

Dark Matter Freeze-out Beyond the WIMP Paradigm

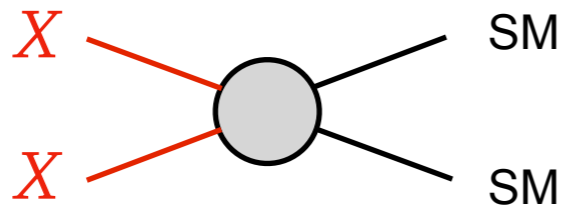
Jan Heisig



The Dark Side of the Universe - DSU2024
Corfu, September 8-14, 2024

Freeze-out of dark matter

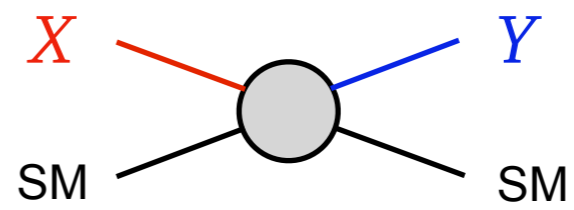
annihilation



WIMP

VS

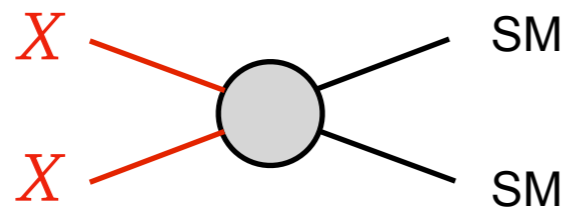
conversion



beyond WIMP

Freeze-out of dark matter

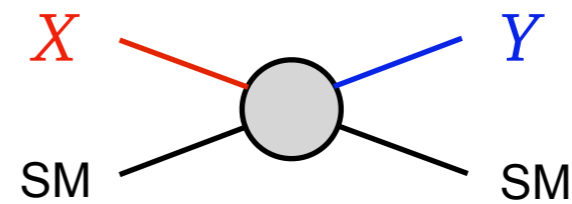
annihilation



WIMP

vs

conversion



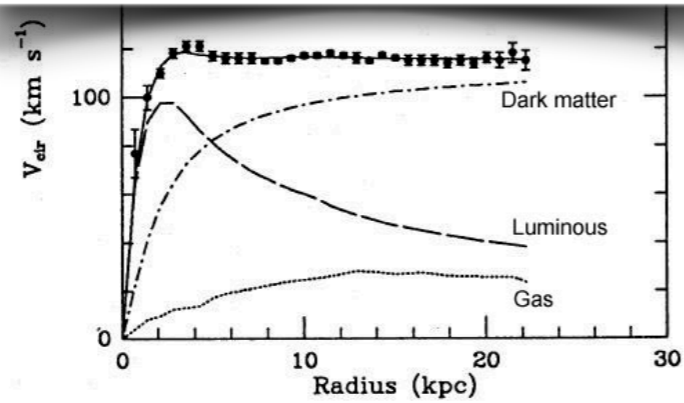
beyond WIMP

Outline

- Conversion-driven freeze-out
- How to search for it at LHC
- Intriguing link to baryogenesis

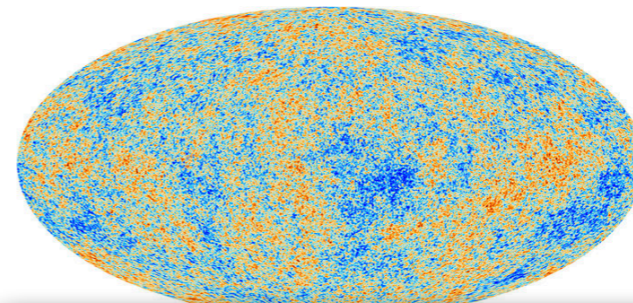
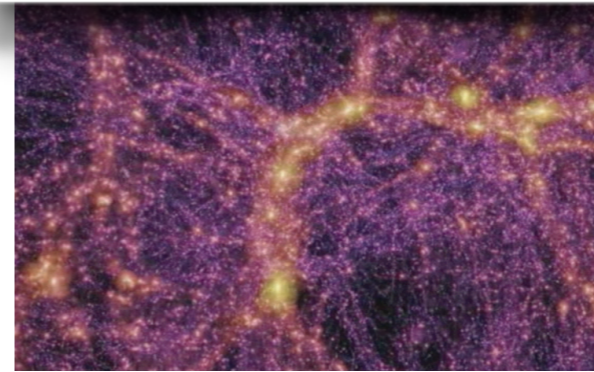
The phenomena of Dark Matter

Galaxy (cluster) dynamics



Gravitational lensing

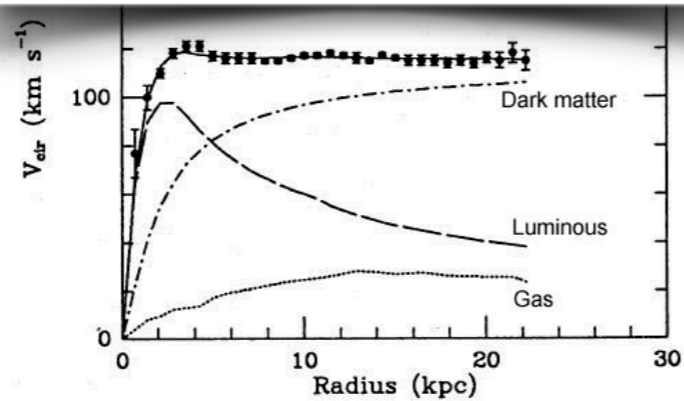
Structure formation



CMB anisotropies

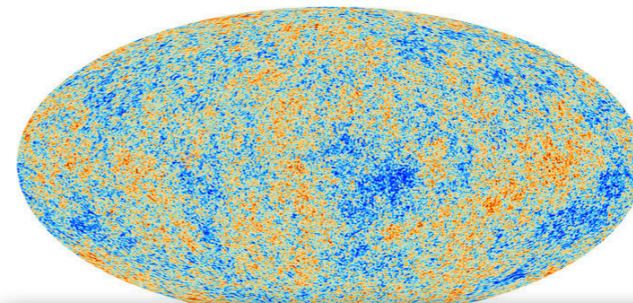
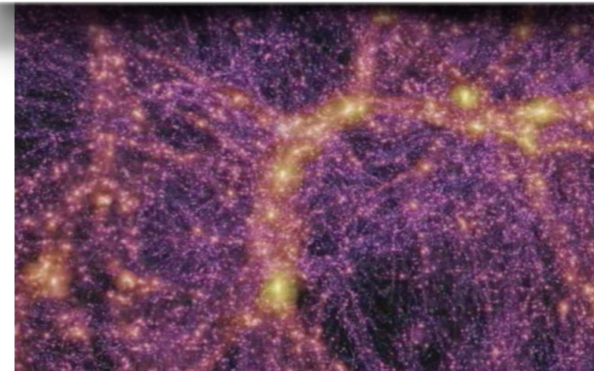
The phenomena of Dark Matter

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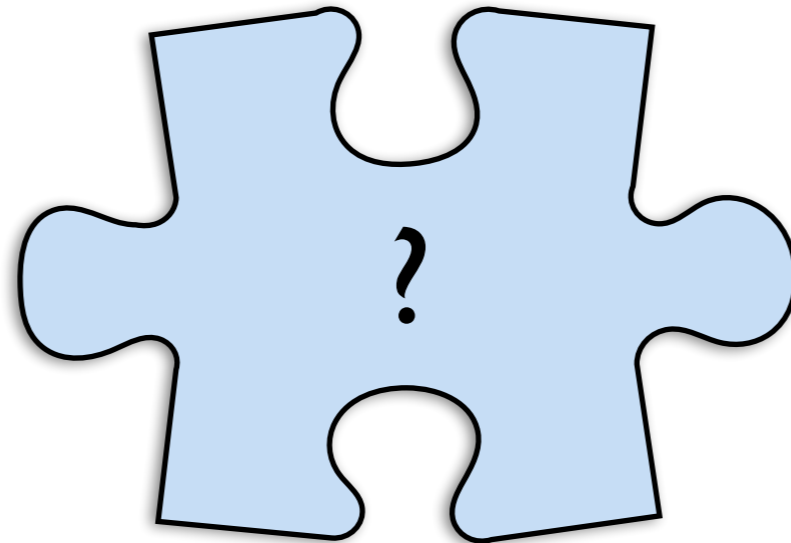


CMB anisotropies

[Planck 2020]

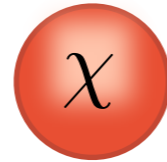
$\Omega_{\text{DM}} h^2 = 0.12 \pm 0.001$

The nature of Dark Matter



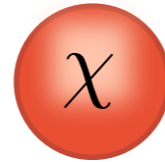
The nature of Dark Matter

New particle(s) beyond the SM

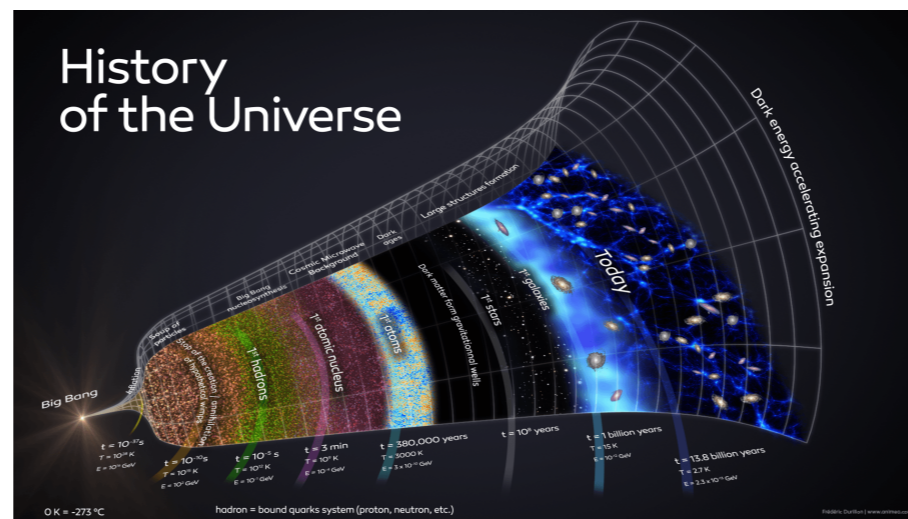


The nature of Dark Matter

New particle(s) beyond the SM

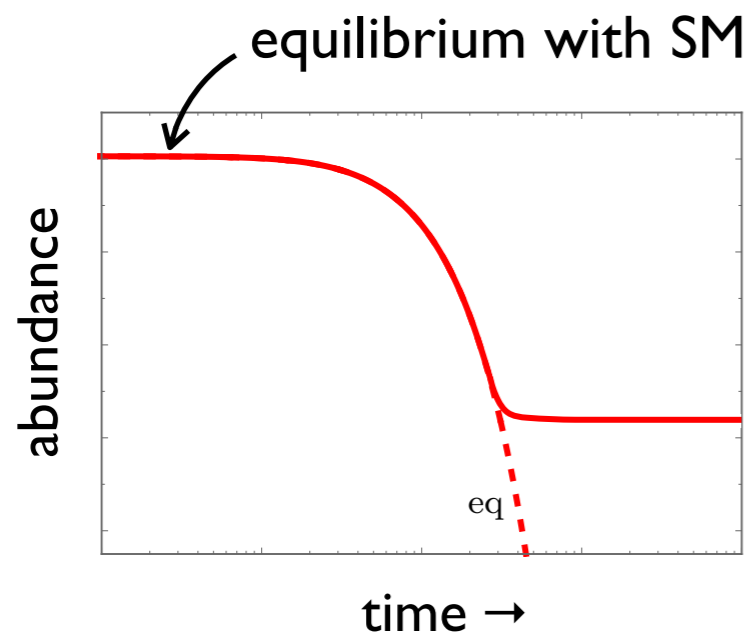
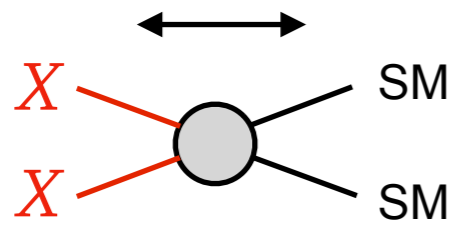


Thermal relic



Thermal relic dark matter

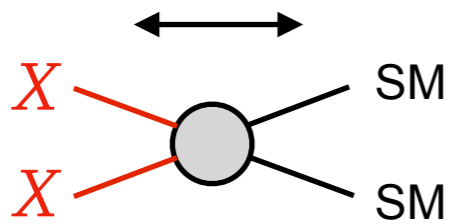
Thermalised



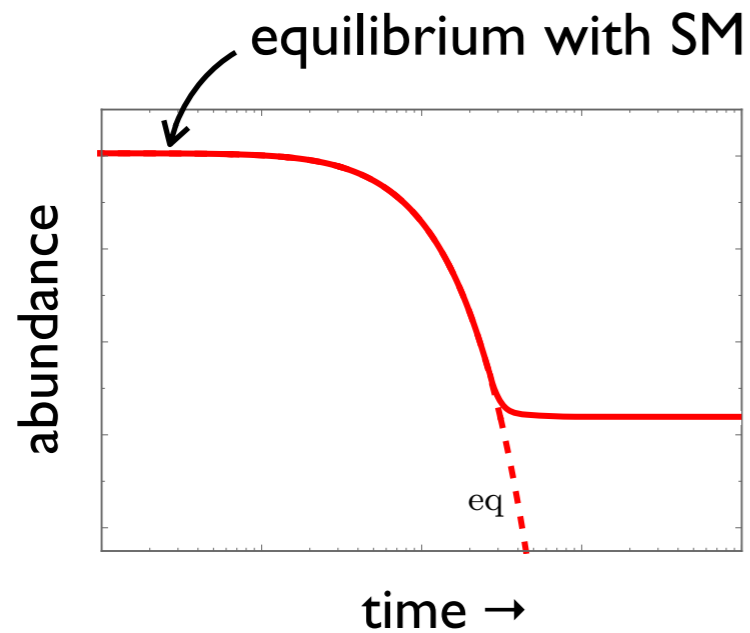
WIMP(-like)

Thermal relic dark matter

Thermalised



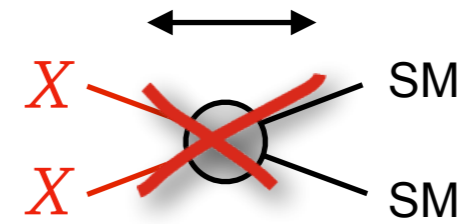
- Thermalization: predictive power
- Provides cold dark matter
- Testable (but facing null-results)



WIMP(-like)

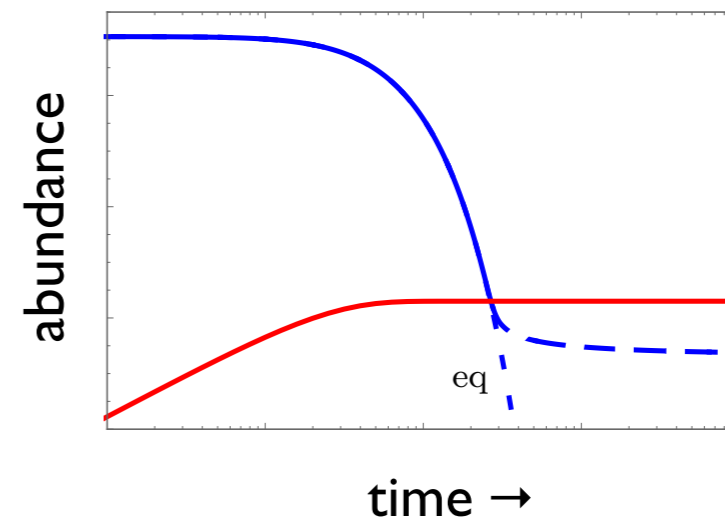
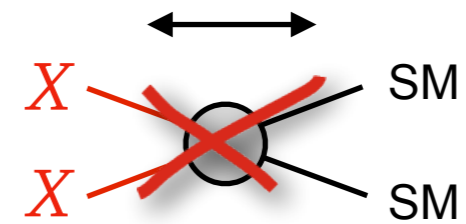
Thermal relic dark matter

Non-thermalised



Thermal relic dark matter

Non-thermalised

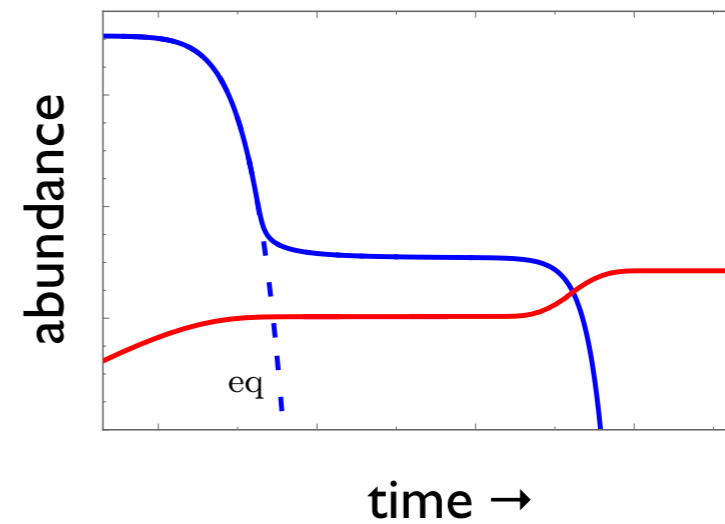
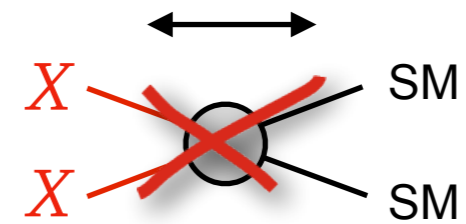


Freeze-in production

[McDonald 2002; Asaka *et al.* 2006; Hall *et al.* 2009]

Thermal relic dark matter

Non-thermalised



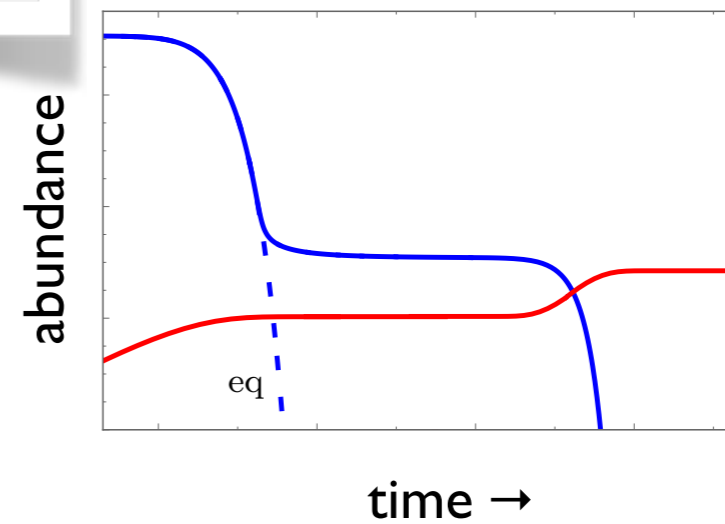
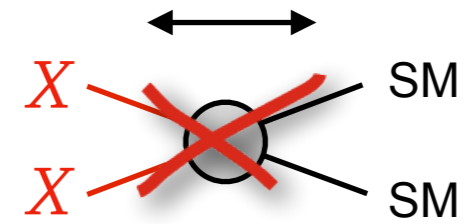
superWIMP production

[Covi *et al.* 1999; Feng *et al.* 2003]

Thermal relic dark matter

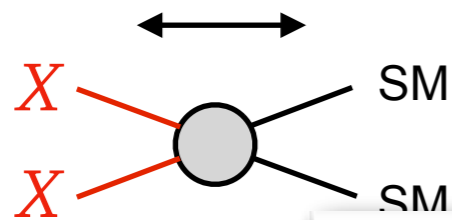
- Fine with null-results
- Depend on initial conditions
- Not necessarily cold dark matter
- Only partly testable

Non-thermalised

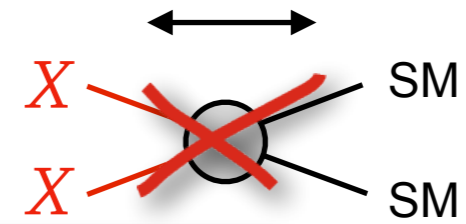


Thermal relic dark matter

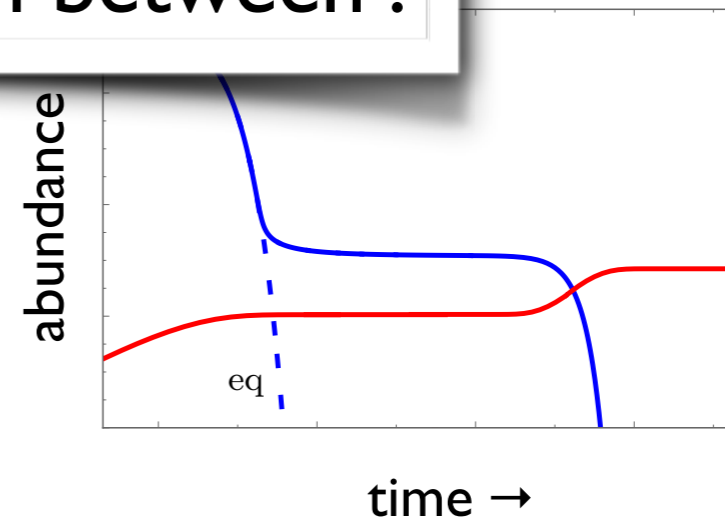
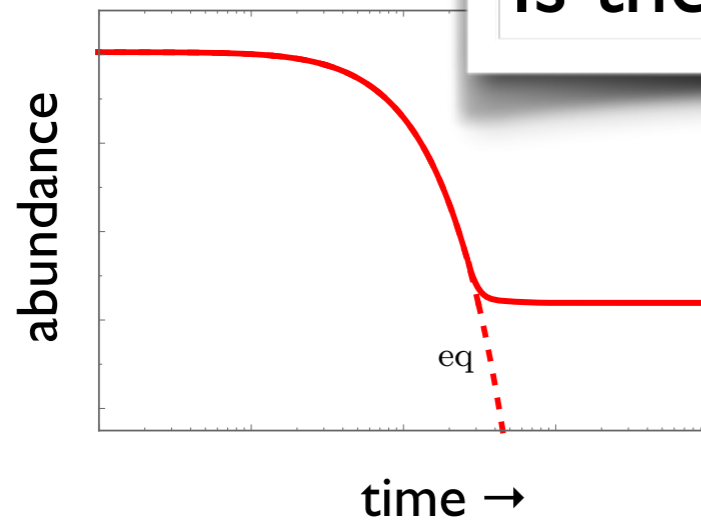
Thermalised



Non-thermalised



Is there something 'in between'?

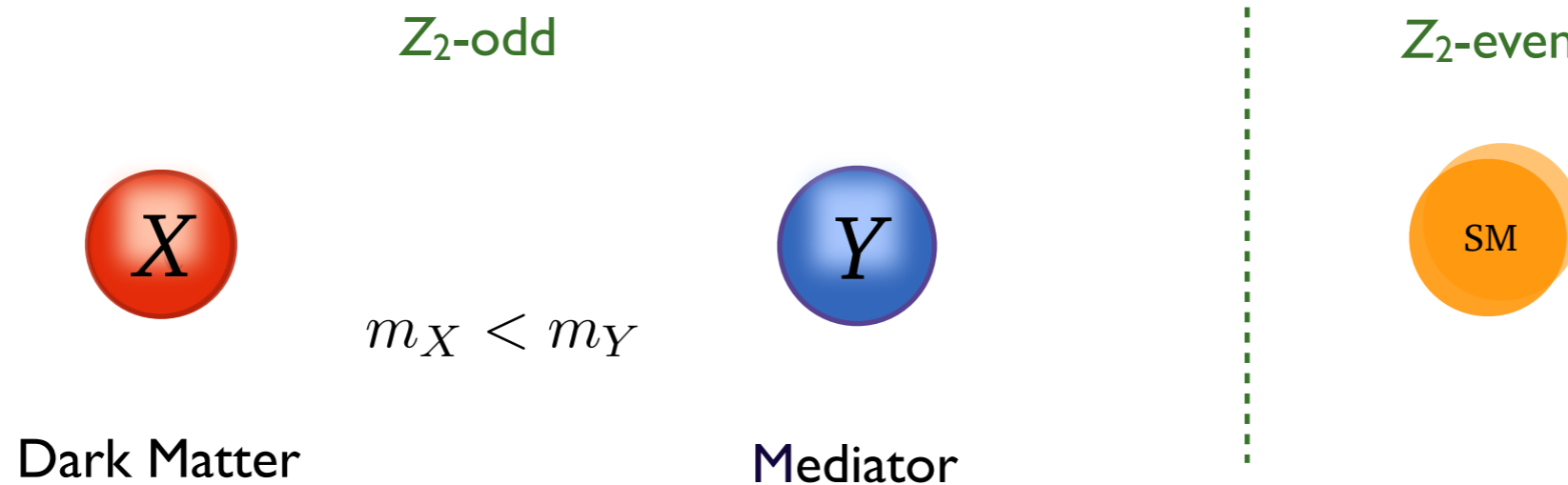


Conversion-driven freeze-out

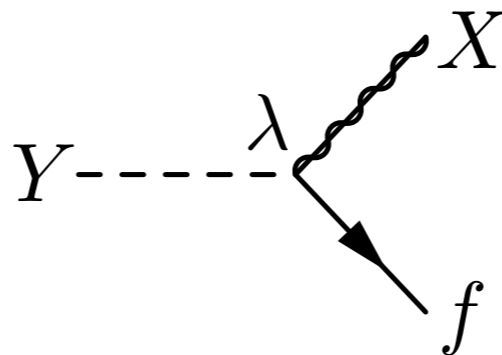
(aka co-scattering)

[Garny, JH, Lülz, Vogl 1705.09292; D'Agnolo, Pappadopulo, Ruderman 1705.08450]

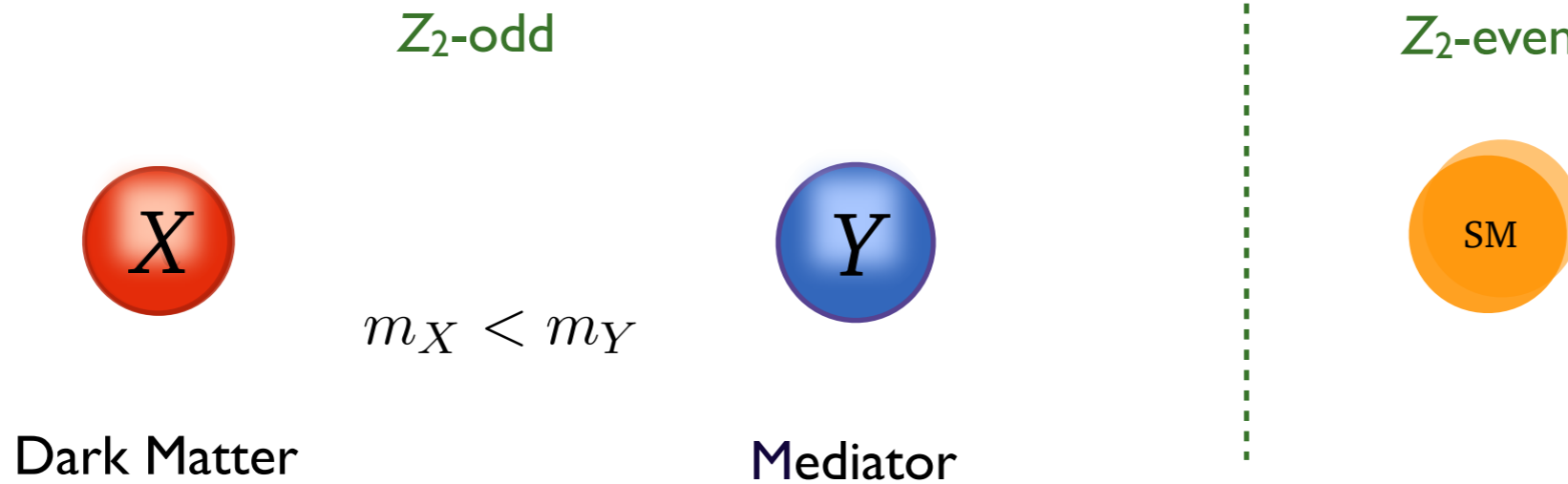
Minimal t -channel mediator model



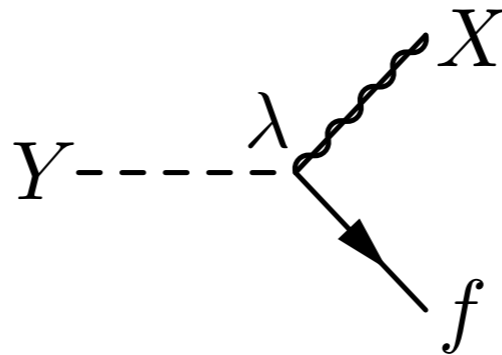
$$\mathcal{L} \supset \lambda Y \bar{f} X$$



