

Asymptotic Safety Landscapes

at the intersection
between positivity bounds and swampland conjectures

Alessia Platania

Based on:

Basile, Platania - arXiv:2107.06897

Knorr, Platania - arXiv:2405.08860

Corfu Summer Institute '24

Corfu, 20.09.2024



The Niels Bohr
International Academy

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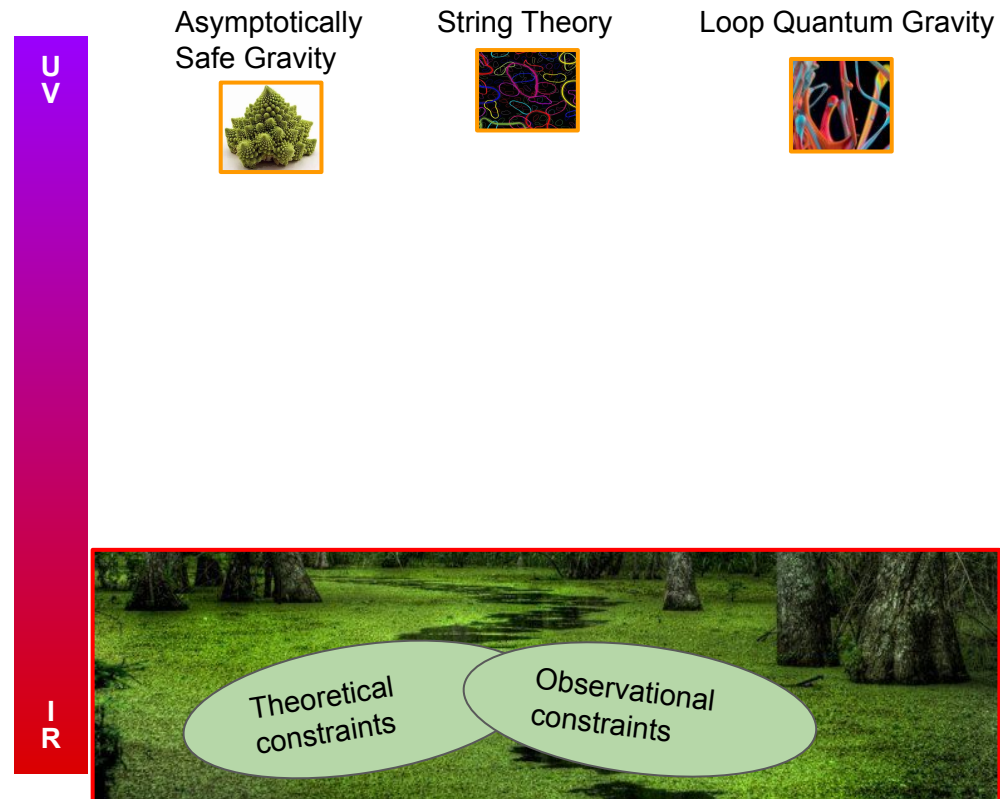
Some reflections on the status of the field

- *QG is a multi-scale problem*
 - Different theories / UV completions \Rightarrow different fundamental properties (and different conceptual and technical problems). Details relevant at trans-Planckian scales.
 - Observations spanning intermediate to large distances (cosmology, dark energy, gravitational waves)
 - EFT: consistency constraints in the IR

- *Technical and conceptual interrelated difficulties in connecting UV and IR, and different UVs*
 - Theory is not driven by experiment (scale separation)
 - Difficult to make predictions from scratch
 - Equivalent theories?
Comparing approaches in the UV is like comparing apples with bananas!

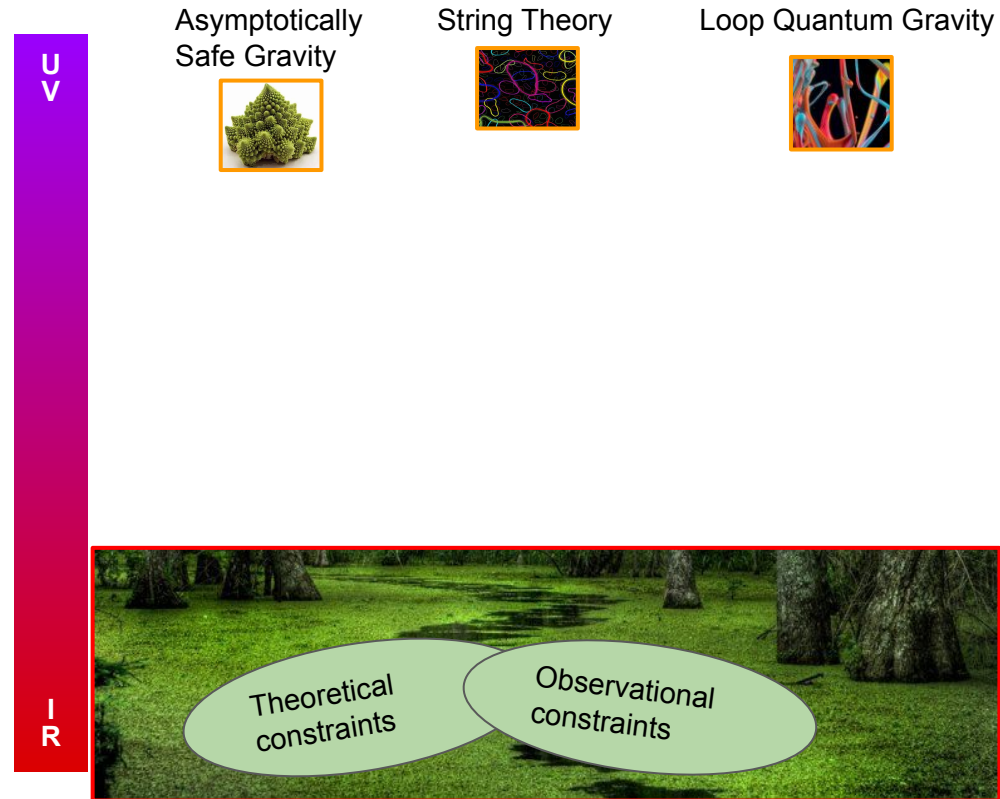
- *A “decoupling phenomenon” in gravity*
 - “Formal” QG communities: mostly focus on the UV
 - Pheno & EFT communities: mostly focus on the IR

- **Task**: define map/recipe to connect UV and IR
- **Expectation/hope**: not everything goes, QG is predictive



