# **Aspects of Models with Vector-Like Singlet Quarks**

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(2022) 4, 360; arXiv: 2304.10561, Vector-like Singlet Quarks: a Roadmap

- G. C. Branco **CFTP-ULisboa, IST** 
  - Talk given at

- Works done in collaboration with Francisco Albergaria, J. Alves, José Filipe Bastos, Francisco Botella,
- arXiv: 2307.13073; arXiv: 2103.13409, JHEP07 (2021)099; arXiv: 2111.15402, Eur Phys J. C. 82







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# European Union





# Possible motivations to introduce isosinglet vector-like quarks

Vector-like fermions arise for instance in grand unified models

Naturally small violation of 3x3 unitarity of the VCKM and non-vanishing but naturally suppressed flavour-changing r (FCNC)

This opens up many interesting possibilities for rare K and B decays as well as CP asymmetries in neutral B dec

Adding isosinglet quarks to the SM leads to new sources of CP violation

In particular one may achieve spontaneous CP violation in this framework with the addition of a complex scalar singlet to the Higgs sector

Possibility of solving the strong CP problem a la Barr and Nelson

Possibility of having a Common Origin for all CP Violations

Bento, Branco, Parada, 1991

Branco, Parada, MNR, 2003



# Fundamental properties of the CKM matrix

G. C Branco, L. Lavoura, J. P. Silva "CP Violation" Oxford University Press 1999

$$\mathscr{L}_{CC} = \left(\overline{u} \ \overline{c} \ \overline{t}\right)_{L} \gamma^{\mu} \begin{pmatrix} V_{ud} \ V_{us} \ V_{ub} \\ V_{cd} \ V_{cs} \ V_{cb} \\ V_{td} \ V_{ts} \ V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{L} W^{+}_{\mu} + \text{H.c.}$$

The CKM matrix is complex but not all its phases have physical meaning

$$u_{\alpha} = e^{i \varphi_{\alpha}} u'_{\alpha}, \qquad d_k = e^{i \varphi_k} d'_k$$

There is freedom to rephase the mass eigenstate quark fields. As a result:

$$V'_{\alpha k} = e^{i(\varphi_k - \varphi_\alpha)} V_{\alpha k}$$

Only rephasing invariant quantities have physical meaning. The simplest rephasing invariants of the CKM matrix are moduli and "quartets"

$$|V_{\alpha k}| \qquad \qquad Q_{\alpha i\beta j} \equiv V_{\alpha i} V_{\beta j} V_{\alpha j}^* V_{\beta i}^* \qquad \text{with } \alpha \neq \beta \text{ and } i \neq j.$$

Higher order Invariants can in general be written in terms of these .

# Details about Rephasing invariant quantities

# **Example :** $Q = V_{us} V_{cb} V_{cs}^* V_{ub}^*$

is essentially the sine of the Cabibbo angle and it is a parameter appearing in the Wolfenstein parametrisation of the CKM matrix

# the strength of CP violation in the SM.

 $Q = V_{us} V_{cb} V_{cs}^* V_{ub}^*$ Im  $Q = Im_6 Q_{inf} arg Q_{inf} arg Q_{inf} arg Q_{inf} Q_{inf}$ 

is of order 1

Ilm QI has the same value for all quartets and measures

# Differences between the imaginary parts of the quartets

In the SM, one can show that all imaginary parts of rephasing invariant quartets:

$$V_{us}V_{cb}V_{ub}^*V_{cs}^* = Q_{uscl}$$

$$V_{cd} V_{ts} V_{td}^* V_{cs}^* = Q_{cdt}$$

## have the same modulus

In the presence of VLQs one obtains a different result, for example:

 $Im Q_{2112} - Im Q_{1132} = Im Q_{1142}$ 



# Changes in the unitarity relations in the presence of VLQs

# Moduli differences:

In the SM, 3x3 unitarity of the CKM matrix leads to an "asymmetry" defined as:

$$\mathbf{a} \equiv |V_{31}|^2 - |V_{13}|^2 = |V_{23}|^2 - |V_{32}|^2 = |V_{12}|^2 - |V_{21}|^2$$

In an SM extension with one up-type VLQ the quark mixing matrix consists of the first three columns of a 4x4 unitary matrix:

$$V = \begin{pmatrix} V_{11} & V_{12} & V_{13} & V_{14} \\ V_{21} & V_{22} & V_{23} & V_{24} \\ V_{31} & V_{32} & V_{33} & V_{34} \\ V_{41} & V_{42} & V_{43} & V_{44} \end{pmatrix}$$

Albergaria, gcb, 2023

# Changes in the unitarity relations in the presence of VLQs

From unitarity of first row and first column of V, one derives:

$$a_{12,13} \equiv \left( |V_{12}|^2 - |V_{21}|^2 \right) - \left( |V_{31}|^2 - |V_{13}|^2 \right) = |V_{41}|^2 - |V_{14}|^2$$