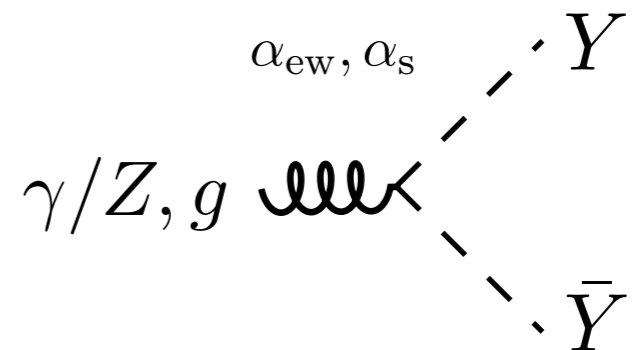
Minimal t -channel mediator model



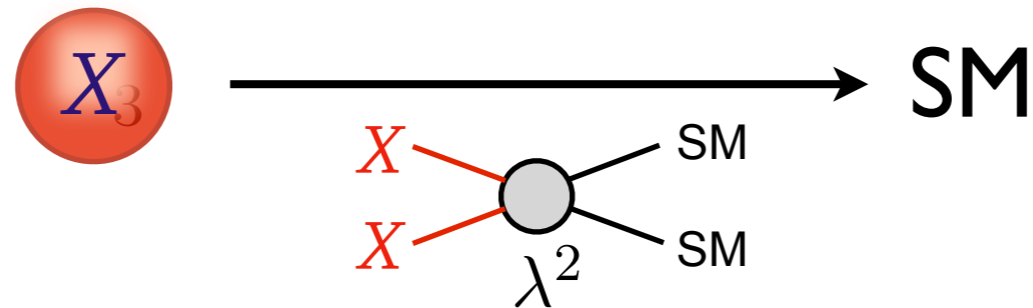
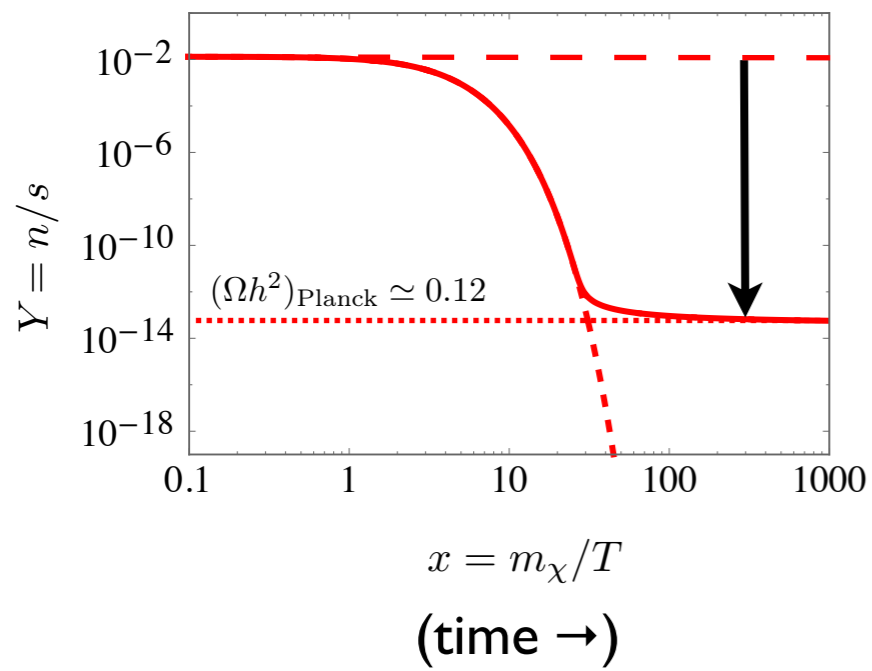
$$\mathcal{L} \supset \lambda Y \bar{f} X$$



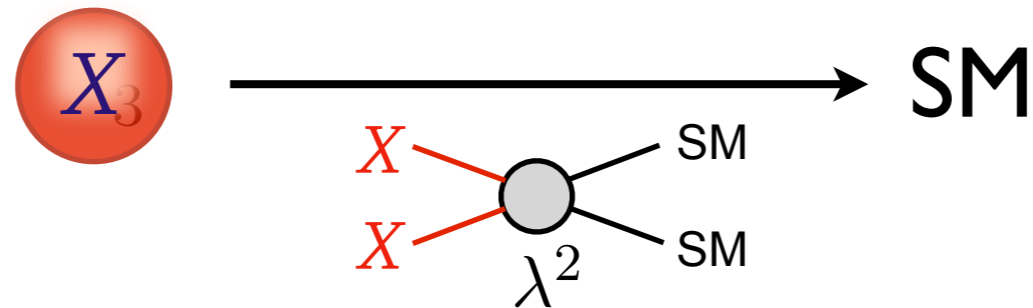
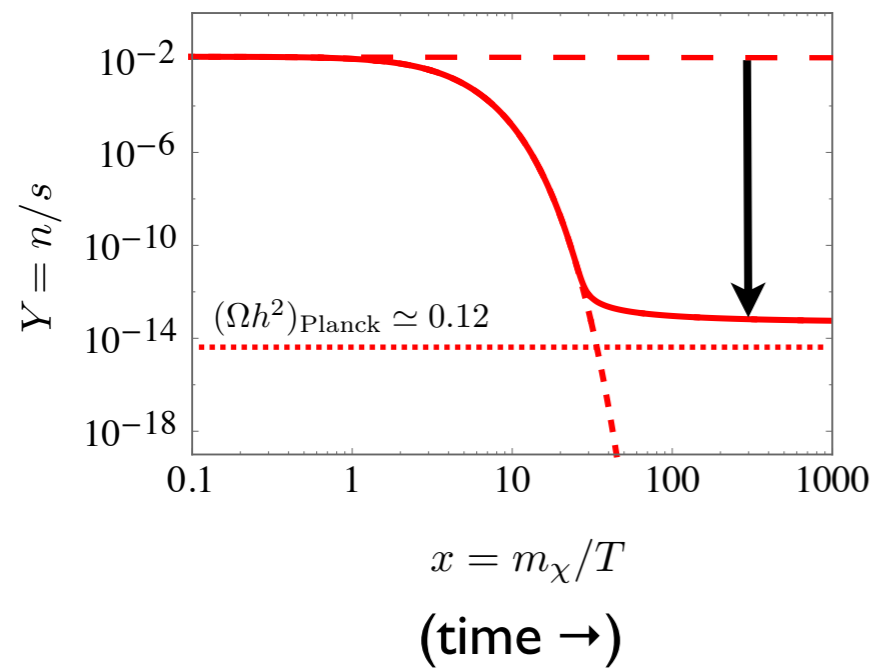
Mediator same gauge quantum no. as $f \Rightarrow$ (color-)charged:



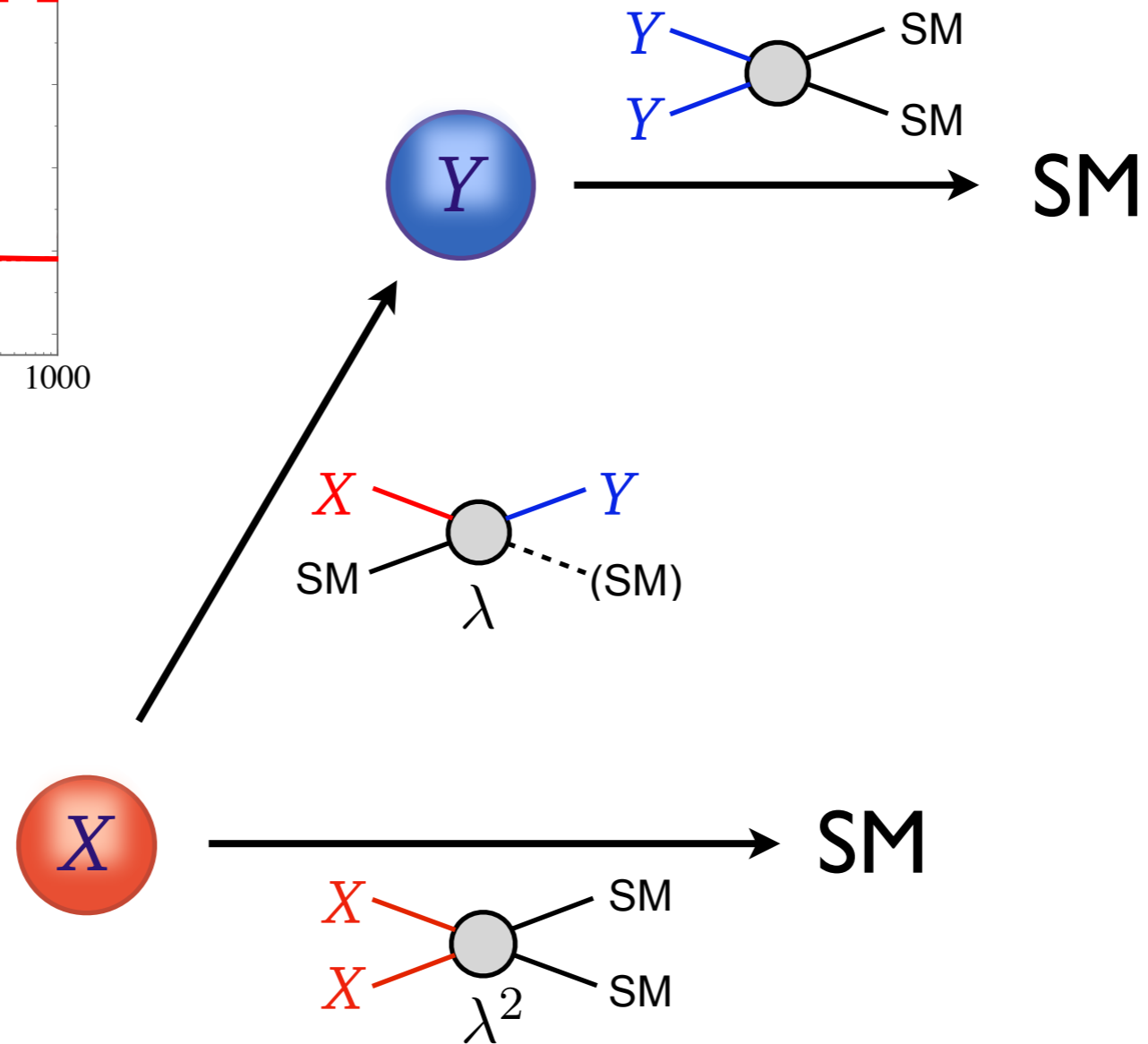
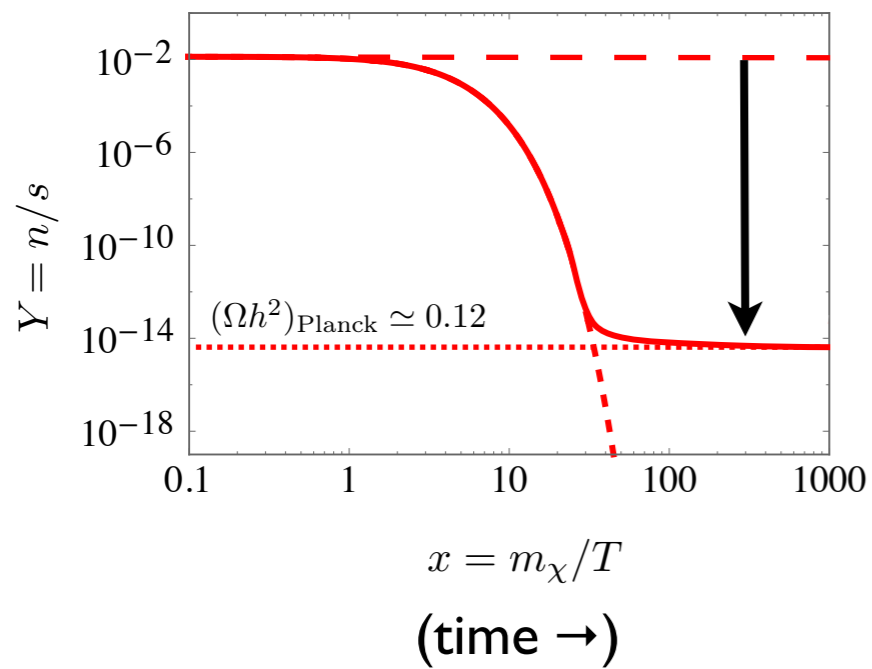
Dark matter freeze-out



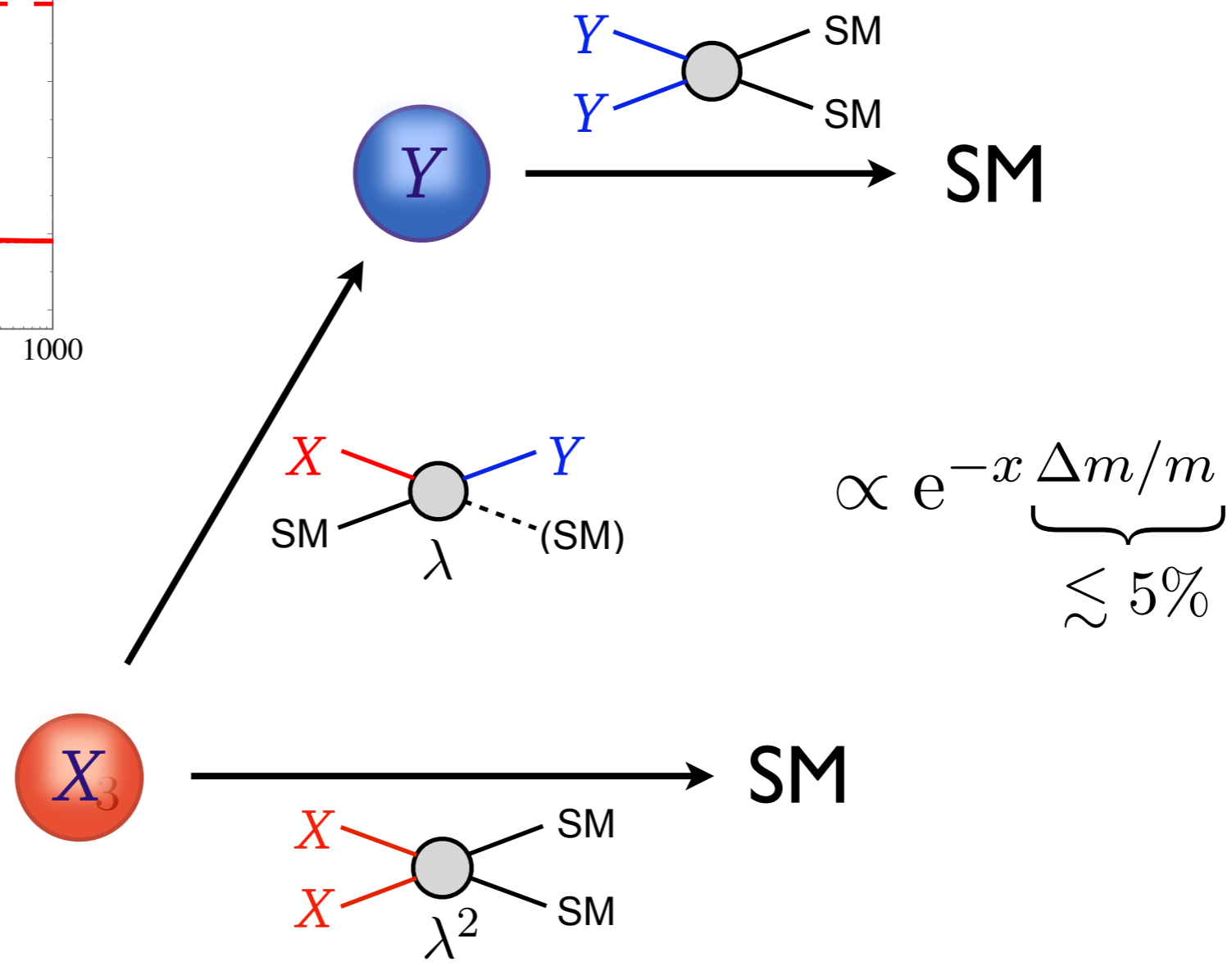
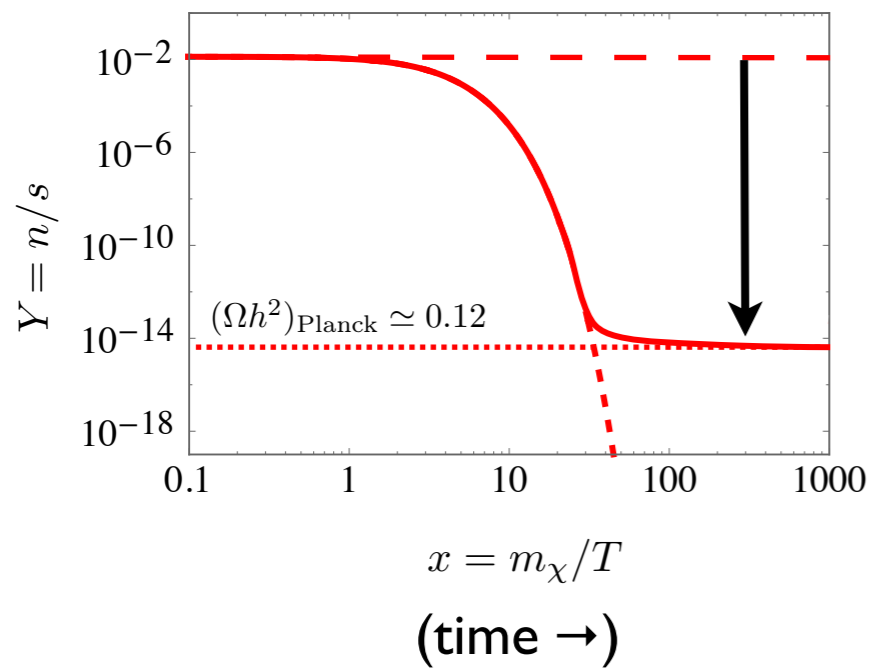
Dark matter freeze-out



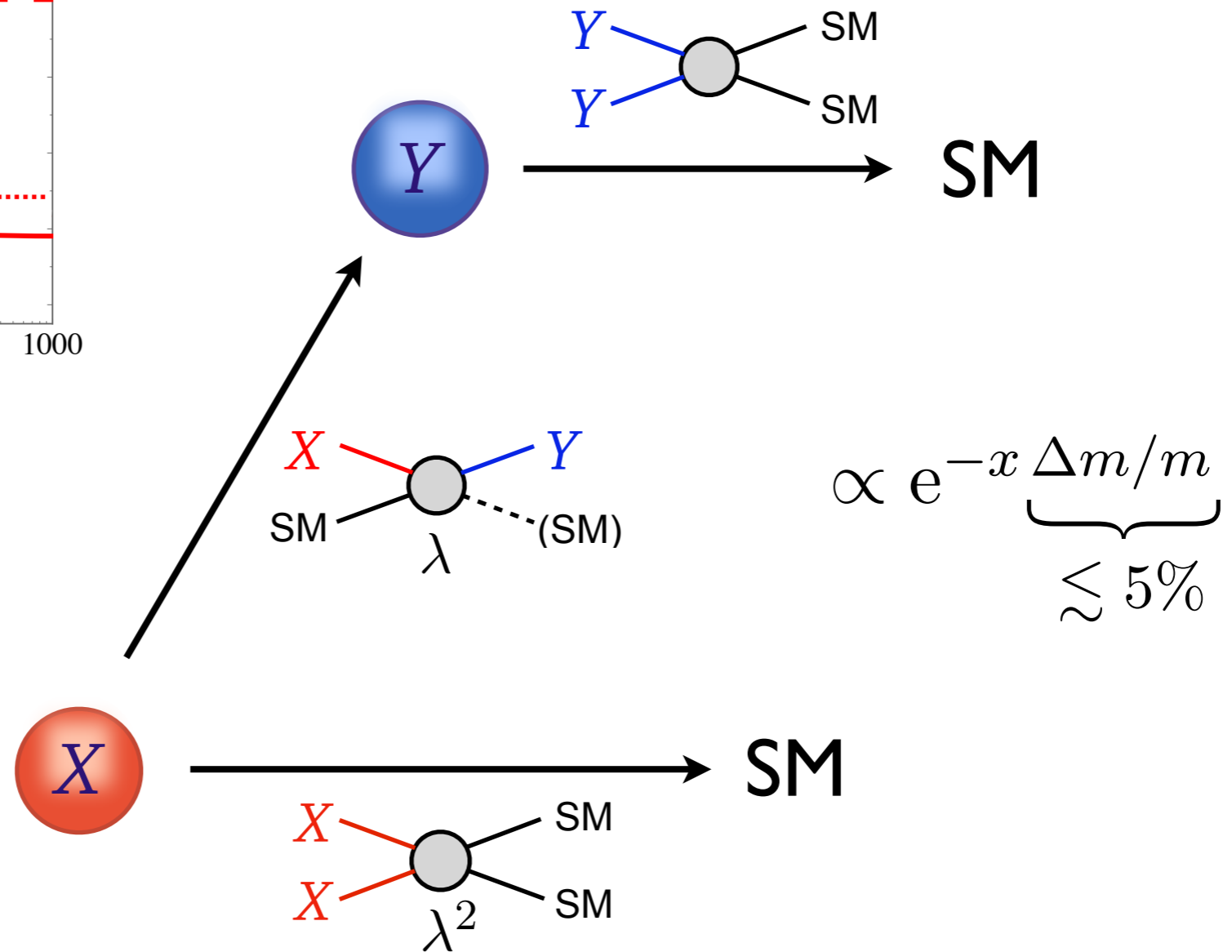
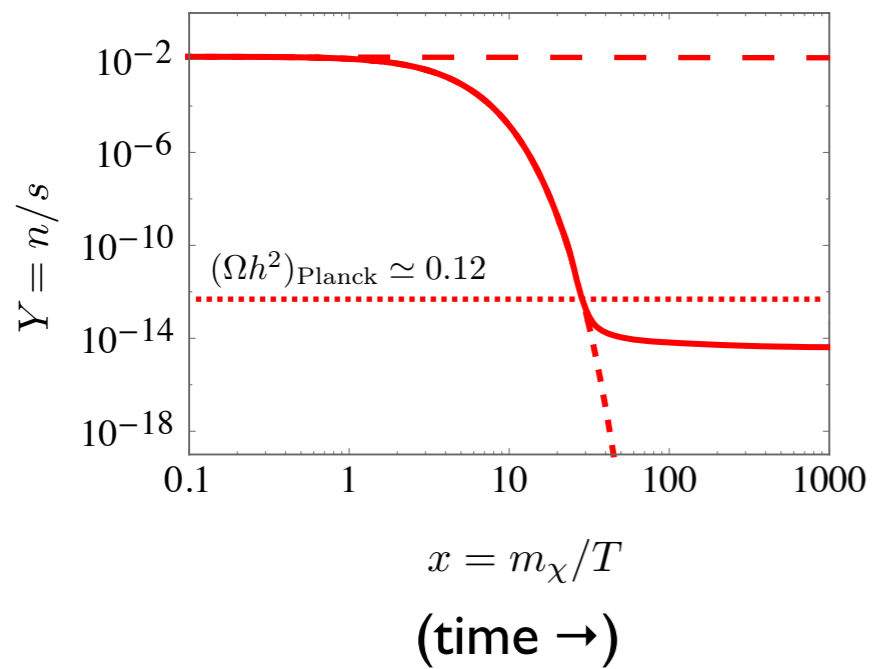
Dark matter freeze-out: coannihilation



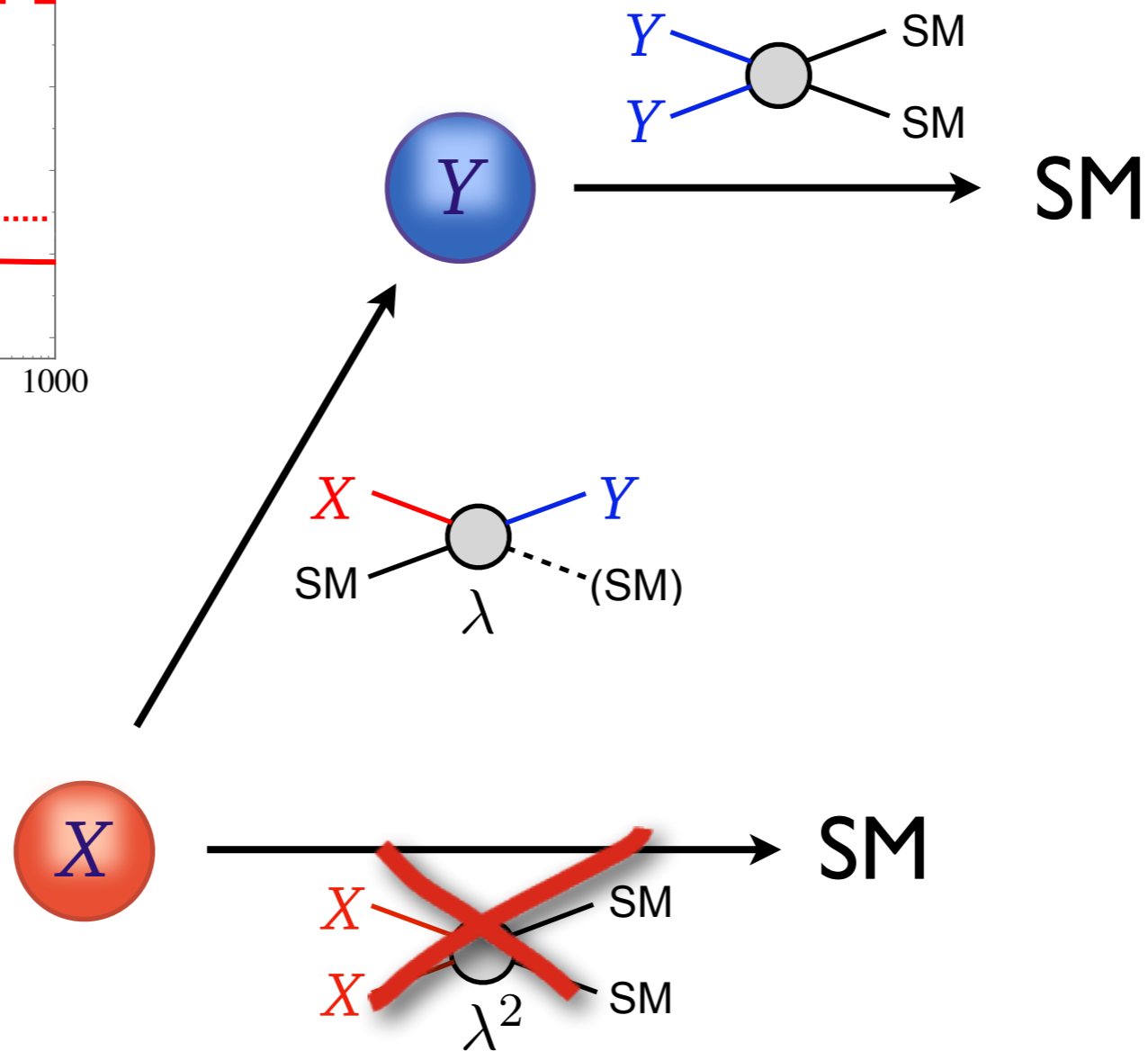
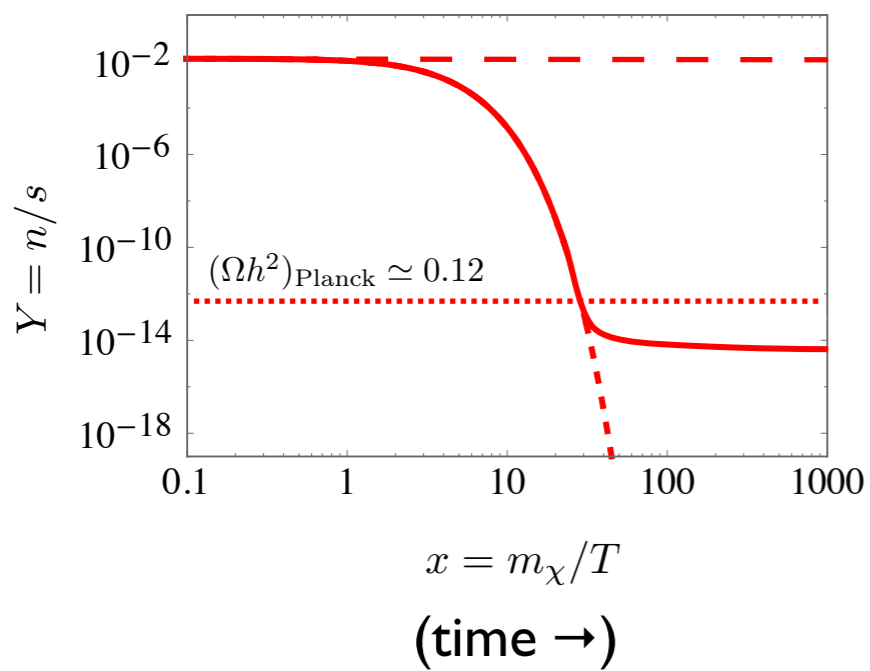
Dark matter freeze-out: coannihilation



