

# Anomalous $Z'$

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Based on

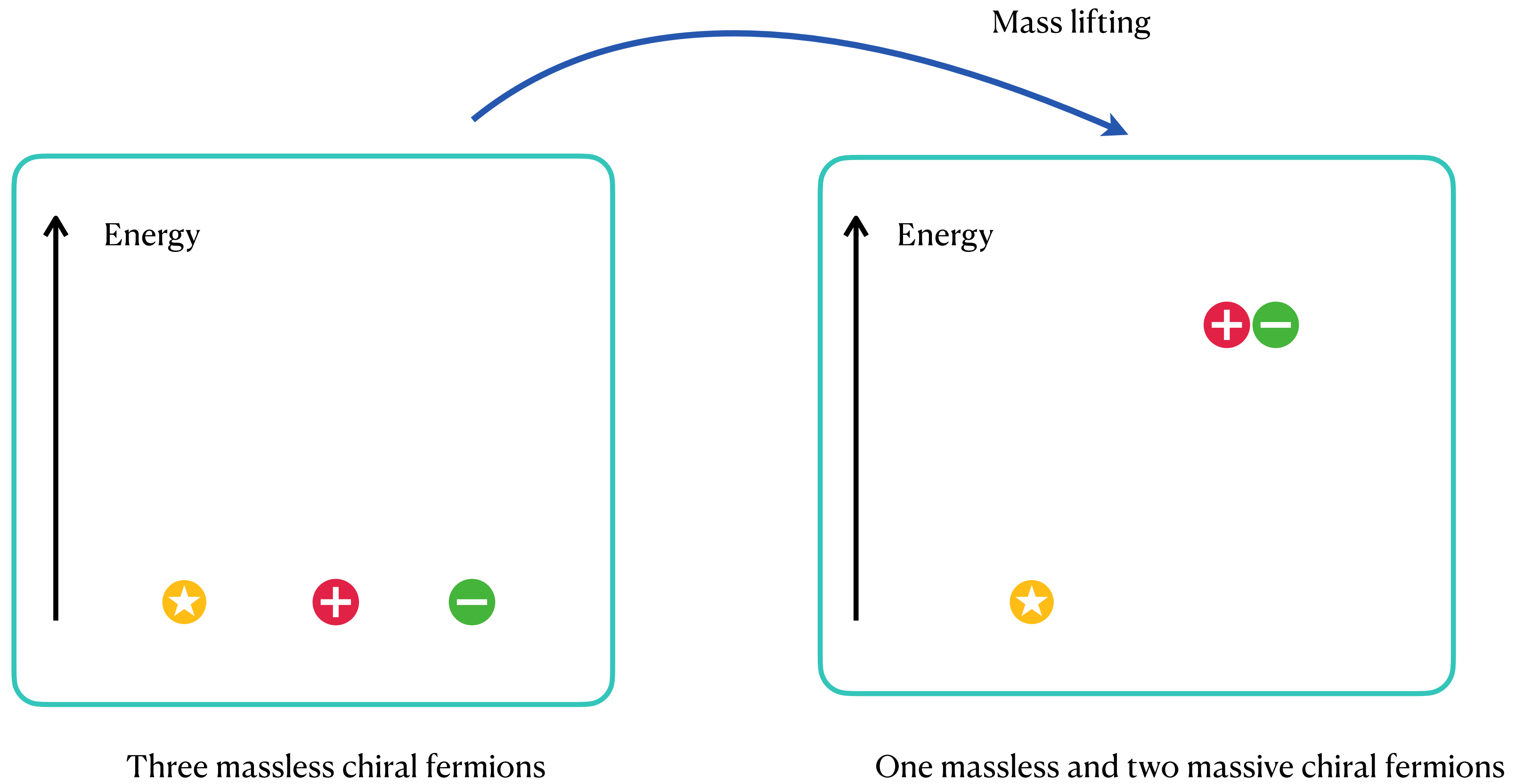
Pascal Anastasopoulos, Ignatios Antoniadis, K.B., François Rondeau *JHEP* 07 (2024) 232  
+ Arno Goudeau (in progress ...)