Using unitarity of other rows and columns of V one obtains:

$$a_{12,32} \equiv \left( |V_{12}|^2 - |V_{21}|^2 \right) - \left( |V_{23}|^2 - |V_{32}|^2 \right) = |V_{24}|^2 - |V_{42}|^2,$$
  
$$a_{13,23} \equiv \left( |V_{13}|^2 - |V_{31}|^2 \right) - \left( |V_{32}|^2 - |V_{23}|^2 \right) = |V_{34}|^2 - |V_{43}|^2.$$

 $|V_{14}|^2 |V_{24}|^2$ 

From  $D_0 - \overline{D_0}$  mixing, we know that, in models with one up-type VLQ, we have

$$^{2} < (2.1 \pm 1.2) \times 10^{-8}.$$

# In the SM it is not possible to generate the Baryon Asymmetry of the **Universe (BAU)**

$$\mathcal{I}_{\rm CP} = {\rm tr}[y_u y_u^{\dagger}, y_d y_d^{\dagger}]^3$$

# In models with VLQs one may have CP odd invariants of much lower mass scale

Example:

 $\operatorname{tr}\left(\left[h_u, h_d^s\right] H_u^{(2)}\right)$ 

One of the reasons is that in the SM CP violation is too small:

$$\sim \frac{\mathrm{tr}[h_u, h_d]^3}{v^{12}} \sim 10^{-25}$$

$$H_u^{(r)} \equiv m_u (m_u^{\dagger} m_u + M_u^{\dagger} M_u)^{r-1} m_u^{\dagger}$$
$$h_d \equiv m_d m_d^{\dagger}$$



A surprising result: In the 3x3 <sup>5</sup> up corner of a V<sup>CKM</sup> matrix of arbi-trary size one has: 9-5=4 repairing invariant flow The following these commution may be dosen, in general ang  $V^{3\times3} = \begin{pmatrix} 0 & \beta \times & \delta \\ \pi & 0 & 0 \\ -\beta & \pi \cdot \beta & 0 \end{pmatrix} V = \begin{pmatrix} V_{CKM} \\ \hline |V_{ud}| & |V_{us}| e^{i\chi'} & |V_{ub}| e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ \hline |V_{td}| e^{-i\beta} & -|V_{ts}| e^{i\chi} & |V_{tb}| \\ \hline \vdots & \vdots & \vdots & \ddots \end{pmatrix}$ 



The phases &, B, B, B, Bx are arguments of replacing invariant quartits: V = ang (- Vud Veb Vub Ved) B= ang (-Ved Veb Veb Veb Veb) Bs= ang (-Vcb Ves Veb) PK = arg (-Vus Ved Vud Ves) Sometimes one also introduces & song(-Yellus ud es Which is unnearcy, became  $\alpha \equiv \pi - \beta - \delta$  By definition !!!

Within the SM, 3x3 unitarity implies some exact relations among rephasing invariant quantities: Vubl = Sinß [Vtb] [Vtd] = Sing [Vtb] [Vtd] = Sing [Vud]  $sin \beta_{s} = \frac{|Vtd| |V_{cd}|}{|Vts| |V_{cs}|} sin \beta = O(\lambda^{2})$  $\sin \beta_{K} = \frac{|V_{ab}|}{|V_{as}|} \frac{|V_{cb}|}{|V_{cs}|} \sin \delta = O(14)$ 

## Experimental data suggests:

B. Belfatto, R. Beradze and Z. Berezhiani, The CKM unitarity problem: A trace of new physics at the TeV scale?, Eur. Phys. J. C 80 (2020) 149 [1906.02714].

 $\Delta \equiv \Delta_1 = 1 - |V_{ud}|^2 - |V_{us}|^2 - |V$  $\sqrt{\Delta} \sim 0.04$ 

isosinglet quark is especially interesting since experimental limits on FCNC in the up sector are less stringent than those in the down sector

Recent measurements of  $|V_{us}|$  and  $|V_{ud}|$  indicate that unitarity of the first row may be violated,  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 < 1$ , at the level of two or three standard deviations. This

$$|\mathcal{V}_{ub}|^2 = |\mathcal{V}_{L_{41}}^*|^2 = s_{14}^2$$

Several references in our work, e.g, FLAG Review 2021 (Flavour Lattice Averaging group) (2111.09849)

BBB suggested the addition of a down-type (Q=-1/3) vector-like isosinglet quark

In alternative, the introduction of an up-type (Q=2/3) vector-like

Yukawa terms and bare mass terms (notation):

$$-\mathcal{L}_{u} \supset Y_{ij}^{u} \overline{Q}_{Li}^{0} \tilde{\phi} u_{Rj}^{0} + \overline{Y}_{i} \overline{Q}_{Li}^{0} \tilde{\phi} T_{R}^{0}$$
$$+ \overline{M}_{i} \overline{T}_{L}^{0} u_{Ri}^{0} + M \overline{T}_{L}^{0} T_{R}^{0} + \text{h.c.},$$

