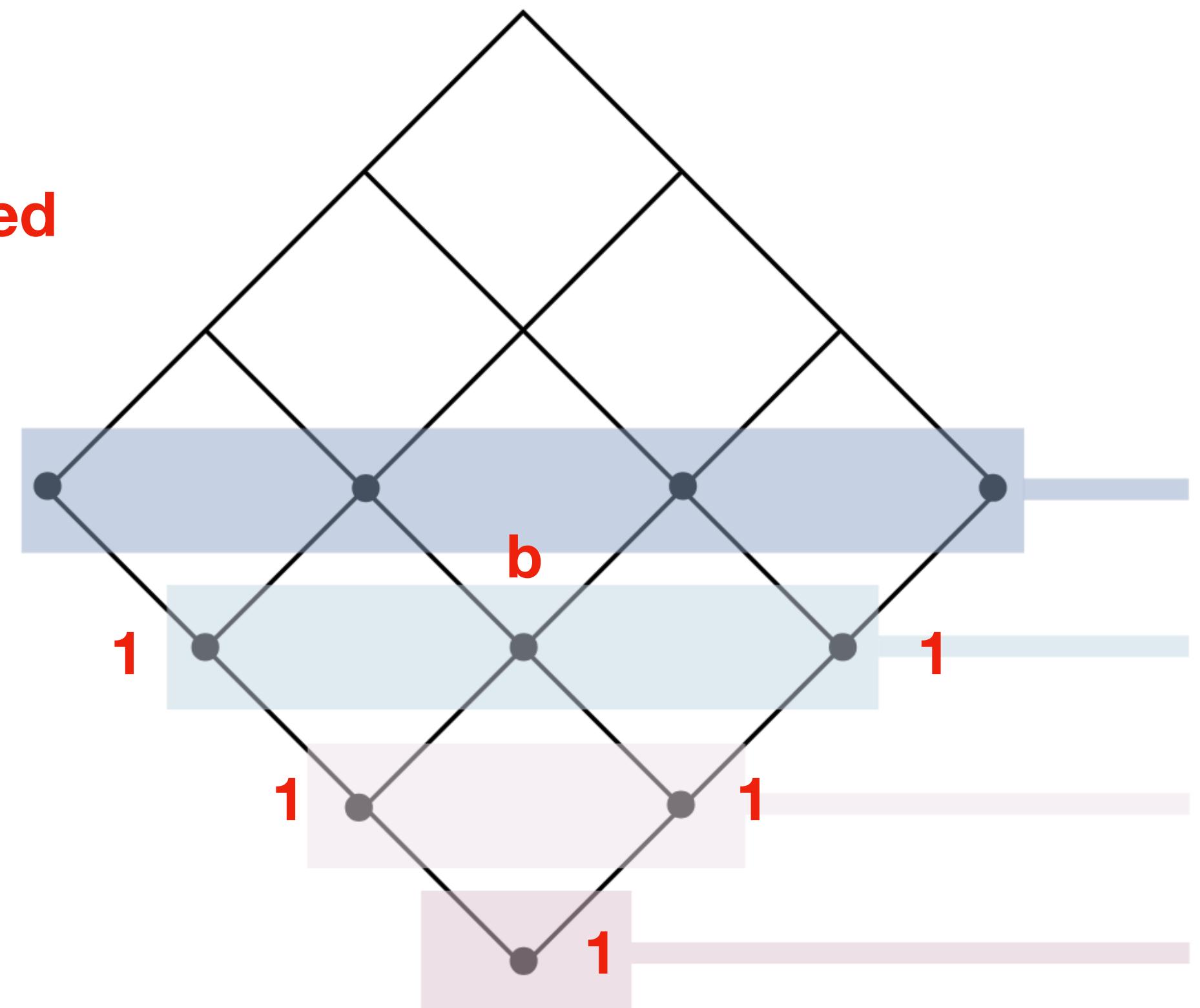
fibration

$$T^d \hookrightarrow \Gamma \rightarrow B_{3-d}$$

real (3-d) cycle on  
(3-d) intersection  
locus

Geometric limiting mixed  
**Hodge structure**

[Deligne '71/'74]  
[Morrison'84]



[Friedrich, Monnee,TW,Wiesner'25]  
[Monnee,TW,Wiesner'25]

type I (finite distance)

type II

$$S^1 \hookrightarrow \Gamma^a \rightarrow C_2^a$$

type III

$$T^2 \hookrightarrow \Gamma^{(A,B)} \rightarrow S_1^{(A,B)}$$

type IV

$$\Gamma = T^3$$

# Vanishing 3-cycles in type II, III, IV

Infinite distance limit in complex structure  
moduli space of **Type IIB on CY 3-fold  $V$**