Quantum gravity through the lens of effective field theory

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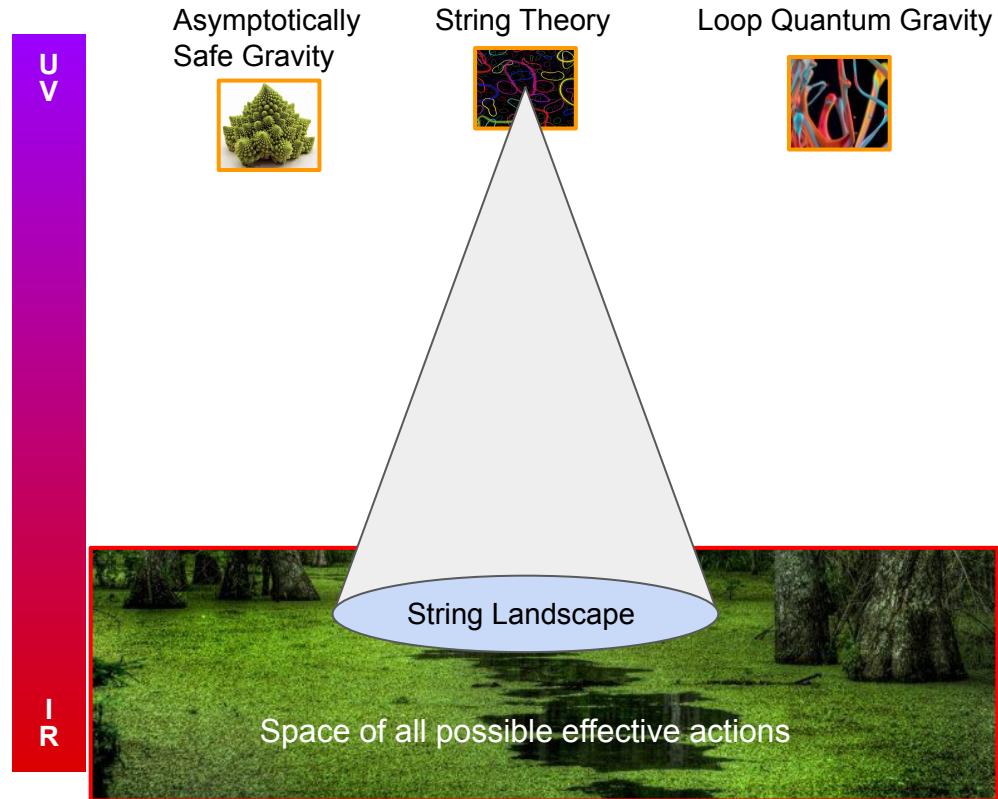
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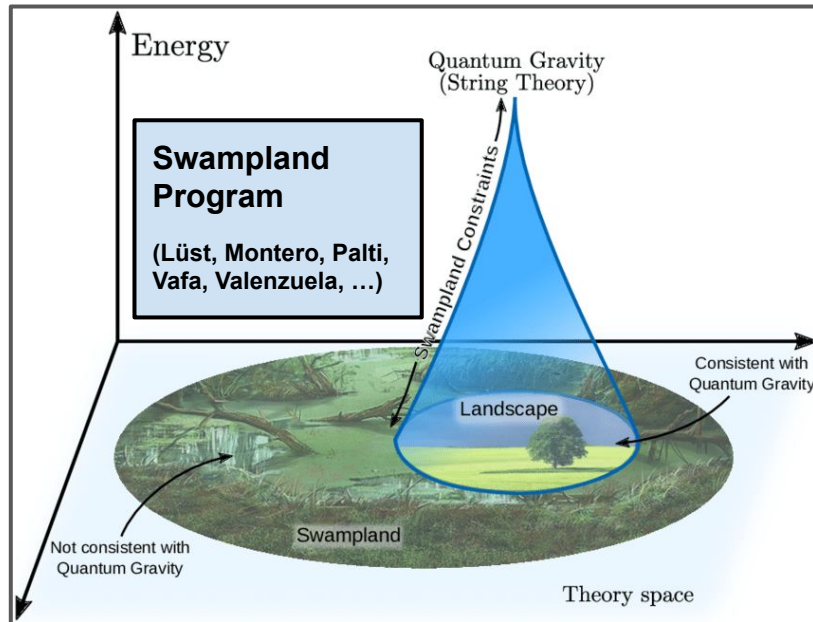
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Quantum gravity through the lens of effective field theory

One attempt within String Theory: the “swampland program”

- Find criteria that select consistent EFTs (that come from UV-complete QG+matter)
- Criteria inspired by universal patterns in string constructions or derived from EFT/BH arguments



UV
IR

Asymptotically Safe Gravity



String Theory



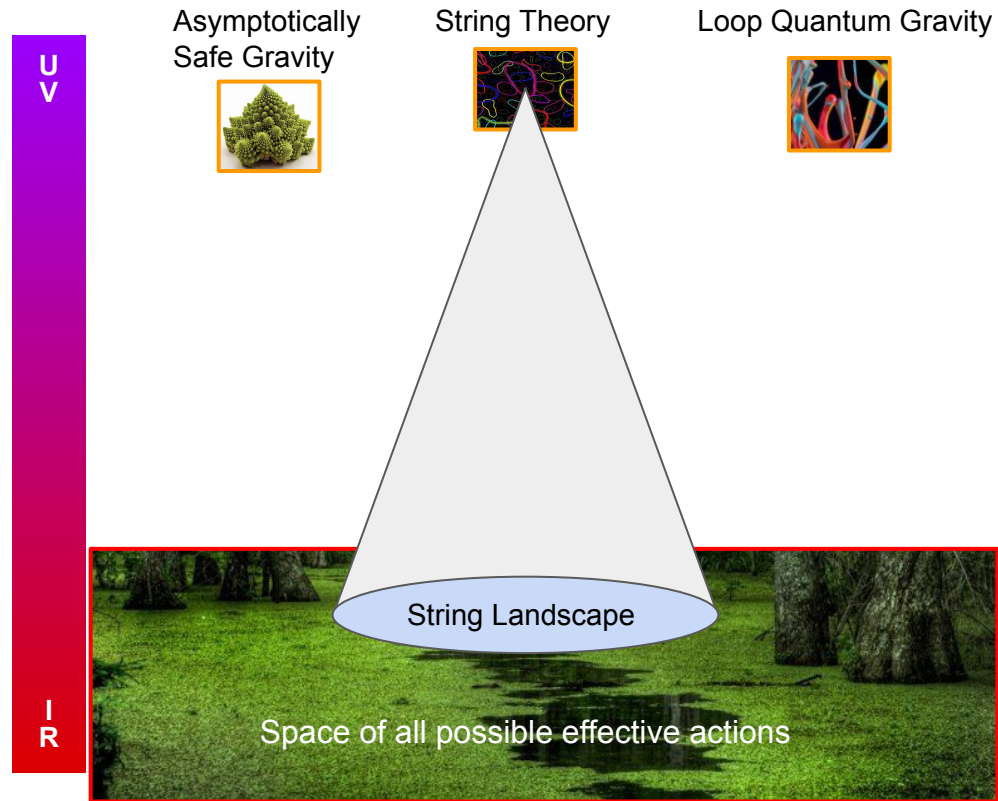
Loop Quantum Gravity



Quantum gravity through the lens of effective field theory

Can the “big picture” of the swampland program be generalized?