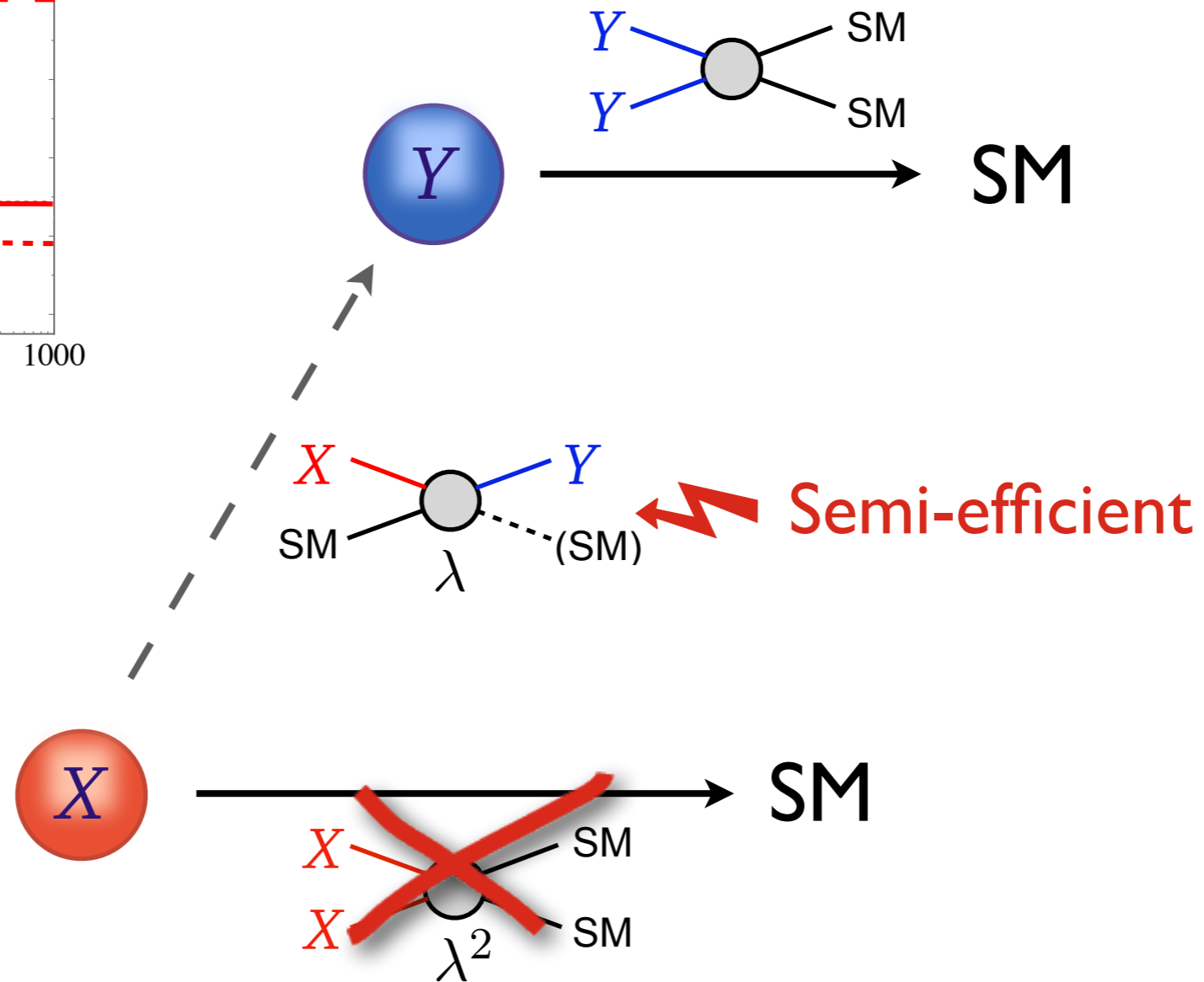
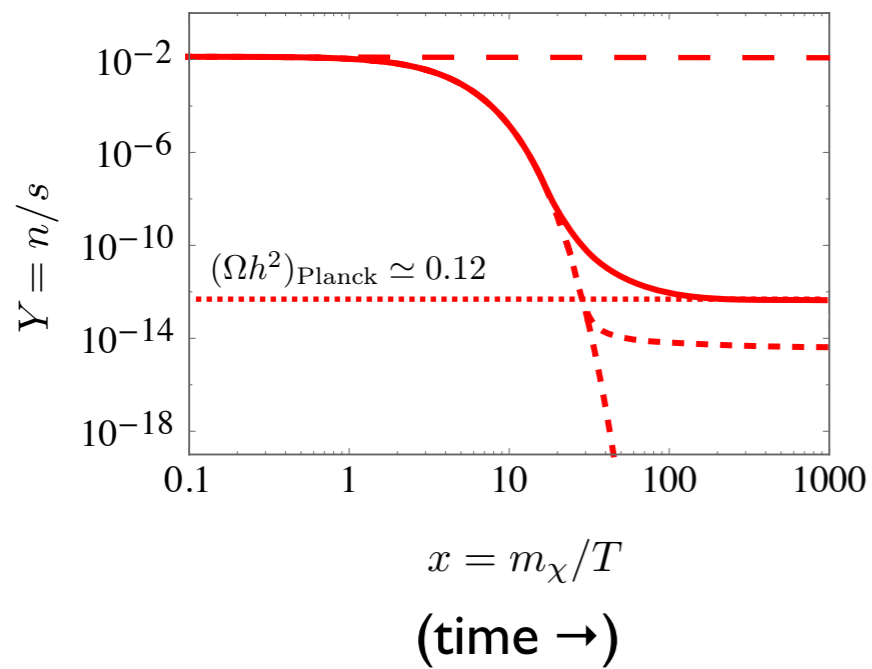
Dark matter freeze-out: coannihilation



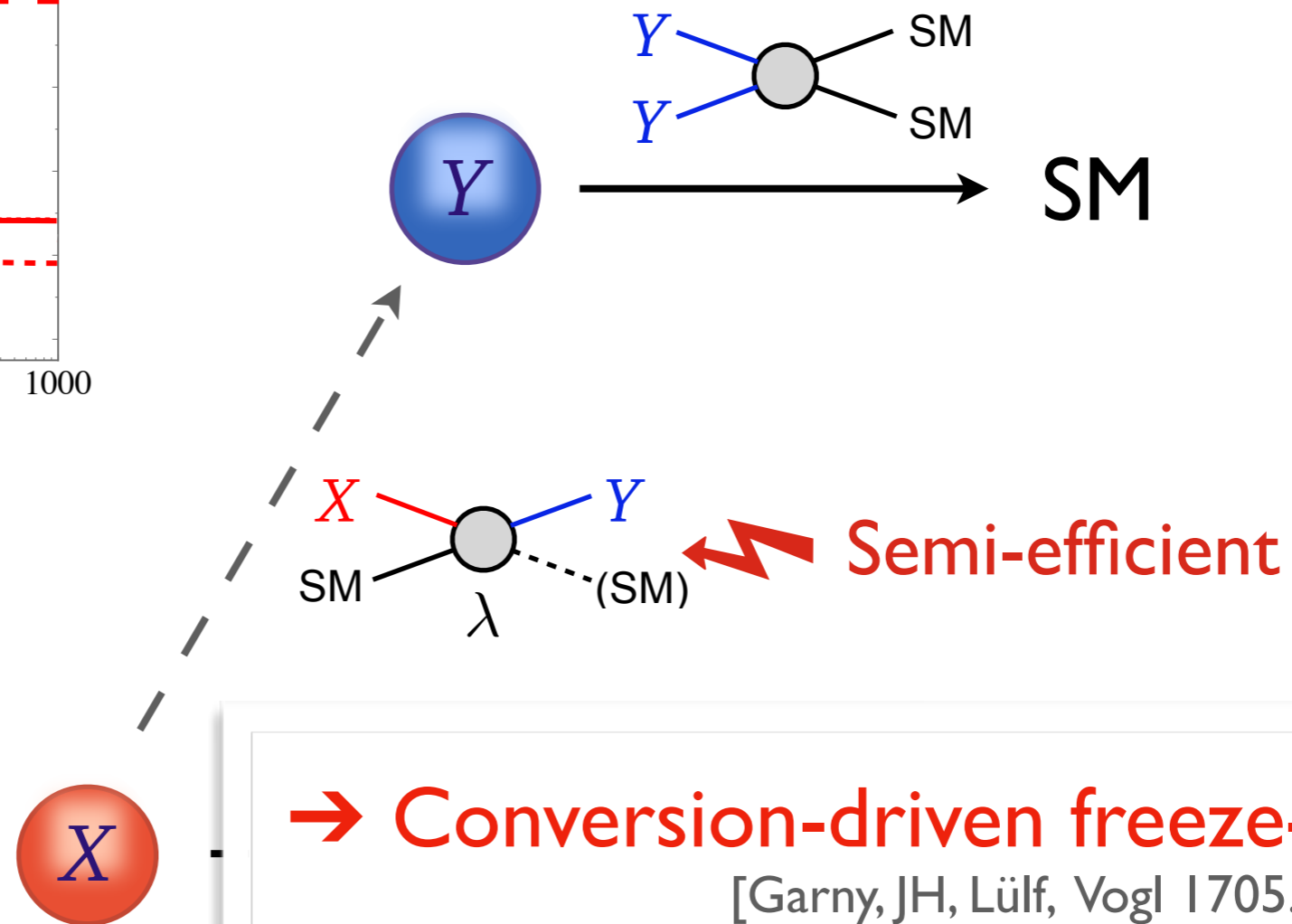
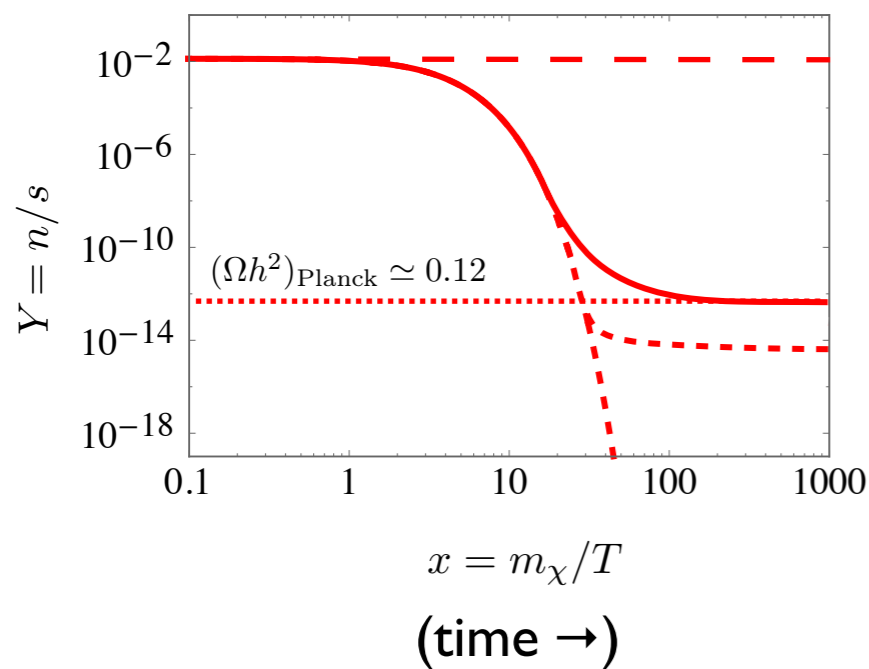
Dark matter freeze-out: small λ



Dark matter freeze-out: very small λ



Dark matter freeze-out: very small λ

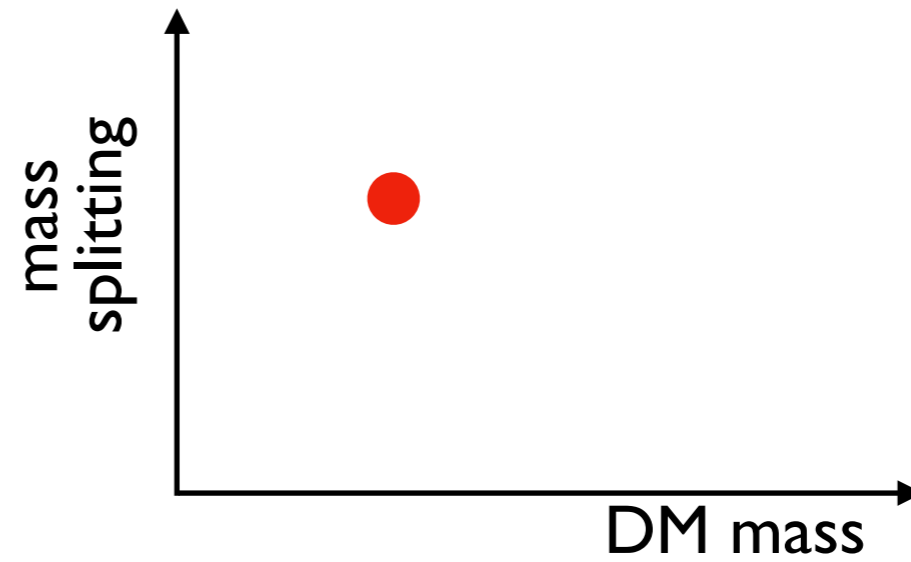
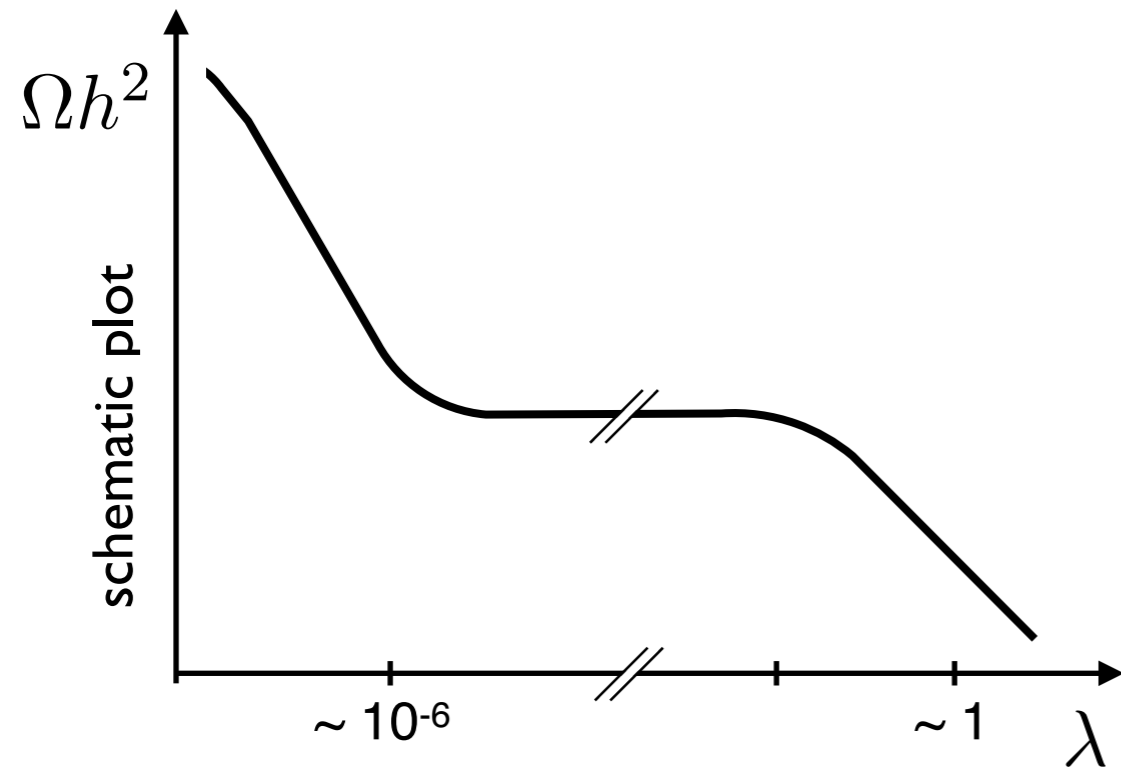


→ Conversion-driven freeze-out

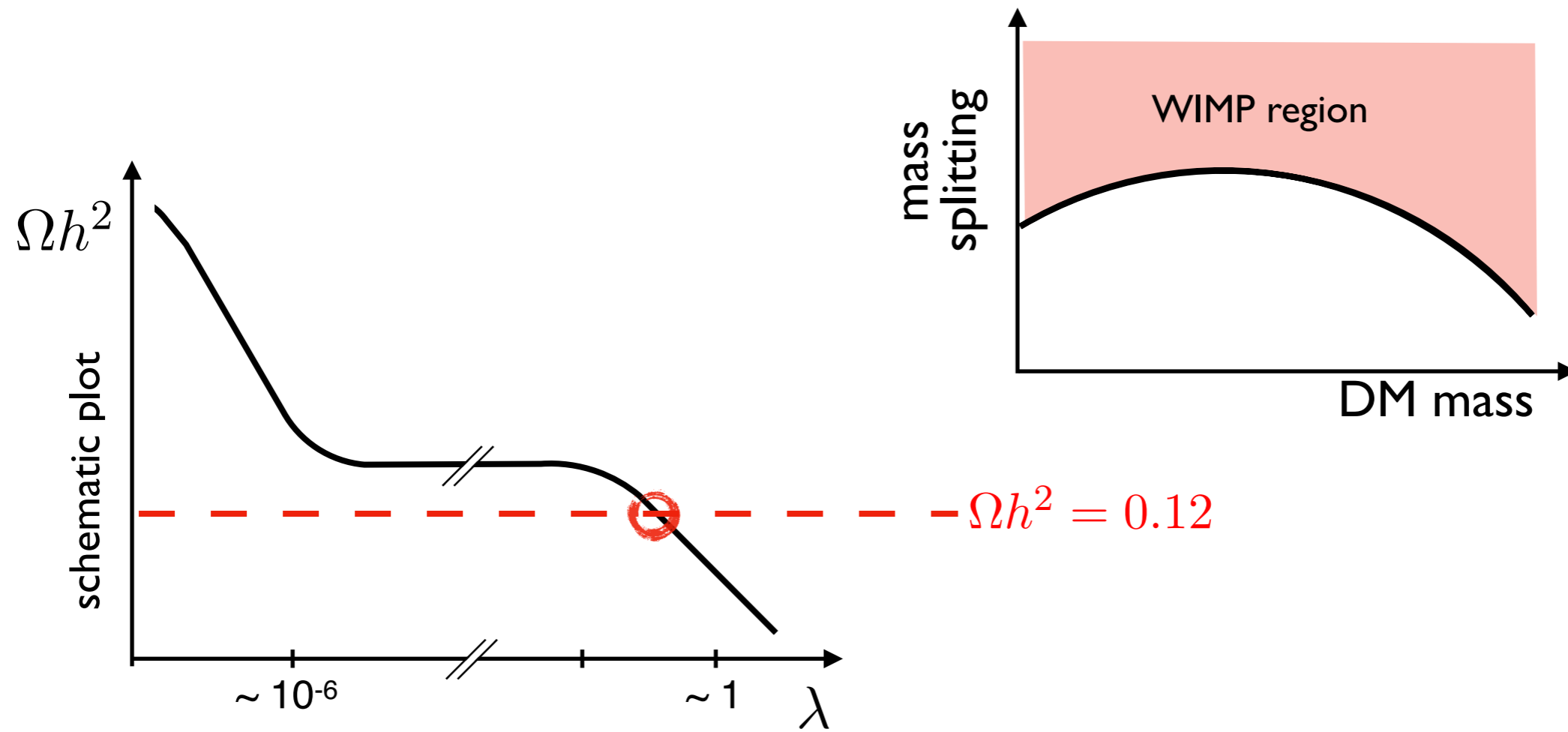
[Garny, JH, Lulf, Vogl | 705.09292;

D'Agnolo, Pappadopulo, Ruderman | 705.08450]

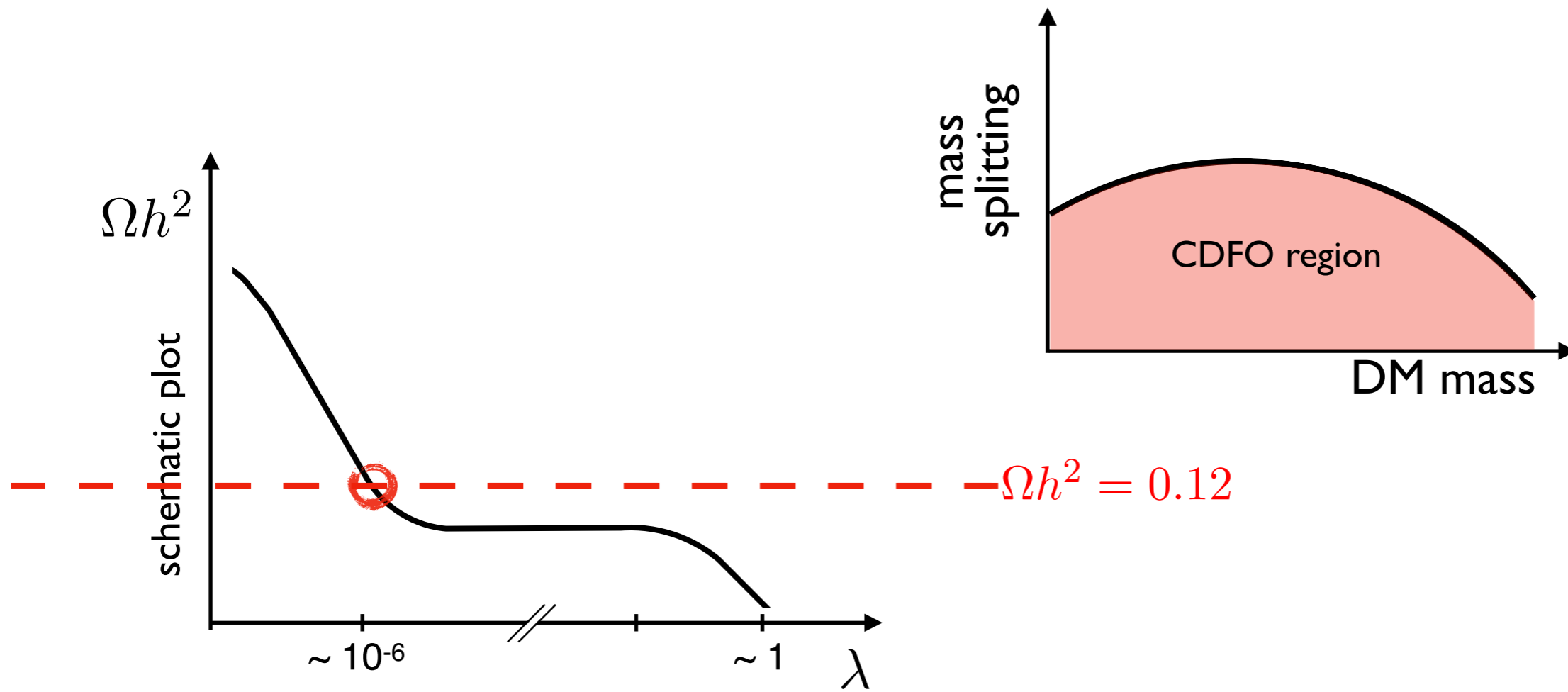
Accessible parameter space



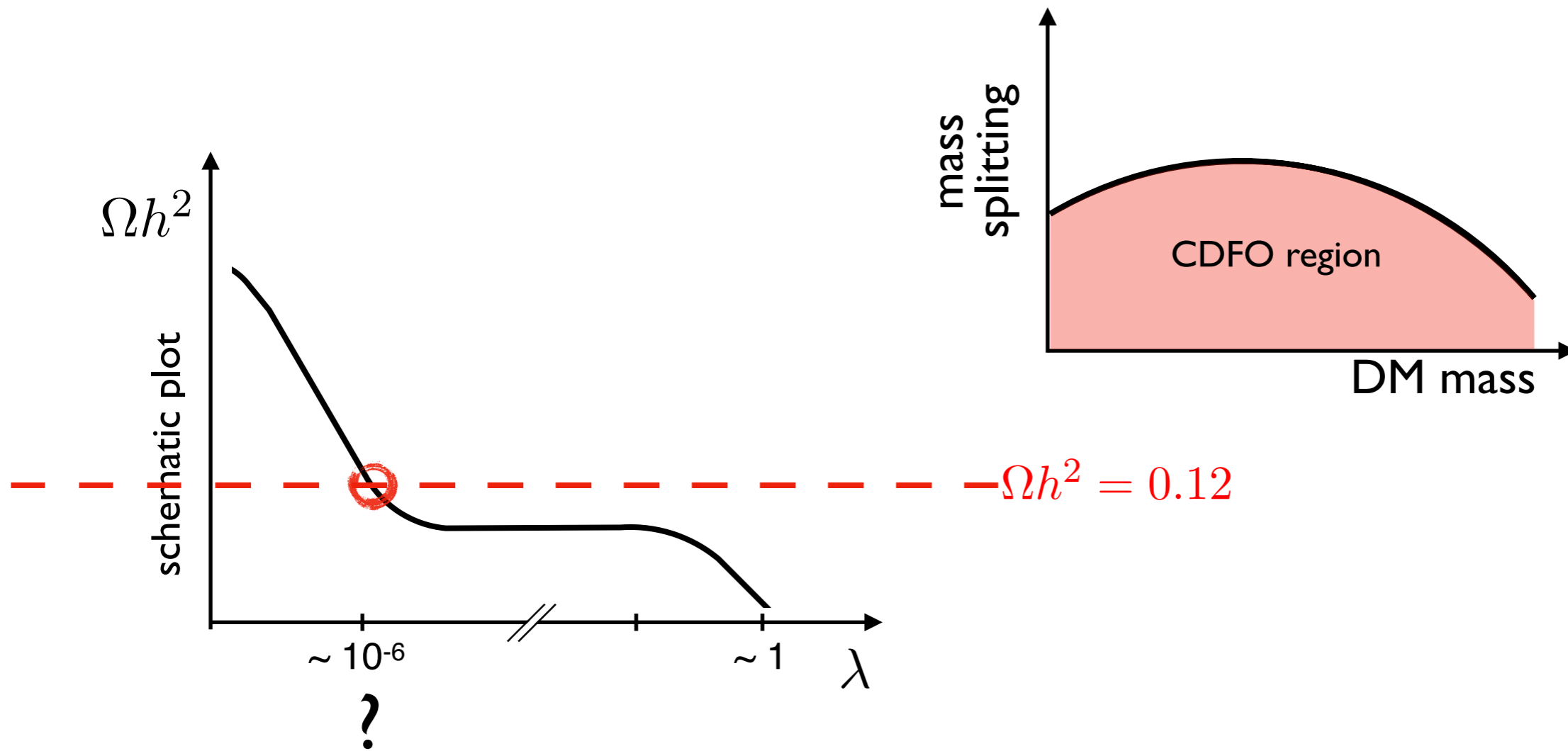
Accessible parameter space



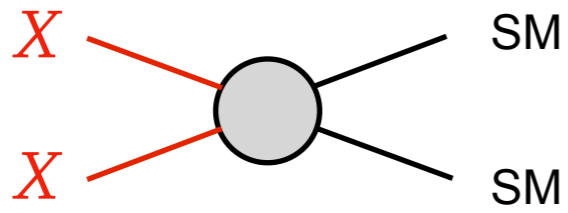
Accessible parameter space



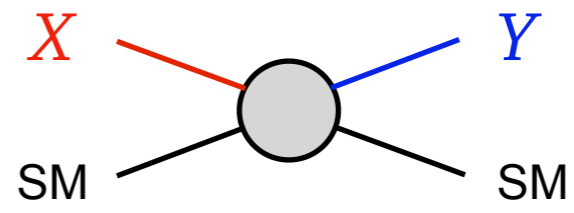
Accessible parameter space



Typical coupling



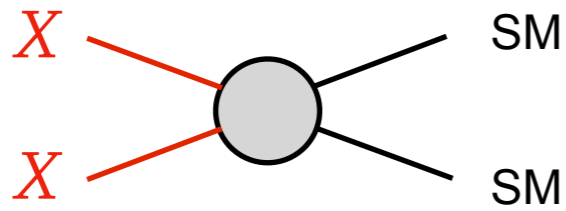
VS



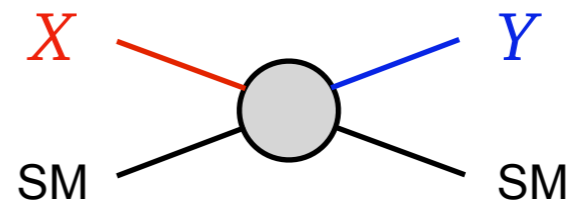
$$\Gamma_{\text{ann}} = n_X \langle \sigma v \rangle_{\text{ann}}$$

$$\Gamma_{\text{con}} = n_{\text{SM}} \langle \sigma v \rangle_{\text{con}}$$

Typical coupling



VS

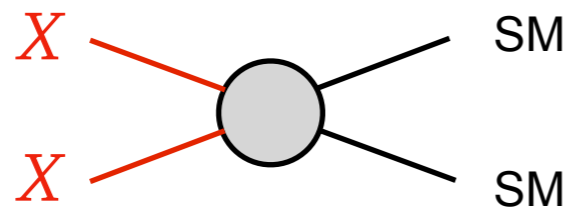


$$\Gamma_{\text{ann}} = n_X \langle \sigma v \rangle_{\text{ann}}$$

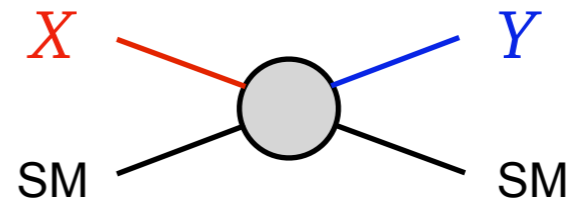
$$\uparrow$$
$$e^{-m_X/T_{\text{fo}}} \sim 10^{-12}$$

$$\Gamma_{\text{con}} = n_{\text{SM}} \langle \sigma v \rangle_{\text{con}}$$

Typical coupling



VS



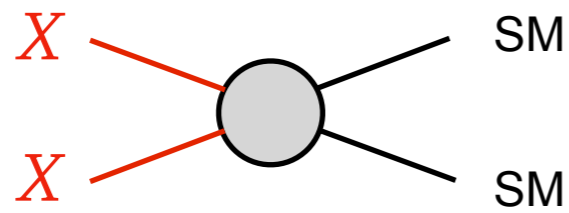
$$\Gamma_{\text{ann}} = n_X \langle \sigma v \rangle_{\text{ann}}$$

$$\uparrow$$
$$e^{-m_X/T_{\text{fo}}} \sim 10^{-12}$$

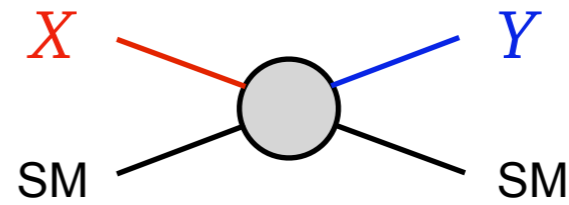
$$\Gamma_{\text{con}} = n_{\text{SM}} \langle \sigma v \rangle_{\text{con}}$$