$$\frac{\log u^j}{2\pi i} = a^j + is^j \rightarrow i\infty$$

↗      ↗  
axions      saxions

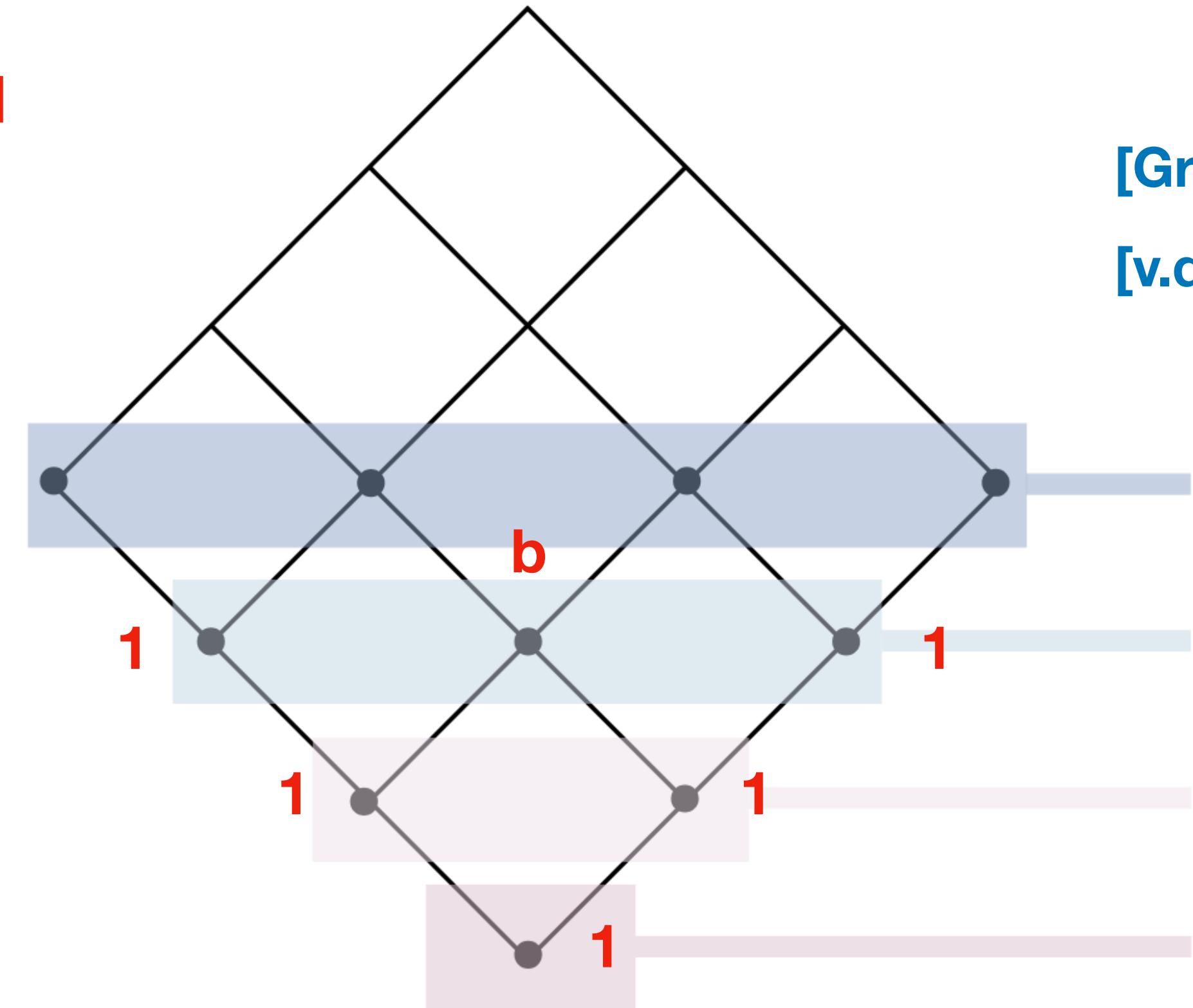
**Algebraic limiting mixed  
Hodge structure**

$$H^3(V, \mathbb{C}) = \bigoplus_{\ell=0}^6 \mathrm{Gr}_\ell$$

$$\mathrm{vol}(\Gamma) \sim s^{-1}$$

$$\mathrm{vol}(\Gamma) \sim s^{-2}$$

$$\mathrm{vol}(\Gamma) \sim s^{-3}$$



[Grimm,Palti,Valenzuela'18] [Grimm,Li,Palti'18] ...  
[v.d. Heisteeg'22] [Monne'24]

type I (finite distance)

type II

type III

type IV

$$S^1 \hookrightarrow \Gamma^a \rightarrow C_2^a$$

$$T^2 \hookrightarrow \Gamma^{(A,B)} \rightarrow S_1^{(A,B)}$$

$$\Gamma = T^3$$

# Physics interpretation

Infinite distance limit in complex structure  
moduli space of **Type IIB on CY 3-fold  $V$**

$$\frac{\log u^j}{2\pi i} = a^j + i s^j \rightarrow i\infty$$

↗      ↘  
**axions**      **saxions**

$$\text{vol}(\Gamma) \sim s^{-1}$$

$$\text{vol}(\Gamma) \sim s^{-2}$$

$$\text{vol}(\Gamma) \sim s^{-3}$$

**Algebraic mixed  
Hodge structure**

type II

$$S^1 \hookrightarrow \Gamma^a \rightarrow C_2^a$$

**Emergent string limits**

type III

$$T^2 \hookrightarrow \Gamma^{(A,B)} \rightarrow S_1^{(A,B)}$$

**Decompactification  $4d \rightarrow 6d$**

type IV

$$\Gamma = T^3$$

**Decompactification  $4d \rightarrow 5d$**

+

**Geometric mixed  
Hodge structure**



**Physics**

## Type IV as decompactification $4d \rightarrow 5d$

1 leading vanishing 3-cycle  $\Gamma$  of topology  $T^3 \implies$  1 tower of BPS states from wrapped D3-branes  
**behaving like 1 KK tower**

**Reason:**

$$\text{BPS index: } \Omega(n\Gamma) = \Omega(\Gamma), \quad n > 0$$

[Monne,TW,Wiesner'25]

From this we can in fact show:  $\Omega(\Gamma) = -\chi(V)$

$$\Omega_{\text{BPS},5d}^{(0)} = - \sum_{j_R} (-1)^{2j_R} (2j_R + 1) n_{(j_L, j_R)}^0 = -2n_H^{(0)} + 2n_V^{(0)} + 4 \quad n_H^{(0)} = h^{1,1}(V) + 1, \quad n_V^{(0)} = h^{2,1}(V) - 1$$

Known by mirror symmetry for large complex structure points,  
but **true more generally for all type IV degenerations and without using mirror symmetry!**

# Type III as decompactification $4d \rightarrow 6d$

2 leading vanishing 3-cycles  $\Gamma^{A,B}$  of topology  $T^3 \implies$  2 towers of BPS states from wrapped D3-branes  
**behaving as 2 KK towers**

In fact:

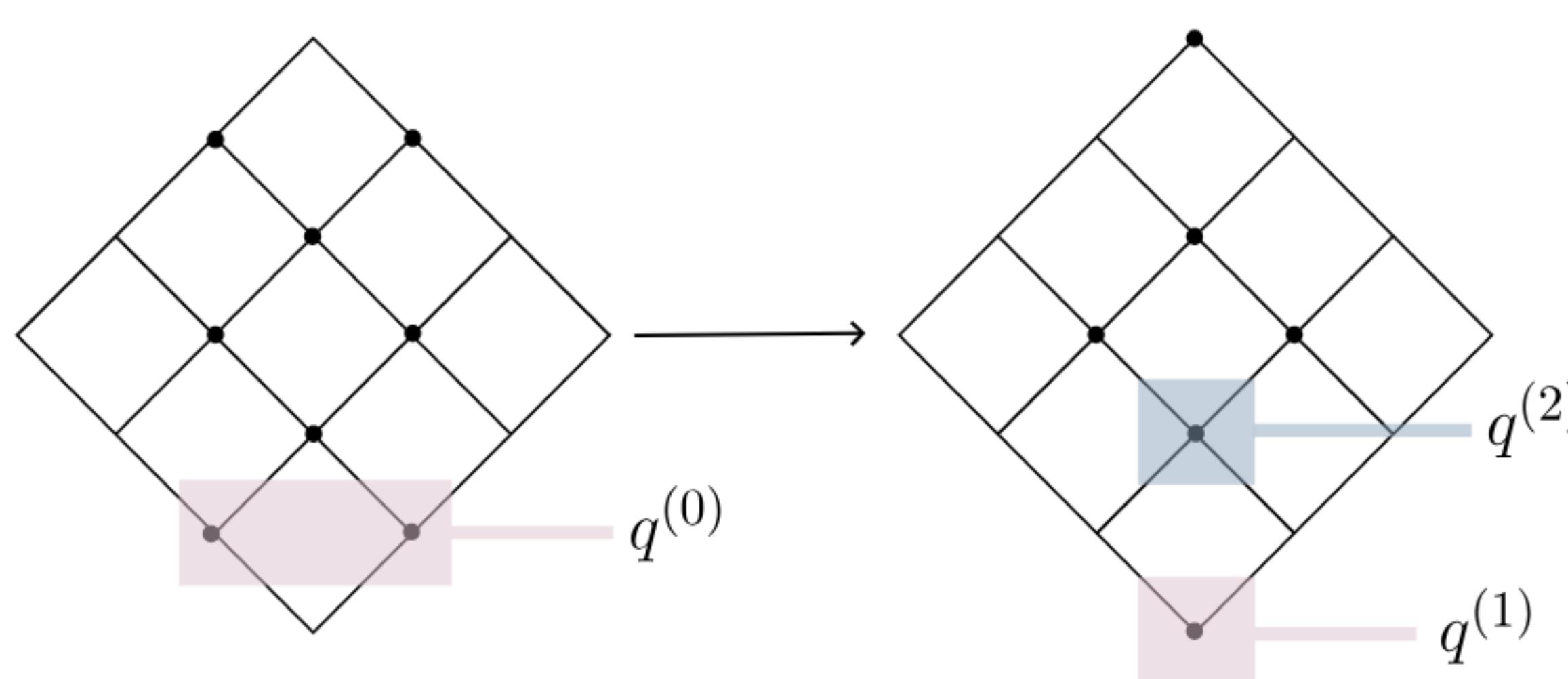
$$\text{BPS index: } \Omega(n\Gamma^{(i)}) = \Omega(\Gamma^{(i)}) = -\chi(V), \quad n > 0 \quad i = A, B$$

III

IV

[Monne,TW,Wiesner'25]