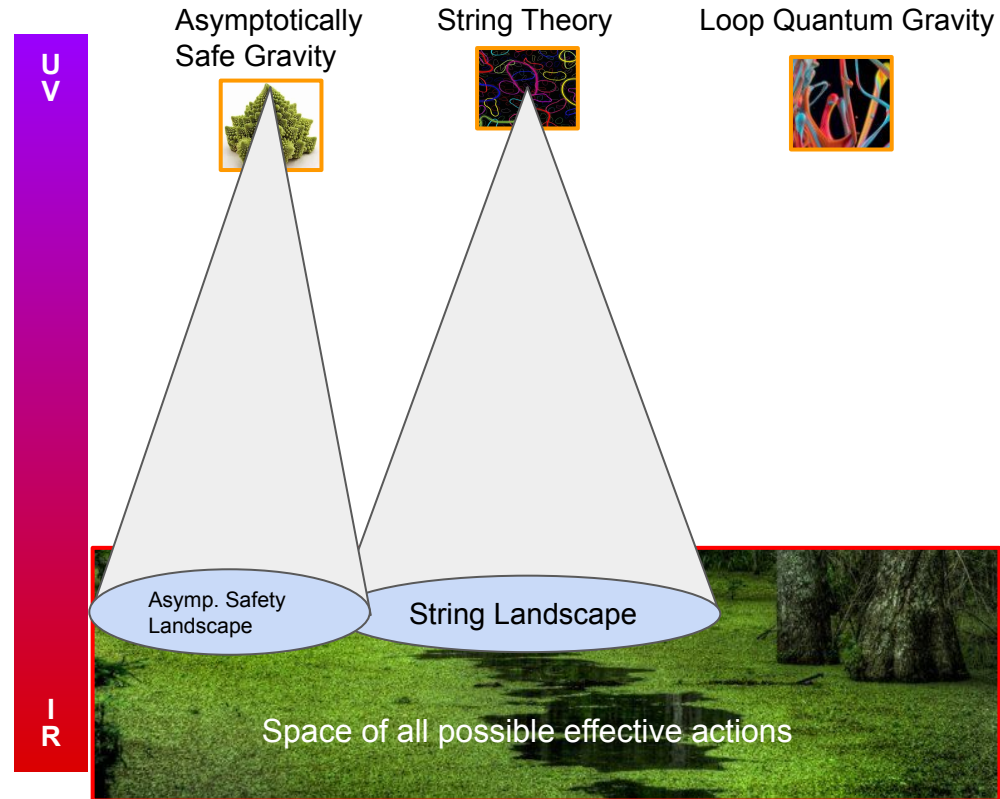
[Basile, AP, '21]



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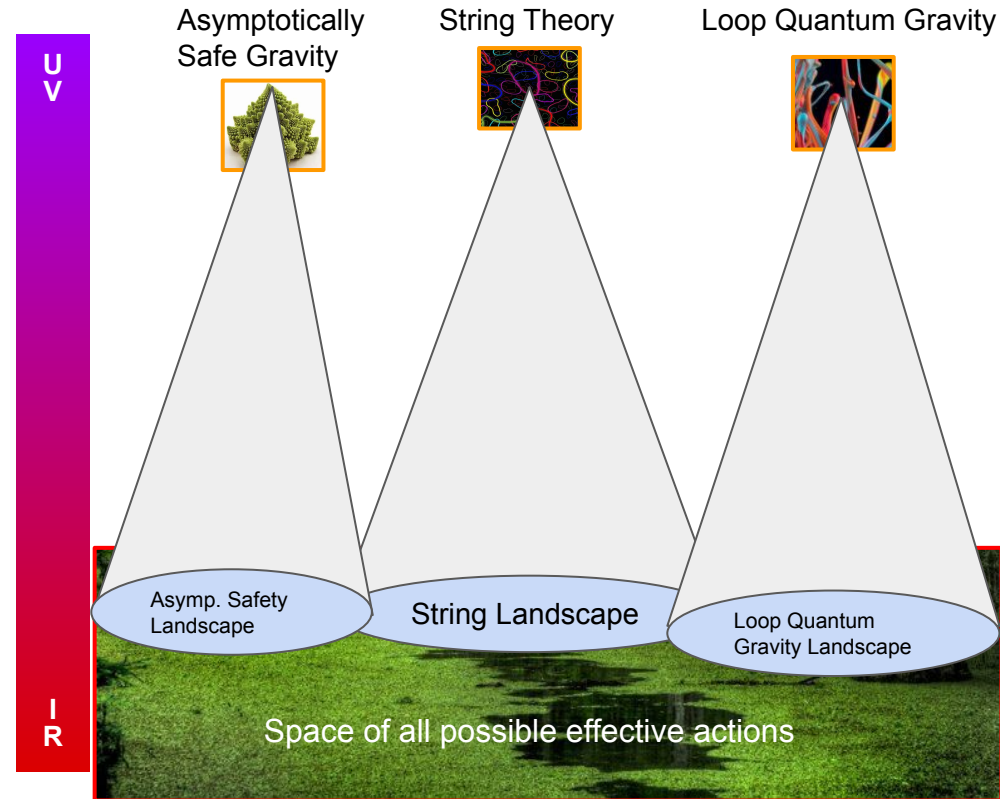
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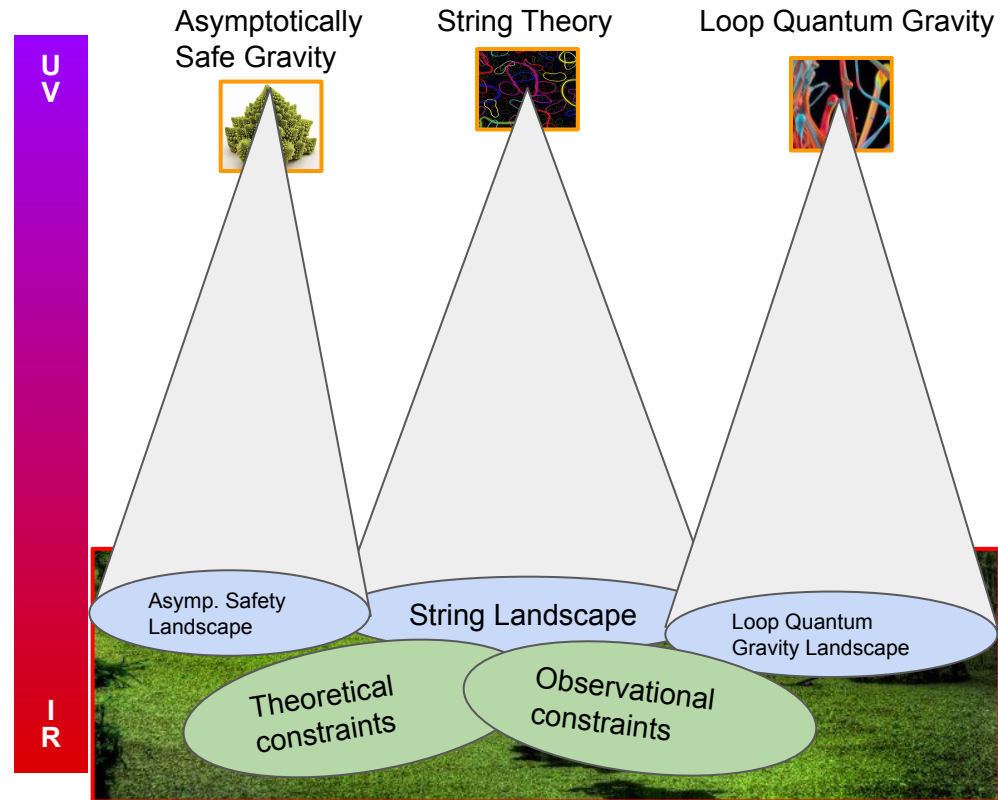
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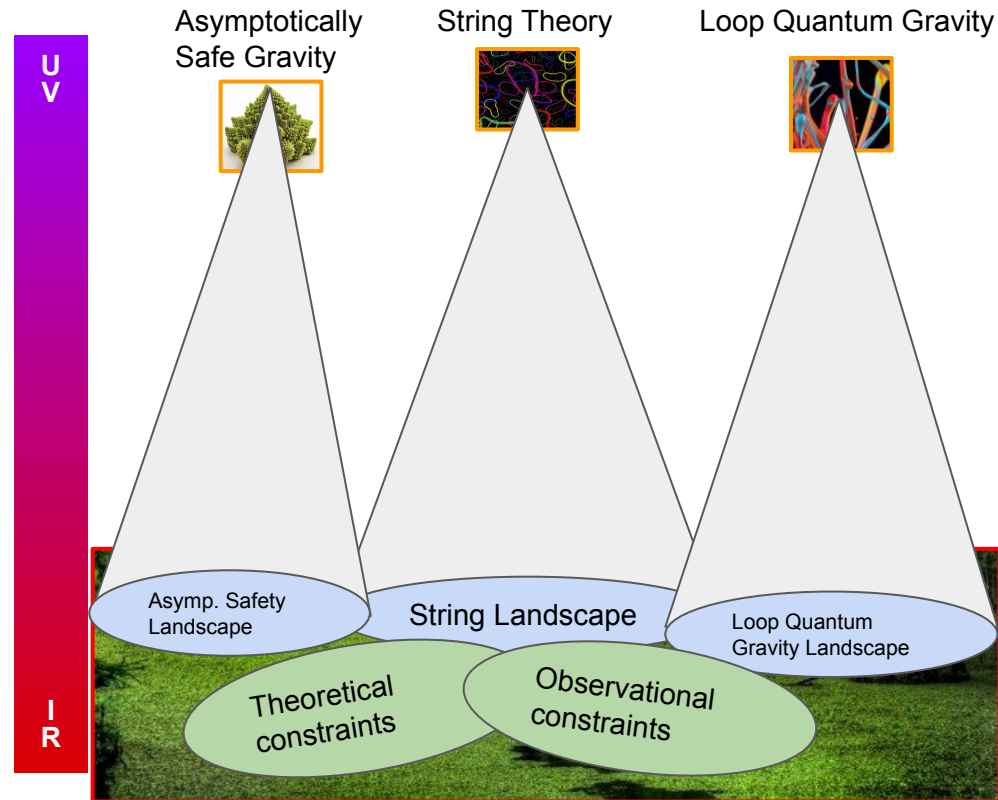
Quantum gravity through the lens of effective field theory