Thermal decoupling condition: $\Gamma \sim H$

Typical coupling



VS



$$\Gamma_{\text{ann}} = n_X \langle \sigma v \rangle_{\text{ann}}$$

$$\uparrow$$
$$e^{-m_X/T_{\text{fo}}} \sim 10^{-12}$$

$$\Gamma_{\text{con}} = n_{\text{SM}} \langle \sigma v \rangle_{\text{con}}$$

Thermal decoupling condition: $\Gamma \sim H$

$$\frac{\langle \sigma v \rangle_{\text{con}}}{\langle \sigma v \rangle_{\text{ann}}} \sim 10^{-12} \quad \Rightarrow \quad \lambda \sim 10^{-6}$$

Conversion-driven freeze-out – summary

- Conversions initiate thermal decoupling $\lambda \sim 10^{-6}$
- Accommodate null-results of WIMP searches
- Still, conversions supply thermalisation

Conversion-driven freeze-out – summary

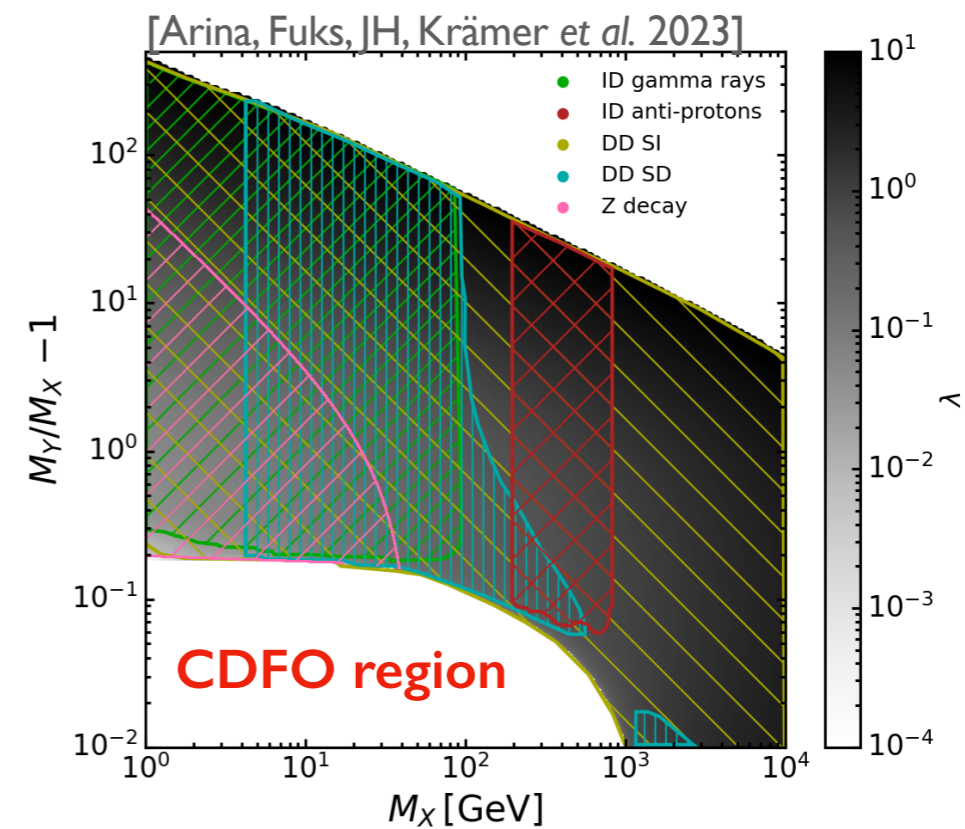
- Conversions initiate thermal decoupling $\lambda \sim 10^{-6}$
- Accommodate null-results of WIMP searches
- Still, conversions supply thermalisation

- Wide range of viable model realizations

[Garny+ 2018, Bharucha+ 2018, D'Agnolo+ 2018, Cheng+ 2018, Junius+ 2019, Belanger+ 2022, Alguero+ 2022, Díaz Sez 2024, ...]

- Link to neutrino masses [Heeck, JH, Thapa 2023]

- Link to baryogenesis [JH 2024]



How to search for it at LHC

How to search for it at LHC?

Conversion rate on the edge of being efficient:

$$\Gamma_{\text{con}} \sim H$$

$$\Rightarrow \Gamma_{\text{dec}} \lesssim H$$

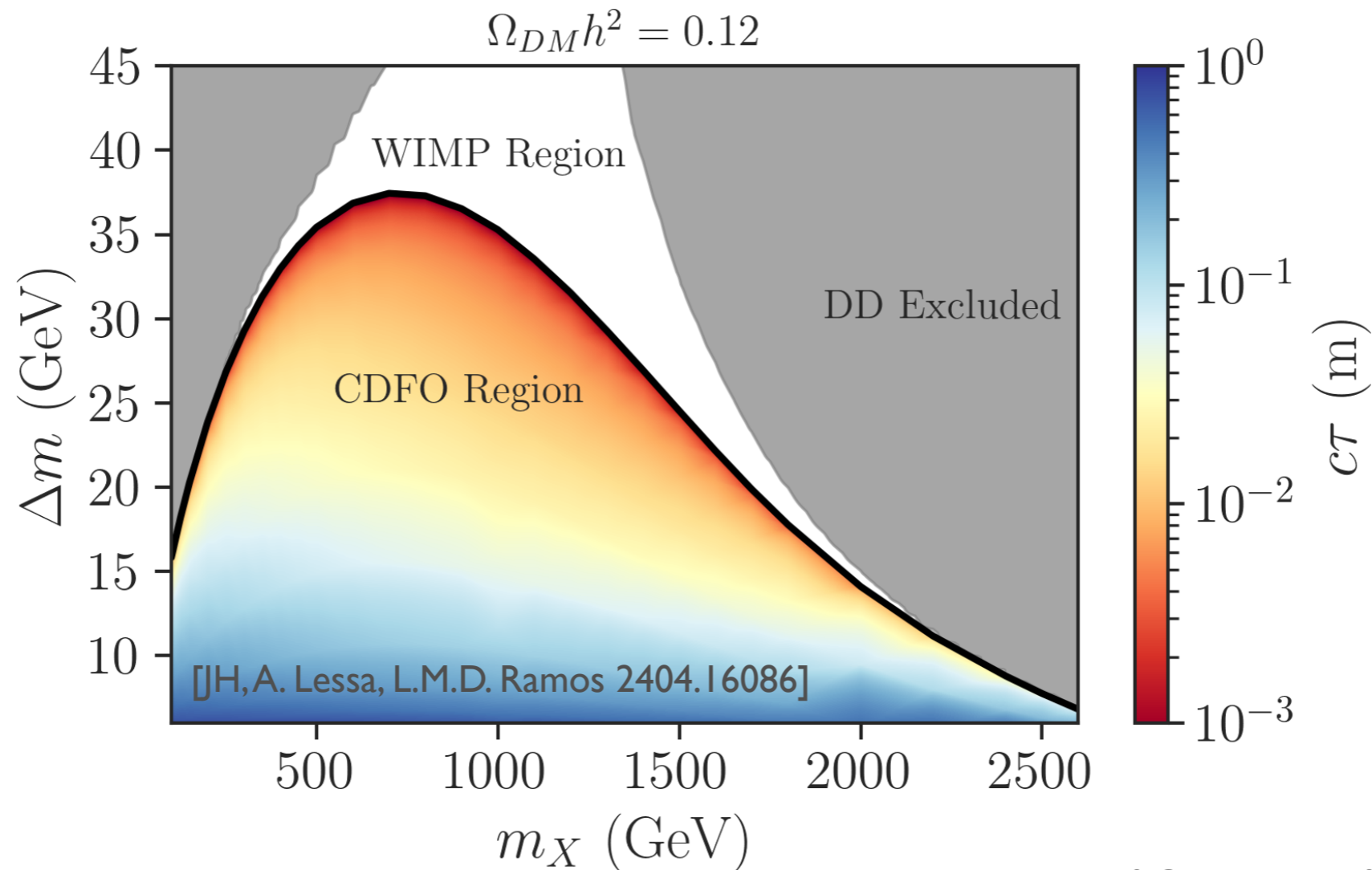
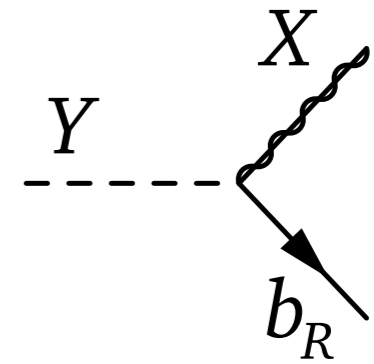
$$c\tau \gtrsim H^{-1} \simeq 1.5 \text{ cm} \left(\frac{(100 \text{ GeV})^2}{T_{\text{fo}}^2} \right)$$

\Rightarrow Long-lived particles (LLPs) at LHC!

Bottom-philic example

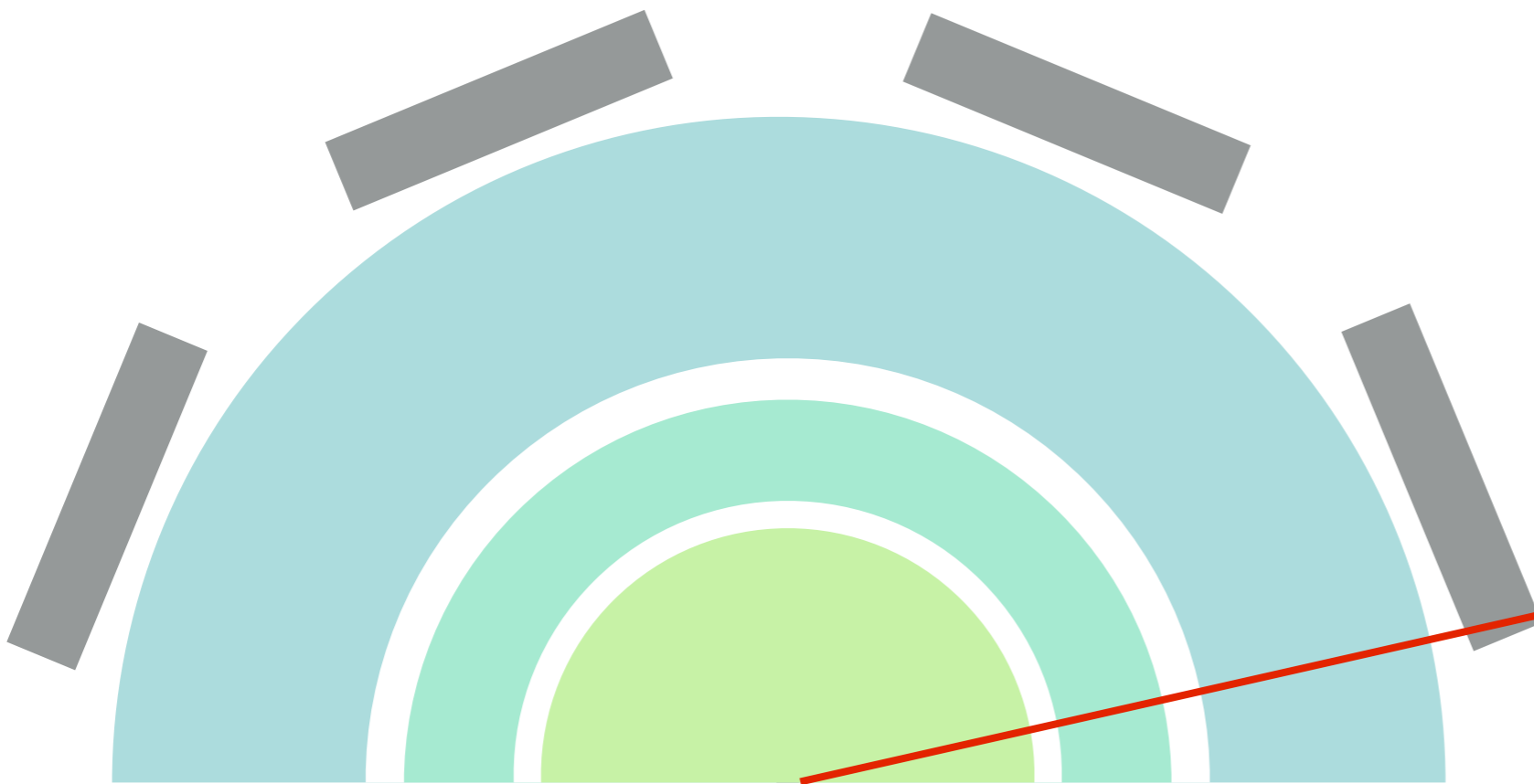
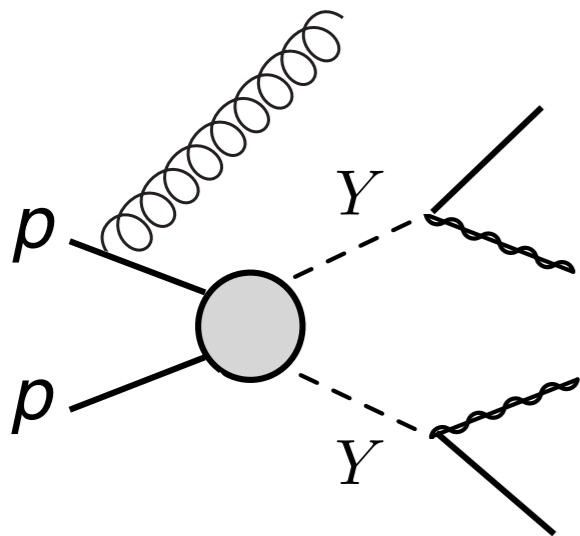
X : Majorana dark matter

Y : Scalar mediator (bottom-partner)



[cf. Garny, JH, Lulf, Vogl 1705.09292;
bound state effects from Garny, JH 2112.01499]

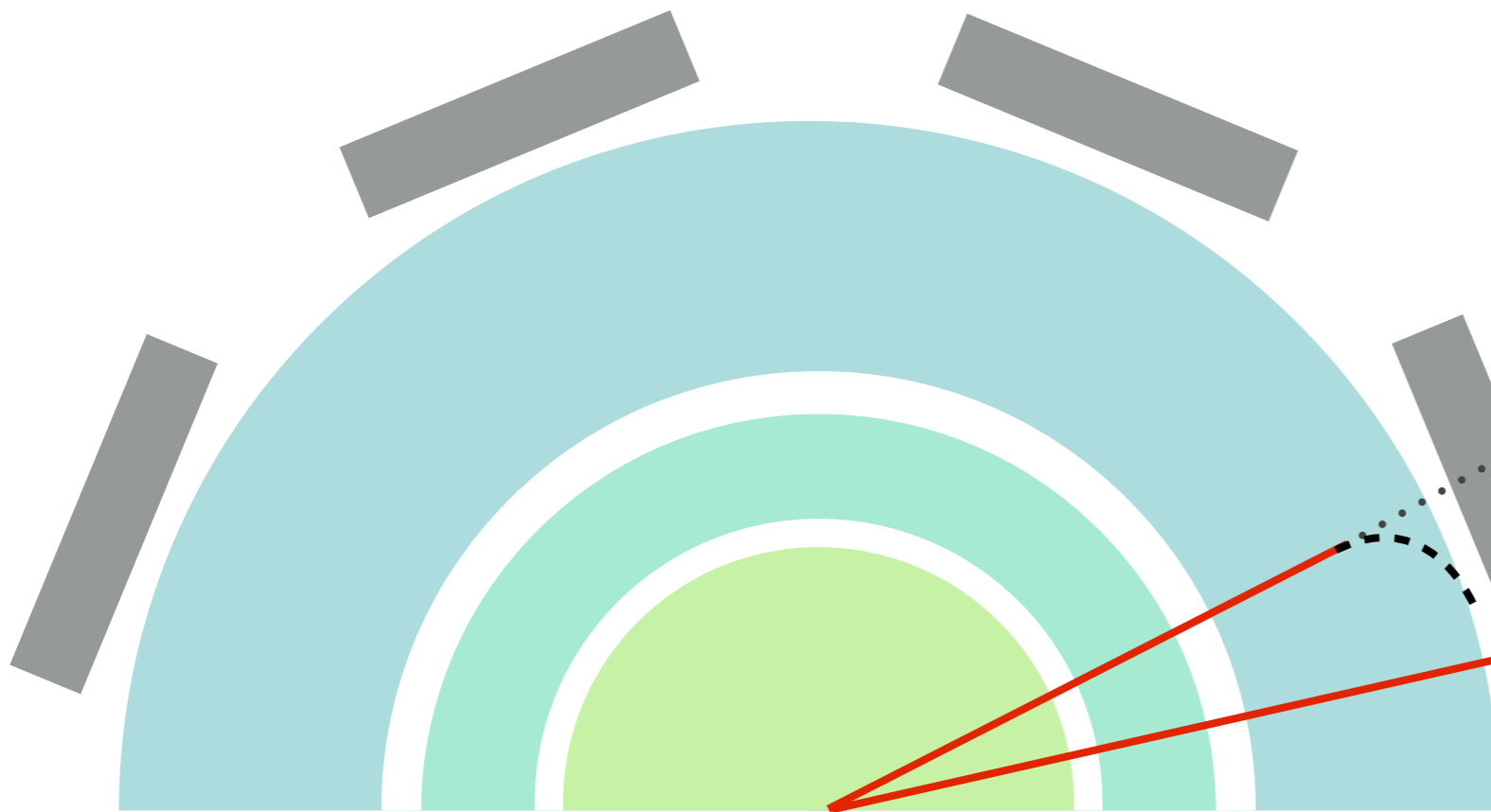
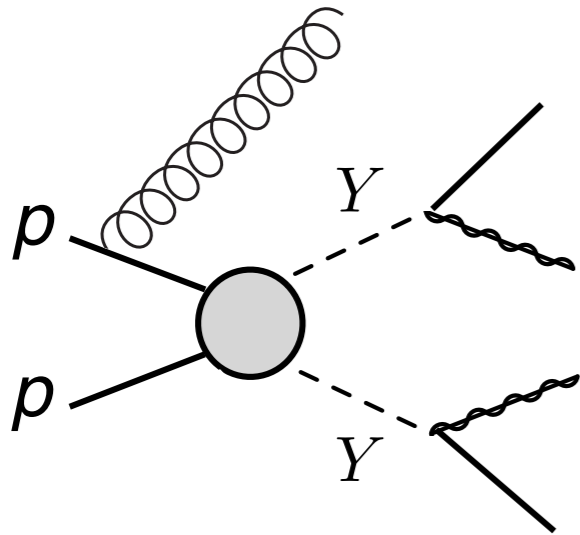
LHC Signature



Anomalous tracks
(Heavy stable charged
particle searches)

$$c\tau_Y > 1 \text{ m}$$

LHC Signature



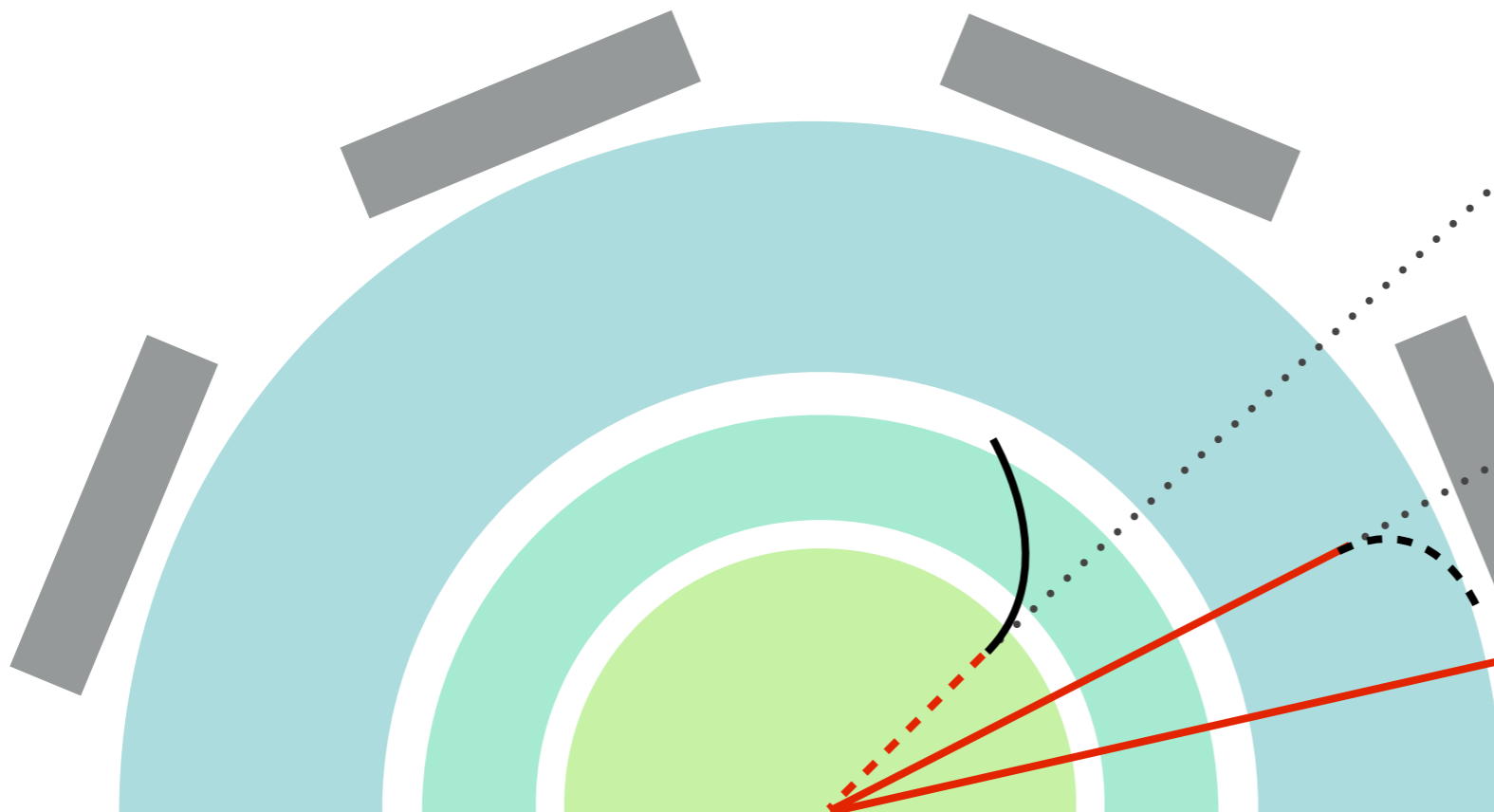
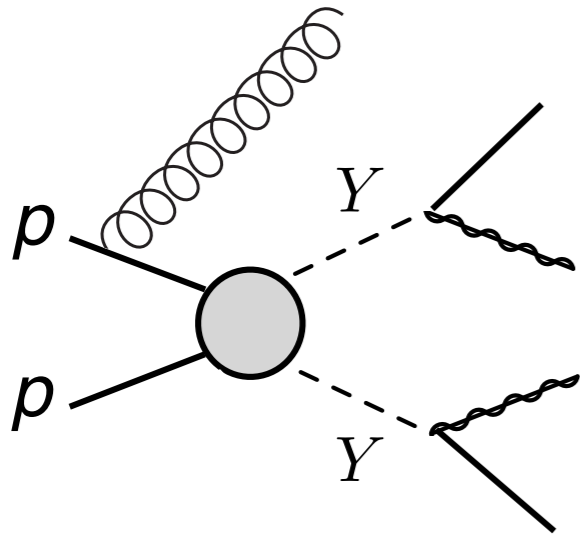
Disappearing tracks

$$10 \text{ cm} \lesssim c\tau_Y \lesssim 1 \text{ m}$$

Anomalous tracks
(Heavy stable charged
particle searches)

$$c\tau_Y > 1 \text{ m}$$

LHC Signature

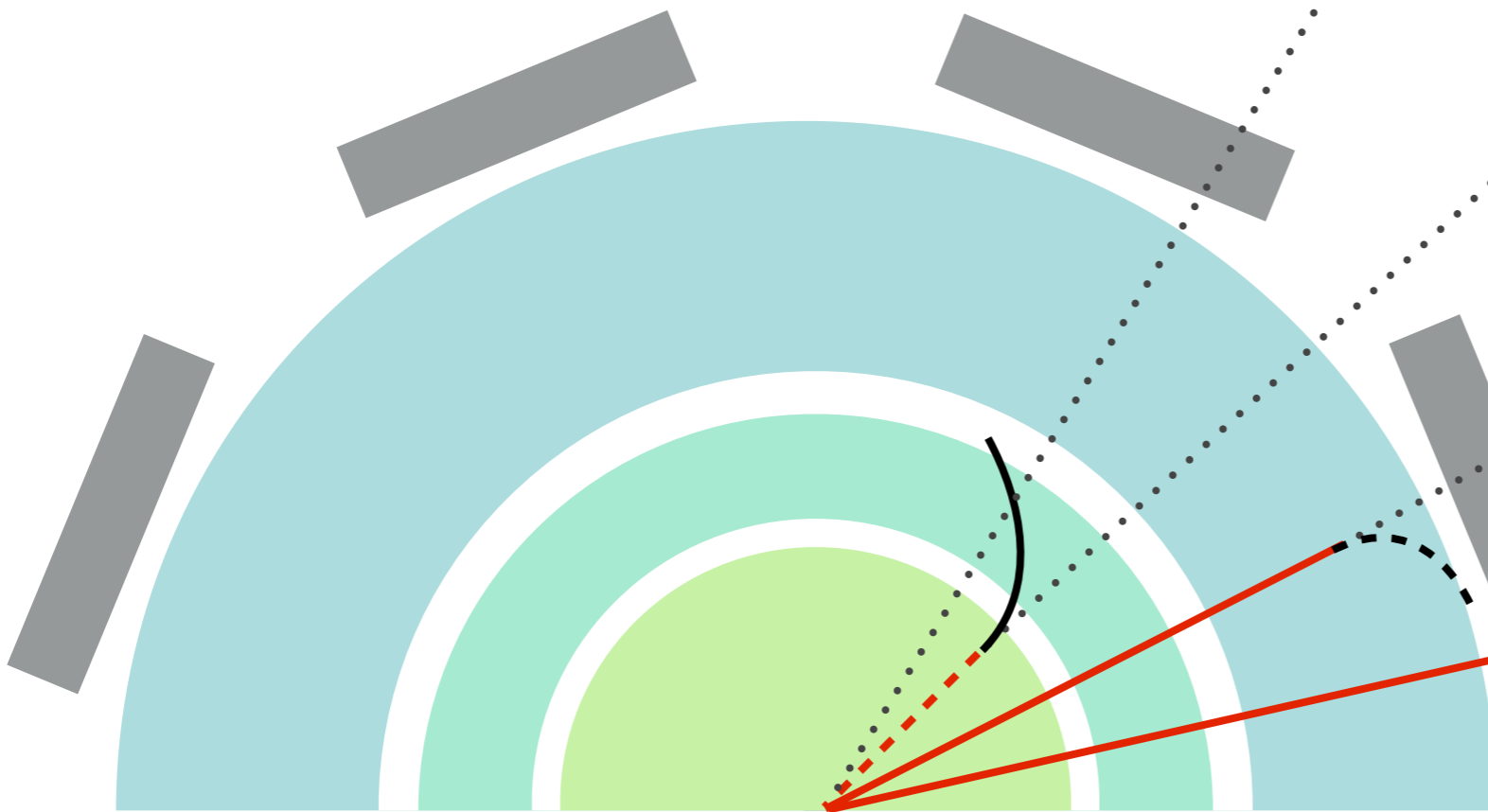
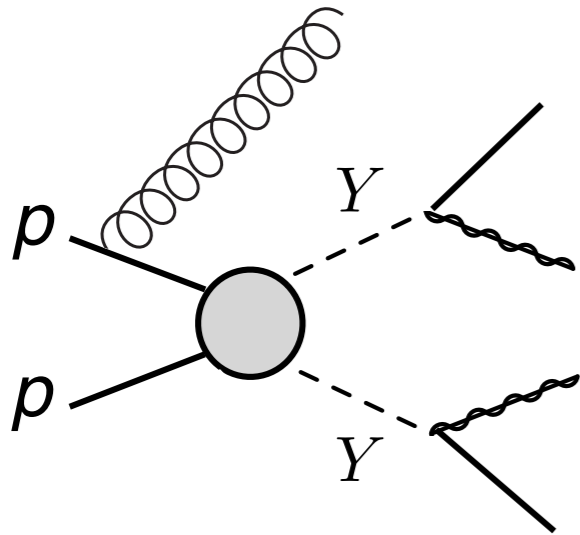