By noting that enhancement type III to IV is always possible



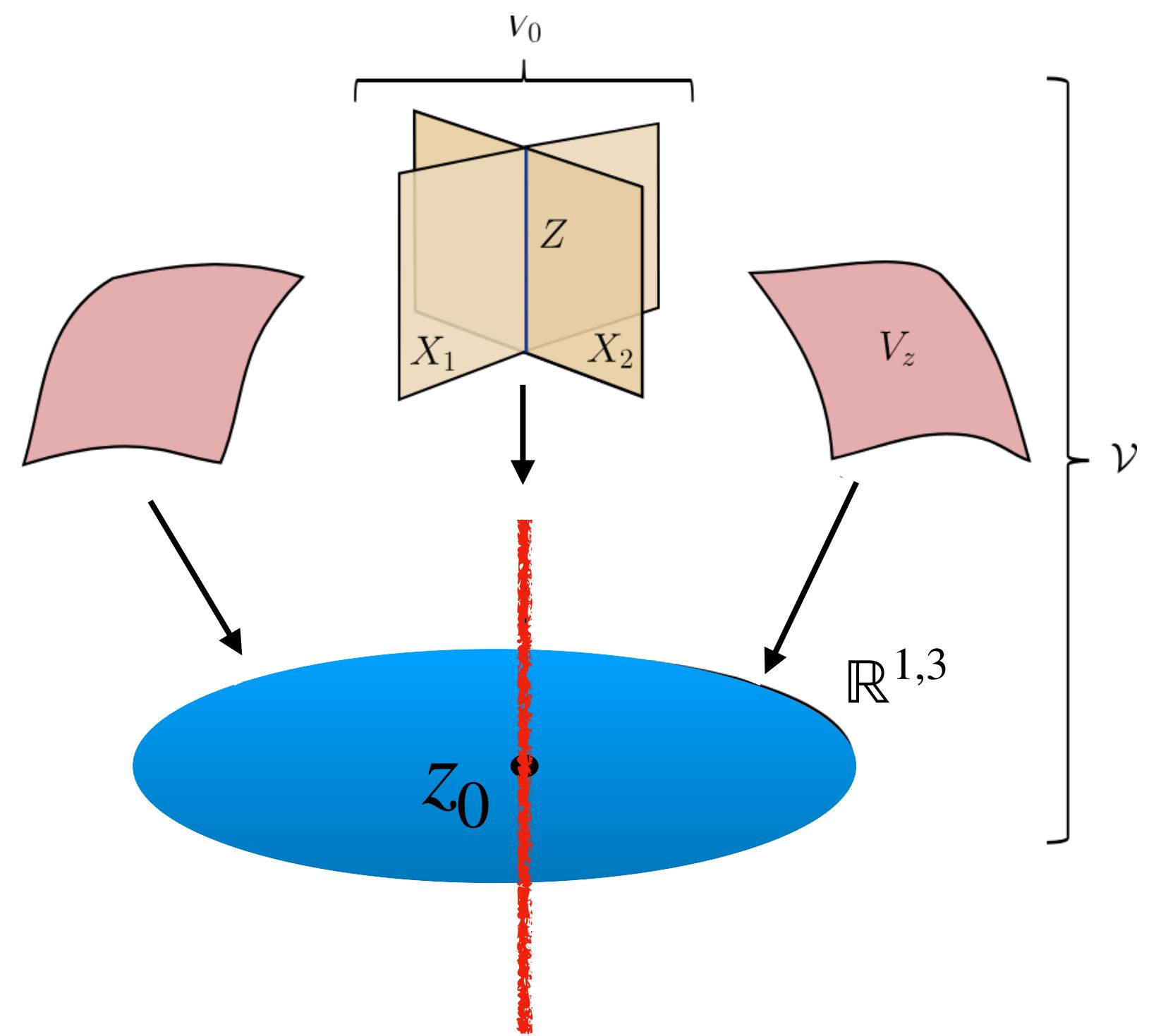
# Type II as emergent string limit

By identifying tensionless SUGRA BPS string (EFT string)  
as a heterotic or critical string

**Key:**  $V_{12}$  is K3 or  $T^4$

D3 branes on  $\Gamma^{(a)}$  : Dual winding states of that string

Details: [Friedrich,Monnee,Wiesner,TW'25]



# Interpretation of enhancement chains

1) EFT string limits:  $s^{k_1} \sim s^{k_2} \sim \lambda \rightarrow \infty$

Physics determined by type of enhanced singularity

2) Non-EFT string limits:  $s^{k_1} \sim \lambda, s^{k_2} \sim \lambda^{\alpha_{k_2}} \quad \alpha_{k_2} < 1, \dots$

Gravitational frame determined by type of first singularity with subsequent limits taken therein

II  $\rightarrow$  III: 6d decomp.

II  $\rightarrow$  IV: 5d decomp.

III  $\rightarrow$  IV: 5d decomp.

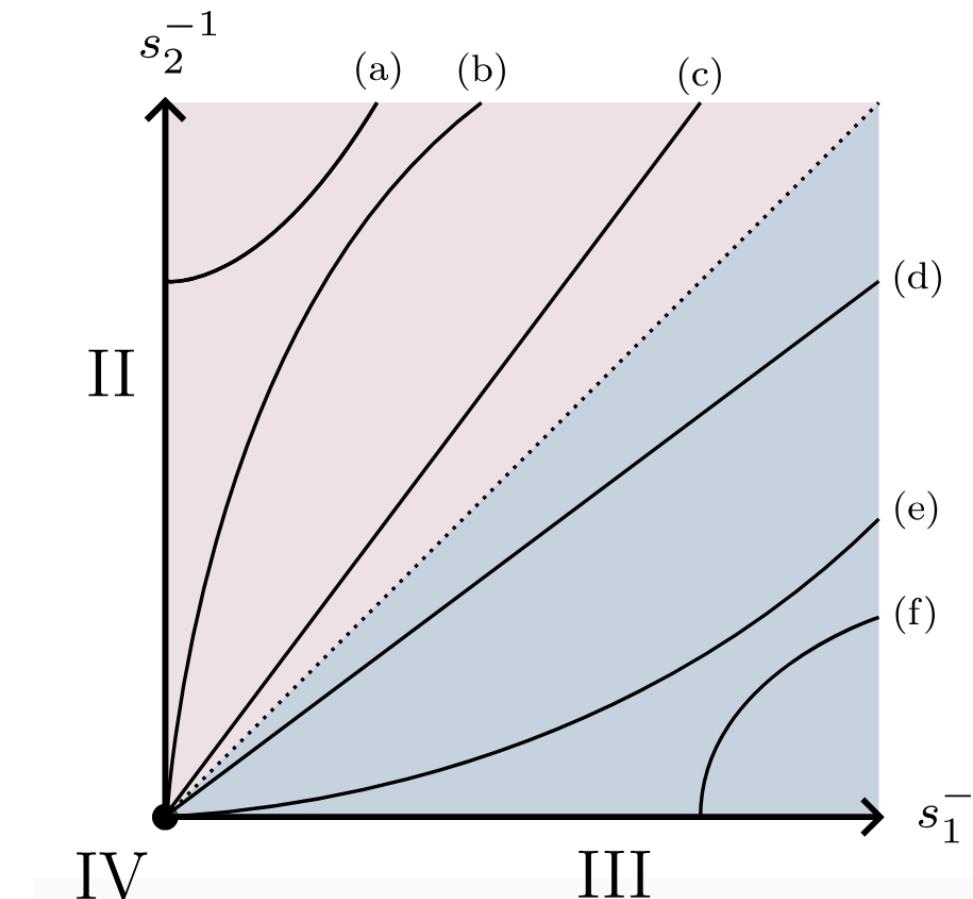
cf.

[Lanza, Marchesano, Martucci, Valezuela'20/21]

[Catellano, Ibanez, Herrea'22]

[Castellano, Ruiz, Valenzuela'23]

....