Several interesting questions at the intersections:

- **Consistency**, e.g., compatibility of QG predictions with positivity bounds (unitarity, causality, stability)
- **Tests of Swampland Constraints & string “universality”**: are they all general? Do they apply to all (consistent) QG or they only identify EFTs stemming from ST?

c.f. **String Lamppost Principle** [Montero, Vafa, '21]:
“All consistent quantum gravity theories are part of the string landscape”

- Comparison between **predictions of different QG approaches**? Connections between approaches?
- Comparison with bounds from **observations**?



Quantum gravity through the lens of effective field theory

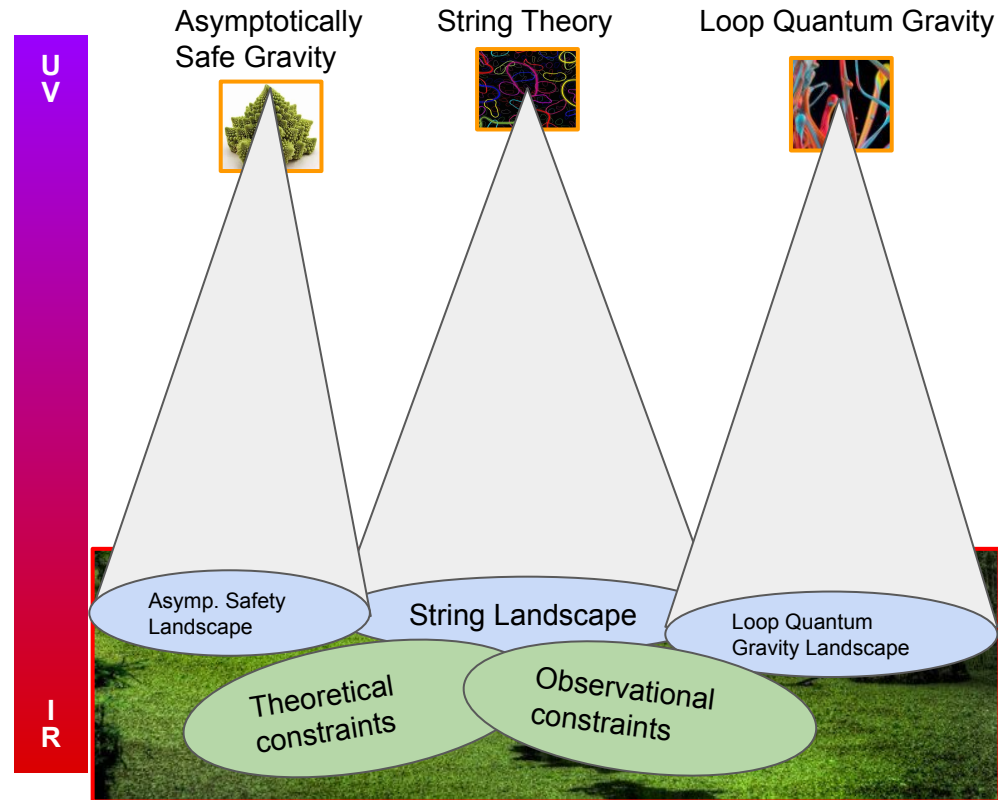
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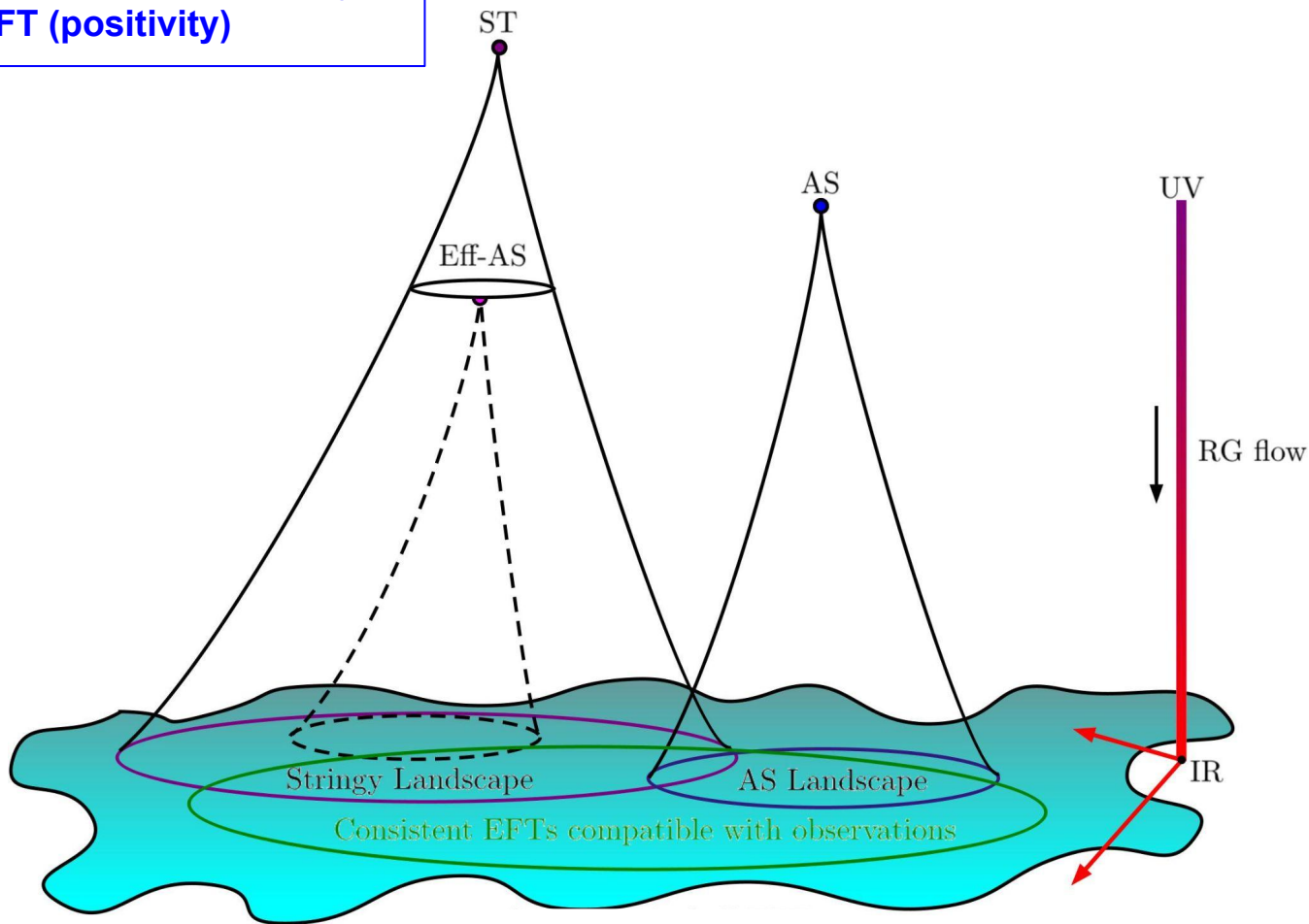
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Focus of this talk: AS