(artificial splitting of R-handed components)

$$-\mathcal{L}_d = Y_{ij}^d \overline{Q}_{Li}^0 \phi \, d_{Rj}^0 + \text{h.c.}$$

Following the spontaneous breakdown of electroweak symmetry:

$$-\mathcal{L} \supset \left(\overline{u}_{L}^{0} \quad \overline{T}_{L}^{0}\right) \mathcal{M}_{u} \begin{pmatrix} u_{R}^{0} \\ T_{R}^{0} \end{pmatrix} + \overline{d}_{L}^{0} \mathcal{M}_{d} d_{R}^{0} + \text{h.c.}$$

$$= \underbrace{\frac{v}{\sqrt{2}} Y^{u}}_{\sqrt{2}} \quad \overline{m} = \underbrace{\frac{v}{\sqrt{2}} \overline{Y}}_{\sqrt{2}} \quad v \simeq 246 \text{ GeV} \qquad \mathcal{M}_{u} = \begin{pmatrix} m & \overline{m} \\ \overline{m} \\ \overline{M} & M \end{pmatrix}$$

$$3 \times 3 \qquad 3 \times 1 \qquad \qquad 4 \times 4$$

$$m = \frac{v}{\sqrt{2}} Y^{u} \qquad \overline{m} = \frac{v}{\sqrt{2}} \overline{Y}$$
$$3 \times 3 \qquad 3 \times 1$$

Possible to choose WB where the down quark mass matrix is real diagonal

$$\mathcal{V}_L^\dagger \, \mathcal{M}_u \, \mathcal{V}_R \, = \, \mathcal{D}_u$$



# Non-Unitary mixing

$$\mathcal{L}_W = -\frac{g}{\sqrt{2}} \overline{u}_{Li}^0 \left(\gamma^{\mu} W_{\mu}^+\right) d_{Li}^0 = -\frac{g}{\sqrt{2}} \overline{u}_{L\alpha} \left(\gamma^{\mu} W_{\mu}^+\right) \left(\mathcal{V}^\dagger\right)^{\alpha i} d_{Li}$$

$$\mathcal{V}^{CKM}$$
 corresponds to

 $\mathcal{V}^{CKM}$  =

$$\mathcal{V}^{\dagger} = O_{34} V_{24} V_{14} \cdot V_4^{PDG}$$

$$\mathcal{V}_{L}^{\dagger} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & c_{34} & s_{34} \\ 0 & 0 & -s_{34} & c_{34} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{24} & 0 \\ 0 & 0 & 1 \\ 0 & -s_{24}e^{i\delta_{24}} & 0 \end{pmatrix}$$

 $\Delta \equiv \Delta_1 = 1 - |V_{ud}|^2 - |V_{us}|^2 - |V_{us}|^2$ 

the  $4 \times 3$  block of the matrix  $\mathcal{V}^{\dagger}$ 

$$= \left( \mathcal{V}^{\dagger} \right)^{(4 \times 3)} = A_L^{\dagger}$$

**Useful Parametrisation** 

F. Botella, L-L. Chau. 1986

$$V_{4}^{PDG} = \begin{pmatrix} \begin{bmatrix} V^{PDG} \end{bmatrix}^{(3\times3)} & 0 \\ & & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$
$$\stackrel{0}{\underset{24e^{-i\delta_{24}}}{\overset{0}{\underset{24}}} \begin{pmatrix} c_{14} & 0 & 0 & s_{14}e^{-i\delta_{14}} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ -s_{14}e^{i\delta_{14}} & 0 & 0 & c_{14} \end{pmatrix} V_{4}^{PDG}$$

$$|\mathcal{V}_{ub}|^2 = |\mathcal{V}_{L_{41}}^*|^2 = s_{14}^2 \qquad \sqrt{\Delta} \sim 0.04$$

# Couplings of the Z boson

$$\mathcal{L}_{Z} = -\frac{g}{c_{W}} \left[ \frac{1}{2} \left( \overline{u}_{Li}^{0} \gamma^{\mu} u_{Li}^{0} - \overline{d}_{Li}^{0} \gamma^{\mu} d_{Li}^{0} \right) - \frac{2}{3} s_{W}^{2} \left( \overline{u}_{i}^{0} \gamma^{\mu} u_{i}^{0} + \overline{T}^{0} \gamma^{\mu} T^{0} \right) + \frac{1}{3} s_{W}^{2} \left( \overline{d}_{i}^{0} \gamma^{\mu} d_{i}^{0} \right) \right] Z_{\mu}$$