Displaced vertices (+MET)
 $4 \text{ mm} \lesssim c\tau_Y \lesssim 30 \text{ cm}$

Disappearing tracks
 $10 \text{ cm} \lesssim c\tau_Y \lesssim 1 \text{ m}$

Anomalous tracks
(Heavy stable charged
particle searches)
 $c\tau_Y > 1 \text{ m}$

LHC Signature



Just missing energy (MET)

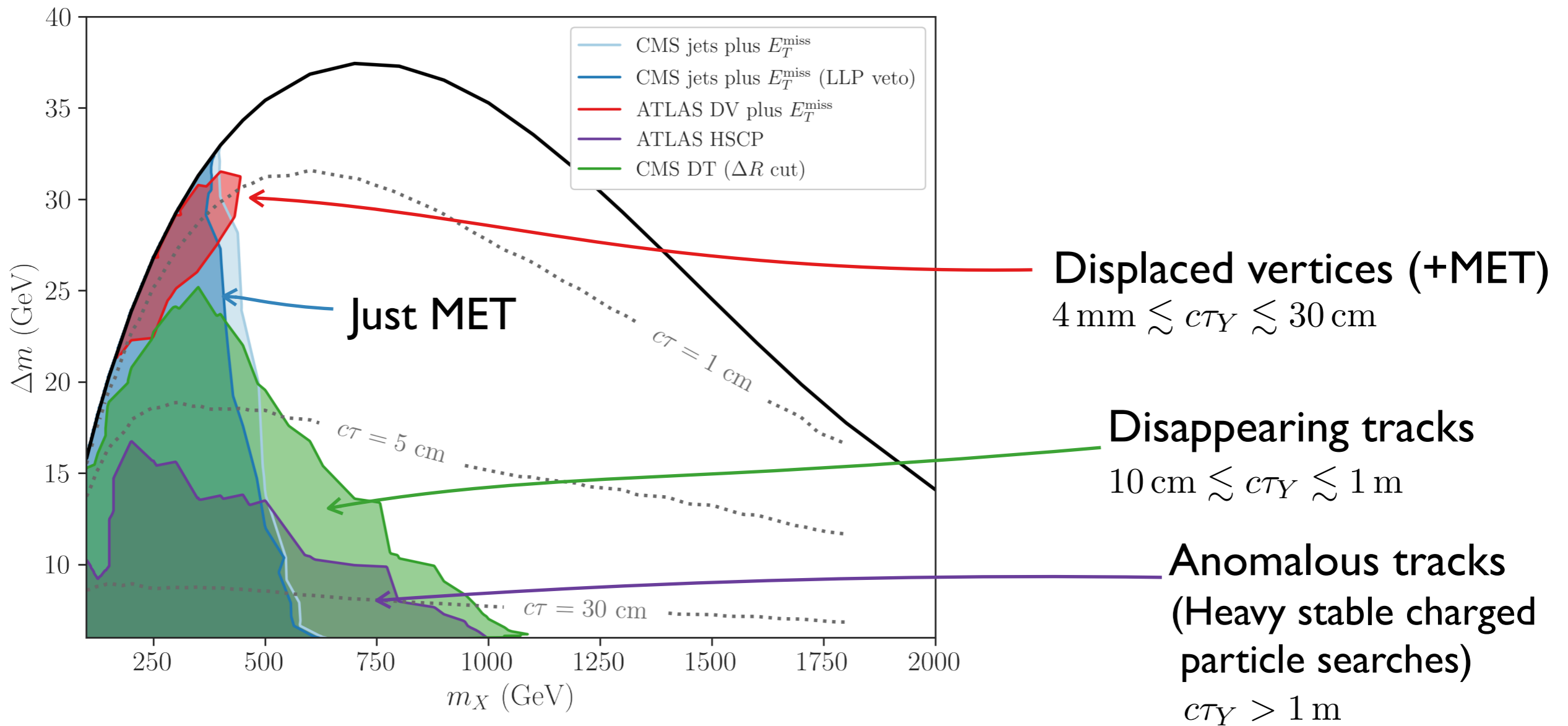
Displaced vertices (+MET)
 $4 \text{ mm} \lesssim c\tau_Y \lesssim 30 \text{ cm}$

Disappearing tracks
 $10 \text{ cm} \lesssim c\tau_Y \lesssim 1 \text{ m}$

Anomalous tracks
(Heavy stable charged
particle searches)
 $c\tau_Y > 1 \text{ m}$

Current LHC constraints

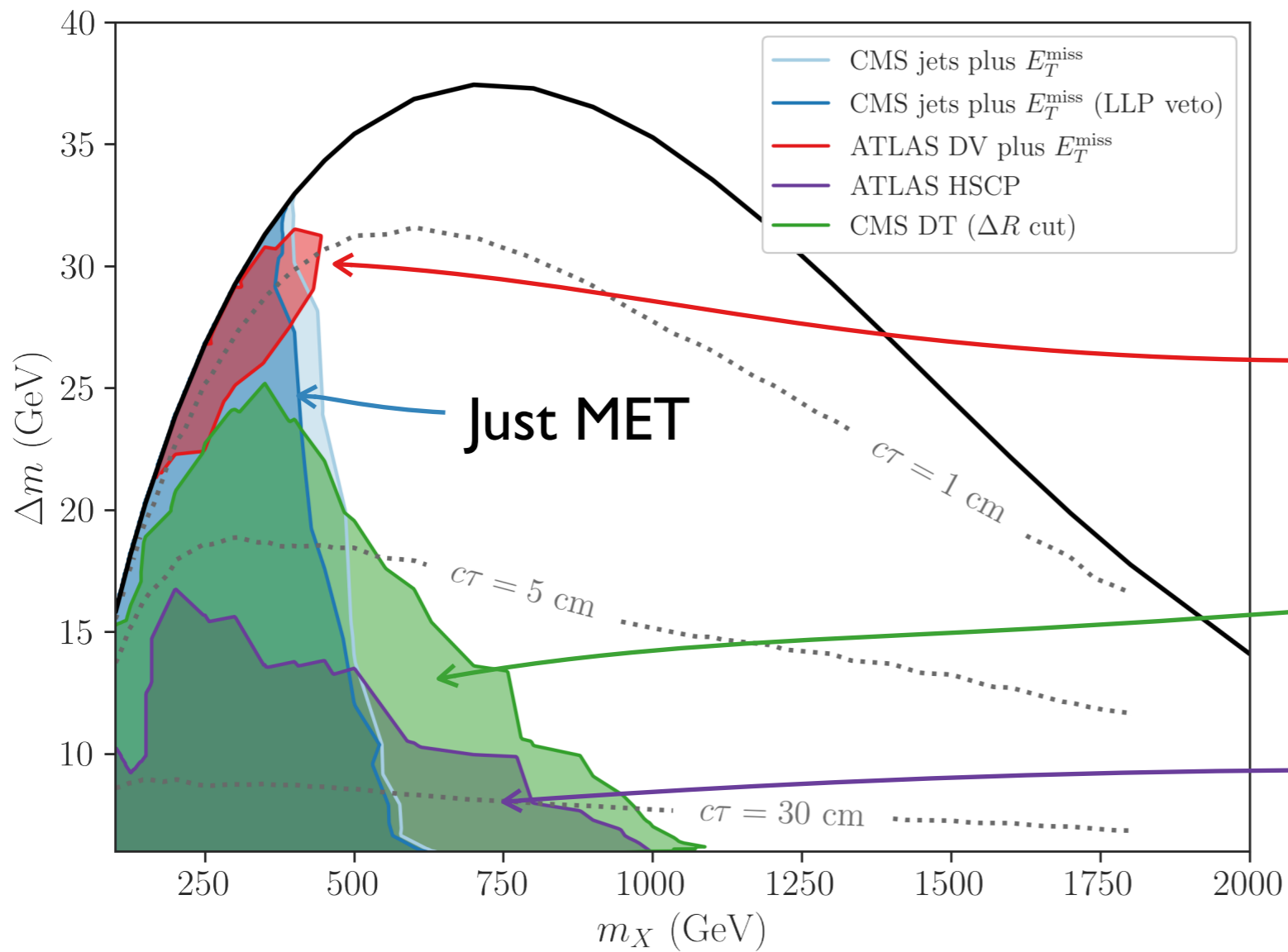
[JH, A. Lessa, L.M.D. Ramos 2404.16086]



[see also Fuks *et al.*, contr. 7 in 2002.12220]

Current LHC constraints

[JH, A. Lessa, L.M.D. Ramos 2404.16086]



Why poor performance?

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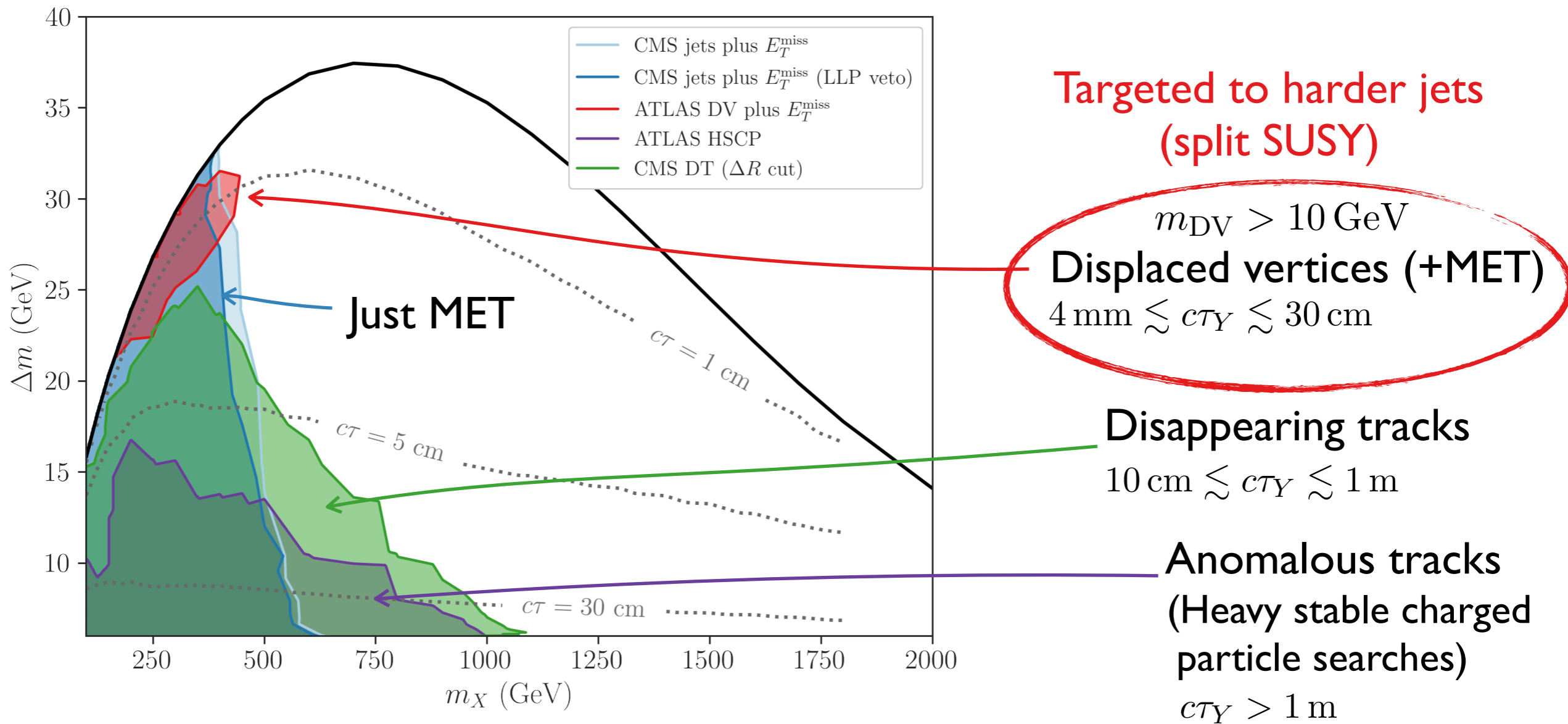
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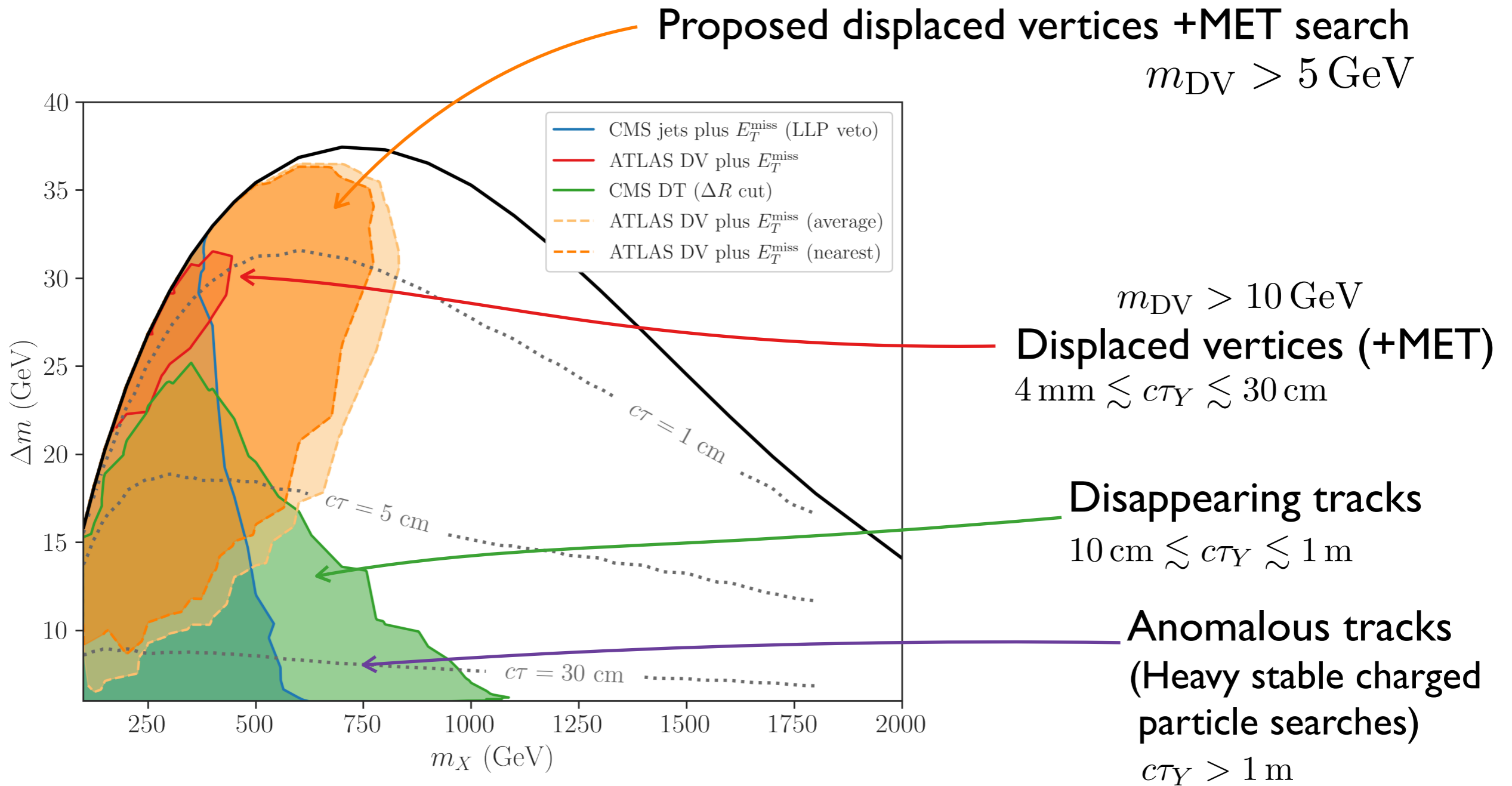
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[JH, A. Lessa, L.M.D. Ramos 2404.16086]



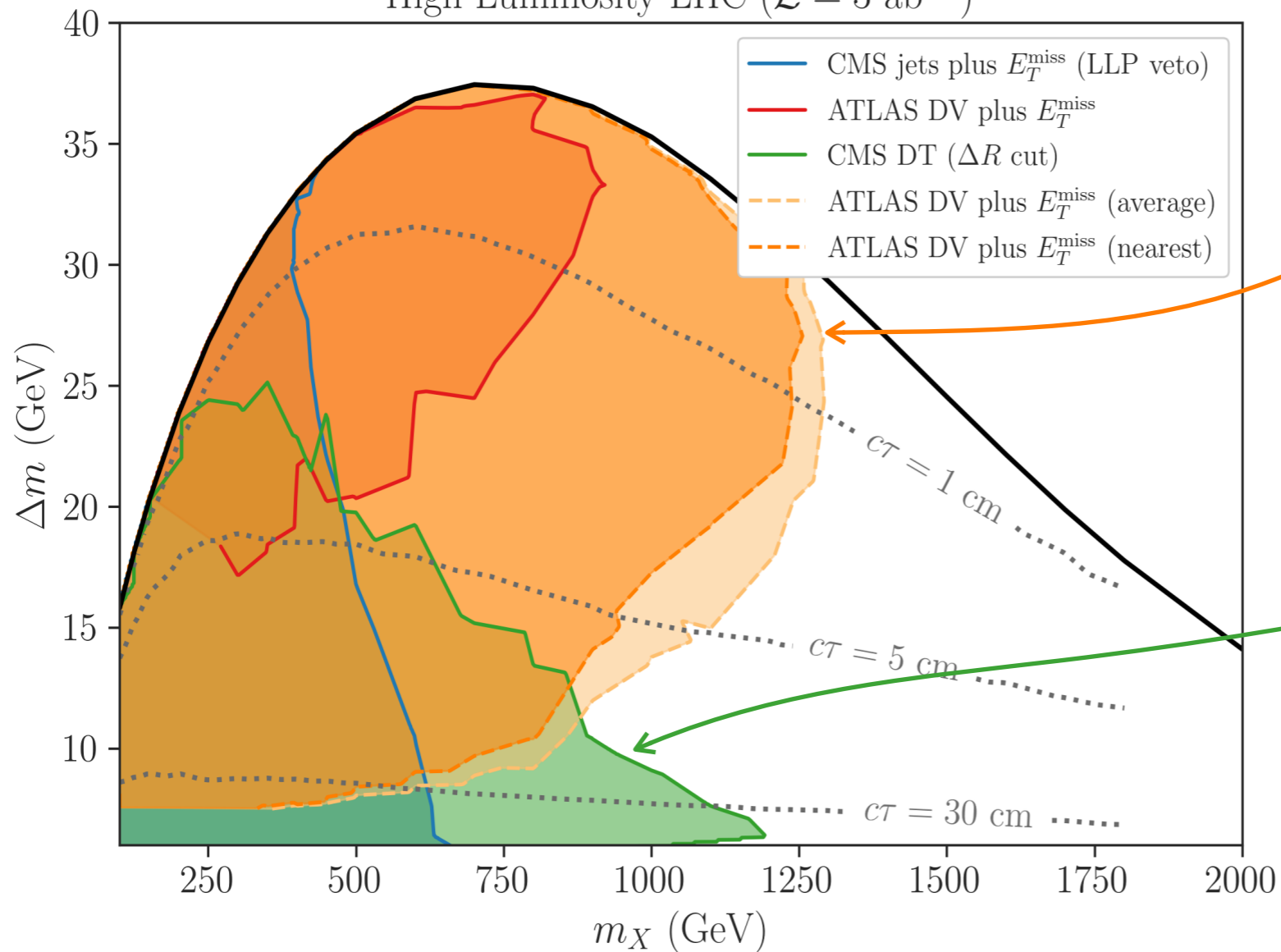
HL-LHC projections

[JH, A. Lessa, L.M.D. Ramos 2404.16086]

Proposed displaced vertices +MET search

$m_{\text{DV}} > 5 \text{ GeV}$

High Luminosity LHC ($\mathcal{L} = 3 \text{ ab}^{-1}$)

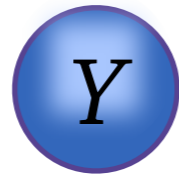


Disappearing tracks

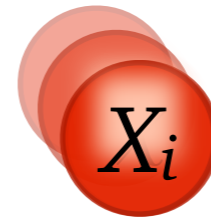
$10 \text{ cm} \lesssim c\tau_Y \lesssim 1 \text{ m}$

Link to baryogenesis

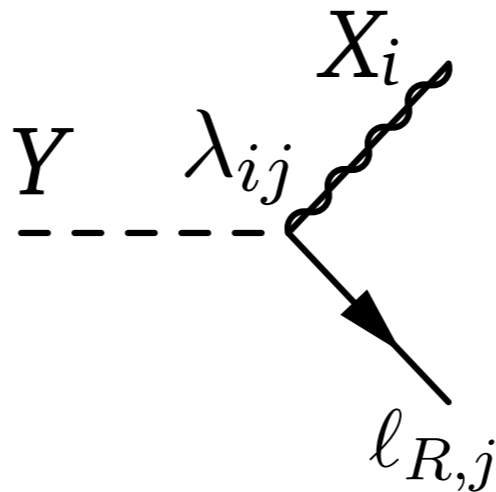
Link to baryogenesis



Charged mediator



Dark Matter Multiplet

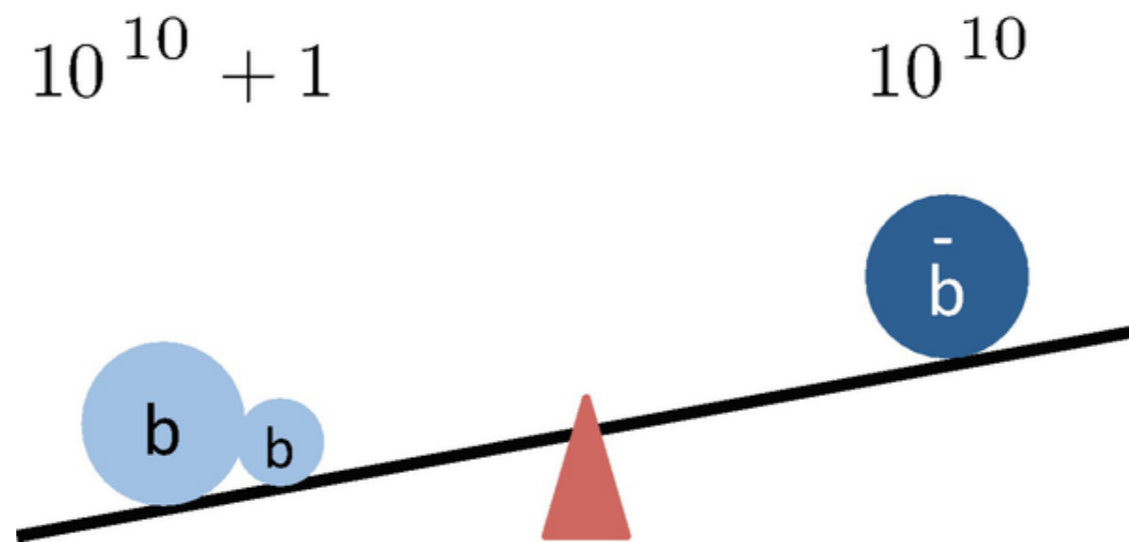


Motivation:

Simultaneously explain dark matter and baryon asymmetry
via *conversion-driven leptogenesis*

[JH 2404.12428]

Baryon asymmetry

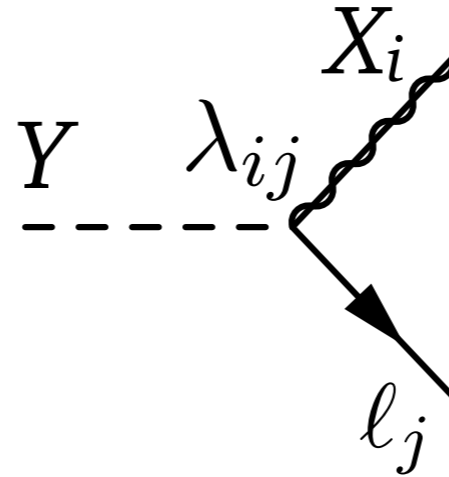


Fuyuto 2018

Sakharov conditions:

- C/CP -violation
- Baryon number violation
- Out-of-equilibrium processes

New source of CP -violation



$\lambda \sim 10^{-6}$: large CP -phases allowed

Not challenged by constraints from
charge lepton flavor violation and EDMs

Baryon number violation

In SM, sphaleron processes violate B by washing out $B + L$

$B - L$ effectively conserved at TeV scale

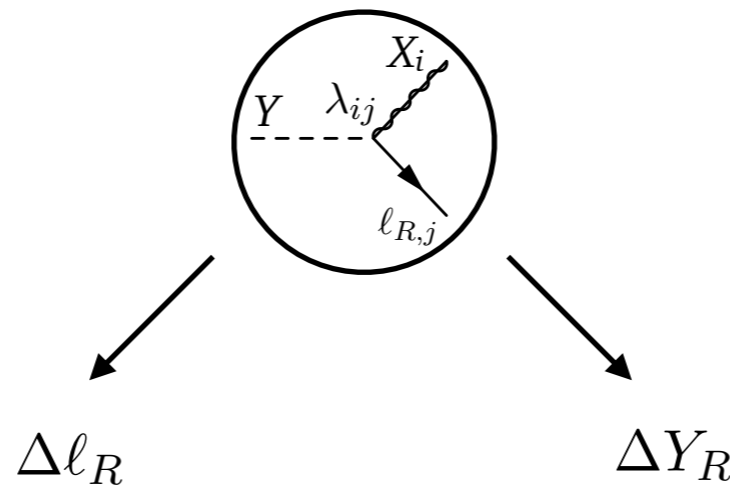
Used in leptogenesis: break $L \Rightarrow \Delta L \rightarrow \Delta B$

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Conversion-driven leptogenesis w/o need to break L