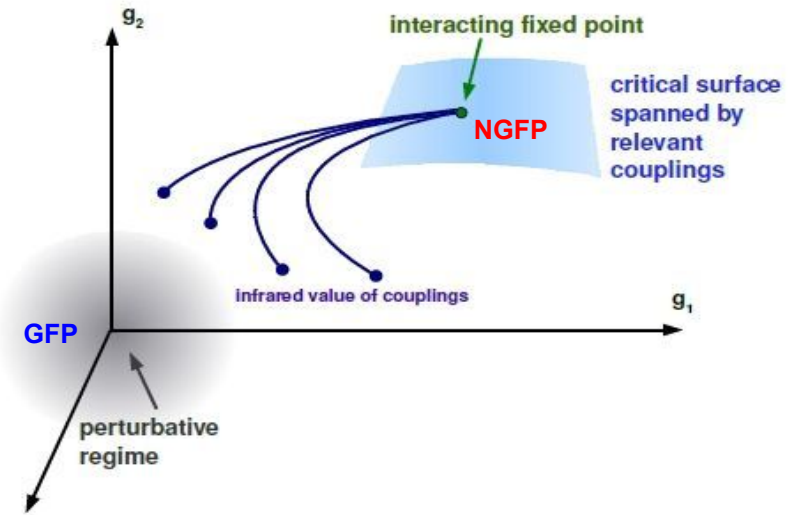
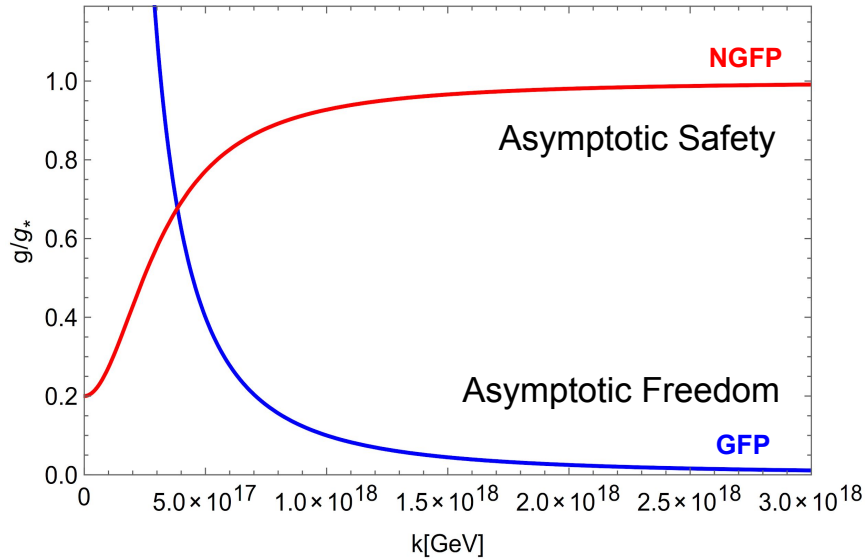
This talk:

- AS vs ST (some swamp conjs)
- AS vs EFT (positivity)



**Landscapes
in Asymptotically Safe Gravity**

Asymptotic Safety in a Nutshell



Idea: *gravity non-perturbatively renormalizable, interacting UV-completion*

(Weinberg, '76)

Testing asymptotic safety:

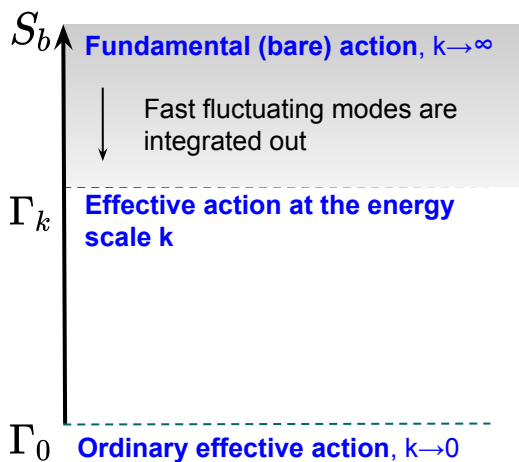
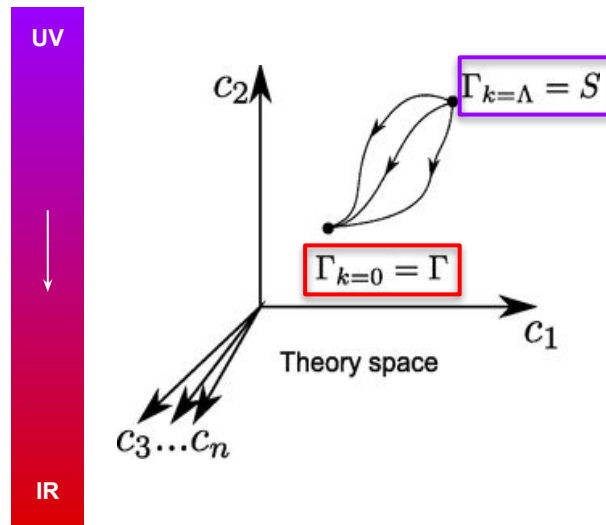
- **Lattice-like computations:** causal/euclidean dynamical triangulations
- **Semi-analytical computations:** exact renormalization group ("AS community")