$$\rightarrow -\frac{g}{c_{W}} \left[ \frac{1}{2} \left( \overline{u}_{L} \quad \overline{T}_{L} \right) F^{u} \gamma^{\mu} \begin{pmatrix} u_{L} \\ T_{L} \end{pmatrix} - \frac{1}{2} \overline{d}_{Li} \gamma^{\mu} d_{Li} - \frac{2}{3} s_{W}^{2} \left( \overline{u}_{i} \gamma^{\mu} u_{i} + \overline{T} \gamma^{\mu} T \right) + \frac{1}{3} s_{W}^{2} \left( \overline{d}_{i} \gamma^{\mu} d_{i} \right) \right] Z_{\mu},$$

$$F^{u} = A_{L}^{\dagger} A_{L} = 1 - B_{L}^{\dagger} B_{L}$$

# Couplings of the Higgs boson

$$\mathcal{L}_{h} = -\frac{1}{\sqrt{2}} \overline{u}_{Li}^{0} \left( Y_{ij}^{u} u_{Rj}^{0} + \overline{Y}_{i}^{u} T_{R}^{0} \right) h - \frac{1}{\sqrt{2}} Y_{ij}^{d} \overline{d}_{Li}^{0} d_{Rj}^{0} h + \text{h.c.}$$
  

$$\rightarrow - \left( \overline{u}_{L} \quad \overline{T}_{L} \right) F^{u} \mathcal{D}_{u} \begin{pmatrix} u_{R} \\ T_{R} \end{pmatrix} \frac{h}{v} - \overline{d}_{L} \mathcal{D}_{d} d_{R} \frac{h}{v} + \text{h.c.}$$

Similarly to the case of Z-mediated FCNC, the strength of Higgs-mediated FCNC is controlled by the off-diagonal entries of the matrix  $F^u$  and by the ratios  $m_q/v$ , (q = u, c, t, T)



$N^0 - \overline{N}^0$	$m_N \; [{ m MeV}]$	$\Delta m_N^{\mathrm{exp}}$ [MeV]	$f_N \; [{ m MeV}]$	$B_N$
$K^0 - \overline{K}^0$	$497.611 \pm 0.013$	$(3.484 \pm 0.006) \times 10^{-12}$	$155.7\pm0.3$	$0.717 \pm 0.024$
$B^0$ - $\overline{B}^0$	$5279.65\pm0.12$	$(3.334 \pm 0.013) \times 10^{-10}$	$190.0 \pm 1.3$	$1.30\pm0.10$
$B^0_s$ - $\overline{B}^0_s$	$5366.88 \pm 0.14$	$(1.1683 \pm 0.0013) \times 10^{-8}$	$230.3 \pm 1.3$	$1.35\pm0.06$

**Table 1:** Mass and mixing parameters [38] and decay constants and bag parameters [55] for the neutral meson systems with down-type valence quarks considered in section 3.2.

Observable	$m_T = 1 \text{ TeV}$
$\Delta m_K$	$\left V_{Td}\right \left V_{Ts}\right  < 7.4 \times 1$
$\Delta m_B$	$\left V_{Td}\right \left V_{Tb}\right  < 6.7 \times 1$
$\Delta m_{B_s}$	$\left V_{Ts}\right \left V_{Tb}\right  < 3.2 \times 1$
$ \epsilon_K $	$\left V_{Td}\right  \left V_{Ts}\right  \sqrt{\left \sin 2\Theta\right } < 8$

**Table 2:** Constraints from neutral meson observables on products of mixing matrix elements ( $\Theta = \arg V_{Ts}^* V_{Td}$ ) for two benchmark masses of the new heavy top quark.  $V = A_L^{\dagger}$ 

 $m_T = 3 \text{ TeV}$   $10^{-4} |V_{Td}| |V_{Ts}| < 2.7 \times 10^{-4}$   $10^{-4} |V_{Td}| |V_{Tb}| < 3.4 \times 10^{-4}$   $10^{-3} |V_{Ts}| |V_{Tb}| < 1.6 \times 10^{-3}$   $8.8 \times 10^{-5} |V_{Td}| |V_{Ts}| \sqrt{|\sin 2\Theta|} < 3.1 \times 10^{-5}$ 

Rare top decays  $t \rightarrow qZ$  (leading new physics contribution is tree level)

$$\operatorname{Br}(t \to q_i Z)_{\operatorname{NP}} \simeq \frac{\left|\mathcal{V}_{L_{4i}}^* \mathcal{V}_{L_{43}}\right|^2}{2\left|V_{tb}\right|^2} \left(1 - \frac{M_Z^2}{m_t^2}\right)^2 \left(1 + 2\frac{M_Z^2}{m_t^2}\right) \left(1 - 3\frac{M_W^4}{m_t^4} + 2\frac{M_W^6}{m_t^6}\right)^{-1}$$

$$\operatorname{Br}(t \to uZ)_{\exp} < 1.7 \times 10^{-4}$$
 Br(

$$Br(t \to uZ)_{SM} \sim 10^{-16}$$
 Br

contribution by several orders of magnitude.