Workshop on the Standard Model and Beyond, Corfu 2024



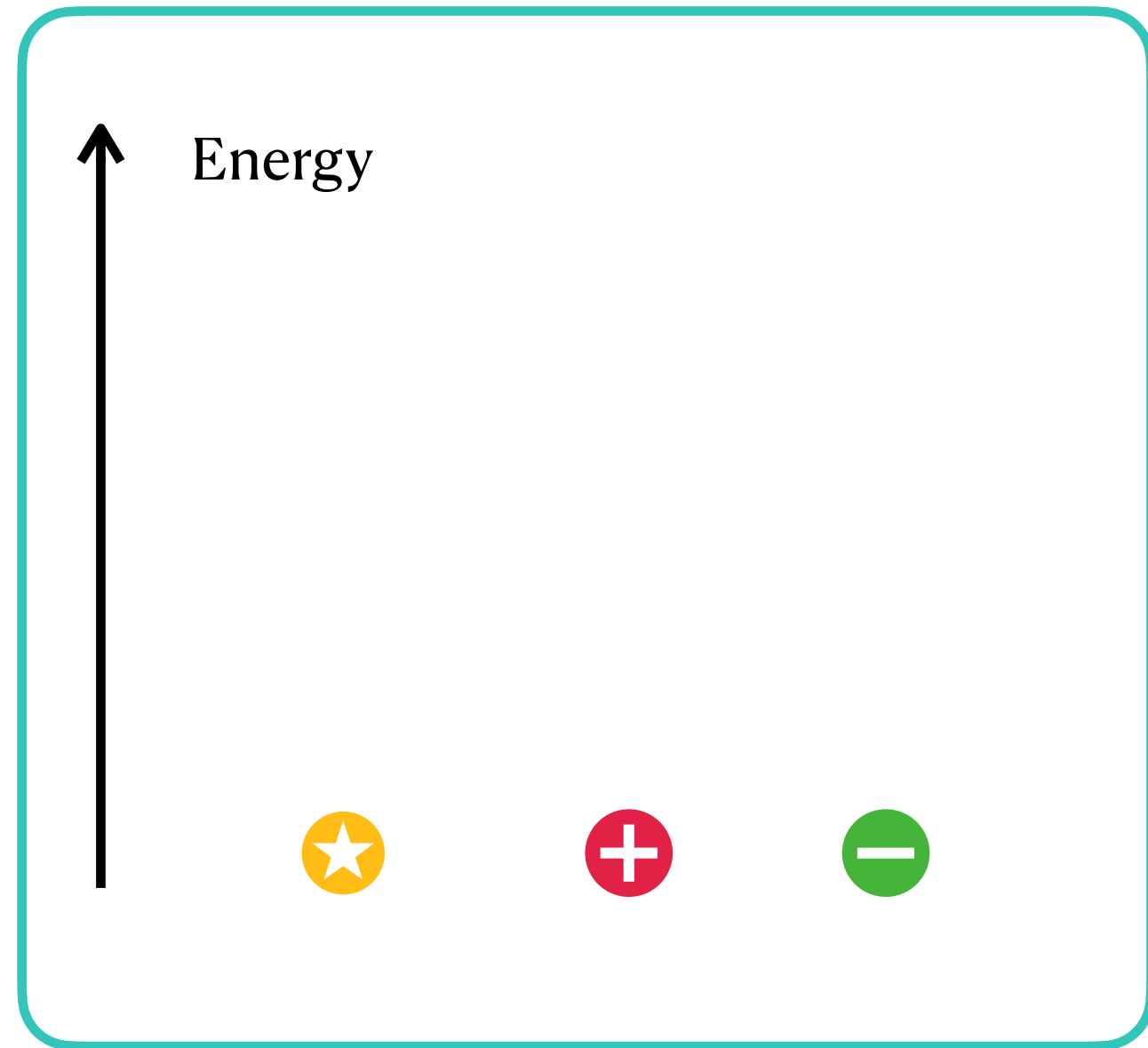
**The general idea**

*Separating the chiral fermions*



*The EFT will look anomalous*

Higgs mechanism



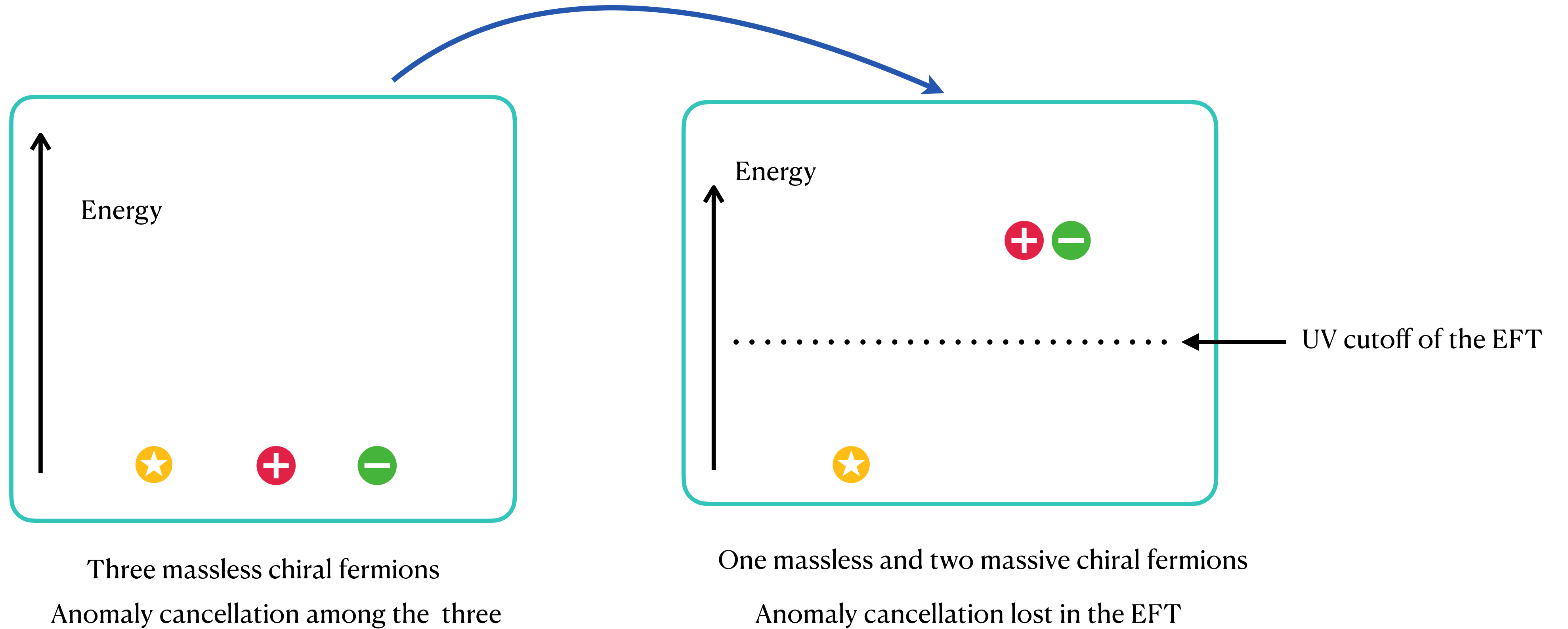
Three massless chiral fermions

Anomaly cancellation among the three



One massless and other massive fermions

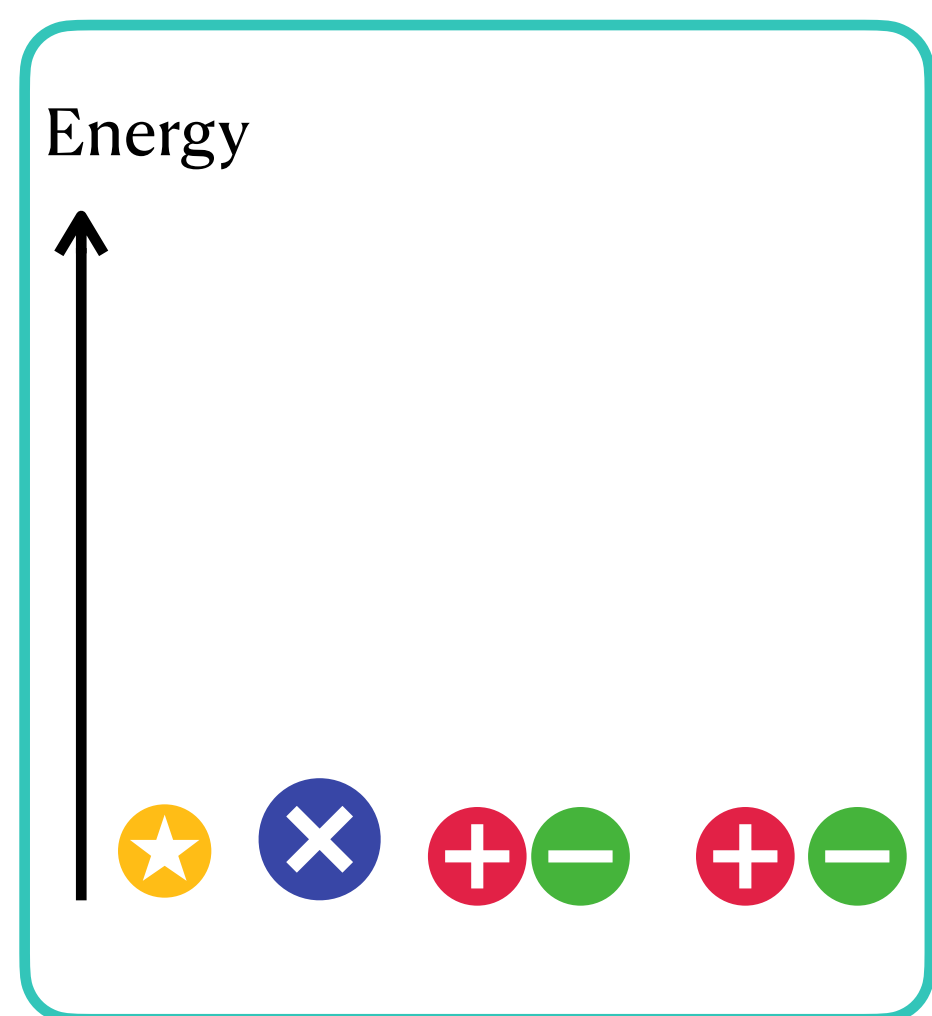
*The EFT will look anomalous*



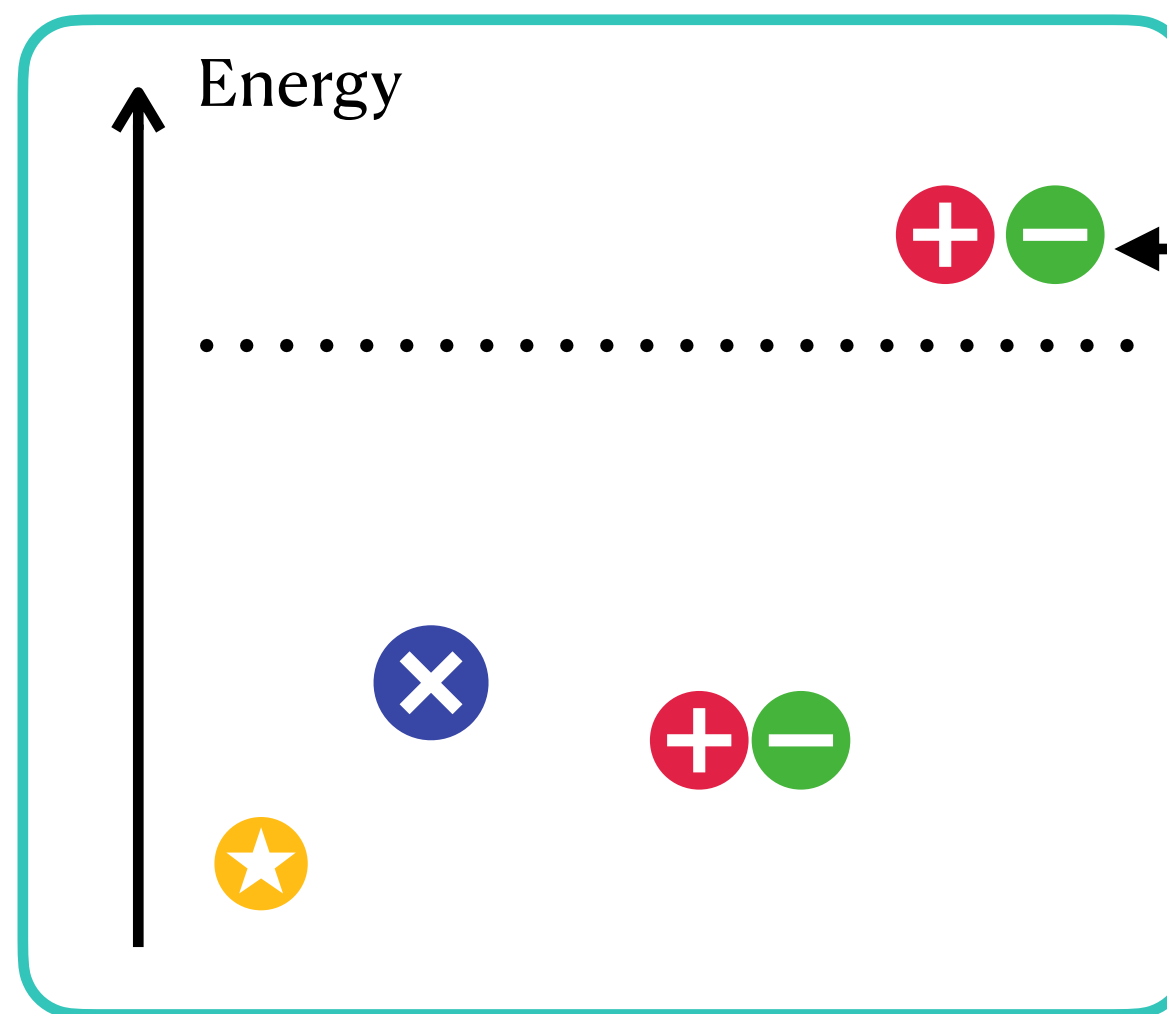
Old story but very few explicit realizations