Functional Renormalization Group

Solving the **quantum theory** is equivalent to solve the functional **renormalization group equation**

$$k\partial_k \Gamma_k = \frac{1}{2} \text{STr} \left\{ \left(\Gamma_k^{(2)} + \mathcal{R}_k \right)^{-1} k\partial_k \mathcal{R}_k \right\}$$

C. Wetterich. *Phys. Lett. B* 301:90 (1993)
 M. Reuter. *Phys. Rev. D.* 57 (2): 971 (1998)



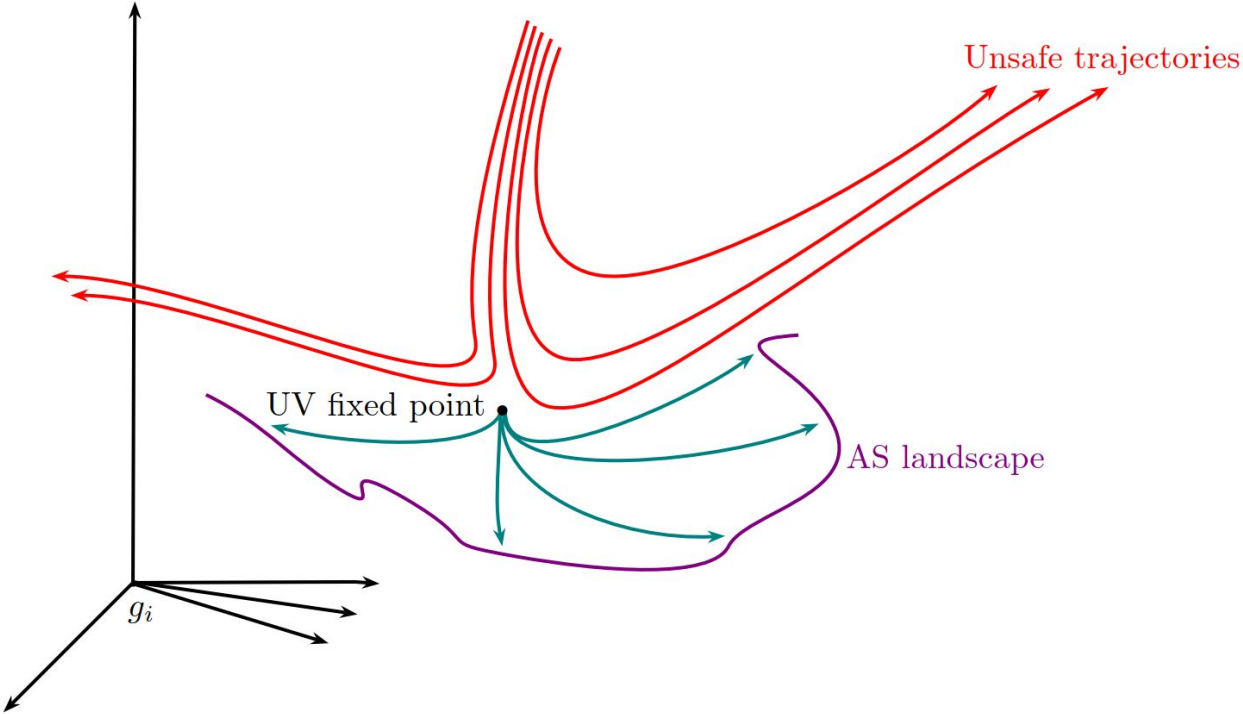
UV fixed points = bare actions, N relevant directions

Effective action (limit $k \rightarrow 0$), infinitely many terms parametrized by N free parameters

⇒ **S-matrix, Wilson coefficients, observables**

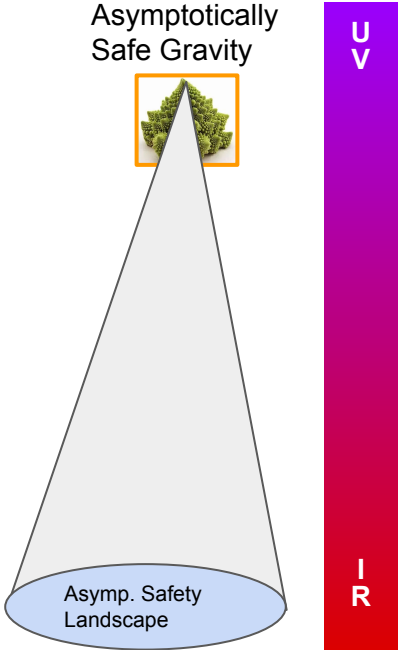
Implementation in AS: defining the asymptotic safety landscape

Theory space of dimensionless running couplings

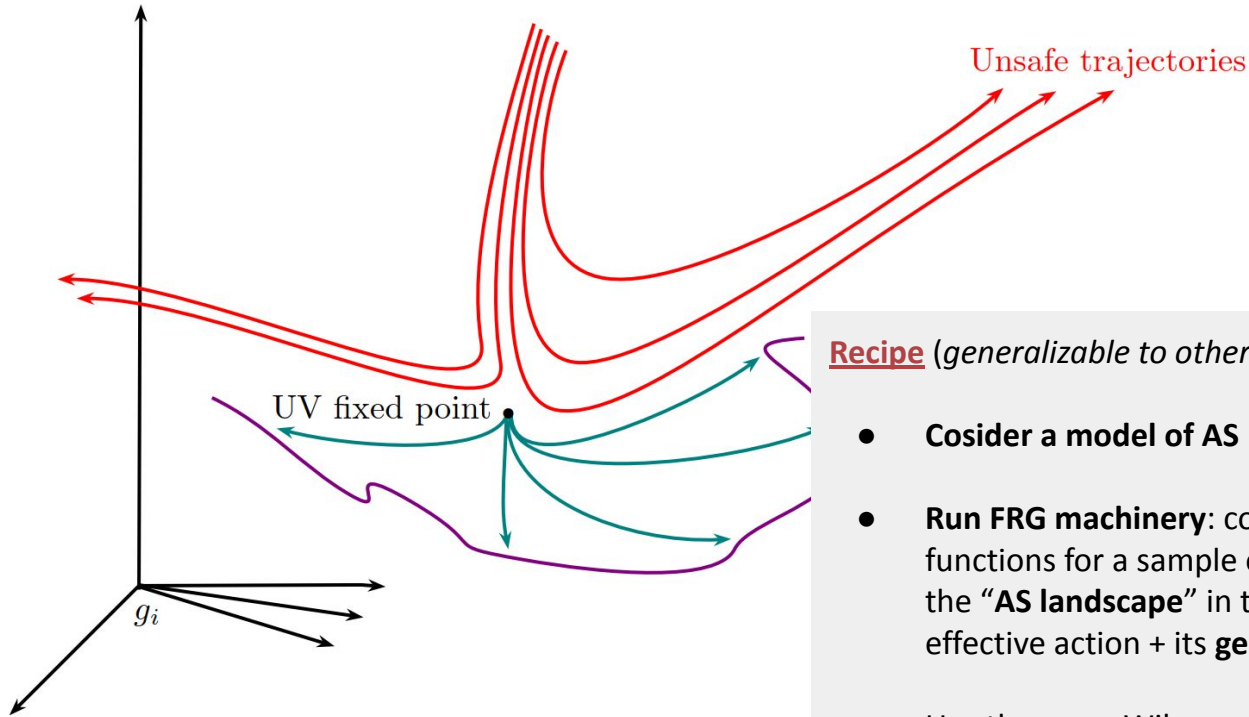


So far:

- Much focus of the AS community on UV fixed points and a few RG trajectories
- Less about constraining the Wilson coefficients and their intersections with bounds



Implementation in AS: defining the asymptotic safety landscape



Recipe (generalizable to other approaches?)