[Monnee, TW, Wiesner'25]

II  $\rightarrow$  III: emergent string, decompactified to 6d

II  $\rightarrow$  IV: emergent string, decompactified to 5d

III  $\rightarrow$  IV: anisotropic 6d decompactification

II  $\rightarrow$  III  $\rightarrow$  IV: emergent string, decompactified to anisotropic 6d

## Part 2:

Testing perturbative heterotic string theory with  
ALP coupling-to-mass ratios

[Agrawal,Nee,Reig'22, '24] [Reig,TW'25]

# Axions in the heterotic string

i) model independent axion:  $a = \int_X B_6$

ii) model independent axions:  $b_i = \int_{C_i} B_2$

iii) non-perturbative axions:  $\tilde{b}_r = \int_{\Gamma_r} \tilde{B}_2$  from NS5-branes along curve  $\Gamma_r$

Couplings  $\int_{\mathbb{R}^{1,3}} (\text{axion}) F \wedge F$  from Green-Schwarz terms :

$$\rightarrow S_{GS} = -\frac{1}{768\pi^3} \int_{\mathbb{R}^{1,3} \times X} B_2 \wedge X_8$$

$$X_8 = -(\text{tr}_1 \mathcal{F}^2 + \text{tr}_2 \mathcal{F}^2) \text{tr} \mathcal{R}^2 + 2 [(\text{tr}_1 \mathcal{F}^2)^2 + (\text{tr}_2 \mathcal{F}^2)^2 - \text{tr}_1 \mathcal{F}^2 \text{tr}_2 \mathcal{F}^2] + \text{tr} \mathcal{R}^4 + \frac{1}{4} (\text{tr} \mathcal{R}^2)^2$$

$\rightarrow$  5-brane dependent counter-terms

$$S_{GS}^{\text{new}, 2} = \frac{1}{64\pi^3} \sum_r N_r \int_{\Gamma_r} \tilde{B}_2^{(r)} \wedge (\text{tr}_1 \mathcal{F}^2 - \text{tr}_2 \mathcal{F}^2)$$

# Axion couplings in the heterotic string

**Result:**

$$\mathcal{L} = \frac{\theta_1}{8\pi} \text{tr}_1 F^2 + \frac{\theta_2}{8\pi} \text{tr}_2 F^2$$

$$E_8^{(1)}$$

$$E_8^{(2)}$$

$$n_i^{1,2} = \int_X \frac{1}{16\pi^2} \beta_i \wedge \left( \text{tr}_{1,2} F^2 - \frac{1}{2} \text{tr} R^2 + \frac{1}{3} \sum_r N_r \bar{\gamma}_r \right)$$

$$\text{tr}_1 \bar{F}^2 + \text{tr}_2 \bar{F}^2 - \text{tr} \bar{R}^2 = \sum_r N_r [\Gamma_r]$$

$$a = \int_X B_6$$

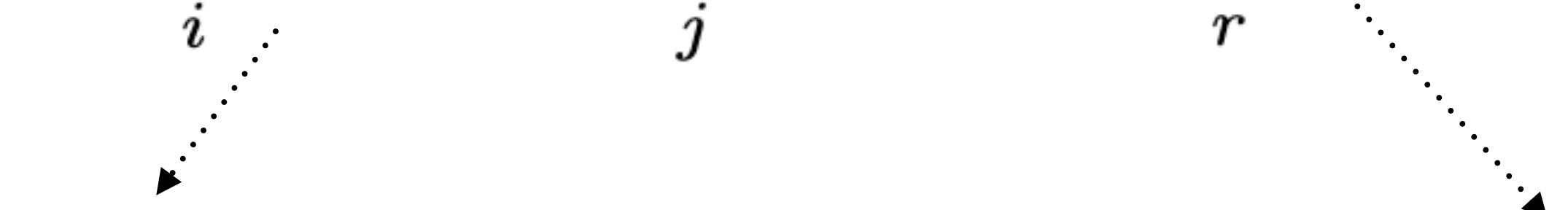
$$b_i = \int_{C_i} B_2$$

field theory  
axions

$$\tilde{b}_r = \int_{\Gamma_r} \tilde{B}_2$$

$$\theta_1 = a + \sum_i n_i^{(1)} b_i + \sum_j m_j^{(1)} c_j + \sum_r N_r \tilde{b}_r ,$$

$$\theta_2 = a + \sum_i n_i^{(2)} b_i + \sum_j m_j^{(2)} c_j - \sum_r N_r \tilde{b}_r .$$



# ALP coupling-to-mass ratios

$$\mathcal{L} = \frac{\theta_1}{8\pi} \text{tr}_1 F^2 + \frac{\theta_2}{8\pi} \text{tr}_2 F^2$$

- If  $SU(3) \times SU(2) \times U(1)_Y \subset E_8^{(1)}$ : Every axion coupling directly to  $U(1)_{e.m.}$  also couples to QCD!
- Any other axion coupling to  $U(1)_{e.m.}$  can do so only through kinetic or mass mixing with QCD axion  
e.g. for light axions mass mixing suppressed by  $m_a^2/m_{a,\text{QCD}}^2$