*A perturbative EFT field description*

Higgs mechanism



Many massless chiral fermions  
+  
Gauge bosons



Hierarchy of Yukawa couplings  
Hierarchy gauge vs Yukawa couplings

Hierarchy might lead to non-perturbative coupling

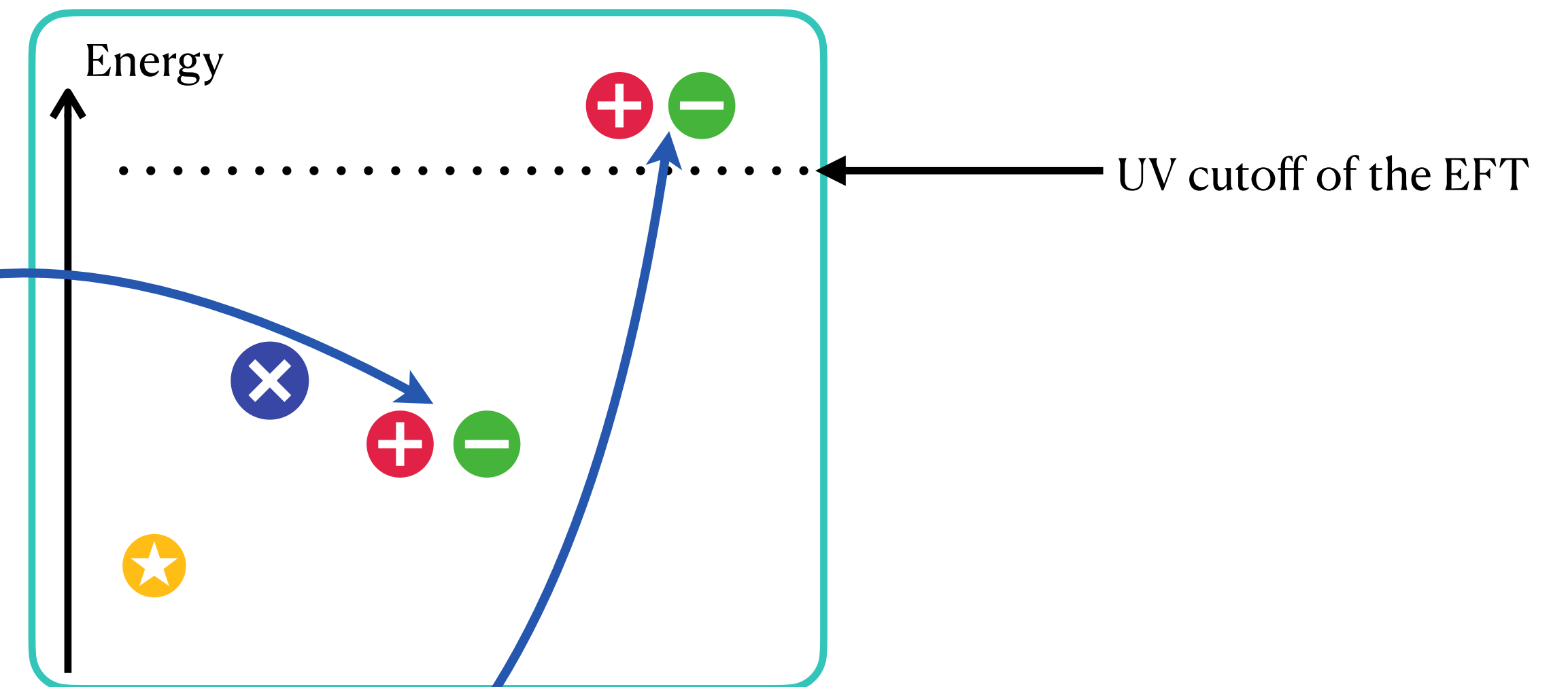
Example: top quark in SM

*Aiming for:*

Our objective is:

To orchestrate a situation in which the contributions to **the anomalies** of the  $U(1)_A$  gauge symmetry **cancel out between:**

- the **light fields** present in the effective field theory
- and
- the (non-observable) **heavier chiral fermions**.



Picture after Higgs mechanism

## *An explicit Model:*

Our objective is:

To orchestrate a situation in which the contributions to **the anomalies** of the  $U(1)_A$  gauge symmetry **cancel out between:**

- the **light fields** present in the effective field theory = **Standard Model**

and

- the (non-observable) **heavier chiral fermions** = **New (secluded) sector**



# The Model Field Content

Our objective is:

To orchestrate a situation in which the contributions to **the anomalies** of the  $U(1)_A$  gauge symmetry **cancel out between:**

- the **light fields** present in the effective field theory

and

- the (non-observable) **heavier chiral fermions.**

			$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
SM sector	$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
	$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
	$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
	$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
	$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
	$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_\nu^f$
Secluded sector	$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
	$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\widetilde{q}_{\mathbf{L}}^i$
	$\psi_L^{e_j}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
	$(\psi_R^{e_j})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\widetilde{q}_e^j$
	$\psi_L^{d_k}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
	$(\psi_R^{d_k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\widetilde{q}_d^k$
	$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
	$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\widetilde{q}_{\mathbf{Q}}^m$

**Table 1:** The particle content of the model

# Masses through Higgses

$$\langle H \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}, \quad \langle S \rangle = \frac{v_S}{\sqrt{2}},$$

$$v \ll v_S$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_\nu^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}^i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}^i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\tilde{q}_{\mathbf{L}}^i$
$\psi_L^{e^j}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{e^j})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\tilde{q}_e^j$
$\psi_L^{d^k}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{d^k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\tilde{q}_d^k$
$\psi_L^{\mathbf{Q}^m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}^m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\tilde{q}_{\mathbf{Q}}^m$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$

## Masses through Higgses

$$\langle H \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}, \quad \langle S \rangle = \frac{v_S}{\sqrt{2}},$$