- Consider a model of AS (truncation of the action)
- Run FRG machinery: compute beta functions, solve beta functions for a sample of UV-complete trajectories, identify the “AS landscape” in terms of Wilson coefficients in the effective action + its geometry
- Use the same Wilson coefficients to identify the region allowed by positivity bounds / swampland conjectures (string landscape) / other QG landscapes / observational bounds...
- Find the intersections between AS landscape and other sets

Implementation in AS: defining the asymptotic safety landscape

Defining the Wilson Coefficients (+ caveats)

- Defining the Wilson coefficients with the FRG:

$$W_{G_i} \equiv \lim_{k \rightarrow 0} G_i(k)$$

- **Or, actually: we only measure dimensionless quantities**, thus we need one unit mass scale (e.g., Newton coupling) and N-1 dimensionless Wilson coefficients to parametrize the landscape of EFTs (N=number of relevant directions)

$$w_{G_i} \equiv \lim_{k \rightarrow 0} G_i(k) M_{Pl}^p$$

- **CAVEAT 1: Wick rotation needed! FRG is typically based on Euclidean computations. But the results may be the same as in Lorentzian settings**

[Fehre, Litim, Pawłowski, Reichert '21]

- **CAVEAT 2: Defining Wilson coefficients in the presence of Log running in the IR is ambiguous, and one needs a prescription. Our prescription: use the transition scale to QG.**

$$w = a + b \log(k^2 / M_{Pl}^2) + b(\log(k_0^2) - \log(k^2))$$

[Basile, AP '21]

$$= \tilde{a} + \tilde{b} \log(k/k_0^2)$$

[Knorr, AP '24]

Case Study 1

AS landscapes in one-loop
quadratic gravity
vs
Swampland Constraints

- **AS toy model**: one-loop quadratic gravity

$$\mathcal{L} = \frac{2\Lambda - R}{16\pi G} + \frac{1}{2\lambda} C^2 - \frac{\omega}{3\lambda} R^2 + \frac{\theta}{\lambda} E$$

- **Three dimensionless Wilson coefficients** (+ gauss-bonnet, but decoupled)
One dimensionful coupling sets the mass unit scale!

$$G\Lambda, \quad g_R = -\frac{\omega}{3\lambda}, \quad g_C = \frac{1}{2\lambda}$$

- Beta function and fixed points [(Codello, Percacci, 2006)]

$$\lambda_* = 0, \quad \omega_* = \omega_{\pm} \equiv \frac{-549 \pm 7\sqrt{6049}}{200}, \quad \theta_* = \frac{56}{171}$$

$$\tilde{\Lambda}_* \approx 0.221, \quad \tilde{G}_* \approx 1.389$$

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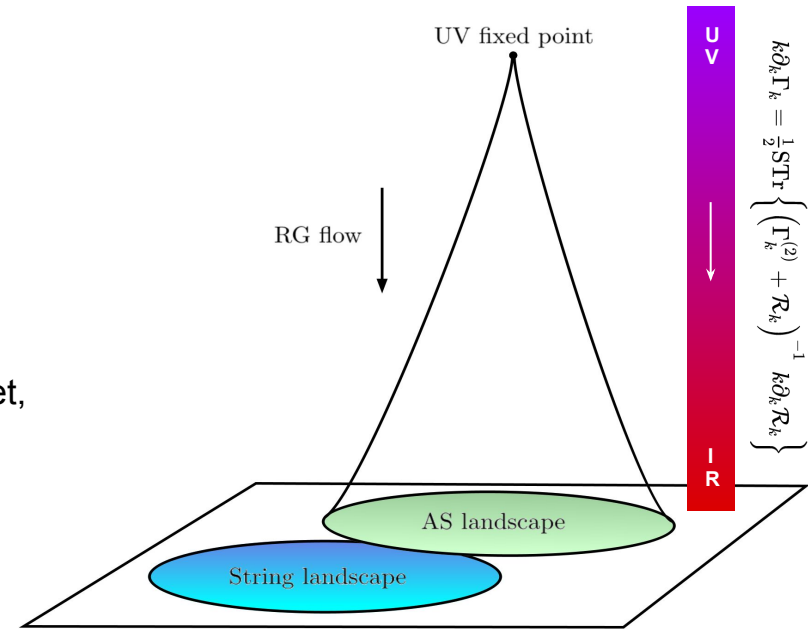
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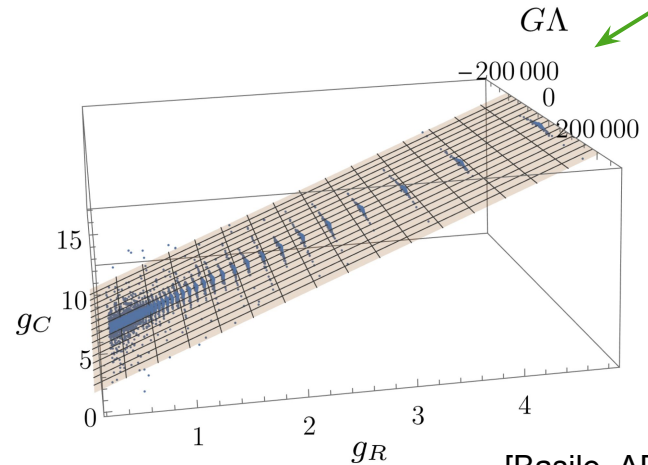
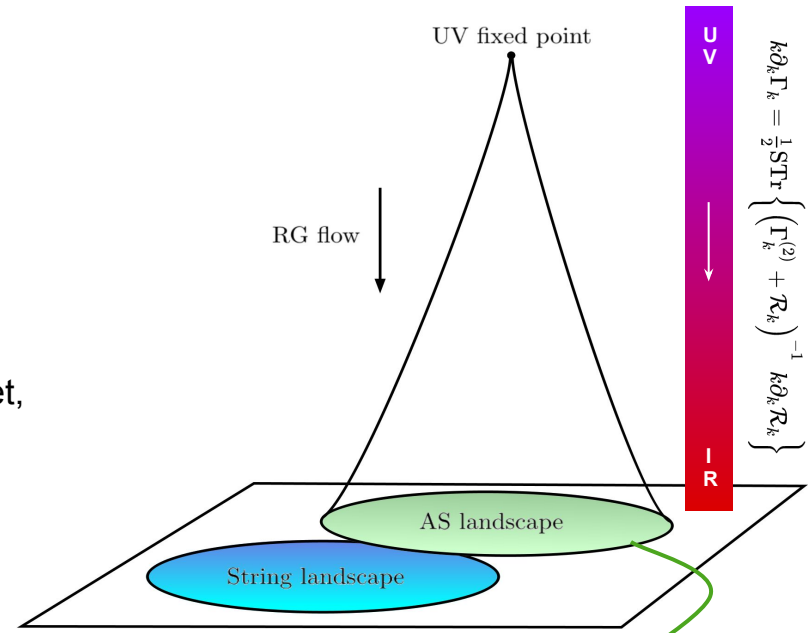
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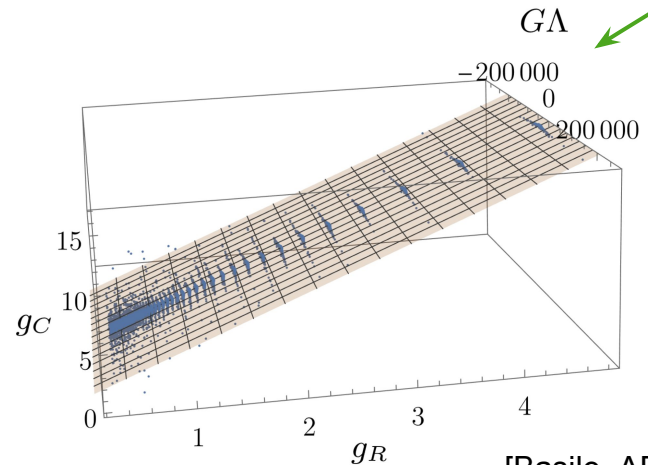
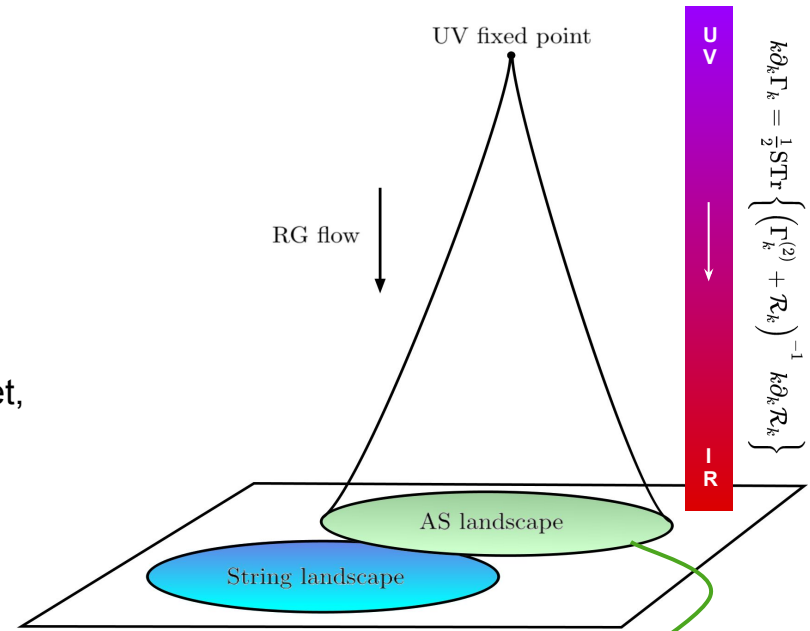
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The Wilson coefficients stemming from an AS fixed point lie on a plane