Tree level NP contributions to the rare decays

are suppressed with respect to

due to the additional suppression by the ratios

J. Aguilar-Saavedra, 2004

 $(t \to cZ)_{\rm exp} < 2.4 \times 10^{-4} \ (95\% \ {\rm CL})$ **ATLAS 2018**  $c(t \rightarrow cZ)_{
m SM} \sim 10^{-14}$  J. Aguilar-Saavedra, 2004

 $Br(t \to q_i Z)_{NP} \simeq 0.46 \,\theta_{i4}^2 \,\theta_{34}^2 \sim \Delta_i \,\Delta_3$ , which for  $\mathcal{O}(0.01)$  angles still exceeds the SM

 $t \to qh$  $t \to qZ$  $m_q/v$ 

# Results of numerical analysis

## Take CKM from PDG without assuming unitarity

 $|K_{\rm CKM}| = \begin{pmatrix} 0.97370 \pm 0.00014 & 0.2245 \pm 0.0008 & (3.82 \pm 0.24) \times 10^{-3} \\ 0.221 \pm 0.004 & 0.987 \pm 0.011 & (41.0 \pm 1.4) \times 10^{-3} \\ (8.0 \pm 0.3) \times 10^{-3} & (38.8 \pm 1.1) \times 10^{-3} & 1.013 \pm 0.030 \end{pmatrix}$ 

Results after imposing previous constraints, and assuming that the phase \gamma remains unchanged:

- relatively large values for  $\theta_{14} \simeq \sqrt{\Delta}$  and  $\theta_{34}$  are preferred

- disfavoured  $\theta_{34} = 0$  at more than  $2\sigma$ 

- conversely  $\theta_{24}$  is compatible with zero

- fixing  $\sqrt{\Delta} = 0.04$ , one finds  $m_T \lesssim 5 \text{ TeV}$ 

## For several correlation plots and a benchmark point see our work

very interesting work B. Belfatto and Z. Berezhiani, 2103.05549

(constraint coming from  $D^0 - \overline{D}^0$  mixing leads to preference for small values) - no reason for common "wisdom" that T couples more strongly to third generation - maximum value for  $m_T$  depends on the size of the deviations from unitarity.

taking into account the full  $3\sigma$  region of the fit, the bound becomes  $m_T \leq 7$  TeV

Identification of the Small numbers in VCKM. Vub/~3.6×10 IIm Q1~ 3x 105 Q > Rephasing invariant quartet of VCKM In the SM, [Im Q] has the same value for all quarters and gives the stringth of CP violation in the SM



# The generation of V\_ub and ImQ

# from New Physics

# We propose that the CKM matrix is generated from three different contributions

$$V_{\rm CKM}^{\rm eff} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \\ & & & \text{up} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{12} \\ & & & \text{NP} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{13} & 0 \\ 0 & 0 & 1 \\ & & & \text{dow} \end{pmatrix}$$

# Conjecture:

$$M_d = \begin{pmatrix} m_{11}^d & m_{12}^d & 0\\ m_{21}^d & m_{22}^d & 0\\ 0 & 0 & m_{33}^d \end{pmatrix}$$

# It can be shown that one can obtain these patterns through the introduction of a Z\_4 symmetry at the Lagrangian level

In order to implement the structure we assume that there is a basis where the down and up quark matrices take the form:

$$M_u = \begin{pmatrix} m_{11}^u & 0 & 0 \\ 0 & m_{22}^u & m_{23}^u \\ 0 & m_{32}^u & m_{33}^u \end{pmatrix}$$



Without the introduction of New Physics, one simply obtains a simplified and reduced CKM mixing, where

$$V_{\text{CKM}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \\ & & \text{up} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \\ & & \text{dow} \end{pmatrix} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12}c_{23} & c_{23}c_{12} & -s_{23} \\ -s_{23}s_{12} & s_{23}c_{12} & c_{23} \end{pmatrix}$$

At this level one has:  $|V_{31}| = |V_{12}| |V_{23}|$  and  $V_{13} = 0$ Our conjecture offers an explanation why:  $|V_31| > |V_13| !!!$ 

 $V_{13} = 0$  also leads to vanishing CP violation

# Introduce an up-type VLQ and assume the 4x4 up-type quark matrix to be of the form:

$$\mathcal{M}_{u} = \begin{pmatrix} 0 & 0 & 0 & m_{14} \\ 0 & m_{22} & m_{23} & m_{24}e^{i\beta} \\ 0 & m_{32}e^{i\alpha} & m_{33} & 0 \\ m_{41} & 0 & -m_{43}e^{i\delta} & M \end{pmatrix}$$