$$v \ll v_S$$

$U(1)_A$  gauge boson mass

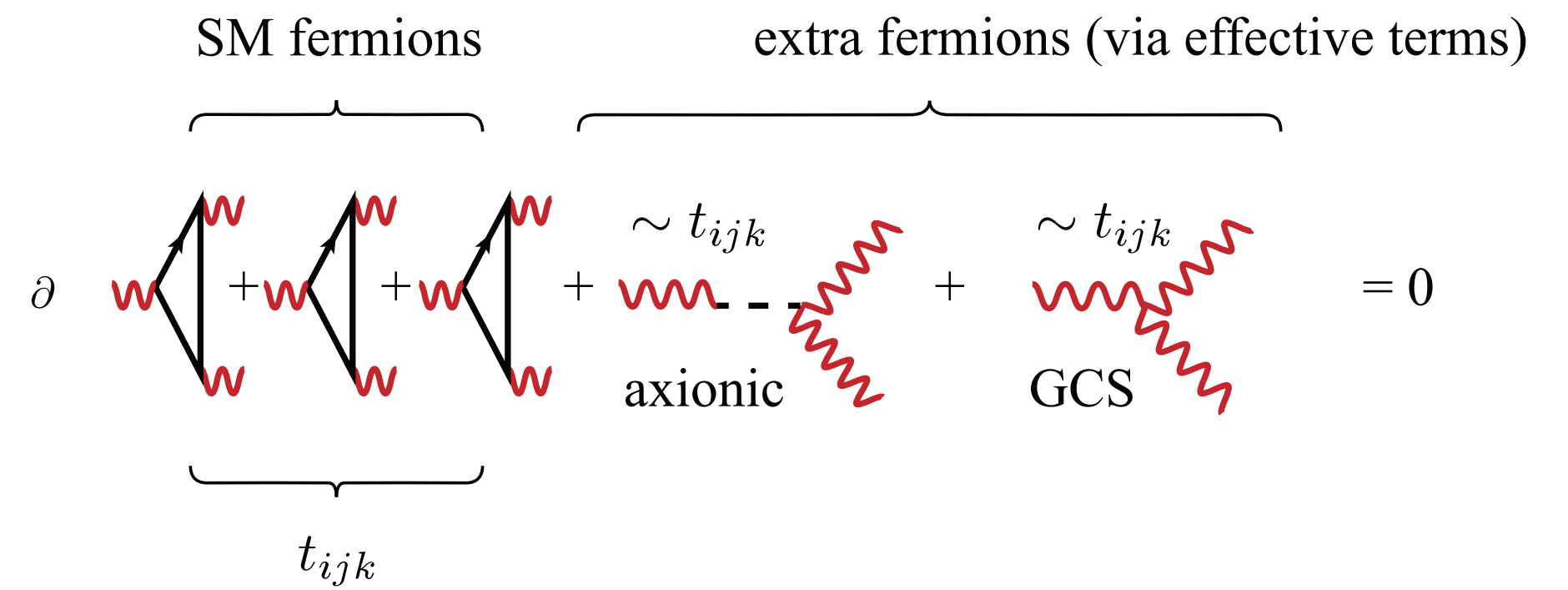
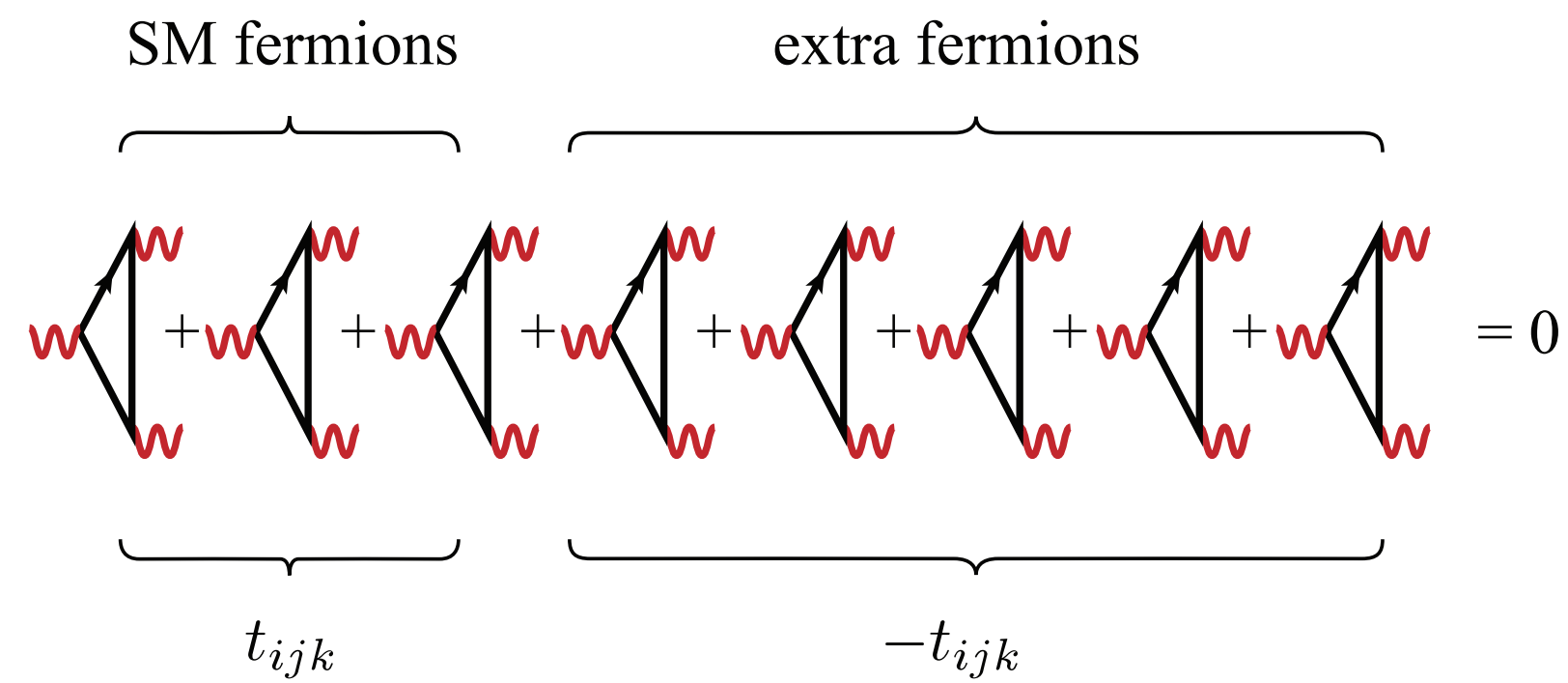
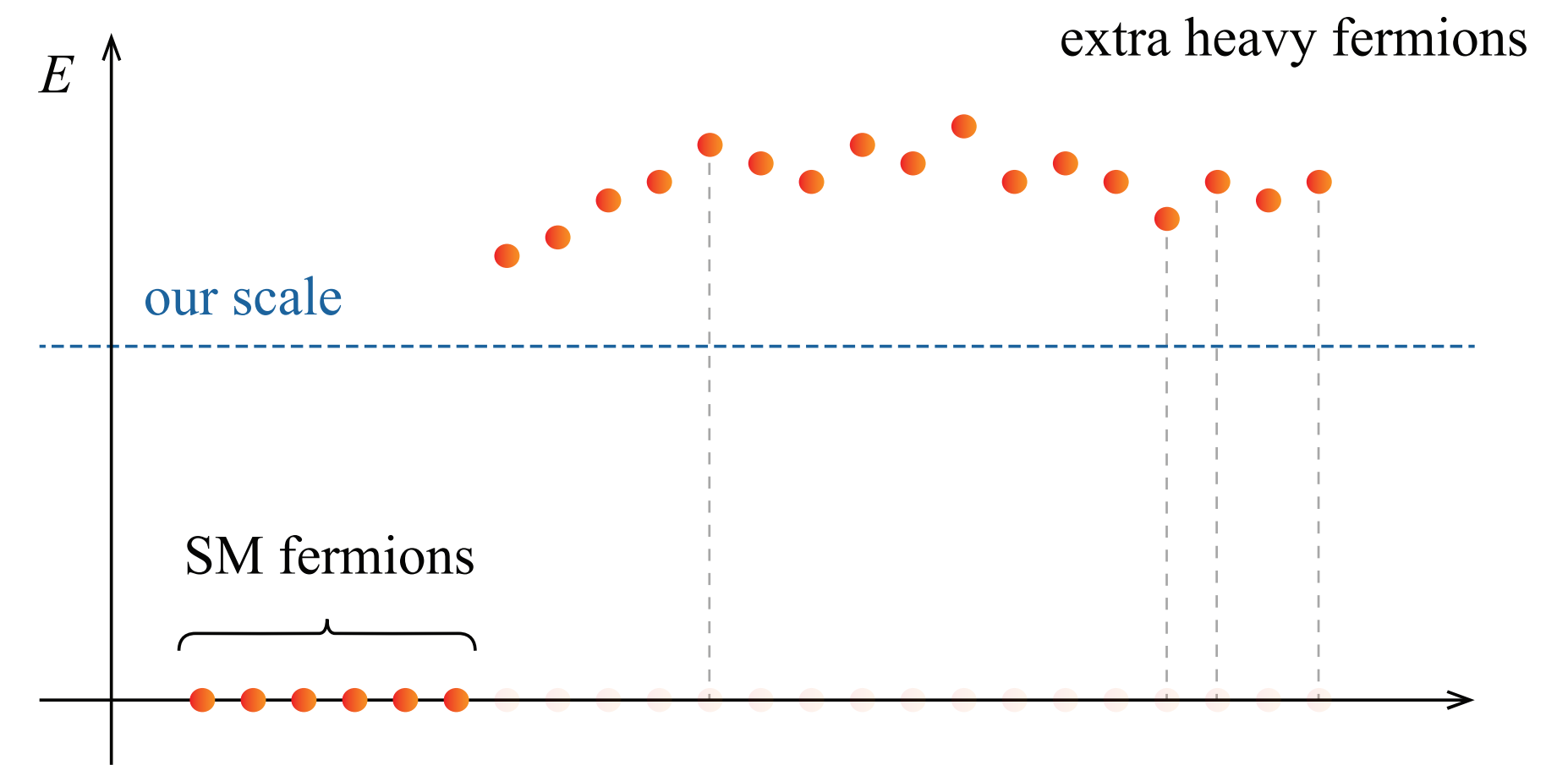
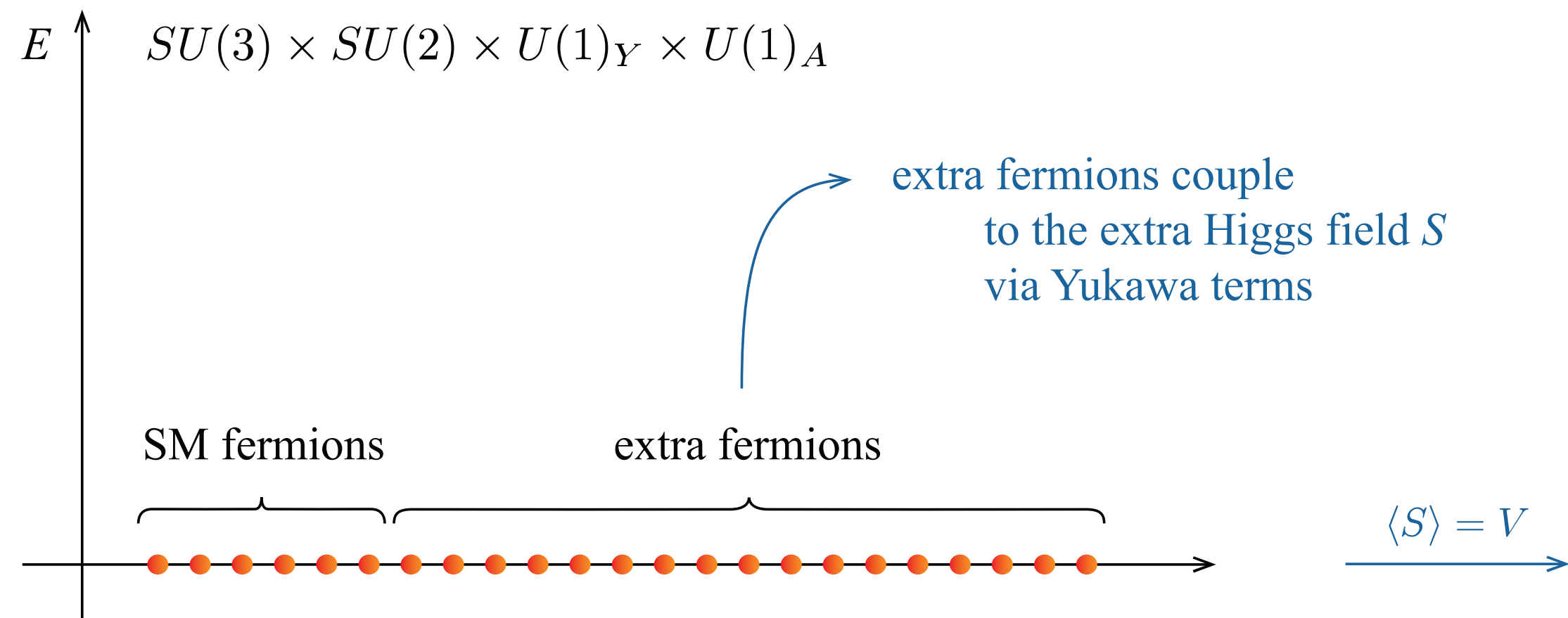
$$M_A \sim g_A |q_S| v_S.$$

Yukawa terms  $Y_{ij} \bar{\psi}_L^i \psi_R^j \tilde{S}$ , where by  $\tilde{S}$  we denote  $S$  or  $S^*$

$$M_{\psi,ij} = Y_{ij} v_S$$

$$Y_{ij} \propto \delta_{ij}$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_{\nu}^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\tilde{q}_{\mathbf{L}}^i$
$\psi_L^{ej}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{ej})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\tilde{q}_e^j$
$\psi_L^{dk}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{dk})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\tilde{q}_d^k$
$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\tilde{q}_{\mathbf{Q}}^m$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$



# Exploration of potential models

# The Complete Model anomaly cancellation equations

## Cancellation of the anomalies contributions

$$Tr[Y]_{SM} = Tr[Y]_{secluded} = 0,$$

$$Tr[YYY]_{SM} = Tr[YYY]_{secluded} = 0,$$

$$Tr[YT_2T_2]_{SM} = Tr[YT_2T_2]_{secluded} = 0,$$

$$Tr[YT_3T_3]_{SM} = Tr[YT_3T_3]_{secluded} = 0,$$

$$Tr[T_3T_3T_3]_{SM} = Tr[T_3T_3T_3]_{secluded} = 0,$$

$$Tr[q_A]_{SM} = -Tr[q_A]_{secluded} \equiv t_A,$$

$$Tr[YYq_A]_{SM} = -Tr[YYq_A]_{secluded} \equiv t_{YYA},$$

$$Tr[Yq_Aq_A]_{SM} = -Tr[Yq_Aq_A]_{secluded} \equiv t_{YAA},$$

$$Tr[q_Aq_Aq_A]_{SM} = -Tr[q_Aq_Aq_A]_{secluded} \equiv t_{AAA},$$

$$Tr[q_AT_2T_2]_{SM} = -Tr[q_AT_2T_2]_{secluded} \equiv t_2,$$

$$Tr[q_AT_3T_3]_{SM} = -Tr[q_AT_3T_3]_{secluded} \equiv t_3.$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_Q^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_L^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_\nu^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}^i}$		$\mathbf{1}$	$\mathbf{2}$	$y_L^i$	$q_L^i$
$(\psi_R^{\mathbf{L}^i})^c$	$i = 1, \dots, N_L$	$\mathbf{1}$	$\mathbf{2}$	$-y_L^i$	$\tilde{q}_L^i$
$\psi_L^{e_j}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{e_j})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\tilde{q}_e^j$
$\psi_L^{d_k}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{d_k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\tilde{q}_d^k$
$\psi_L^{\mathbf{Q}^m}$		$\mathbf{3}$	$\mathbf{2}$	$y_Q^m$	$q_Q^m$
$(\psi_R^{\mathbf{Q}^m})^c$	$m = 1, \dots, N_Q$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_Q^m$	$\tilde{q}_Q^m$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$