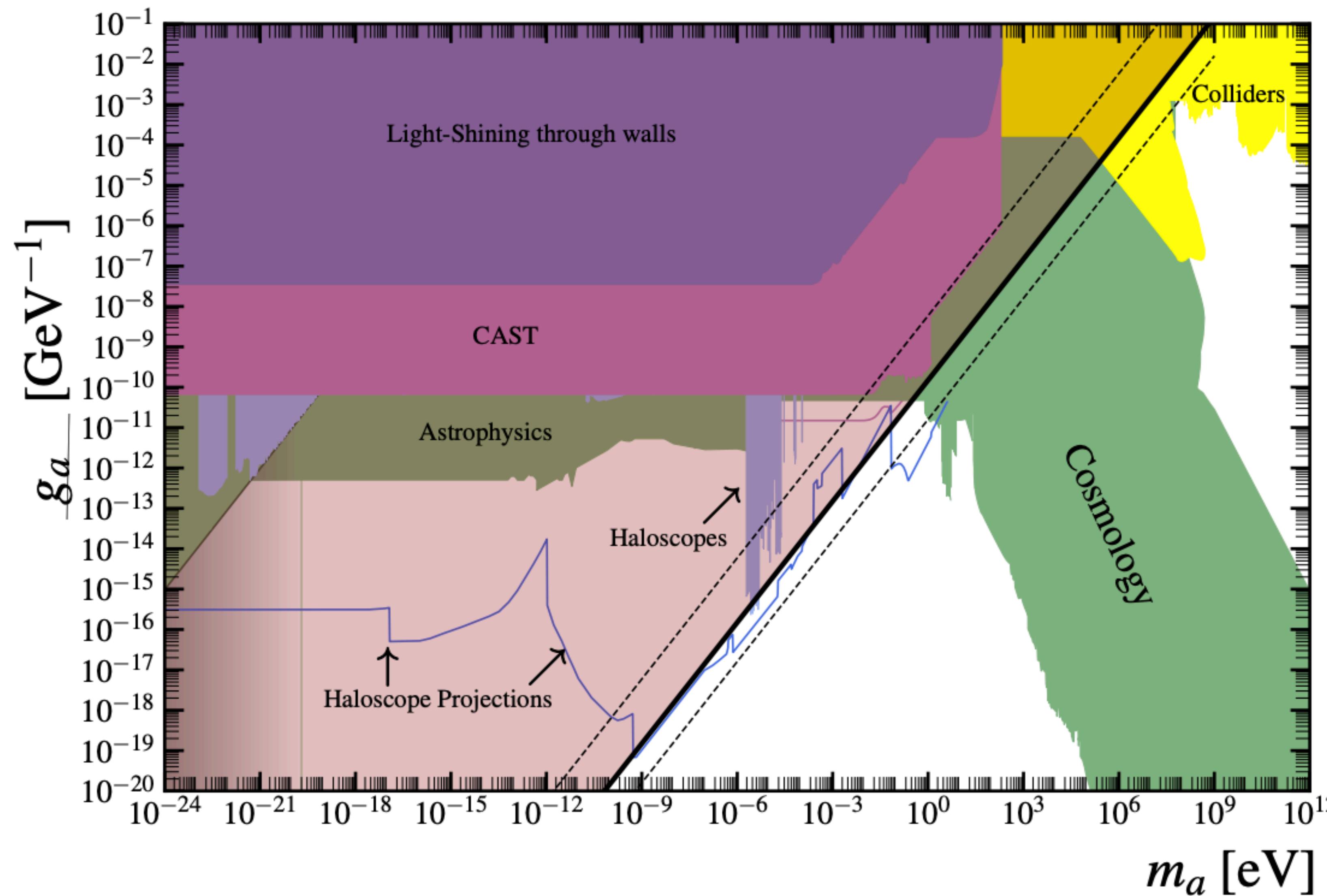
Key consequence:

$$\frac{g_{ALP,\gamma}}{m_{ALP}} \leq \frac{g_{a_{\text{QCD}},\gamma}}{m_{a_{\text{QCD}}}}$$

[Agrawal, Nee, Reig '22]  
[Agrawal, Nee, Reig '24]

holds for any general GUT!

# ALPs and heterotic GUTs



[Agrawal, Nee, Reig '22 + '24]

Finding an ALP above black line  
would rule out any GUT, including  
heterotic string with SM inside one  $E_8$

# Non-standard embeddings

**Loophole:** Non-standard embedding of SM into both  $E_8^{(1)}$  and  $E_8^{(2)}$

Most interesting case: **Hypercharge** embedded into **both**  $E_8^{(i)}$

# [Blumenhagen,Moster,TW'06] [Blumenhagen,Honecker,TW'05]

Can be achieved by embedding gauge backgrounds with **non-trivial first Chern class (U(1) flux)**

$$\begin{array}{ccc}
E_8^{(1)} \times E_8^{(2)} & \rightarrow & (G_1 \times \prod_{m_1} U(1)_{m_1}) \times (G_2 \times \prod_{m_2} U(1)_{m_2}) \\
& & \downarrow \quad \quad \quad \downarrow \\
& m_1 & \vdots & m_2 & \vdots \\
& & \downarrow & & \downarrow \\
& & SU(3) \times SU(2) \times U(1)_0 & & U(1)_1 \times (\text{rest}) \\
& & \searrow \dots \swarrow & & \searrow \dots \swarrow \\
& & & & U(1)_Y = aU(1)_0 + bU(1)_1
\end{array}$$

A large, dark gray checkmark icon, indicating a correct or approved status.

Examples with  
exactly 3 generations of  
SM matter  
and no chiral exotics  
on simply connected  
CY 3-folds

# Stückelberg massless combination

# Gauge coupling unification

**Non-standard  
hypercharge embedding**

$$\frac{1}{\alpha_Y} = \frac{5/3}{\alpha_{\text{GUT}}} + \frac{k_1^{(2)}}{\alpha_{\text{GUT}}} + \Delta_Y$$

[Blumenhagen, Moster, TW'06]

$k_1^{(2)}$ : level of embedding of  $U(1)_Y$  into  $E_8^{(2)}$

$$\text{e.g. for 2 U(1): } k_1^{(2)} = \frac{5}{3} \left( \frac{\kappa_{0,0} \ell_0}{\kappa_{1,1} \ell_1} \right)^2 \frac{\eta_{1,1}}{\eta_{0,0}}$$

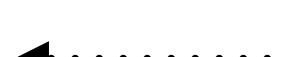
$\Delta_Y$ : 1-loop threshold corrections

$$\kappa_{i,i} : \text{tr}_{E_8} F^2 = \kappa_{i,i} f_i^2 + \dots \quad \eta_{i,i} : \text{tr} F \bar{F} = \eta_{i,i} f_i \bar{f}_i + \dots$$

$$c_1(L_i) = \ell_i v \in H^2(X)$$

Required:

$$0 = \frac{k_1^{(2)}}{\alpha_{\text{GUT}}} + \Delta_Y + \Delta$$



from intermediate  
mass states

# Axions in the heterotic string

New: **Two ALPs** coupling to electro-magnetism due to U(1) fluxes

$$\begin{aligned} \mathcal{L} = & \frac{\theta_1}{8\pi} \left[ k_3^{(1)} \alpha_3 \text{tr} G \tilde{G} + \left( \frac{(k_1^{(1)})^2}{k_1^{(1)} + k_1^{(2)}} + k_2^{(1)} \right) \alpha_{\text{em}} F_{\text{em}} \tilde{F}_{\text{em}} \right] \\ & + \frac{\theta_2}{8\pi} \left( \frac{(k_1^{(2)})^2}{k_1^{(1)} + k_1^{(2)}} \right) \alpha_{\text{em}} F_{\text{em}} \tilde{F}_{\text{em}} + \frac{\varphi}{8\pi} \frac{(\kappa_{0,0} \ell_0)^2}{\eta_{0,0}} k_1^{(1)} \alpha_{\text{em}} F_{\text{em}} \tilde{F}_{\text{em}} . \end{aligned}$$