# then one can generate:



$$\frac{\mathcal{K}}{\mathcal{H}}\Big|_{3} \neq 0 \quad |ImQ| \neq 0$$

$$M_d = \begin{pmatrix} 0.002923 \\ 0.000673 \\ 0 \end{pmatrix}$$

 $m_d = 0.003, \quad m_s = 0.060, \quad m_b = 2.9,$ 

$$\mathcal{M}_u = \begin{pmatrix} 0 & 0 \\ 0 & 0.5998 \\ 0 & -0.0239 \\ 0.046526 & 0 \end{pmatrix}$$

 $m_u = 0.002, \quad m_c = 0.60, \quad m_t = 173, \quad m_T = 1251.$ 

# Numerical example:

Mass matrices in GeV at the m\_Z scale:

 $\begin{array}{ccc} 0.0134741 & 0 \\ 3705 & 0.0584675 & 0 \\ 0 & 2.9 \end{array}$ 

53.73340 -6.91815  $1.250e^{-0.285i}$ 52172.8629936 0  $14.886e^{-1.190i}$ 1250

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The CKM matrix is the  $4 \times 3$  left-sub-matrix of the following full  $4 \times 4$  mixing matrix

 $|\mathcal{V}| = \begin{pmatrix} 0.97354 & 0.224413 & 0.00370431 & 0.0429468 \\ 0.224536 & 0.973644 & 0.0399975 & 0.000996211 \\ 0.00833917 & 0.0393001 & 0.999192 & 0.00151171 \\ 0.0416344 & 0.0105585 & 0.001674 & 0.999076 \end{pmatrix}$ 



0.000996211 0.999076

# These mass matrices lead to:

CP violation rephasing invariant phases are

- $\gamma \equiv \arg\left(-V_{ud}V_{cb}V_{ub}^*V_{cd}^*\right) \simeq 68.0^{\circ},$
- $\sin(2\beta) \equiv \sin[2 \arg(-V_{cd}V_{tb}V_{cb}^*V_{td}^*)] \simeq 0.746,$
- $\chi \equiv \arg\left(-V_{ts}V_{cb}V_{cs}^*V_{tb}^*\right) \simeq 0.020,$
- $\chi' \equiv \arg\left(-V_{cd}V_{us}V_{cs}^*V_{ud}^*\right) \simeq 5.71 \times 10^{-4}.$

CP-odd invariant quantity  $I_{\rm CP} = |{\rm Im}Q| \equiv |{\rm Im}(V_{ub}V_{cd}V_{ud}^*V_{cb}^*)|$  $I_{\rm CP} \simeq 3.00 \times 10^{-5}.$ 

VLQs may play an important rôle in providing an explanation for the VCKM unitarity problem. Nus/=1/ud/2+1/ub/2<1 at the arel of 2,3 standard deviation. See J.T. Penedo, Pedro Pereira, M.N. Adul published in JHEP GCB See also nice work by Belfatto and Berezhiani

VLQs Provide a simple framework where there are New Physics (NP) contributions to B2-B2 mixing, B-B3 mixing and/or Do-Do mixing; Also new contribulion to to CZn may receive Type - level contributions in models with up-type VLQs

VLQs may populate the desert between V and some higher scale (Mour?) without worsening the hierarchy problem To my knowledge, this was first empha-sized in a paper by Pierre Ramond. "Fermions in the Desert" (talk given at Erice) Appears in Spirls

# Physics BSM with vector-like quarks (VLQs)

Bare mass terms in the Lagrangian are allowed (as it is the case of neutrino Majorana mass terms)

without worsening the hierarchy problem

Mixing of the new quarks with the SM-like quarks gives rise to: Deviations from unitarity of the VCKM

Z mediated Flavour-Changing-Neutral-Currents

Higgs mediated Flavour-Changing-Neutral-Currents

These new phenomena are suppressed by the ratio of electroweak scale and the masses of the new heavy quarks

# **Rich variety of new Physics**

# VLQs may populate the desert between the EW and the GUT scale

P. Ramond, 1981

Violation of some **Dogmas of the Past!** 



# right-hantded neutrinos. **New Physics including**

There is an intriguing similarity between vector like quarks and This increases the plausibility of Vector-like quarks

Standard Model (SM) and Neutrino Masser . In the SM, nutrinos one strictly mandens No Dirac mass VR is not introduced No Majorana mass neither at tree luch nor at higher orders due to exact B-L conservation. Threfore the SM has been ruled out by experiment. So one is led to: JSM = SM+YR

J/S/J=SM+2RIf one follows "the rules" and writes the most general neutrino man terms, one has: Dirac mans: g, v I ve the. Majorana mans: MRVRCVR Since the Mojorana mass tirm is gauge invariant, one can have MR DV. This leads to the Seesan mechanism with:  $m_{\rm s} \approx (m_{\rm s})^2$ 

So the Haward Group dictated that neutrinos have no mass and the "right GVT" was SU(5) Where neutrinos are again manles du to accidental B-L conservation Kecal the talk by Murray Gell-Mann at Columbia about SO(10)...