Anomalies contributions = Triangular Feynman diagrams

# Exploration of potential models

**STEP 1: Reduce number of parameters**

## Constraints from SM fermions masses

### SM Yukawa couplings

$$\bar{\mathbf{Q}}_L^i H d_R^j \rightarrow -z_{\mathbf{Q}}^i - z_d^j + z_H = 0,$$

$$\bar{\mathbf{Q}}_L^i \tilde{H} u_R^j \rightarrow -z_{\mathbf{Q}}^i - z_{u_R}^j - z_H = 0,$$

$$\bar{\mathbf{L}}^i H e_R^j \rightarrow -z_{\mathbf{L}}^i - z_{e_R}^j + z_H = 0.$$

### Dirac neutrino mass

$$\bar{\mathbf{L}}^i \tilde{H} \nu_R^j \rightarrow -z_{\mathbf{L}}^i - z_{\nu_R}^j - z_H = 0,$$

### Majorana neutrino mass

$$\bar{\nu}_R^{c,i} \nu_R^j \frac{\tilde{S}^n}{\Lambda^{n-1}} \rightarrow z_{\nu_R}^i + z_{\nu_R}^j - (\varepsilon_{\nu}^{ij})^n n q_S = 0,$$

$$\varepsilon_{\nu}^{ij} = \pm 1 \text{ depending if we use } S \text{ or } S^*$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_{\nu}^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\widetilde{q_{\mathbf{L}}^i}$
$\psi_L^{ej}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{ej})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\widetilde{q_e^j}$
$\psi_L^{dk}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{dk})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\widetilde{q_d^k}$
$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\widetilde{q_{\mathbf{Q}}^m}$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$



## Constraints from the extra fermions Yukawa's

### Secluded sector Yukawa couplings

$$\begin{aligned}
 \bar{\psi}_L^{\mathbf{L}^i} \psi_R^{\mathbf{L}^i} \hat{S} &\rightarrow -q_{\mathbf{L}}^i - \widetilde{q}_{\mathbf{L}}^i + \varepsilon_{\mathbf{L}}^i q_S = 0 \\
 \bar{\psi}_L^{e_j} \psi_R^{e_j} \hat{S} &\rightarrow -q_e^j - \widetilde{q}_e^j + \varepsilon_e^j q_S = 0 \\
 \bar{\psi}_L^{d_k} \psi_R^{d_k} \hat{S} &\rightarrow -q_d^k - \widetilde{q}_d^k + \varepsilon_d^k q_S = 0 \\
 \bar{\psi}_L^{\mathbf{Q}^m} \psi_R^{\mathbf{Q}^m} \hat{S} &\rightarrow -q_{\mathbf{Q}}^m - \widetilde{q}_{\mathbf{Q}}^m + \varepsilon_{\mathbf{Q}}^m q_S = 0
 \end{aligned}$$

$\hat{S}$  denotes either  $S$  or  $S^*$

$$\varepsilon_{\mathbf{L}}^i, \varepsilon_e^j, \varepsilon_d^k, \varepsilon_{\mathbf{Q}}^m = \pm 1$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_\nu^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}^i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}^i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\widetilde{q}_{\mathbf{L}}^i$
$\psi_L^{e_j}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{e_j})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\widetilde{q}_e^j$
$\psi_L^{d_k}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{d_k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\widetilde{q}_d^k$
$\psi_L^{\mathbf{Q}^m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}^m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\widetilde{q}_{\mathbf{Q}}^m$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$

## Anomaly equations from SM fermions

### Cancellation of the anomalies contributions

$$\begin{aligned}
 Tr[q_A]_{SM} &= \sum_f [6z_{\mathbf{Q}}^f + 3z_u^f + 3z_d^f + 2z_{\mathbf{L}}^f + z_e^f + z_\nu^f] &&= t_A, \\
 Tr[YYq_A]_{SM} &= \sum_f [6(y_{\mathbf{Q}}^f)^2 z_{\mathbf{Q}}^f + 3(y_u^f)^2 z_u^f + 3(y_d^f)^2 z_d^f + 2(y_{\mathbf{L}}^f)^2 z_{\mathbf{L}}^f + (y_e^f)^2 z_e^f] &&= t_{YYA}, \\
 Tr[Yq_Aq_A]_{SM} &= \sum_f [6y_{\mathbf{Q}}^f (z_{\mathbf{Q}}^f)^2 + 3y_u^f (z_u^f)^2 + 3y_d^f (z_d^f)^2 + 2y_{\mathbf{L}}^f (z_{\mathbf{L}}^f)^2 + y_e^f (z_e^f)^2] &&= t_{YAA}, \\
 Tr[q_Aq_Aq_A]_{SM} &= \sum_f [6(z_{\mathbf{Q}}^f)^3 + 3(z_u^f)^3 + 3(z_d^f)^3 + 2(z_{\mathbf{L}}^f)^3 + (z_e^f)^3 + (z_\nu^f)^3] &&= t_{AAA}, \\
 Tr[q_AT_2T_2]_{SM} &= \sum_f [3z_{\mathbf{Q}}^f + z_{\mathbf{L}}^f] &&= t_2, \\
 Tr[q_AT_3T_3]_{SM} &= \sum_f [2z_{\mathbf{Q}}^f + z_u^f + z_d^f] &&= t_3,
 \end{aligned}$$

### Impose relations from Yukawa coupling constraints:

$$\begin{aligned}
 Tr[q_A]_{SM} &= \sum_f [2z_{\mathbf{L}}^f + z_e^f + z_\nu^f] &&= t_A \\
 Tr[YYq_A]_{SM} &= -\frac{1}{2} \sum_f [3z_{\mathbf{Q}}^f + z_{\mathbf{L}}^f] &&= t_{YYA} \\
 Tr[Yq_Aq_A]_{SM} &= -2 \sum_f [3z_{\mathbf{Q}}^f + z_{\mathbf{L}}^f] z_H &&= t_{YAA} \\
 Tr[q_Aq_Aq_A]_{SM} &= \sum_f [z_H^3 + 3z_H (z_{\mathbf{L}}^f)^2 + (z_{\mathbf{L}}^f)^3 - 3z_H^2 z_{\mathbf{L}}^f - 18z_H^2 z_{\mathbf{Q}}^f + (z_\nu^f)^3] &&= t_{AAA} \\
 Tr[q_AT_2T_2]_{SM} &= \sum_f [3z_{\mathbf{Q}}^f + z_{\mathbf{L}}^f] &&= t_2 \\
 Tr[q_AT_3T_3]_{SM} &= 0 &&= t_3
 \end{aligned}$$

$$t_{YYA} = -\frac{1}{2}t_2, \quad t_{YAA} = -2z_H t_2, \quad t_3 = 0. \quad t_A = 0, \quad t_{AAA} = -6z_H^2 t_2$$

(neutrino Dirac mass constraints)

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_\nu^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\widetilde{q}_{\mathbf{L}}^i$
$\psi_L^{e_j}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{e_j})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\widetilde{q}_e^j$
$\psi_L^{d_k}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{d_k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\widetilde{q}_d^k$
$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\widetilde{q}_{\mathbf{Q}}^m$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$

# Universality hypothesis

Assume universality with respect to both U(1)'s

$$\forall i = 1, \dots, N_L$$

$$\varepsilon_L^i = \varepsilon_L$$

$$y_L^i = y_L$$

$$q_L^i = q_L$$

$$\widetilde{q}_L^i = \widetilde{q}_L$$

$$\forall j = 1, \dots, N_e$$

$$\varepsilon_e^j = \varepsilon_e$$

$$y_e^j = y_e$$

$$q_e^j = q_e$$

$$\widetilde{q}_e^j = \widetilde{q}_e$$

$$\forall k = 1, \dots, N_d$$

$$\varepsilon_d^k = \varepsilon_d$$

$$y_d^k = y_d$$

$$q_d^k = q_d$$

$$\widetilde{q}_d^k = \widetilde{q}_d$$

$$\forall m = 1, \dots, N_Q$$

$$\varepsilon_Q^m = \varepsilon_Q$$

$$y_Q^m = y_Q$$

$$q_Q^m = q_Q$$

$$\widetilde{q}_Q^m = \widetilde{q}_Q$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$Q_L^f$	$f = 1, 2, 3$	<b>3</b>	<b>2</b>	1/6	$z_Q^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	<b>1</b>	-2/3	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	<b>1</b>	1/3	$z_d^f$
$L_L^f$		<b>1</b>	<b>2</b>	-1/2	$z_L^f$
$e_R^{c,f}$		<b>1</b>	<b>1</b>	1	$z_e^f$
$\nu_R^{c,f}$		<b>1</b>	<b>1</b>	0	$z_\nu^f$
$H$		<b>1</b>	<b>2</b>	1/2	$z_H$
$\psi_L^{\mathbf{L}i}$		<b>1</b>	<b>2</b>	$y_L^i$	$q_L^i$
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_L$	<b>1</b>	<b>2</b>	$-y_L^i$	$\widetilde{q}_L^i$
$\psi_L^{e_j}$		<b>1</b>	<b>1</b>	$y_e^j$	$q_e^j$
$(\psi_R^{e_j})^c$	$j = 1, \dots, N_e$	<b>1</b>	<b>1</b>	$-y_e^j$	$\widetilde{q}_e^j$
$\psi_L^{d_k}$		<b>3</b>	<b>1</b>	$y_d^k$	$q_d^k$
$(\psi_R^{d_k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	<b>1</b>	$-y_d^k$	$\widetilde{q}_d^k$
$\psi_L^{\mathbf{Q}m}$		<b>3</b>	<b>2</b>	$y_Q^m$	$q_Q^m$
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_Q$	$\bar{\mathbf{3}}$	<b>2</b>	$-y_Q^m$	$\widetilde{q}_Q^m$
$S$		<b>1</b>	<b>1</b>	0	$q_S$