[Reig, TW'25]

Origin of  $\varphi$ :

$$S_{\text{GS}} \supset \frac{1}{768\pi^3} \int B \wedge \text{tr}_i(F\bar{F})^2 - \frac{1}{768\pi^3} \int B \wedge \text{tr}_1(F\bar{F}) \text{tr}_2(F\bar{F})$$

$$\theta_1 = a + \sum_i n_i^{(1)} b_i + \sum_j m_j^{(1)} c_j + \sum_r N_r \tilde{b}_r ,$$

$$\theta_2 = a + \sum_i n_i^{(2)} b_i + \sum_j m_j^{(2)} c_j - \sum_r N_r \tilde{b}_r .$$

Does this evade the previous bounds?

$$\varphi = \sum_j b_j \int \beta_j \wedge c_1^2(L) = \sum_j \tilde{n}_j b_j$$

# Axions in the heterotic string

**Key observation:**

$\theta_2, \varphi$  receive a potential from small  $E_8^{(2)}$  instantons due to Euclidean NS5-branes

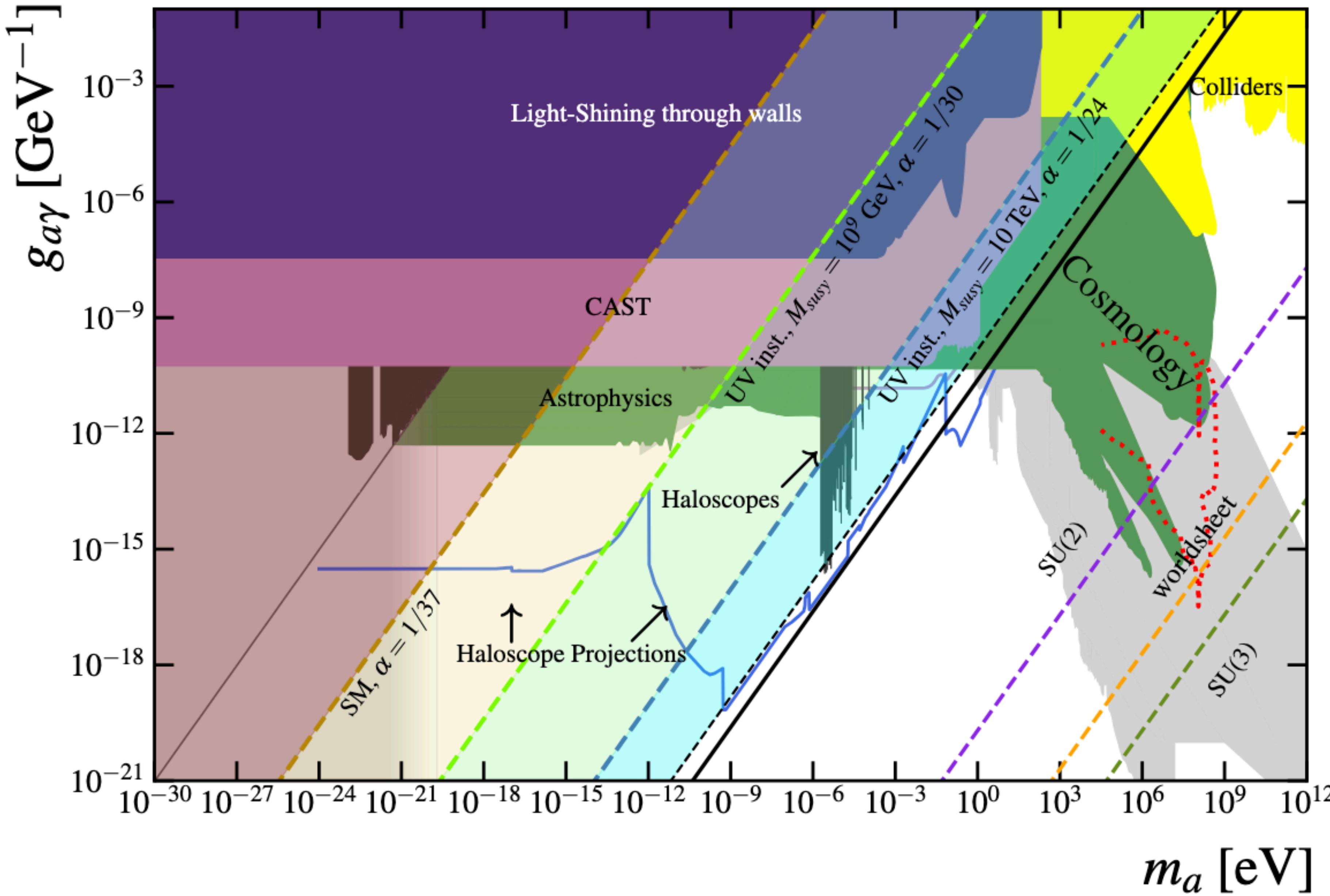
Ignoring effect of gauge threshold corrections for now:

$$V(\theta_2, \varphi) = \frac{16\pi}{\alpha_{\text{GUT}}} \left( \frac{M_{\text{UV}}}{m_f} \right)^{n_f} m_{\text{susy}} M_{\text{UV}}^3 e^{-\frac{2\pi}{\alpha_{\text{GUT}}}} \cos(\theta_2) + (\theta_2 \leftrightarrow \varphi)$$

[Reig,TW'25]

Chiral suppression factor  
from  $n_f$  intermediate superfields:  
increases mass due to  
running of gauge coupling!

at tree-level:  $\alpha_{E_8^{(2)}} = \alpha_{\text{GUT}}$   
precise value key for suppression!