Important feature of UR The Majorana mass term LCLR is SU(2), × U(1) invariant. Threfore MR can be significantly larger than V. MR>V Question: Can one have an analogous Situation in the quark sector? Ammer: Yes! Vector-like quarks: QL, RR transform in the same way under SU(2) with) QLQR in SU(2) × U(1) invariant

# The Lagrangian is CP invariant. CP is spontaneously violated

Field content, Higgs and quark sector:

$$\left(\begin{array}{c}u^{0}\\d^{0}\end{array}\right)_{iL}, u^{0}_{iR}, \ d^{0}_{\alpha R}, \ D^{0}_{L}, \ i=1,2,3, \ \alpha=1,...,4, \ \phi, \ S$$

D is a down-type vector-like quark, S is a scalar singlet

A  $Z_2$  symmetry is imposed in order to naturally suppress strong CP a la Barr and Nelson

 $D^0 \to -D^0, \quad S \to -S$ 

 $SU(2) \times U(1) \times Z_2$  invariant scalar potential

 $V = V_0 (\phi, S) + (\mu^2 + \lambda_1 S^*S + \lambda_2 \phi^{\dagger} \phi)(S^2 + S^{*2}) + \lambda_3 (S^4 + S^{*4})$ 

 $V_0$  contains all terms that are phase independent and includes the SM Higgs

Real coefficients spontaneous CP

violation 
$$\langle \phi^0 \rangle = \frac{v}{\sqrt{2}}, \quad \langle S \rangle = \frac{V \exp(i\beta)}{\sqrt{2}}$$

The Yukawa interactions of the quarks are given by: (all coefficients are real)

 $\mathcal{L}_Y = -\sqrt{2} (\overline{u^0} \ \overline{d^0})^i_L (g_{ij}\phi \ d^0_{iR} + h_{ij}\tilde{\phi} \ u^0_L)$ with (i, j = 1, 2, 3) and the down quark mass matrix is now of the form:

 $\mathcal{M}$ 

Diagonalisation of this mass matrix:

$$\mathcal{M}_d \mathcal{M}_d^{\dagger} U_L = U_L \begin{pmatrix} d_d^2 & \\ & D_d^2 \end{pmatrix} \quad \text{with} \quad U_L = \begin{pmatrix} K & R \\ S & T \end{pmatrix}$$

Working in the weak basis where the up quark mass matrix is diagonal)

$$S \simeq -\frac{1}{D_d^2} (\overline{M_d} \ m_d^{\dagger}) \ K$$
 where here  $\overline{M_{dj}} = f_j \ V e^{i\beta} + f'_j V e^{-i\beta}$ 

$$D_d^2 \simeq (\overline{M_d} \ \overline{M_d}^{\dagger} + M_d^2) \qquad \qquad \mathcal{H}_{eff} = m_d \ m_d^{\dagger} - \frac{1}{D_d^2} (m_d \ \overline{M_d}^{\dagger}) (\overline{M_d} \ m_d^{\dagger})$$

- concerning the generation of a complex VCKM
- Suppression of deviations from unitarity irrespective of which scale dominates

$$(D_{jR}^{0}) - M_d \overline{D_L^0} D_R^0 - \sqrt{2} (f_i S + f'_i S^*) \overline{D_L^0} d_{iR}^0 + \text{h.c.}$$

$$d_d = \left(\begin{array}{cc} m_d & 0\\ \overline{M_d} & M_d \end{array}\right)$$

Bento, gcb, Parada, 1991

- Non decoupling provided the scale of the bare mass term of D does not dominate over the scale of the vev of the scalar singlet,



From the previous page we see that in the Bento, gcb, Parada framework a complex CKM matrix can be generated from spontaneous CP violation at a high energy scale

# Concerning strong CP violation:

$$\mathscr{L} \supset \theta_{\rm QCD} \frac{g_s^2}{64\pi^2} \epsilon^{\mu\nu\alpha\beta} G^a_{\mu\nu} G^a_{\alpha\beta}$$

However, CP violation has not been observed in the strong interactions Furthermore,  $\theta_{\rm QCD}$  is a free parameter Experimentally what is measurable is the combination:  $\theta_{\text{weak}} = \arg(\det \mathcal{M}_u \times \det \mathcal{M}_d)$ 

It is the fact that  $\theta_{.}$ No additional symmetry is restored at Lagrangian level is restored when

- The QCD Lagrangian contains a CP violating term originating from the QCD vacuum

  - $\bar{\theta} = \theta_{\rm QCD} \theta_{\rm weak}$
- Within the SM the electric dipole moment of the neutron which is CP, P and T violating is proportional to  $\overline{\theta}$ .
  - $\theta \lesssim 10^{-10}$ is tiny that constitutes the strong CP problem:
    - $\theta = 0$

# A Common Origin for all CP Violations Strong CP

## Nelson-Barr proposal

- usual quark fields.
- only connect SM quark fields with the additional VLQs.