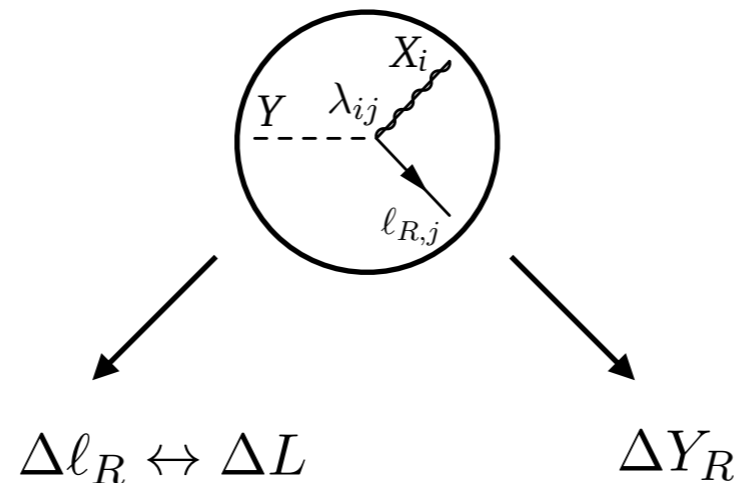
$$\Delta\ell_{R,j} = -\Delta Y_R$$

Baryon number violation

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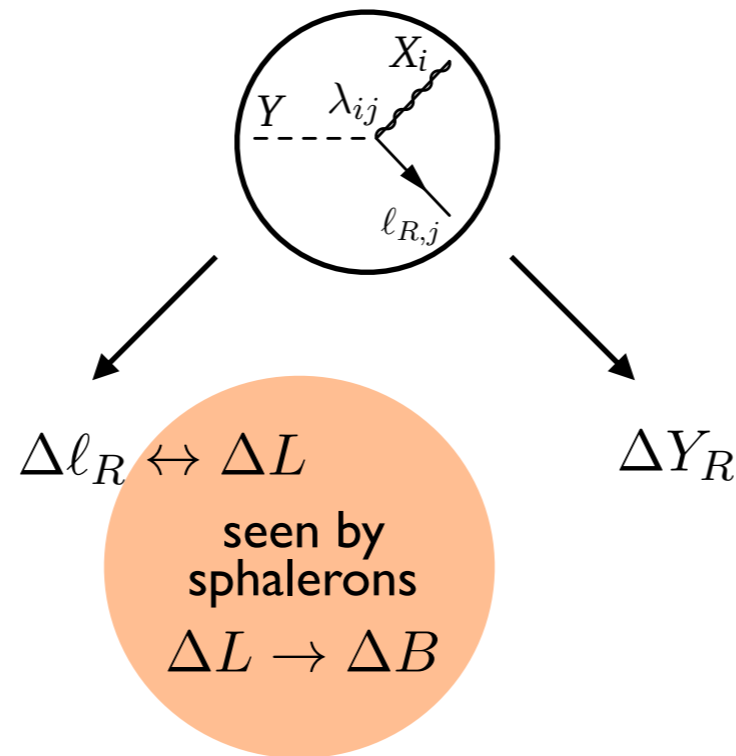


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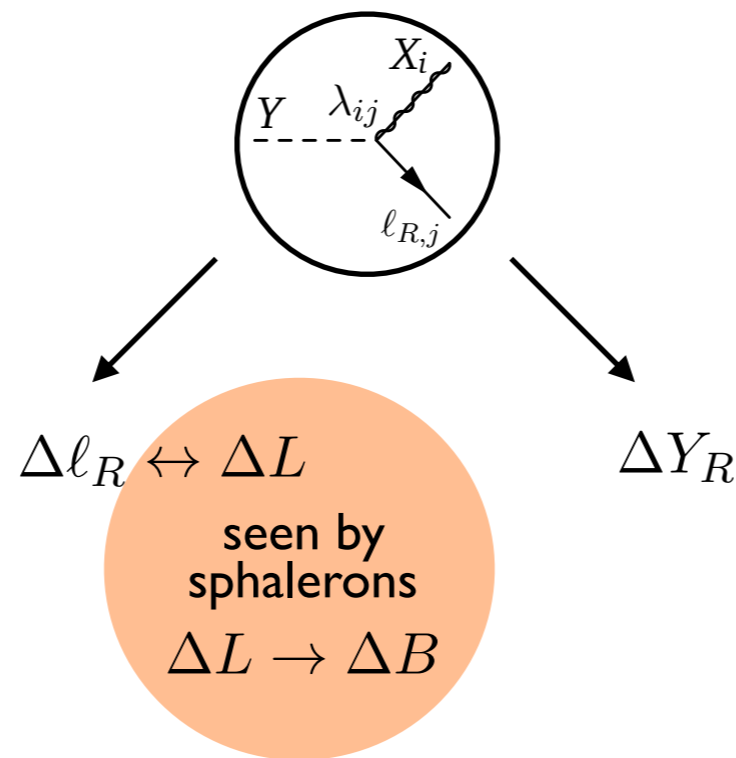
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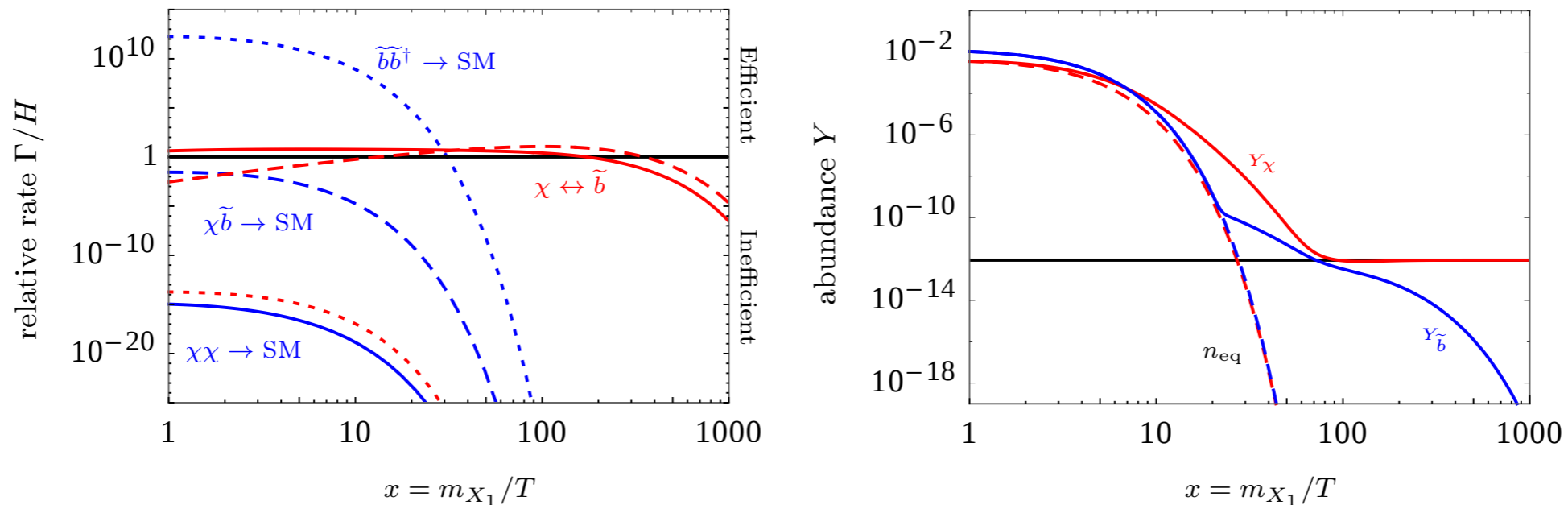
Conversion-driven leptogenesis w/o need to break L



Similar to Dirac leptogenesis
[Dick, Lindner, Ratz, Wright, 2000]

Out-of-equilibrium processes

Conversion rates: shallower in $1/T$ than annihilations, early departure from equilibrium

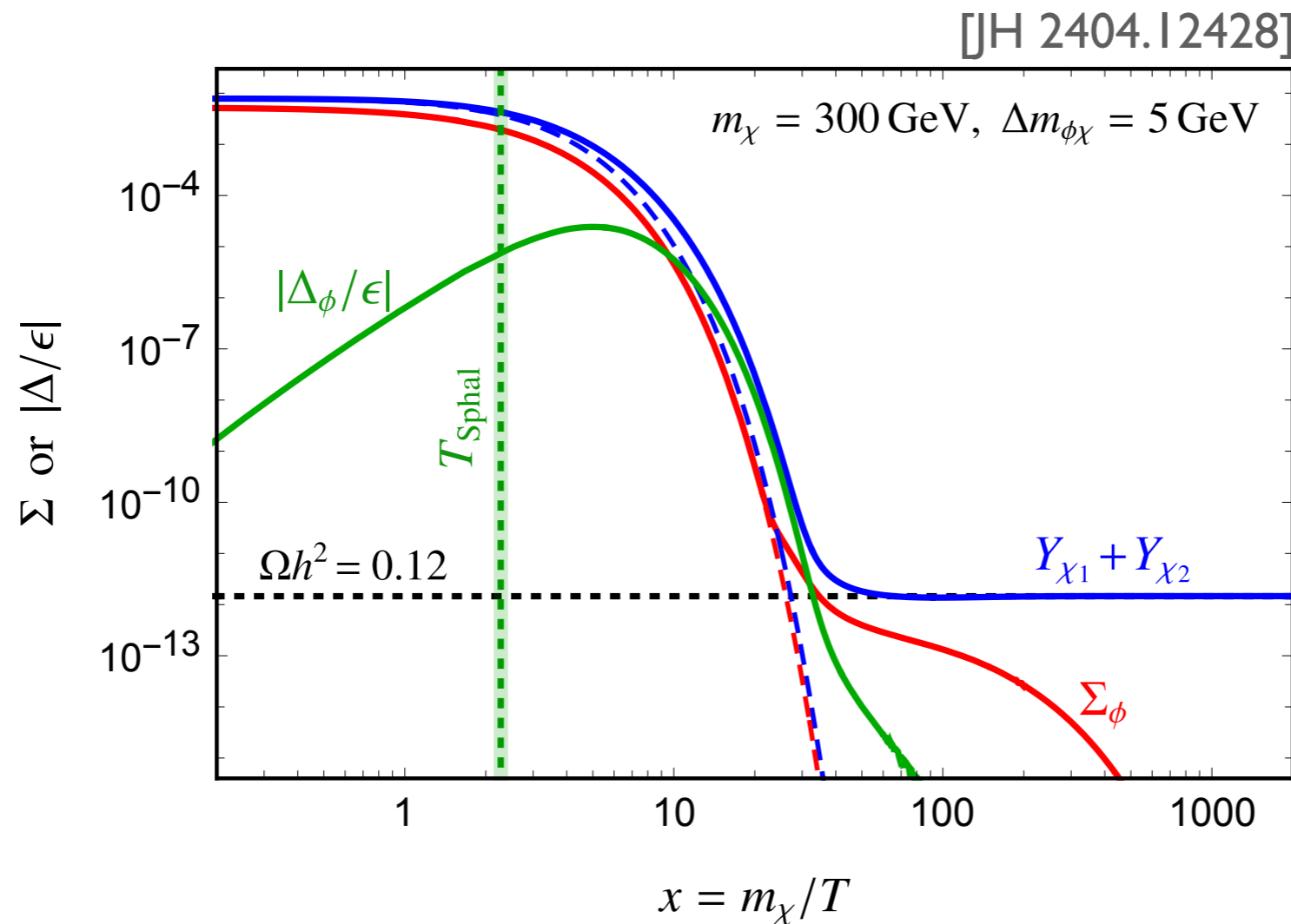


abundances still large \Rightarrow sizeable asymmetries!

$$(\text{Source term of } \Delta_Y) \propto \left(Y_Y - Y_Y^{\text{eq}} \frac{Y_{\chi_i}}{Y_{\chi_i}^{\text{eq}}} \right)$$

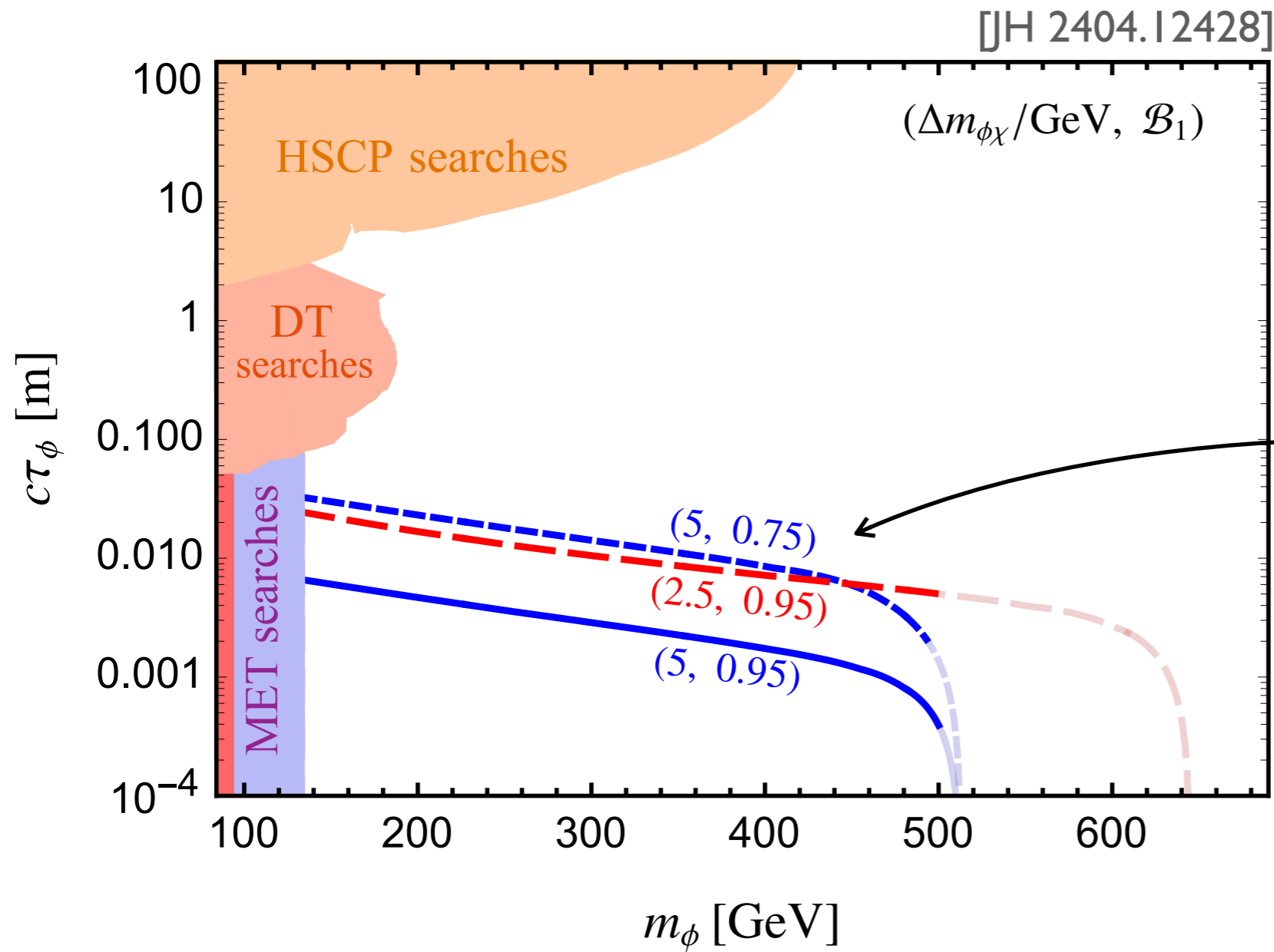
Abundances and asymmetry

Viable parameter point yielding $\Omega h^2 = 0.12, Y_{\Delta B} = 0.9 \times 10^{-10}$
for quasi mass-degenerate X_i



[CP-asymmetry in resonant scenario: Hambye, Teresi 2016;
Frossard, Garny, Hoheneegger, Kartavtsev, Mitrouskas 2013]

Testability at colliders

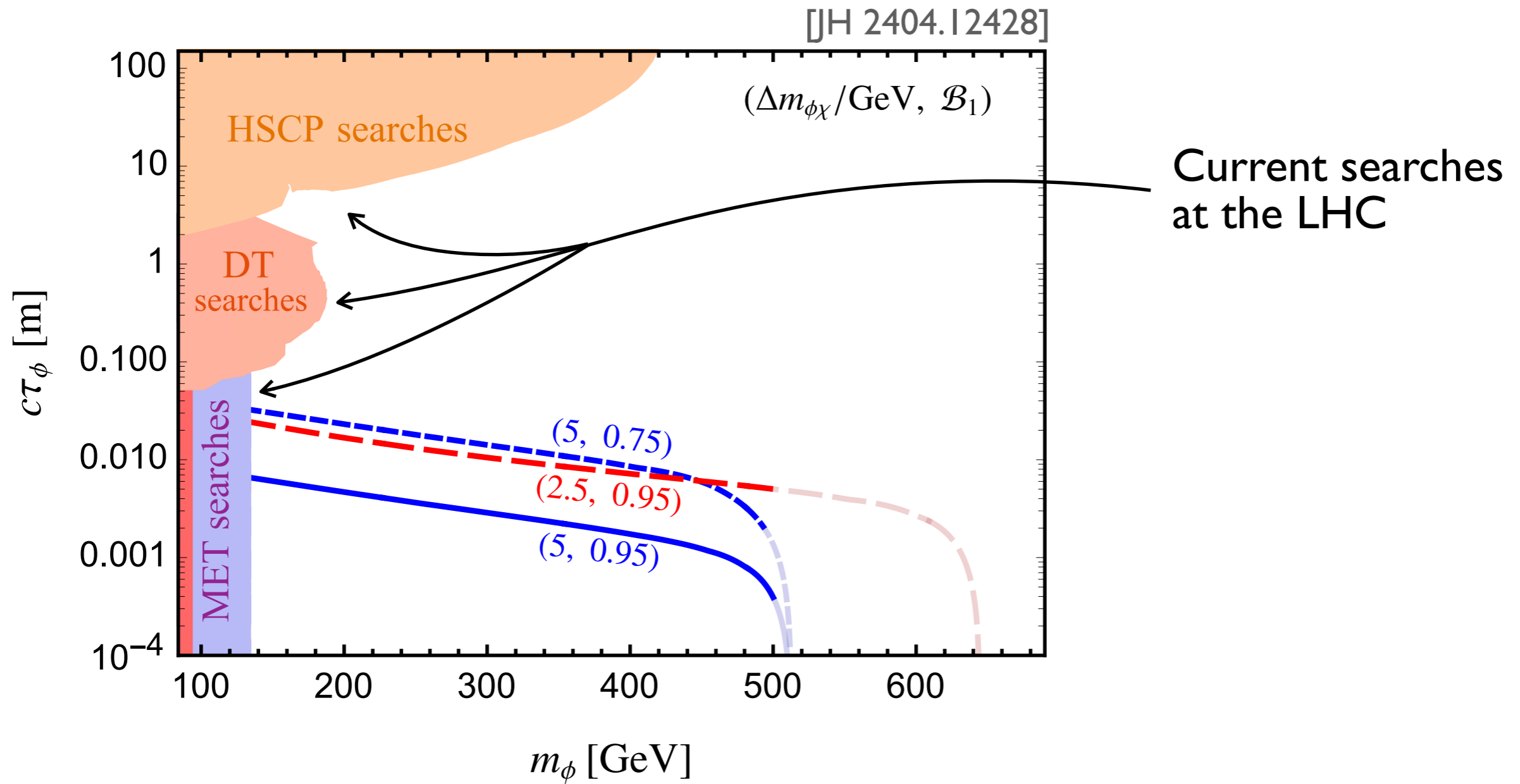


Parameter
slices yielding:

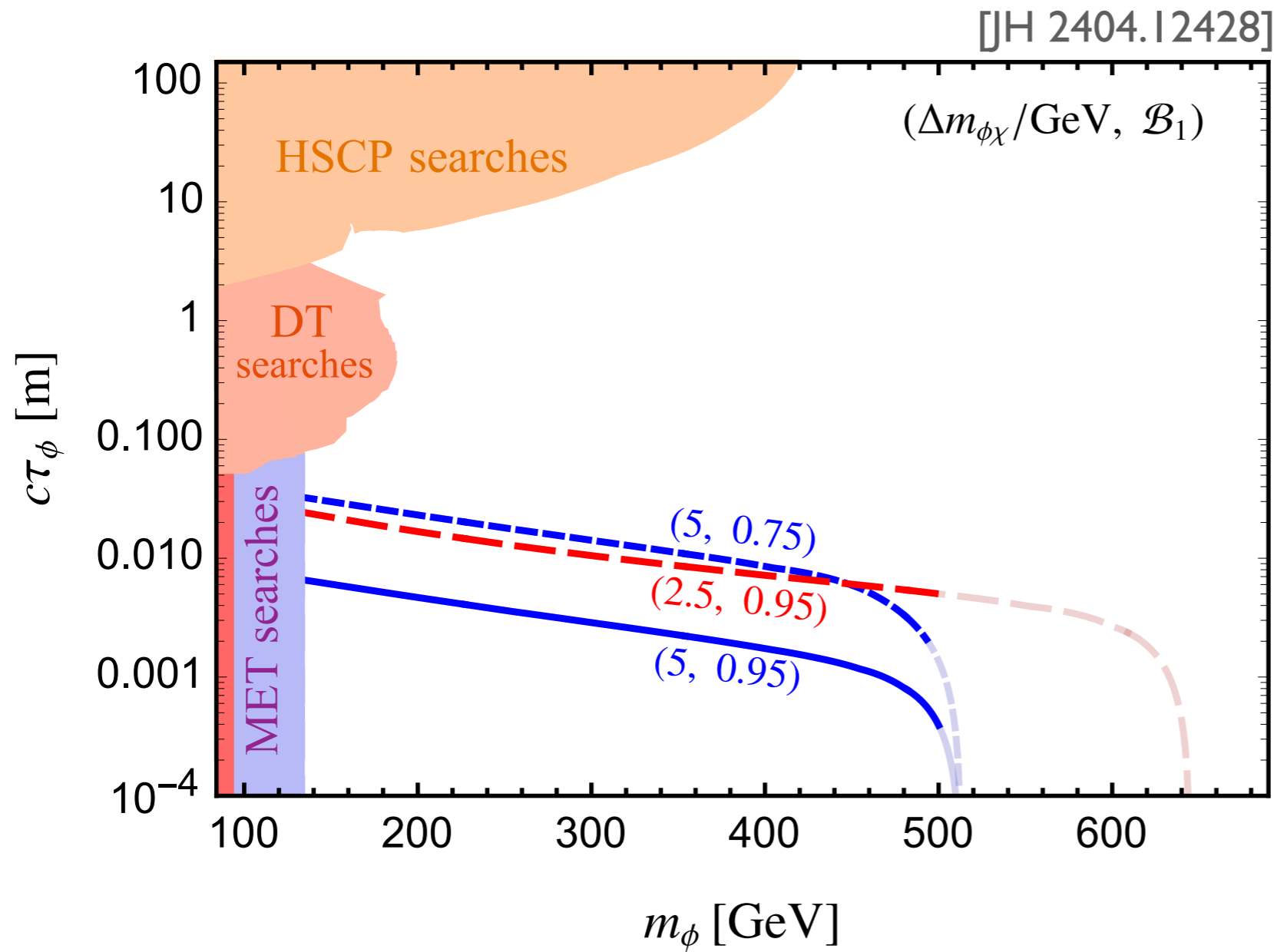
$$\Omega h^2 = 0.12$$

$$Y_{\Delta B} = 0.9 \times 10^{-10}$$

Testability at colliders



Testability at colliders



Displaced leptons?

$p_T > 65$ GeV

[ATLAS 2011.07812]

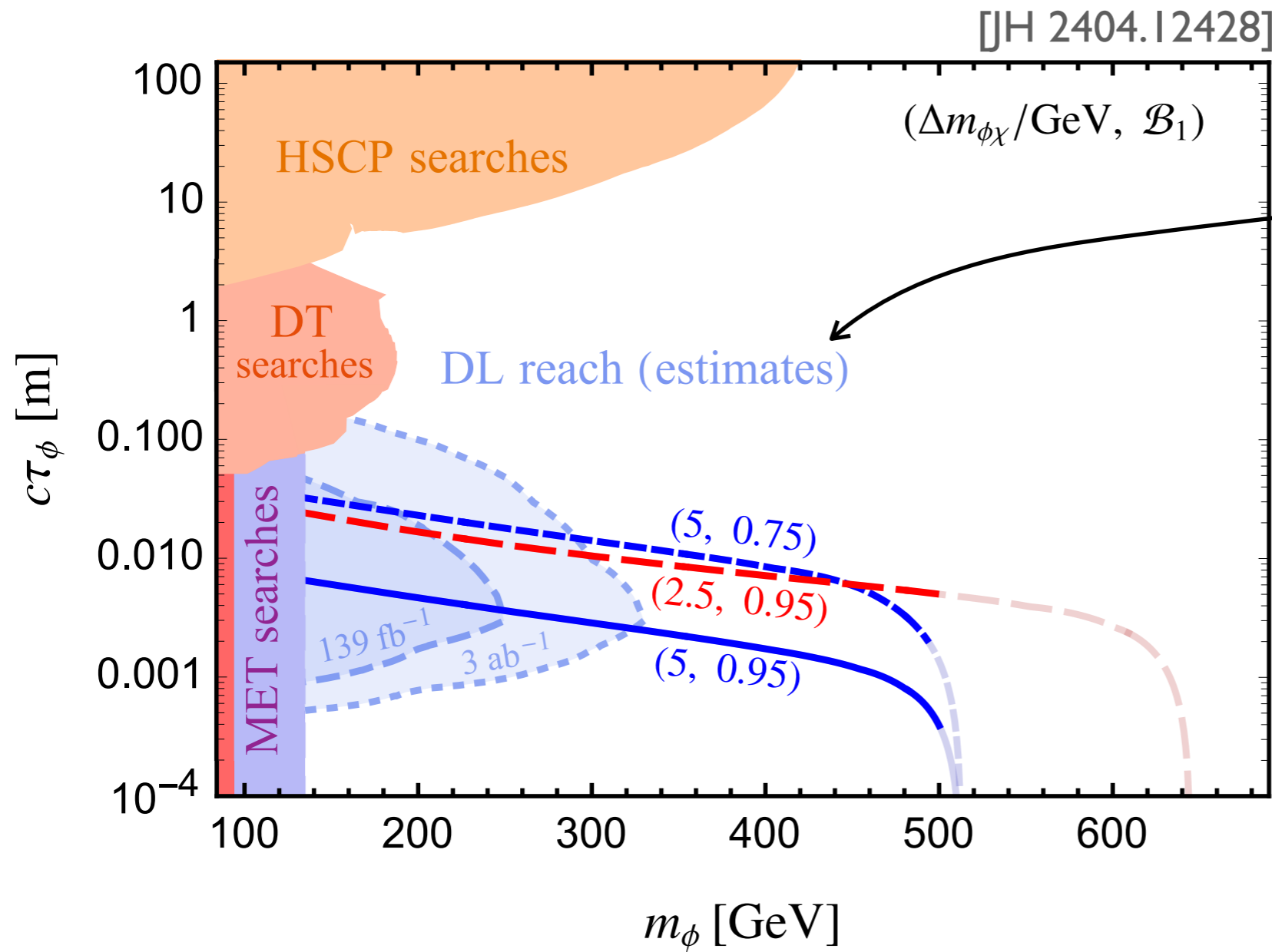
or dileptons with

$p_T > 20$ GeV,

$m_{\text{inv}} > 200$ GeV

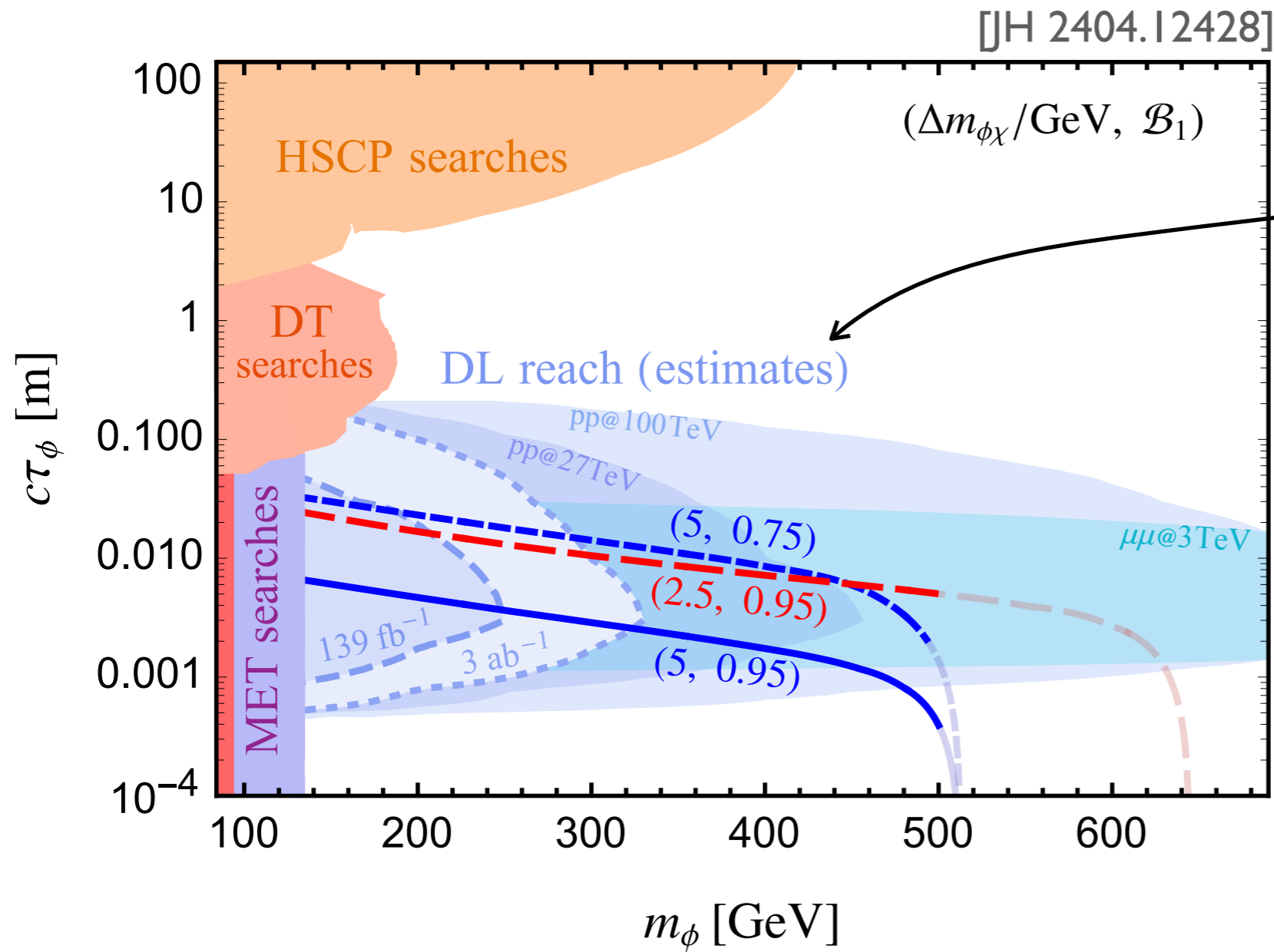
[ATLAS 2305.02005]

Testability at colliders



Assuming similar background reduction with $p_T > 10 \text{ GeV}$ but exploiting MET (maybe timing?)