## Anomalies from the extra fermions

### Cancellation of the anomalies contributions

$$\begin{aligned}
 Tr[q_A]_{secluded} &= \left(2\varepsilon_{\mathbf{L}}N_{\mathbf{L}} + \varepsilon_e N_e + 3\varepsilon_d N_d + 6\varepsilon_{\mathbf{Q}}N_{\mathbf{Q}}\right)q_S = -t_A, \\
 Tr[YYq_A]_{secluded} &= \left(2\varepsilon_{\mathbf{L}}y_{\mathbf{L}}^2 N_{\mathbf{L}} + \varepsilon_e y_e^2 N_e \right. \\
 &\quad \left. + 3\varepsilon_d y_d^2 N_d + 6\varepsilon_{\mathbf{Q}}y_{\mathbf{Q}}^2 N_{\mathbf{Q}}\right)q_S = -t_{YYA}, \\
 Tr[Yq_Aq_A]_{secluded} &= -q_S^2 \left(2y_{\mathbf{L}}N_{\mathbf{L}} + y_e N_e + 3y_d N_d + 6y_{\mathbf{Q}}N_{\mathbf{Q}}\right) \\
 &\quad + 2q_S \left(2\varepsilon_{\mathbf{L}}y_{\mathbf{L}}q_{\mathbf{L}}N_{\mathbf{L}} + \varepsilon_e y_e q_e N_e \right. \\
 &\quad \left. + 3\varepsilon_d y_d q_d N_d + 6\varepsilon_{\mathbf{Q}}y_{\mathbf{Q}}q_{\mathbf{Q}}N_{\mathbf{Q}}\right) = -t_{YAA}, \\
 Tr[q_Aq_Aq_A]_{secluded} &= q_S^3 \left(2\varepsilon_{\mathbf{L}}N_{\mathbf{L}} + \varepsilon_e N_e + 3\varepsilon_d N_d + 6\varepsilon_{\mathbf{Q}}N_{\mathbf{Q}}\right) \\
 &\quad - 3q_S^2 \left(2q_{\mathbf{L}}N_{\mathbf{L}} + q_e N_e + 3q_d N_d + 6q_{\mathbf{Q}}N_{\mathbf{Q}}\right) \\
 &\quad + 3q_S \left(2\varepsilon_{\mathbf{L}}q_{\mathbf{L}}^2 N_{\mathbf{L}} + \varepsilon_e q_e^2 N_e \right. \\
 &\quad \left. + 3\varepsilon_d q_d^2 N_d + 6\varepsilon_{\mathbf{Q}}q_{\mathbf{Q}}^2 N_{\mathbf{Q}}\right) = -t_{AAA}, \\
 Tr[q_A T_2 T_2]_{secluded} &= (\varepsilon_{\mathbf{L}}N_{\mathbf{L}} + 3\varepsilon_{\mathbf{Q}}N_{\mathbf{Q}})q_S = -t_2, \\
 Tr[q_A T_3 T_3]_{secluded} &= (\varepsilon_d N_d + 2\varepsilon_{\mathbf{Q}}N_{\mathbf{Q}})q_S = -t_3.
 \end{aligned}$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_\nu^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\widetilde{q_{\mathbf{L}}^i}$
$\psi_L^{e_j}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{e_j})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\widetilde{q_e^j}$
$\psi_L^{d_k}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{d_k})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\widetilde{q_d^k}$
$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\widetilde{q_{\mathbf{Q}}^m}$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$

# Exploration of potential models

**STEP 2: Solve the anomaly equations**

## Solving in the case where all $N$ 's are non zero

12 parameters:  $y_{\mathbf{L}}, y_e, y_{\mathbf{Q}}, y_d, q_{\mathbf{L}}, q_e, q_{\mathbf{Q}}, q_d, q_S, z_H, N_{\mathbf{L}}$  and  $N_{\mathbf{Q}}$

We demand:

- All charges are rational numbers.
- The lepton-like extra fermions  $\psi^{\mathbf{L}}$  have electric charges 0 or  $\pm 1$ , and  $\psi^e$  electric charge  $\pm 1$ .
- The quark-like extra fermions  $\psi^{\mathbf{Q}}$  and  $\psi^d$  have electric charges  $\pm 1/3$  or  $\pm 2/3$ . Indeed, this condition ensures that when the color forces confine, the resulting bound states can all carry integer charges.
- We will consider  $\varepsilon_{\mathbf{L}} = 1, \varepsilon_e = -1, \varepsilon_d = 1$  and  $\varepsilon_{\mathbf{Q}} = -1$

We get:

$$y_{\mathbf{L}} = \pm \frac{1}{2}, \quad y_{\mathbf{Q}} = \pm \frac{1}{6}, \quad y_d = \pm \frac{2}{3}, \quad y_e = \pm 1, \quad N_{\mathbf{L}} = N_{\mathbf{Q}}.$$

		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$z_{\mathbf{Q}}^f$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$z_u^f$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$z_d^f$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$z_{\mathbf{L}}^f$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$z_e^f$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$z_{\nu}^f$
$H$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$z_H$
$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	$y_{\mathbf{L}}^i$	$q_{\mathbf{L}}^i$
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$-y_{\mathbf{L}}^i$	$\tilde{q}_{\mathbf{L}}^i$
$\psi_L^{ej}$		$\mathbf{1}$	$\mathbf{1}$	$y_e^j$	$q_e^j$
$(\psi_R^{ej})^c$	$j = 1, \dots, N_e$	$\mathbf{1}$	$\mathbf{1}$	$-y_e^j$	$\tilde{q}_e^j$
$\psi_L^{dk}$		$\mathbf{3}$	$\mathbf{1}$	$y_d^k$	$q_d^k$
$(\psi_R^{dk})^c$	$k = 1, \dots, N_d$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$-y_d^k$	$\tilde{q}_d^k$
$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	$y_{\mathbf{Q}}^m$	$q_{\mathbf{Q}}^m$
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{Q}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-y_{\mathbf{Q}}^m$	$\tilde{q}_{\mathbf{Q}}^m$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$q_S$

				Model <i>a</i>		Model <i>b</i>		Model <i>c</i>	
		<i>SU</i> (3)	<i>SU</i> (2)	<i>U</i> (1) <sub><i>Y</i></sub>	<i>U</i> (1) <sub><i>A</i></sub>	<i>U</i> (1) <sub><i>Y</i></sub>	<i>U</i> (1) <sub><i>A</i></sub>	<i>U</i> (1) <sub><i>Y</i></sub>	<i>U</i> (1) <sub><i>A</i></sub>
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	1/6	1/3	1/6	2/3	1/6	1/3
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	-2/3	-10/3	-2/3	-8/3	-2/3	-4/3
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	1/3	8/3	1/3	4/3	1/3	2/3
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	-1/2	1	-1/2	2	-1/2	1
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	1	2	1	0	1	0
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	0	-4	0	-4	0	-2
$H$		$\mathbf{1}$	$\mathbf{2}$	1/2	3	1/2	2	1/2	1
$\psi_L^{\mathbf{L}i}$		$\mathbf{1}$	$\mathbf{2}$	-1/2	-3	-1/2	-3	-1/2	-1
$(\psi_R^{\mathbf{L}i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	+1/2	6	+1/2	5	+1/2	2
$\psi_L^{e_j}$		$\mathbf{1}$	$\mathbf{1}$	-1	-3	+1	-3	-1	-1
$(\psi_R^{e_j})^c$	$j = 1, \dots, 2N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{1}$	+1	0	-1	1	+1	0
$\psi_L^{d_k}$		$\mathbf{3}$	$\mathbf{1}$	-2/3	0	2/3	1/3	-2/3	0
$(\psi_R^{d_k})^c$	$k = 1, \dots, 2N_{\mathbf{L}}$	$\bar{\mathbf{3}}$	$\mathbf{1}$	+2/3	3	-2/3	5/3	2/3	1
$\psi_L^{\mathbf{Q}m}$		$\mathbf{3}$	$\mathbf{2}$	+1/6	0	+1/6	1/3	+1/6	0
$(\psi_R^{\mathbf{Q}m})^c$	$m = 1, \dots, N_{\mathbf{L}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	-1/6	-3	-1/6	-7/3	-1/6	-1
$S$		$\mathbf{1}$	$\mathbf{1}$	0	3	0	2	0	1
$t_2$				6		12		6	
$t_{YYA}$				-3		-6		-3	
$t_{YAA}$				-36		-48		-12	
$t_{AAA}$				-324		-288		-36	

**Table 3.** Examples of anomaly-free solutions, with all  $N_{iS} \neq 0$ . Model *a*: Anomaly-free solution with  $q_{\mathbf{L}} = q_e, q_d = q_{\mathbf{Q}}$ , and  $N_{\mathbf{L}} = 1, z_L = 1$ . Model *b*: Anomaly-free solution with  $q_{\mathbf{L}} = q_e, q_d = q_{\mathbf{Q}}$ , and  $N_{\mathbf{L}} = 3, z_L = 2$ . Model *c*: Anomaly-free solution with  $q_{\mathbf{L}} = q_e, q_d = q_{\mathbf{Q}}$ , and  $N_{\mathbf{L}} = 3, z_L = 1$ .

# Energy domain of validity

**I: The UV cut-off of the EFT**



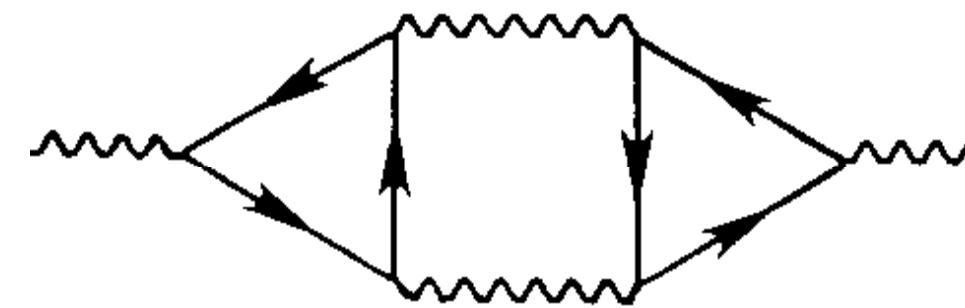
## The EFT UV Cutoff: Preskill bound

The vector boson  $Z'$  obtains its mass  $M_A$  as the sum of two distinct contributions:

$$M_A^{(0)} = g_A |q_S| v_S \qquad M_A^{(1)} \simeq \left| \frac{[g_A^3 t_{AAA}^{(light)} + 2g_A^2 g_Y t_{YAA}^{(light)} + g_A g_Y^2 t_{AYY}^{(light)} + g_A g_2^2 t_2^{(light)} + g_A g_3^2 t_3^{(light)}] \Lambda_{eff}}{64\pi^3} \right|$$

Tree-level Higgs contribution

One-loop radiative contribution



We assume knowledge of the mass  $M_A$  and the coupling constant  $g_A$  of the  $U(1)_A$  gauge boson, denoted as  $Z'$ , either through theoretical calculations or experimental measurements.