## Bento, gcb, Parada model

$$\mathcal{L}_{Y} = -\sqrt{2} (\overline{u^{0}} \ \overline{d^{0}})_{L}^{i} (g_{ij}\phi \ d_{jR}^{0} + h_{ij}\tilde{\phi} \ u_{jR}^{0}) - M_{d}\overline{D_{L}^{0}} \ D_{R}^{0} - \sqrt{2} (f_{i} \ S + f_{i}' \ S^{*}) \ \overline{D_{L}^{0}} \ d_{iR}^{0} + \text{h.c.}$$

Since CP is a symmetry imposed in the Lagrangian

 $\theta_{\text{weak}} = \arg(\det \mathcal{M}_d \times \det m_u).$ 

$$\theta_{\mathrm{weak}} = c$$

1. VEVs that break the SM gauge group cannot break CP and they only connect the

2. VEVs that break CP spontaneously cannot break the SM gauge group and they can

$$\theta_{QCD} = 0$$

$$\mathcal{M}_d = \left(\begin{array}{cc} m_d & 0\\ \overline{M_d} & M_d \end{array}\right)$$

# Extension to the Leptonic sector: three right handed neutrinos are included

$$\mathcal{L}_l = \overline{\psi_l^0} G_l \phi \ e_R^0 + \overline{\psi_l^0} G_\nu \tilde{\phi} \ \nu_R^0 + \frac{1}{2} \nu_R^{0T} C(f_\nu S_\nu)$$

Imposed symmetry:  $\psi_l^0 \to i \psi_l^0$ ,

The initial  $Z_2$  symmetry is thus promoted to a  $Z_4$  symmetry

$$\mathcal{L}_l = \overline{\psi_l^0} G_l \phi \ e_R^0 + \overline{\psi_l^0} G_\nu \tilde{\phi} \ \nu_R^0 + \frac{1}{2} \nu_R^{0T} C$$

the symmetry prevents the existence of bare Majorana terms, however these are generated by the couplings to the field S

there are standard model particles transforming non-trivially under the symmetry

 $\nu S + + f_{\nu}'S^*)\nu_R^0 + h.c.$  all coefficients are real

$$e_R^0 \to i e_R^0, \quad \nu_R^0 \to i \nu_R^0$$

 $C(f_{\nu}S + + f_{\nu}'S^*)\nu_R^0 + h.c.$ 

$$\mathcal{L}_{l} = \overline{\psi_{l}^{0}} G_{l} \phi \ e_{R}^{0} + \overline{\psi_{l}^{0}} G_{\nu} \tilde{\phi} \ \nu_{R}^{0} + \frac{1}{2} \nu_{R}^{0T} C(f_{\nu}S + +f_{\nu}'S^{*}) \nu_{R}^{0} + h.c.$$

$$\mathcal{M} = \begin{pmatrix} 0 & m \\ m^T & M \end{pmatrix}, \quad m_l = \frac{v}{\sqrt{2}} G_l, \quad m$$
$$M = \frac{V}{\sqrt{2}} (f_{\nu}^+ \cos(\alpha) + i f_{\nu}^- \sin(\alpha))$$

In the weak basis where  $m_l$  is to chosen to be real and diagonal

light neutrino masses and low energy leptonic mixing are obtained to an excellent approximation by:

$$-K^{\dagger}m\frac{1}{M}m^{T}K^{*} = d_{\nu} \qquad \text{when} \qquad$$

m is a real matrix, while M is a generic complex matrix, therefore K will also be complex

Leptonic CP violation is generated at low energies. CP violation at high energies can also be generated. Possibility of having Leptogenesis

Lepton number asymmetry is sensitive to the CP violating phases appearing in  $m^{\dagger}m$ 

in the weak basis where m\_I and M are chosen to be real and diagonal

$$= \frac{v}{\sqrt{2}}G_{\nu}$$

$$f_{\pm}^{\nu} \equiv f_{\nu} \pm f_{\nu}'$$

re  $U_{\text{PMNS}}$  can be identified to K.

# CONCLUSIONS

Vector-like quarks are very interesting candidates for physics BSM

Very simple extension of the SM, providing striking new experimental effects

- Vector-like quarks are "cousins" of right-handed neutrinos which
  - provide through seesaw the most plausible explanation of the
    - smallness of neutrino masses



· Weak foint: No firm prediction for the scale of VLQs. This is a universal weak point in all (so far) proposed New Physics !! The SM was an notable exception. Before gauge interactions the sugestion was IVB with 22GeV! istrone diate vector boson ...