Testability at colliders



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Conclusion



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Conclusion



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 - soft displaced objects not well covered yet
 \Rightarrow prime target for future investigations
- Conversion-driven leptogenesis:
 - asymmetry in mediator abundance hidden
 - early out-of-equilibrium provides large asymmetries
 - testable at colliders

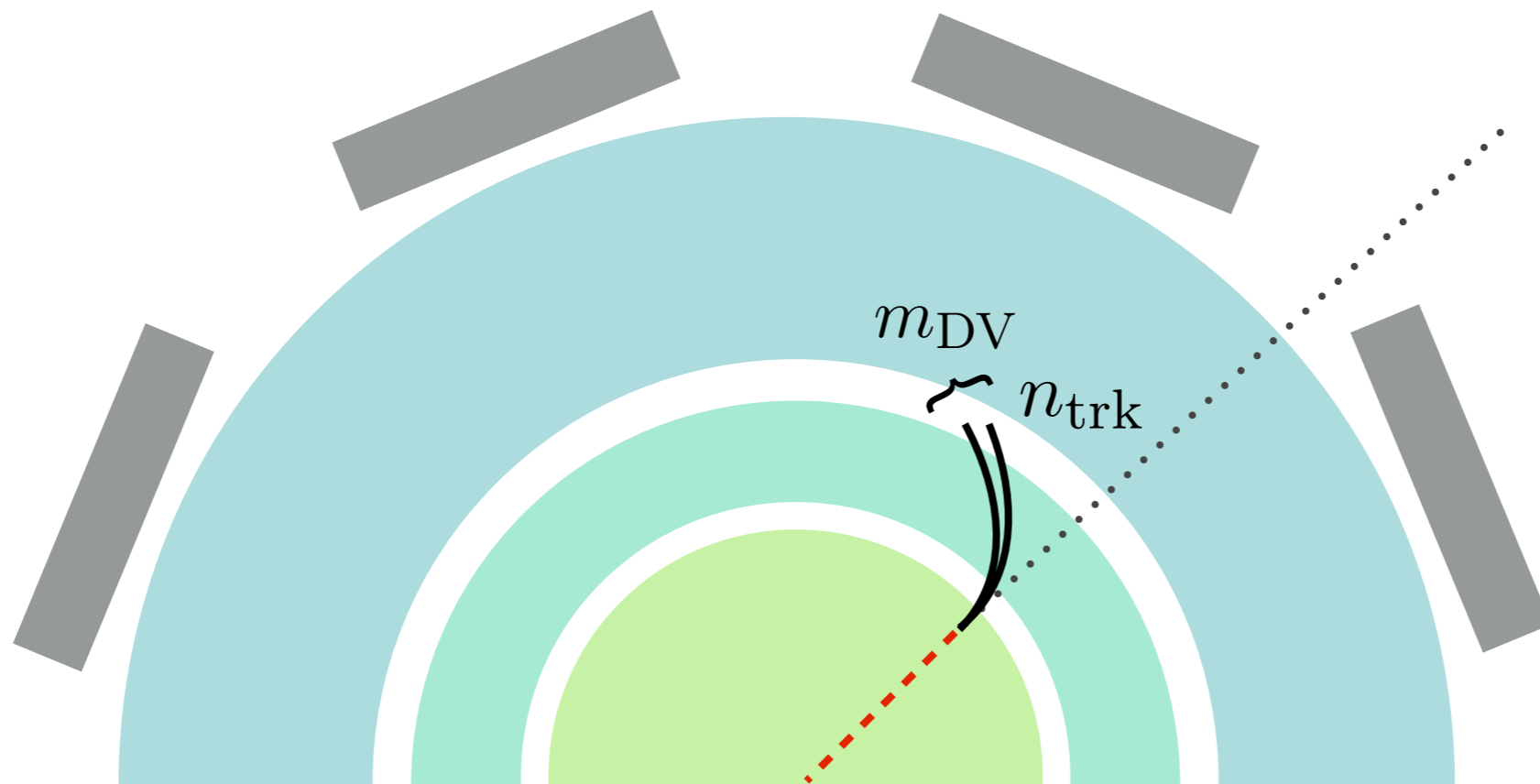
Backup slides

Potential of displaced vertices search

[ATLAS-SUSY-2016-08, 1710.04901]

Search requires:

- Number of displaced tracks: $n_{\text{trk}} \geq 5$
- Invariant mass of displaced vertex: $m_{\text{DV}} > 10 \text{ GeV}$

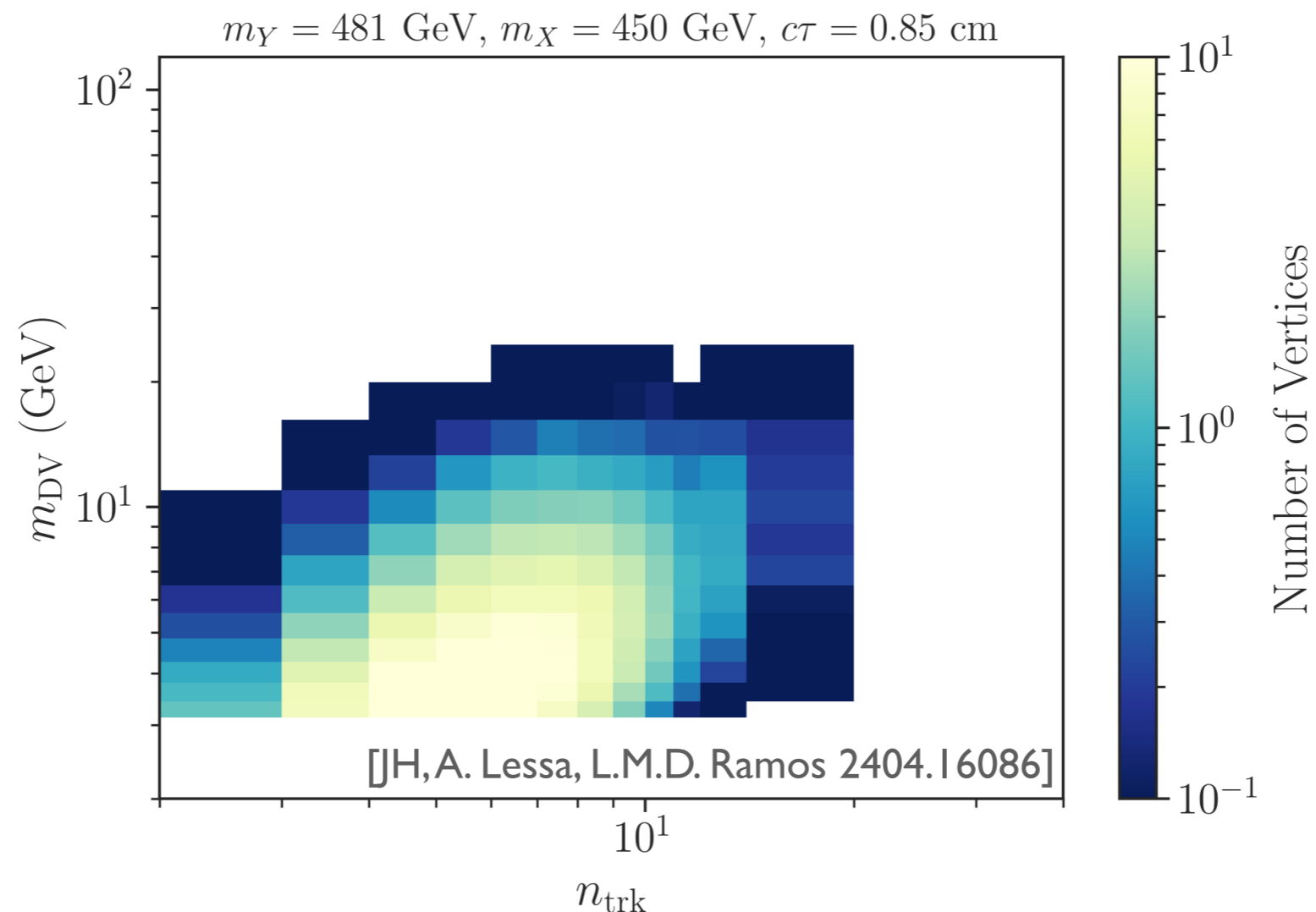


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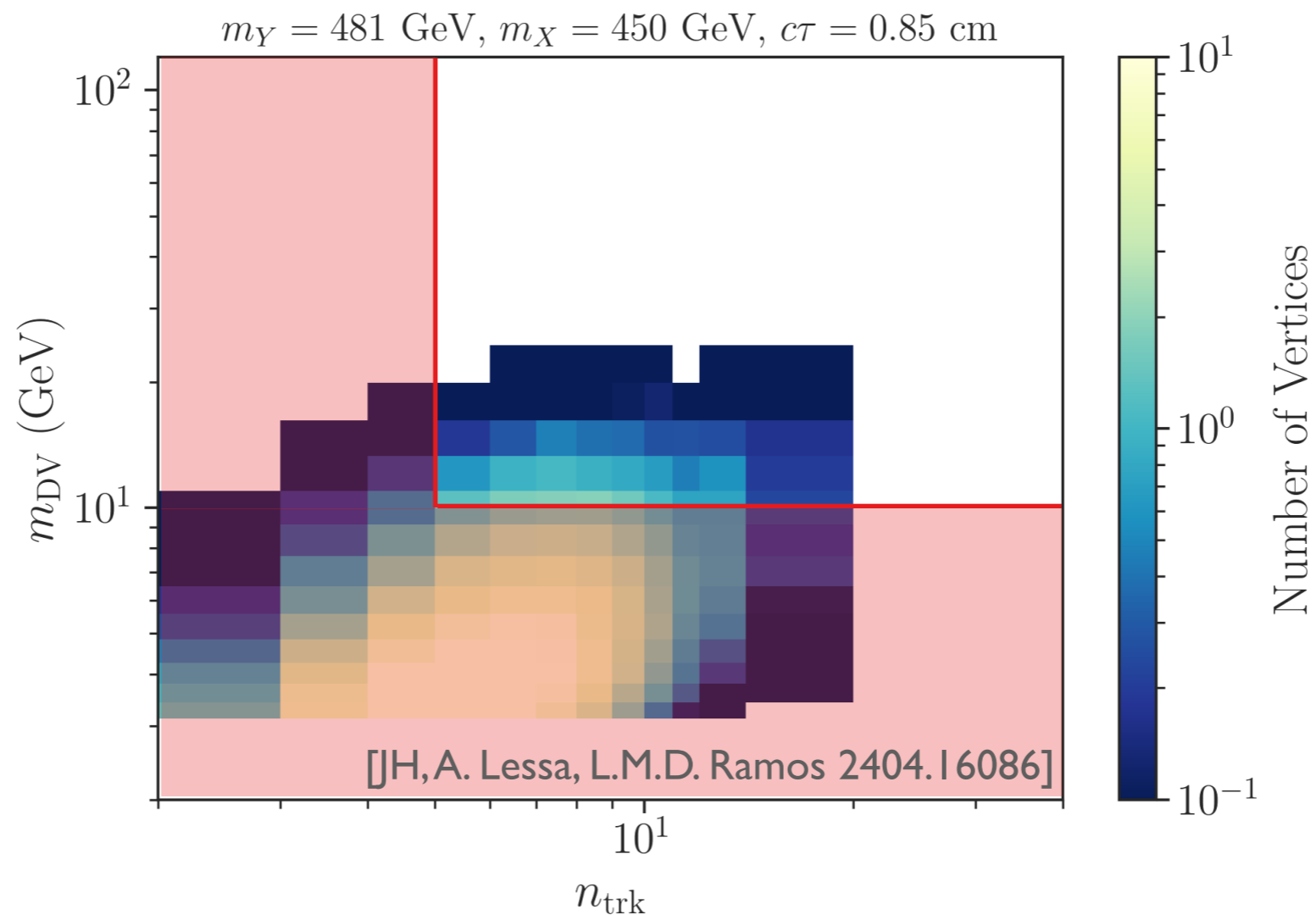


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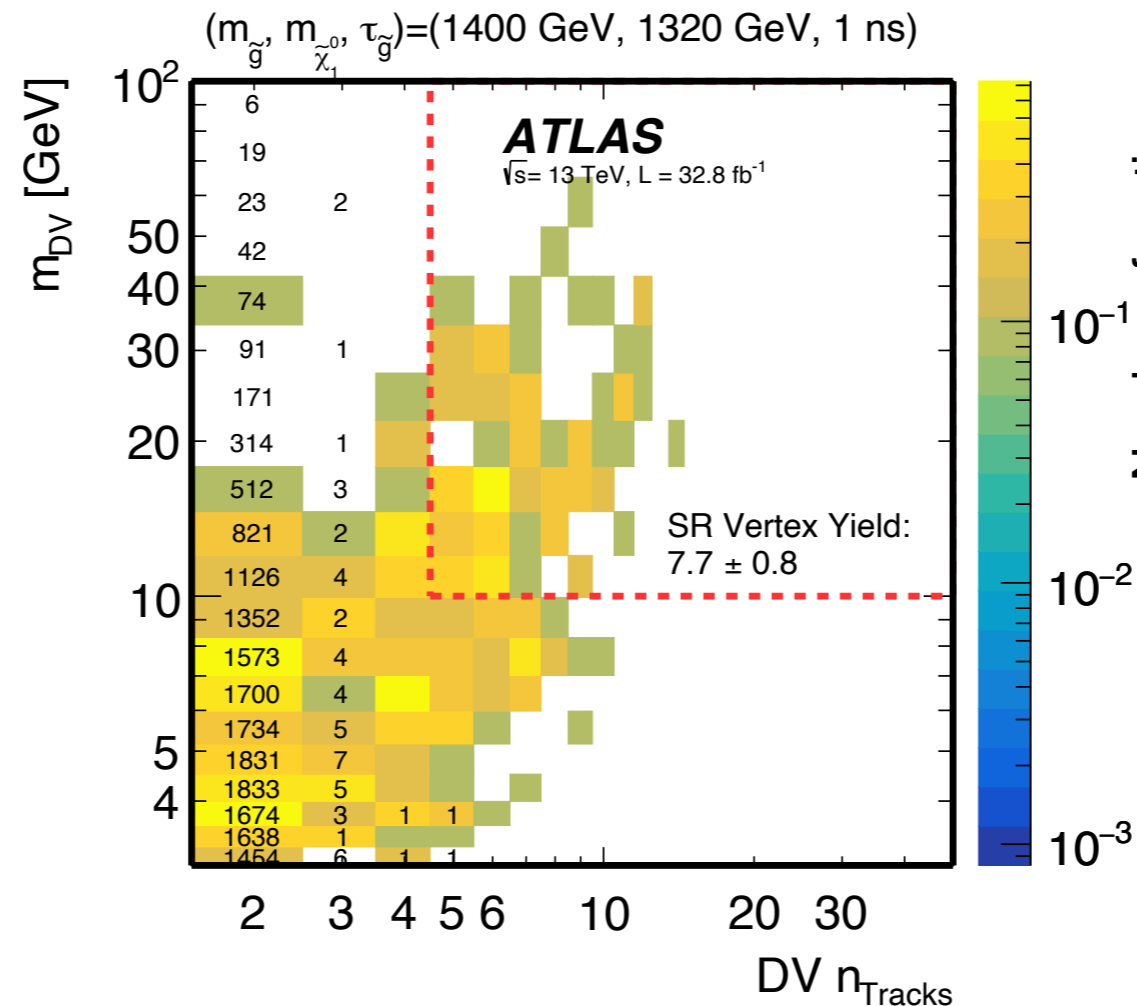


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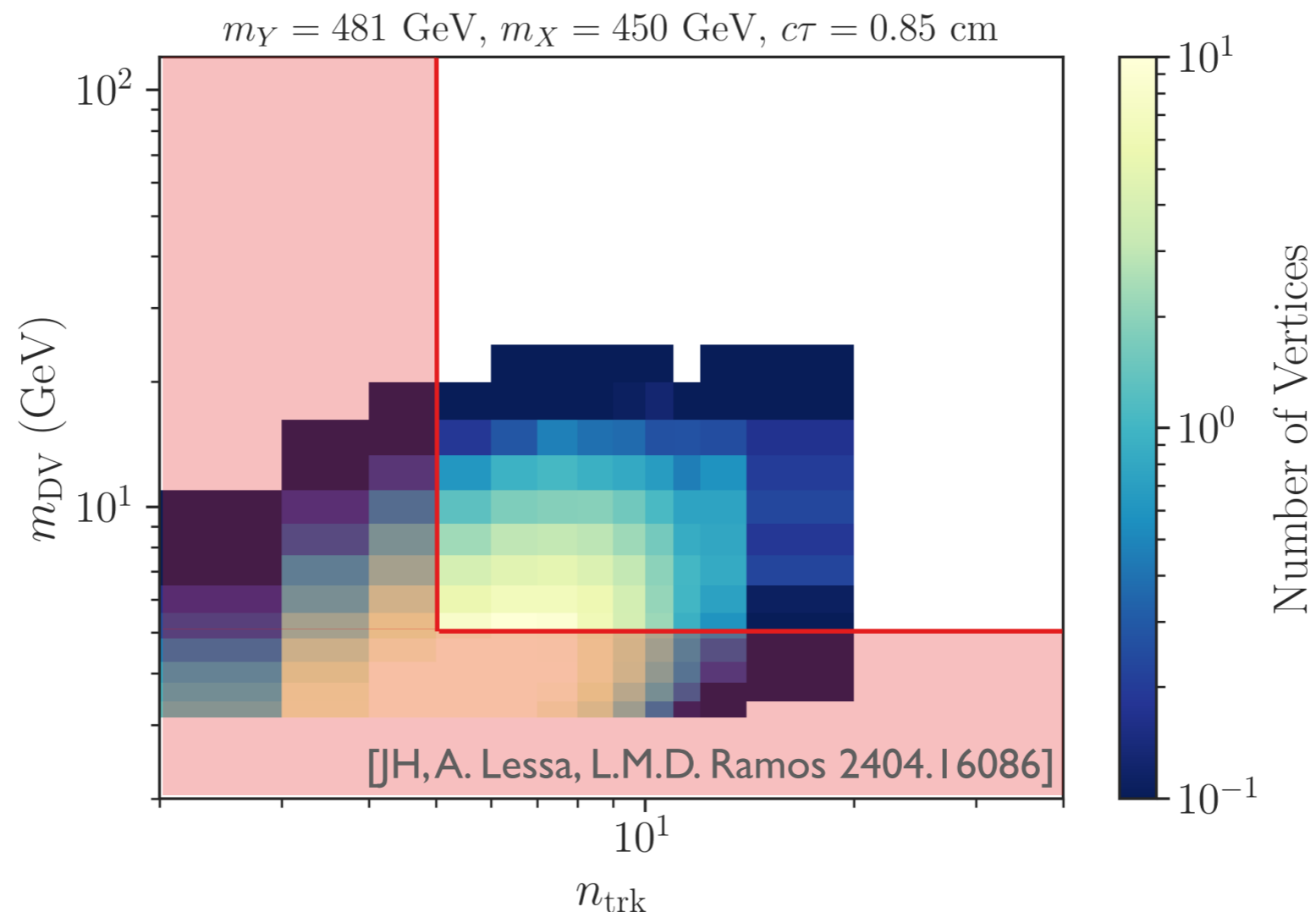


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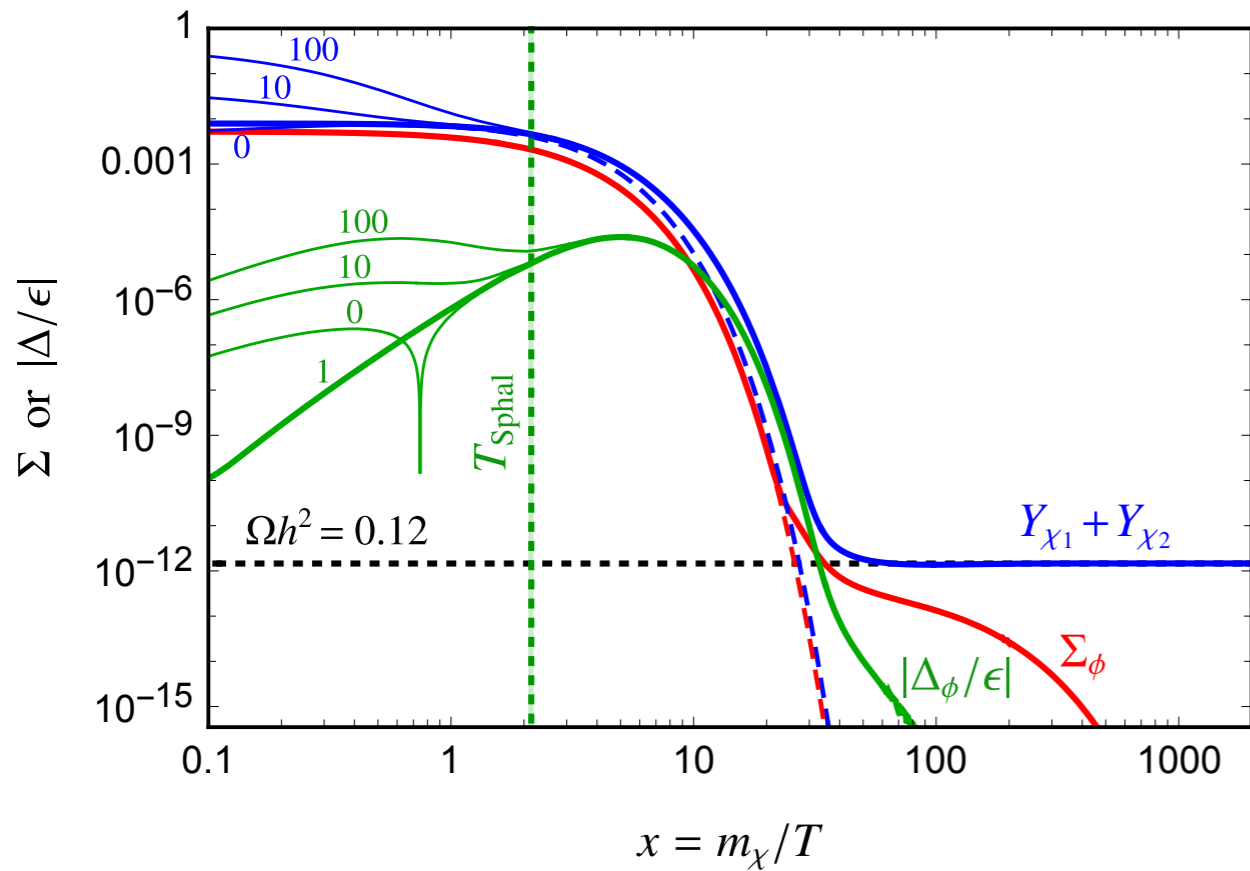
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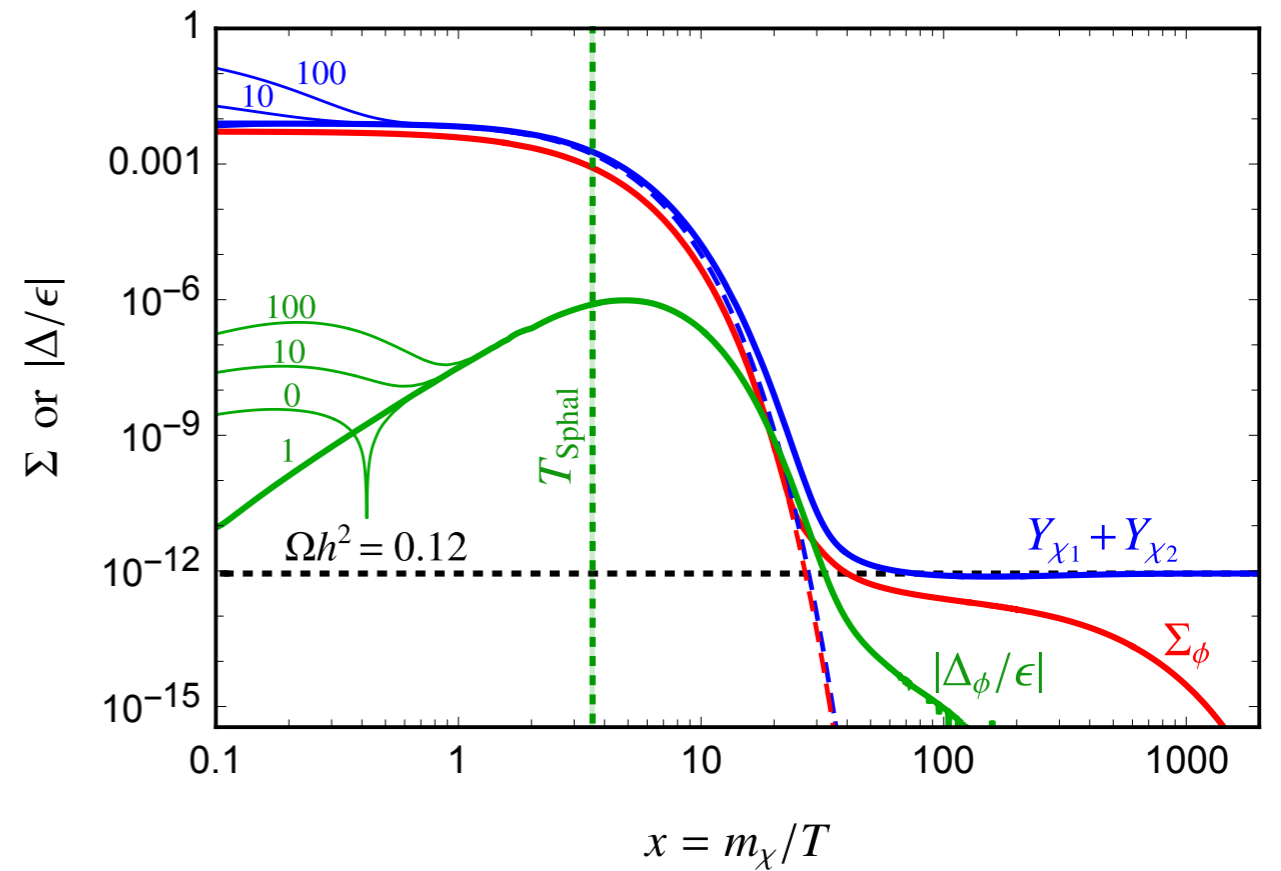