[Reig,TW'25]

conservative bounds  
ignoring thresholds

# Compatibility with gauge couplings

$$\frac{1}{\alpha_Y} = \frac{5/3}{\alpha_{\text{GUT}}} + \frac{k_1^{(2)}}{\alpha_{\text{GUT}}} + \Delta_Y \quad \text{requires} \quad 0 = \frac{k_1^{(2)}}{\alpha_{\text{GUT}}} + \Delta_Y + (\Delta \text{ from intermediate states})$$

All three effects decrease  $g_{a\gamma}/m_a$  for heterotic ALPs!

previous tree-level plot  
is (very!) conservative

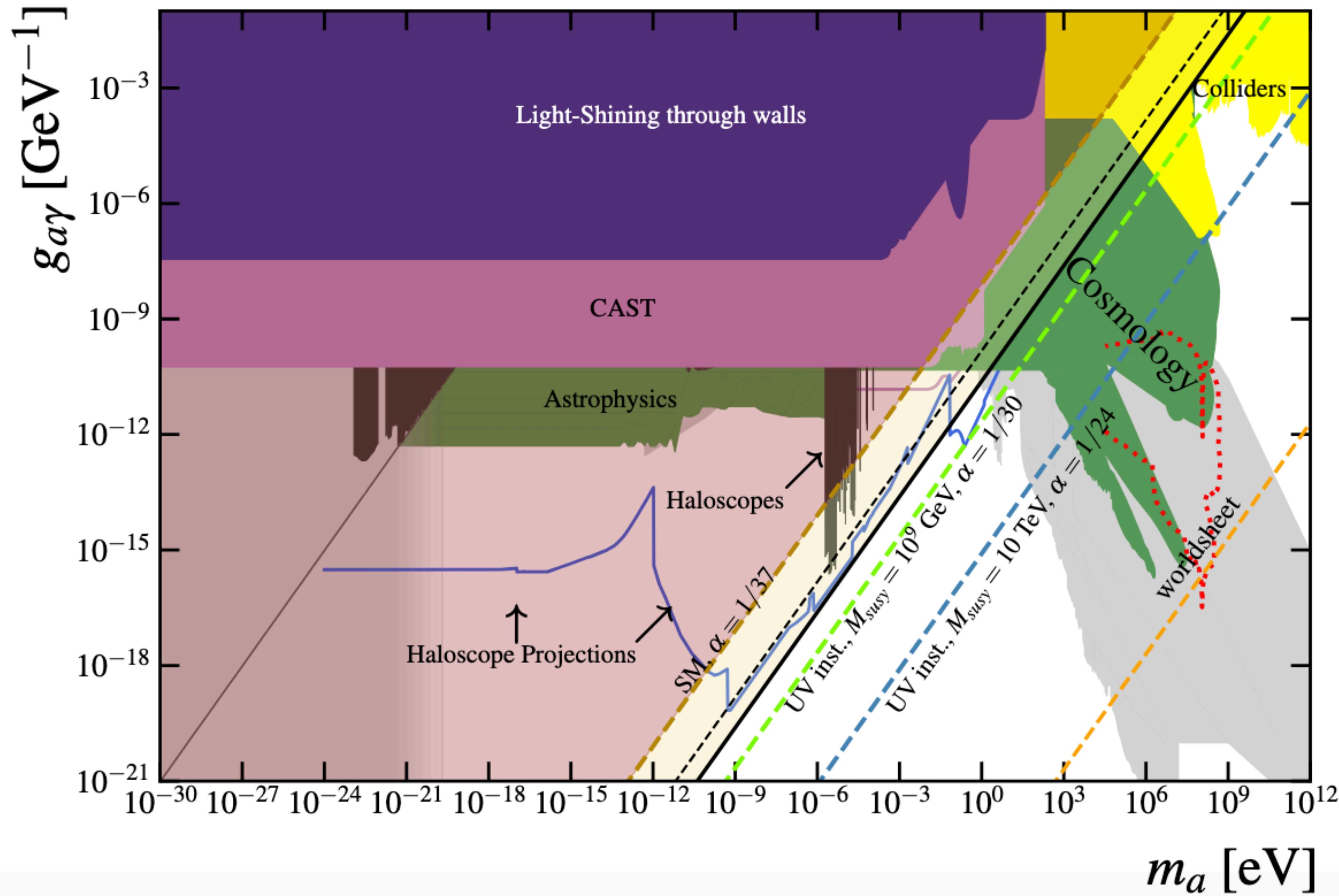
1) **Engineering  $k_1^{(2)} \ll 1$ :** decreases coupling to photons by  $(k_1^{(2)})^2$

2) **Intermediate matter:** increases  $\alpha_{\text{GUT}}$   $\implies$  increases masses

e.g.  $\alpha_{\text{GUT}} \geq \frac{1}{22} \implies$  QCD bound obeyed!

3) **Invoking threshold corrections:**

- more complicated analysis, but unless perturbative control is lost,  $g_{a\gamma}/m_a$  decreases



[Reig,TW'25]

for thresholds  
75% of tree-level  
(borderline perturbative)

Example:  
cosmic birefringence  
axion

$$m_a = 10^{-30} \text{ eV}$$

$$g_{a\gamma} = 10^{-18} \text{ GeV}^{-1}$$

would rule out  
perturbative  
heterotic string!

# Summary

Part 1) Testing ESC via stable degenerations:

$$\text{vol}(\Gamma) \sim s^{-1}$$

type II

$$S^1 \hookrightarrow \Gamma^a \rightarrow C_2^a$$

**Emergent string limits**

$$\text{vol}(\Gamma) \sim s^{-2}$$

type III

$$T^2 \hookrightarrow \Gamma^{(A,B)} \rightarrow S_1^{(A,B)}$$

**Decompactification 4d  $\rightarrow$  6d**

$$\text{vol}(\Gamma) \sim s^{-3}$$

type IV

$$\Gamma = T^3$$

**Decompactification 4d  $\rightarrow$  5d**

Part 2) Testing the perturbative heterotic string via ALP coupling-to-mass ratios:

**Finding an ALP far above QCD line would rule out perturbative heterotic string  
- and comparable GUT(-like) models**