We want to infer the value of the cut-off energy from this information

## *The EFT UV Cutoff: Preskill bound*

Often quoted is the Preskill cutoff


$$\Lambda_{eff} \sim \left| \frac{64\pi^3 M_A}{[g_A^3 t_{AAA}^{(light)} + 2g_A^2 g_Y t_{YAA}^{(light)} + g_A g_Y^2 t_{AYY}^{(light)} + g_A g_2^2 t_2^{(light)} + g_A g_3^2 t_3^{(light)}]} \right|$$

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More precisely, the Preskill bound is

$$\Lambda_{eff} \lesssim \left| \frac{64\pi^3 M_A}{[g_A^3 t_{AAA}^{(light)} + 2g_A^2 g_Y t_{YAA}^{(light)} + g_A g_Y^2 t_{AYY}^{(light)} + g_A g_2^2 t_2^{(light)} + g_A g_3^2 t_3^{(light)}]} \right|$$


## *The EFT UV Cutoff*

The effective theory cut-off scale  $\Lambda_{eff}$  will be approximately equal to the mass scale of the heavy fermions, i.e.,

$$\Lambda_{eff} \simeq M_f$$

the heavy secluded fermion mass originates from the Yukawa coupling

$$M_f \simeq Y_{ij} v_S \simeq v_S$$

## *The EFT UV Cutoff: Preskill's bound domain of validity*

The ratio of the loop-induced mass with respect of the tree-level one is now of order:

$$\frac{M_A^{(1)}}{M_A^{(0)}} \simeq \frac{g_A^2 |t_{AAA}^{(h)}|}{64\pi^3 q_S} \xrightarrow{\text{all extra fermions heavy}} \frac{M_A^{(1)}}{M_A^{(0)}} \simeq \frac{3g_A^2 z_H^2 N_{\mathbf{L}}}{16\pi^3}$$

Indeed, the dominance of the anomaly loop-induced mass for the  $Z'_A$  requires that  $g_A z_H^2 N_{\mathbf{Q}} \sim 10^3$ . To achieve a light  $Z'_A$  with a mass  $M_A \ll M_f$ , it necessitates a coupling  $g_A \ll 1$ . This, in turn, implies significantly large charges and/or a large number of fields  $N_{\mathbf{Q}}$ , especially if we assume  $q_S = 1$ .

## *The EFT UV Cutoff*

One potential resolution to this issue is that only some of the fermions are heavy enough

fermions  $\psi_L^{\mathbf{L}i}$  with large charges  $q_{\mathbf{L}} \gg q_S$  are heavy and inaccessible.

$$\frac{M_A^{(1)}}{M_A^{(0)}} \simeq \frac{g_A^2 |t_{AAA}^{(h)}|}{64\pi^3 q_S} \xrightarrow{N_{\mathbf{L}} \psi_L^{\mathbf{L}} \text{ heavy}} \frac{M_A^{(1)}}{M_A^{(0)}} \simeq \frac{3g_A^2 q_{\mathbf{L}}^2 N_{\mathbf{L}}}{32\pi^3}$$

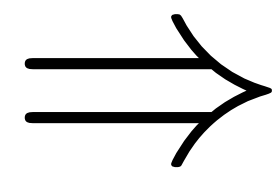
$g_A^2 q_{\mathbf{L}}^2 N_{\mathbf{L}}$  that needs to be of order  $\sim 10^3$ .

## *The EFT UV Cutoff*

$$\Lambda_{eff} \simeq M_f$$

$$M_f \simeq Y_{ij} v_S \simeq v_S$$

$$M_A^{(0)} = g_A |q_S| v_S$$



$$\Lambda_{eff} \simeq \frac{M_A}{g_A q_S} \quad (q_S > 0)$$

In the case where  $g_A$  is hierarchically the smallest coupling in the theory, the magnetic Swampland Conjecture can be used to put a bound as:

$$\Lambda_{eff} \lesssim \Lambda_{QG} \simeq g_A M_P \Rightarrow M_A \lesssim g_A^2 M_P$$

# Energy domain of validity

**II: Above the new fermions scale: the UV model**



To make sense of our UV model description: a perturbative QFT, we request:  
A model which can be valid many orders of energy scales above the new fermions scale

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Mass of  $Z'$   $\ll$  Mass of new fermions

implies:

Coupling of  $Z'$   $\ll$  Yukawa coupling of new fermions

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But:

The coupling of  $Z'$  must not be too small so that we can detect the  $Z'$

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Yukawa couplings of new fermions are of  $O(1)$

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A model which can be valid many orders of energy scales above the new fermions scale  
and

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imply:

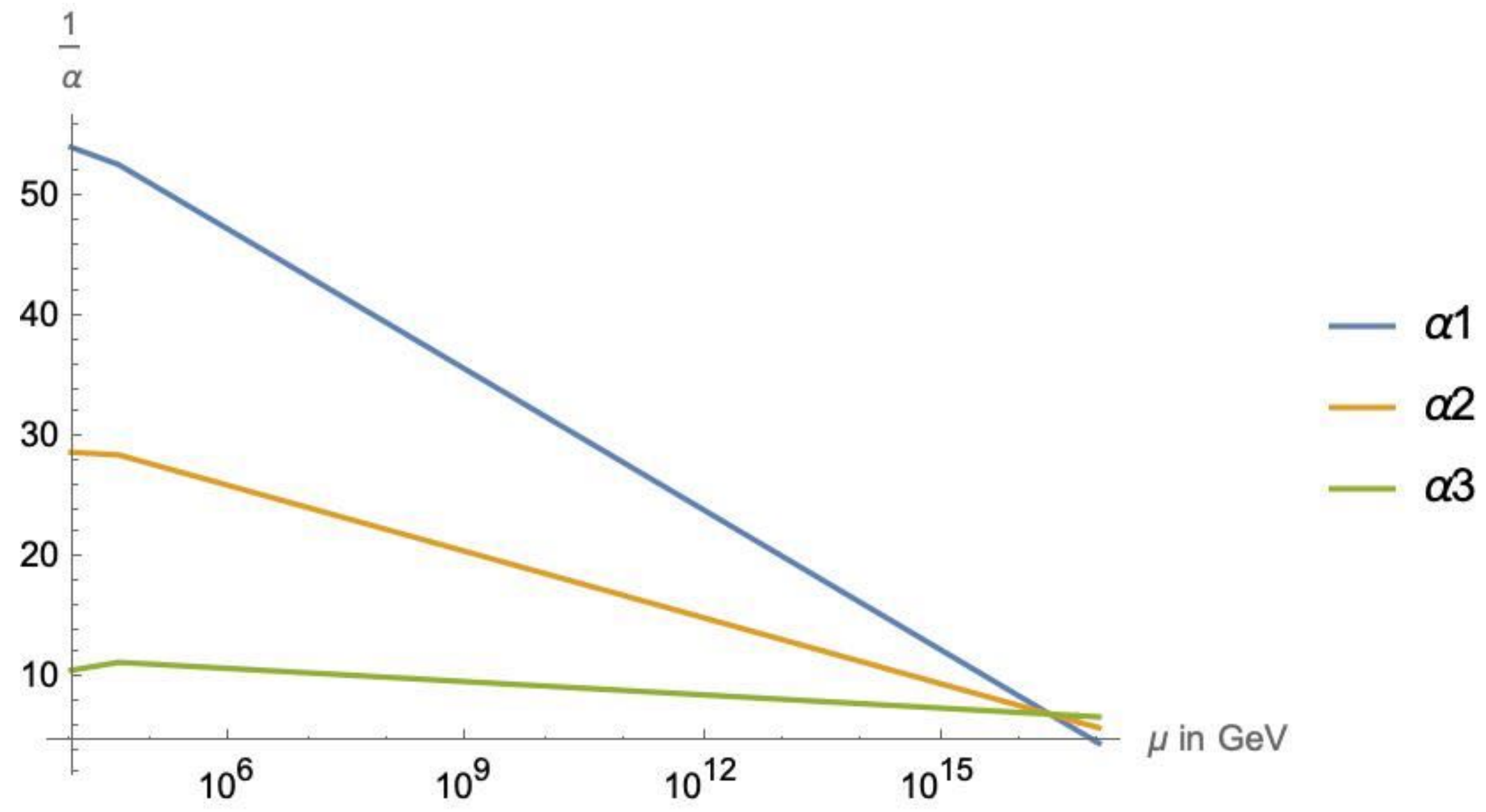
The RGE should make the Yukawa couplings not grow with increasing energy:

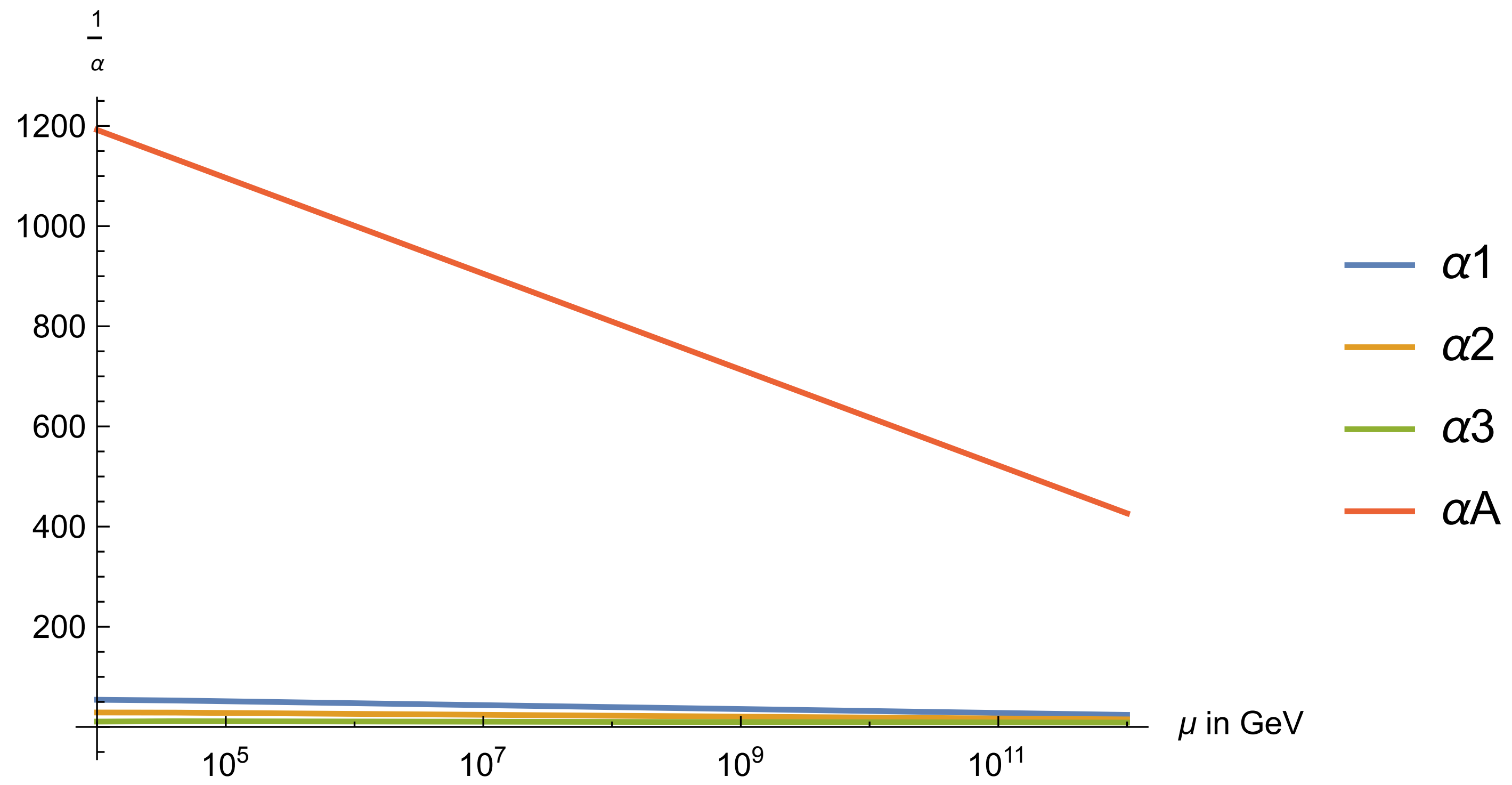
The contributions from gauge interactions to the RGE of the Yukawa couplings should dominate

## *A SUSY example*

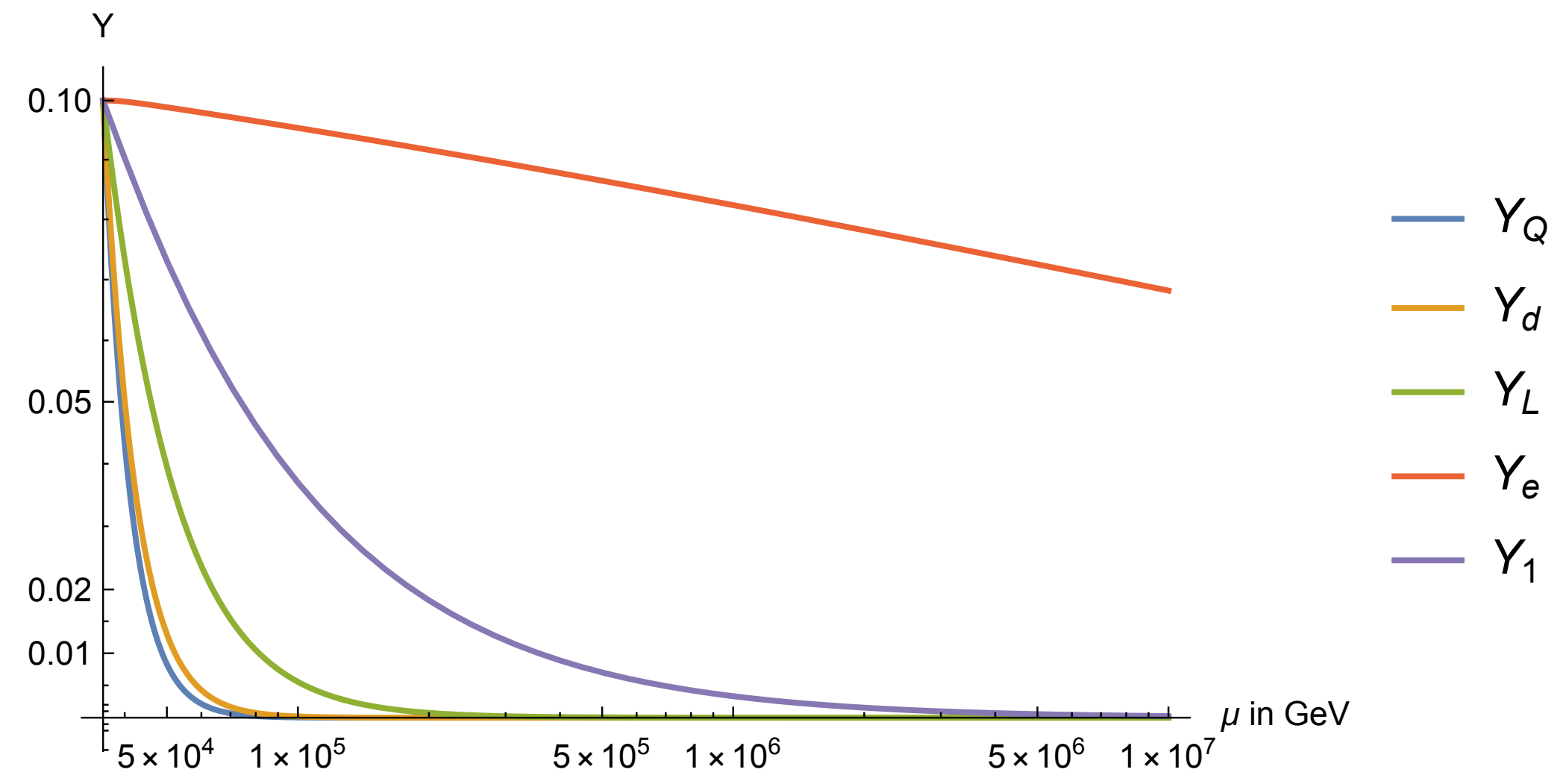
		$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_A$
$\mathbf{Q}_L^f$	$f = 1, 2, 3$	$\mathbf{3}$	$\mathbf{2}$	$1/6$	$-1/48$
$u_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$-2/3$	$97/48$
$d_R^{c,f}$		$\bar{\mathbf{3}}$	$\mathbf{1}$	$1/3$	$-95/48$
$\mathbf{L}_L^f$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$-1/48$
$e_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$1$	$-95/48$
$\nu_R^{c,f}$		$\mathbf{1}$	$\mathbf{1}$	$0$	$97/48$
$H_1$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$-2$
$H_2$		$\mathbf{1}$	$\mathbf{2}$	$1/2$	$2$
$\psi_L^{\mathbf{L}^i}$		$\mathbf{1}$	$\mathbf{2}$	$-1/2$	$35/8$
$(\psi_R^{\mathbf{L}^i})^c$	$i = 1, \dots, N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{2}$	$+1/2$	$9/2$
$\psi_L^e$		$\mathbf{1}$	$\mathbf{1}$	$+1$	$0$
$(\psi_R^e)^c$	$j = 1, \dots, 2N_{\mathbf{L}}$	$\mathbf{1}$	$\mathbf{1}$	$-1$	$0$
$\psi_L^d$		$\mathbf{3}$	$\mathbf{1}$	$-2/3$	$5/4$
$(\psi_R^d)^c$	$k = 1, \dots, 2N_{\mathbf{L}}$	$\bar{\mathbf{3}}$	$\mathbf{1}$	$+2/3$	$-9/8$
$\psi_L^{\mathbf{Q}^m}$		$\mathbf{3}$	$\mathbf{2}$	$+1/6$	$2$
$(\psi_R^{\mathbf{Q}^m})^c$	$m = 1, \dots, N_{\mathbf{L}}$	$\bar{\mathbf{3}}$	$\mathbf{2}$	$-1/6$	$-15/8$
$S$		$\mathbf{1}$	$\mathbf{1}$	$0$	$1/8$
$S'$		$\mathbf{1}$	$\mathbf{1}$	$0$	$-1/8$
$S_2$		$\mathbf{1}$	$\mathbf{1}$	$0$	$-3/2$
$S'_2$		$\mathbf{1}$	$\mathbf{1}$	$0$	$11/8$

SUSY, as a bonus, allows easily to unify the couplings









## *Conclusions*

In summary, we have build models whith an anomalous  $Z'$  in a range of energies and free of anomalies above a scale much below the Planck scale.

In a SUSY set-up, we can find models that allow to unify the couplings.

Work in progress ...

$$\begin{aligned}
 & \text{Diagram 1: A dark red circle vertex with three wavy lines. The left line is labeled } i, \mu \text{, the top-right line is } j, \nu \text{, and the bottom-right line is } k, \rho \text{.} \\
 & = \sum_f \text{Diagram 2: A fermion loop (orange triangle) with wavy lines } i, \mu \text{, } j, \nu \text{, and } k, \rho \text{ entering and exiting. The loop is labeled } \psi_f \text{.} \\
 & \quad \text{Diagram 3: A yellow circle vertex labeled } A \text{ with a coefficient } t_{ijk} \text{, and three wavy lines } i, \mu \text{, } j, \nu \text{, and } k, \rho \text{.} \\
 & \text{the anomalous coupling}
 \end{aligned}$$