Dependence on initial conditions

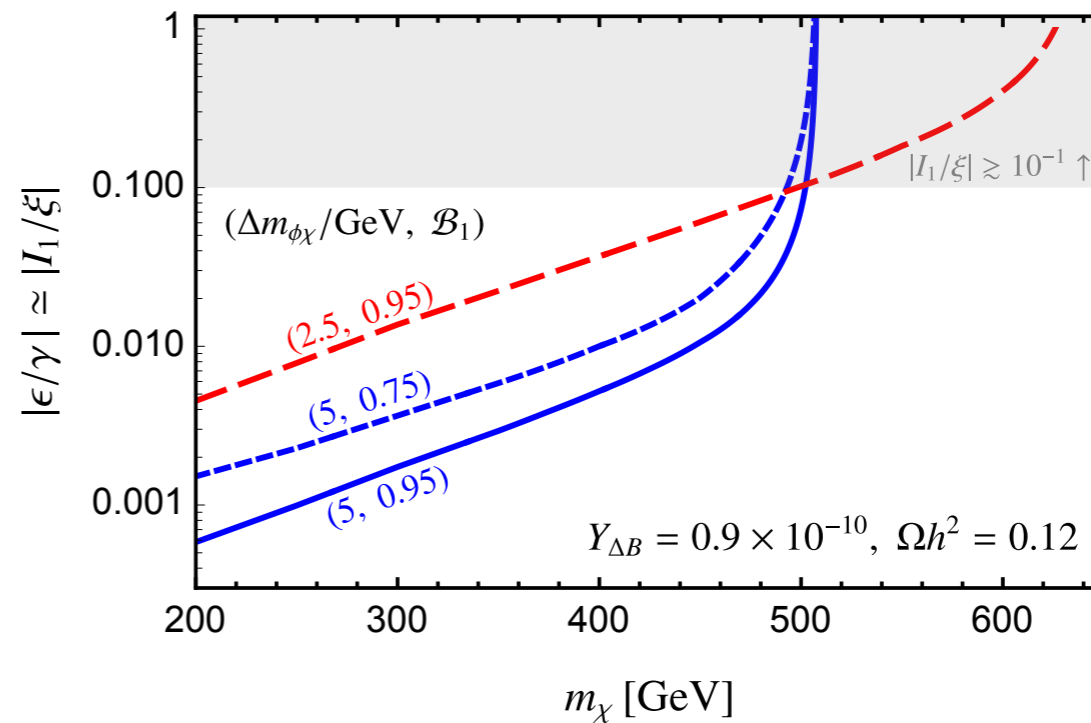
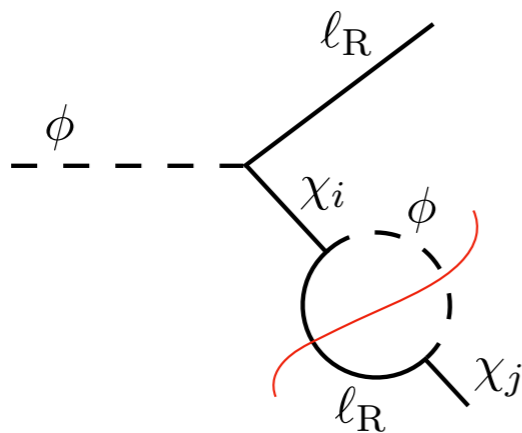
$m_\chi = 300 \text{ GeV}, \Delta m_{\phi\chi} = 5 \text{ GeV}$



$m_\chi = 500 \text{ GeV}, \Delta m_{\phi\chi} = 2.5 \text{ GeV}$



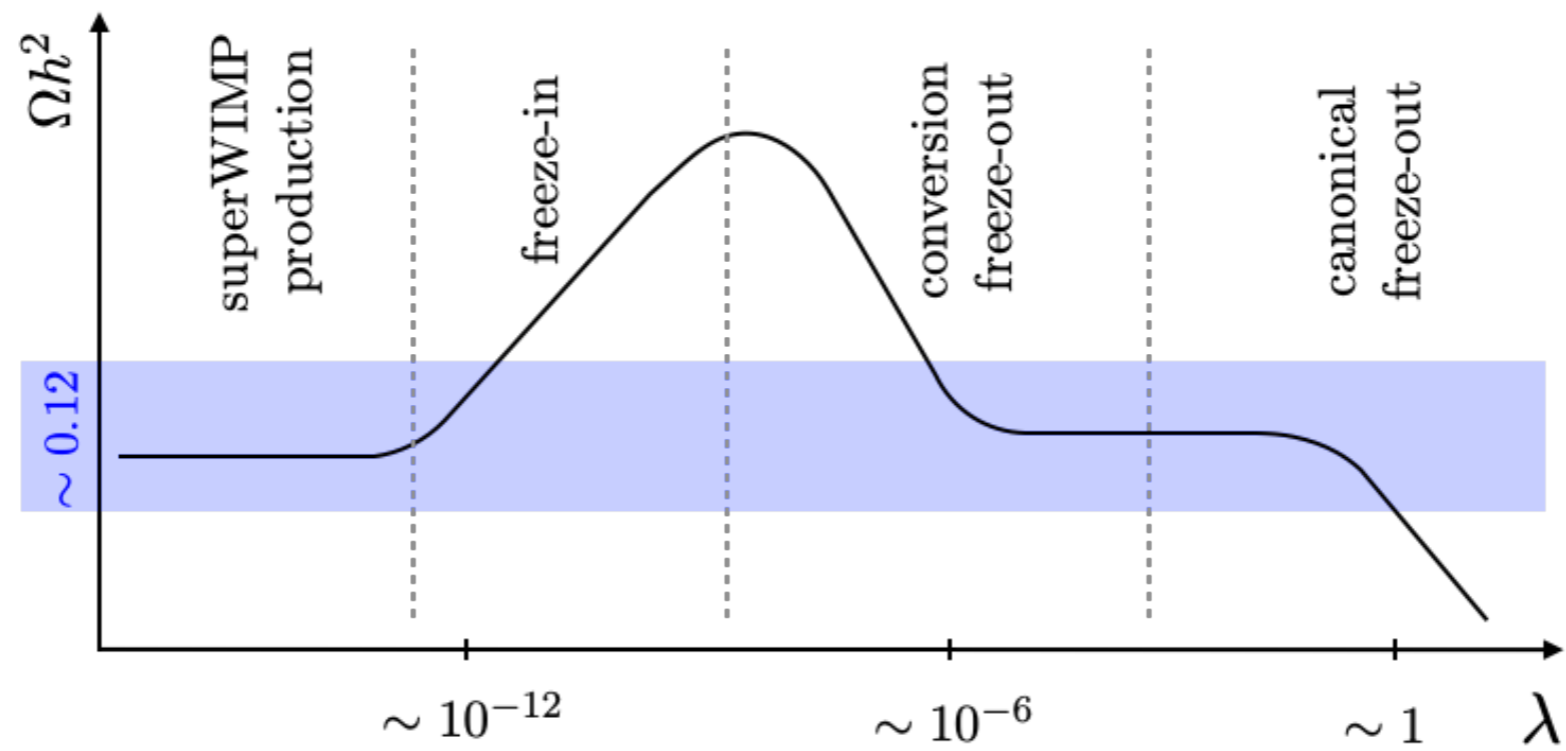
CP-asymmetry



[CP-asymmetry in resonant scenario: Hambye, Teresi 2016;
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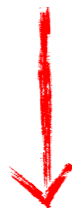
$$I_1 = \Im[(\lambda^\dagger \lambda)_{12}^2] / (|\lambda^\dagger \lambda|_{11} |\lambda^\dagger \lambda|_{22}), \quad \xi = 2\Delta m_{12} / \Gamma_{\chi_2}^0$$

Cosmologically viable regions



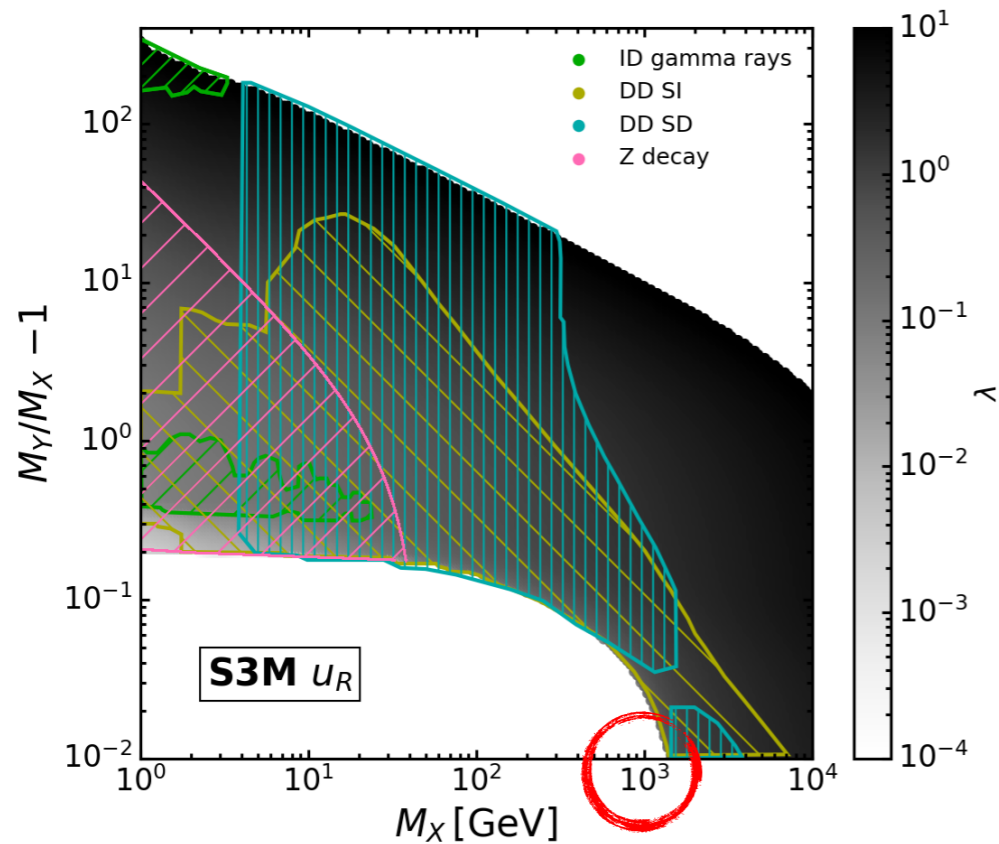
Testability

masses: few TeV
 \Rightarrow testable at colliders



Minimal t-channel models
 thermalised DM:

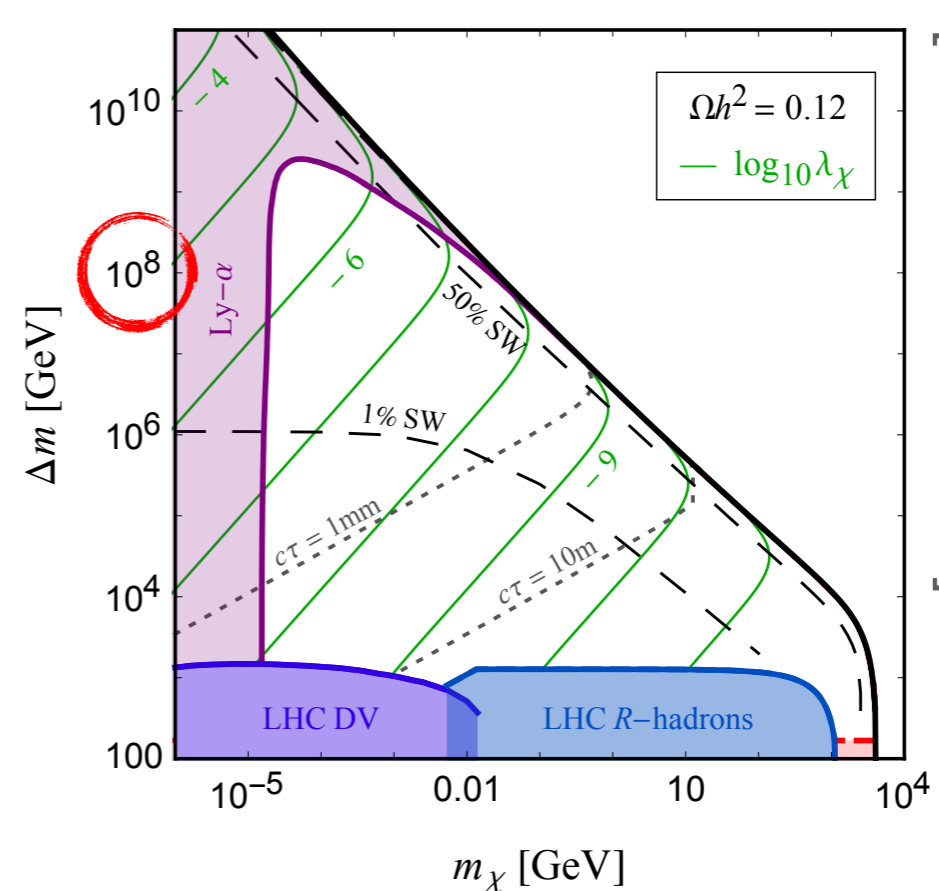
[Arina et al. 2307.10367]



masses up to 10^9 GeV
 \Rightarrow mostly out of reach



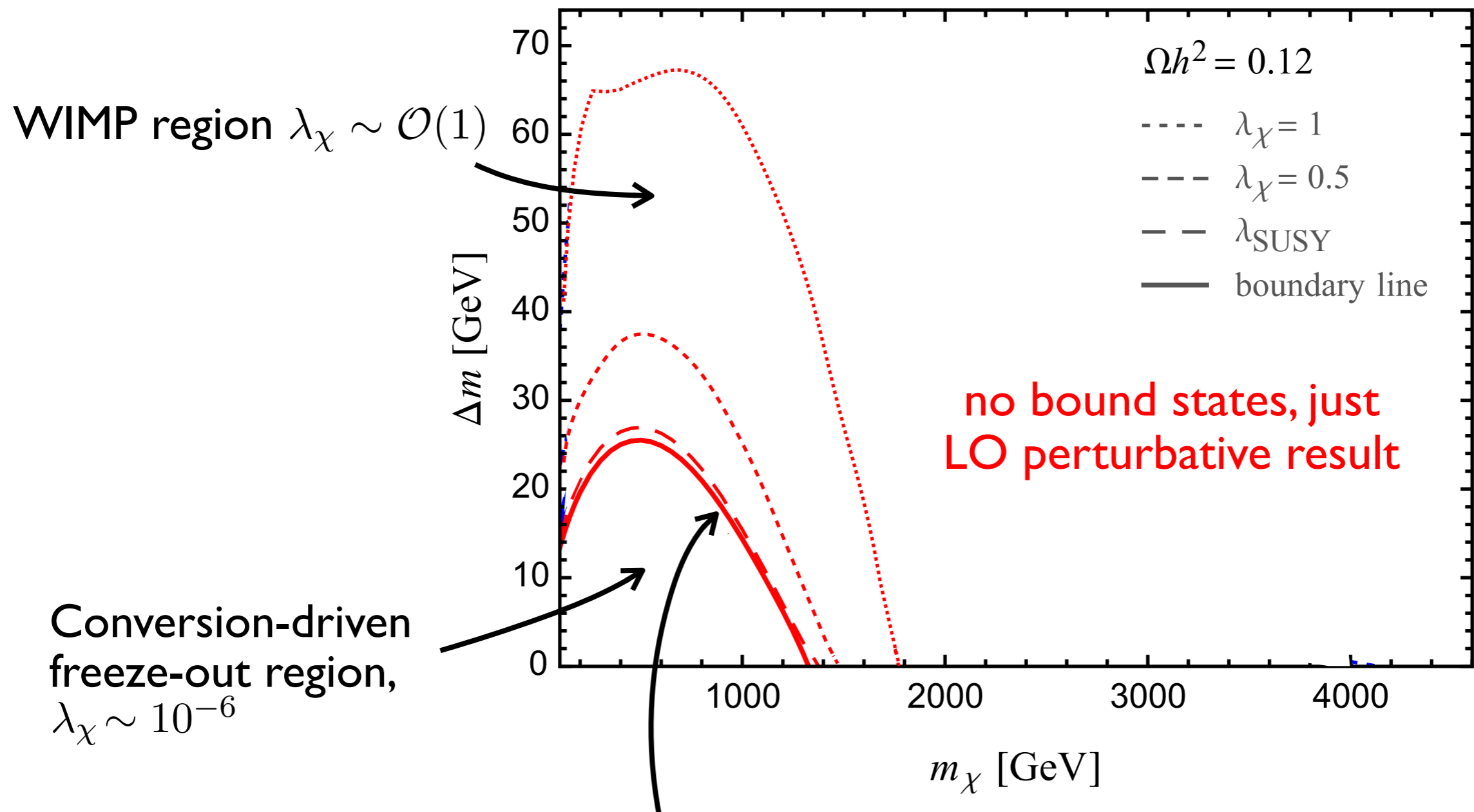
Minimal t-channel models
 non-thermalised DM:



[Decant et al. 2111.09321]

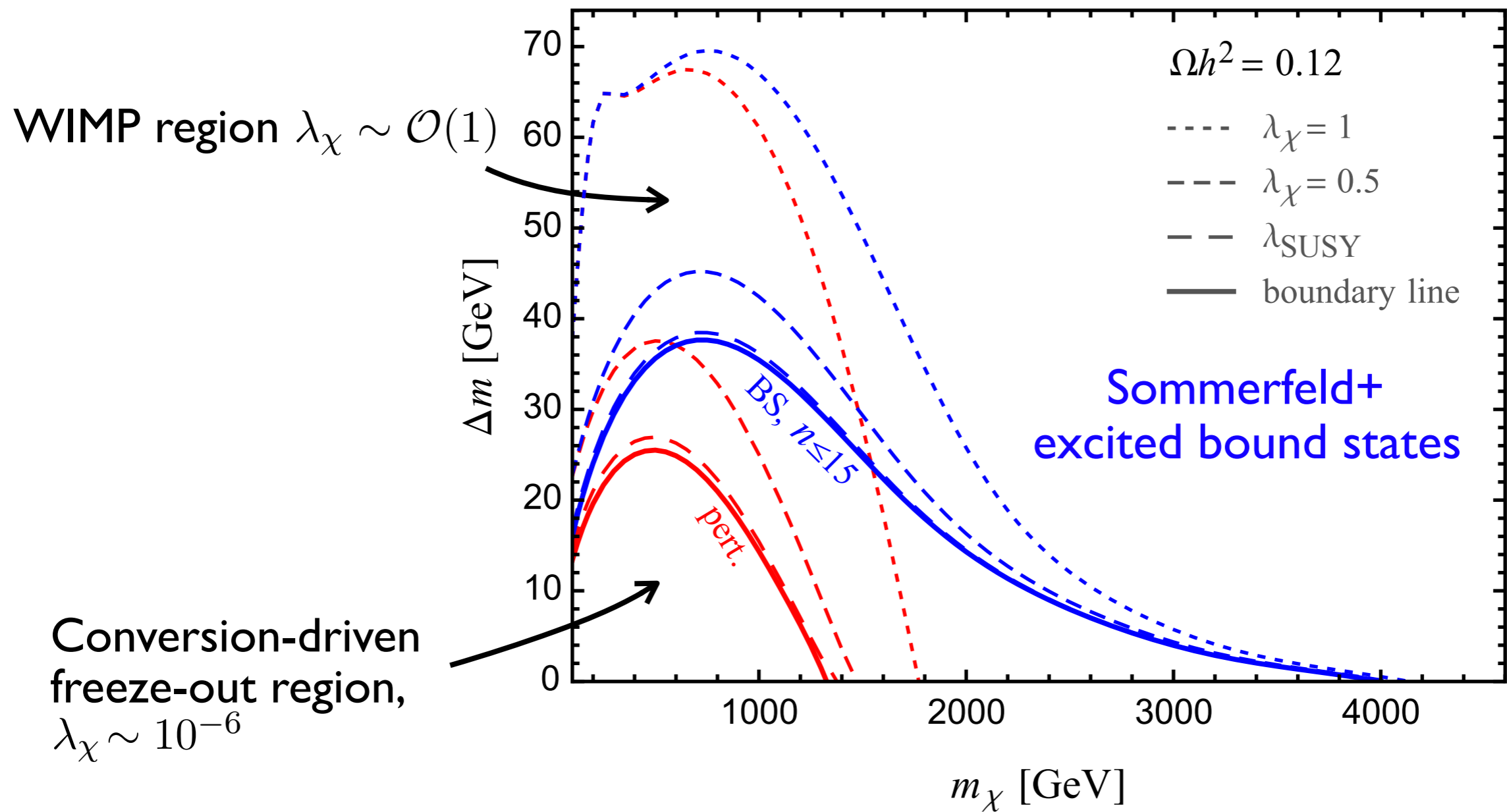
Bound state effects on the parameter space

[Garny, JH 2112.01499]



Bound state effects on the parameter space

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here: no transition limit

Boltzmann equations with excitations

[Binder Filimonova, Petraki, White 2112.00042; Garny, JH 2112.01499]

X pair-annihilation
(hard process+Sommerfeld)

Bound state formation

$$X : \frac{dY_X}{dx} = \frac{1}{3Hs} \frac{ds}{dx} \left[\frac{1}{2} \langle \sigma_{XX^\dagger v} \rangle (Y_X^2 - Y_X^{\text{eq}2}) + \sum_i \frac{1}{2} \langle \sigma_{\text{BSF},i v} \rangle \left(Y_X^2 - Y_X^{\text{eq}2} \frac{Y_{\mathcal{B}_i}}{Y_{\mathcal{B}_i}^{\text{eq}}} \right) \right]$$

$$X : \frac{dY_{\mathcal{B}_i}}{dx} = \frac{1}{3Hs} \frac{ds}{dx} \left[\Gamma_{\text{ion}}^i \left(Y_{\mathcal{B}_i} - Y_{\mathcal{B}_i}^{\text{eq}} \frac{Y_X^2}{Y_X^{\text{eq}2}} \right) + \Gamma_{\text{dec}}^i (Y_{\mathcal{B}_i} - Y_{\mathcal{B}_i}^{\text{eq}}) - \sum_{j \neq i} \Gamma_{\text{trans}}^{j \rightarrow i} \left(Y_{\mathcal{B}_j} - Y_{\mathcal{B}_i} \frac{Y_{\mathcal{B}_j}^{\text{eq}}}{Y_{\mathcal{B}_i}^{\text{eq}}} \right) \right]$$

=0

Ionization

Decay

Bound-to-bound
transition

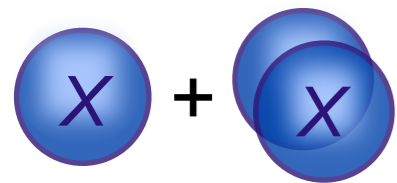
steady-state

Solve for $Y_{\mathcal{B}_i}$ algebraically \rightarrow system of linear equations

[cf. Ellis, Luo, Olive 1503.07142;
Mitridate, Redi, Smirnov, Strumia 1702.01141]

Boltzmann equations with excitations

[Binder Filimonova, Petraki, White 2112.00042; Garny, JH 2112.01499]



$$: \frac{dY_X}{dx} = \frac{1}{3Hs} \frac{ds}{dx} \frac{1}{2} \langle \sigma_{XX^\dagger v} \rangle_{\text{eff}} \left(Y_X^2 - Y_X^{\text{eq}2} \right)$$

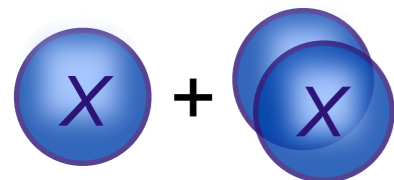
$$\langle \sigma_{XX^\dagger v} \rangle_{\text{eff}} = \langle \sigma_{XX^\dagger v} \rangle + \sum_i \langle \sigma_{\text{BSF},i v} \rangle R_i, \quad 0 \leq R_i \leq 1$$

Contains all rates

[cf. Ellis, Luo, Olive 1503.07142;
Mitridate, Redi, Smirnov, Strumia 1702.01141]

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$$X + X : \frac{dY_X}{dx} = \frac{1}{3Hs} \frac{ds}{dx} \frac{1}{2} \langle \sigma_{XX^\dagger v} \rangle_{\text{eff}} \left(Y_X^2 - Y_X^{\text{eq}2} \right)$$

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No transition limit:

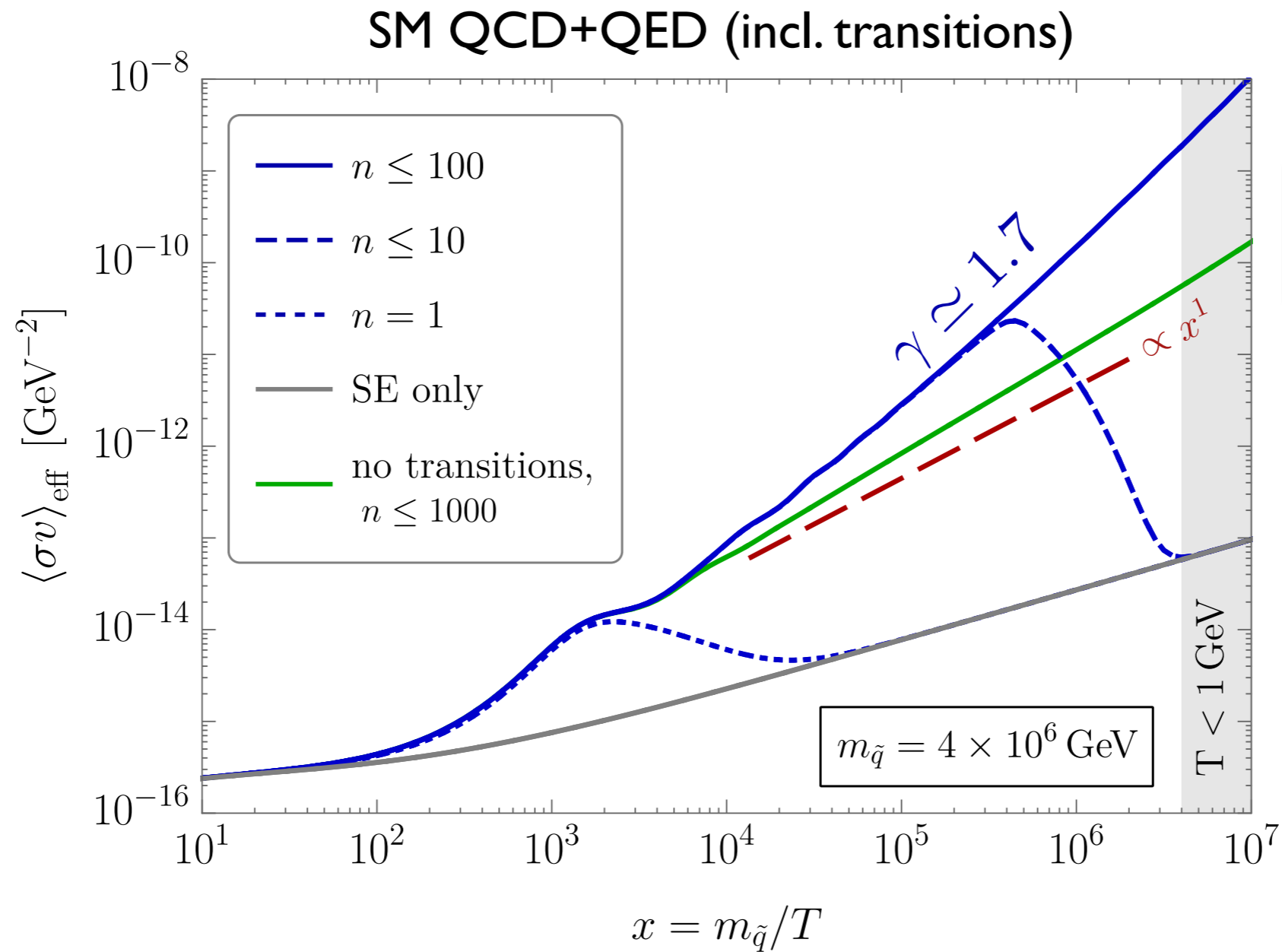
$$\langle \sigma_{XX^\dagger v} \rangle_{\text{eff}} = \langle \sigma_{XX^\dagger v} \rangle + \sum_i \underbrace{\langle \sigma_{\text{BSF},i v} \rangle \frac{\Gamma_{\text{dec}}^i}{\Gamma_{\text{ion}}^i + \Gamma_{\text{dec}}^i}}_{\Gamma_{\text{ion}}^i \gg \Gamma_{\text{dec}}^i}$$

$$\Gamma_{\text{ion}}^i \gg \Gamma_{\text{dec}}^i : \quad \propto e^{E_{B_i}/T} \Gamma_{\text{dec}}^i$$

[cf. Ellis, Luo, Olive 1503.07142;
Mitridate, Redi, Smirnov, Strumia 1702.01141]

Effective annihilation cross section

[Binder, Garny, JH, Lederer, Urban 2308.01336]



$$\langle \sigma v \rangle_{\text{eff}} \propto x^\gamma$$