$$\text{EFT}_{\text{AS}} \approx \left\{ g_R = -0.74655 - \frac{2}{3} \omega_- g_C \right\}$$

$$g_C > 0$$



Result from
~ 10⁷ num
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- **Swampland conjectures:**

→ **Weak gravity conjecture** (Arkani-Hamed, Motl, Nicolis, Vafa, 2006)

$$m/M_{Pl} \leq q \mathcal{O}(1)$$

Black holes remain sub-extremal:

$$Q/M \leq (Q/M)_{extr}$$

Higher derivative corrections [(Kats, Motl, Padi, 2007), (Charles, Larsen, Mayerson, 2017), (Cheung, Liu, Remmen, 2018), (Hamada, Noumi, Shiu, 2019), (Charles, 2019)]:

$$Q/M \leq (Q/M)_{extr} \left(1 - \frac{\Delta}{M^2} \right) \quad \mathcal{L}_{HD} = c_1 R^2 + c_2 R_{\mu\nu} R^{\mu\nu} + c_3 R_{\mu\nu\rho\sigma} R^{\mu\nu\rho\sigma}$$

$$\Delta \propto (1 - \xi)^2 (c_2 + 4c_3) + 10 \xi (1 + \xi) c_3 \stackrel{\text{WGC}}{>} 0, \quad \xi \equiv \sqrt{1 - \frac{Q^2}{M^2}}$$

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In terms of dimensionless couplings, this condition yields

$$g_C > 0$$

Satisfied by AS-EFT

- **Swampland conjectures:**

→ **De Sitter conjecture** [(Obied, Ooguri, Spoyneiko, Vafa, 2018), (Ooguri, Palti, Shiu, Vafa, 2019)]

$$M_{Pl} \|\nabla V\| \geq cV \quad \text{for } \Delta\phi \leq fM_{Pl} \quad f, c \sim \mathcal{O}(1)$$

→ **Trans-Planckian conjecture** [(Bedroya, Vafa, 2020)]

Relevant for early-universe cosmology. Special value of c:

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$$V(\phi) = \frac{M_{Pl}^2}{8\pi} e^{-2\sqrt{\frac{2}{3}} \frac{\phi}{M_{Pl}}} \left(\frac{3m^2}{4} \left(e^{\sqrt{\frac{2}{3}} \frac{\phi}{M_{Pl}}} - 1 \right)^2 + \Lambda \right) \quad g_R = - \frac{M_{Pl}^2}{(8\pi) \cdot 12m^2}$$

⇒ **Non-trivial bounds for different f and c**

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**Can be violated in AS:
deSitter solutions can be
found in AS**

[Basile, AP. 2107.06897]

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⇒ Non-trivial bounds for different f and c .

Case Study 2

**Non-perturbative AS landscapes
of quadratic photon-graviton systems**

VS

**Positivity Bounds
& the Weak Gravity Conjecture**

- **AS model:** photon-graviton systems at quadratic order, only **essential couplings** included

$$\mathcal{L} = -\frac{R}{16\pi G_N} + \Theta_E E + \frac{1}{4} F^{\mu\nu} F_{\mu\nu} + G_2 (F^{\mu\nu} F_{\mu\nu})^2 + G_4 F^\mu{}_\nu F^\nu{}_\rho F^\rho{}_\sigma F^\sigma{}_\mu + G_{CFF} C^{\mu\nu\rho\sigma} F_{\mu\nu} F_{\rho\sigma}$$

- **Three dimensionless Wilson coefficients (redefined for convenience; only one log-presc. ambiguity)**

$$w_+ = \frac{1}{2} \frac{G_2 + G_4}{(16\pi G_N)^2}, \quad w_- = \frac{1}{2} \frac{G_2 - G_4}{(16\pi G_N)^2} + b \ln[16\pi G_N k^2], \quad w_C = \frac{G_{CFF}}{16\pi G_N}$$

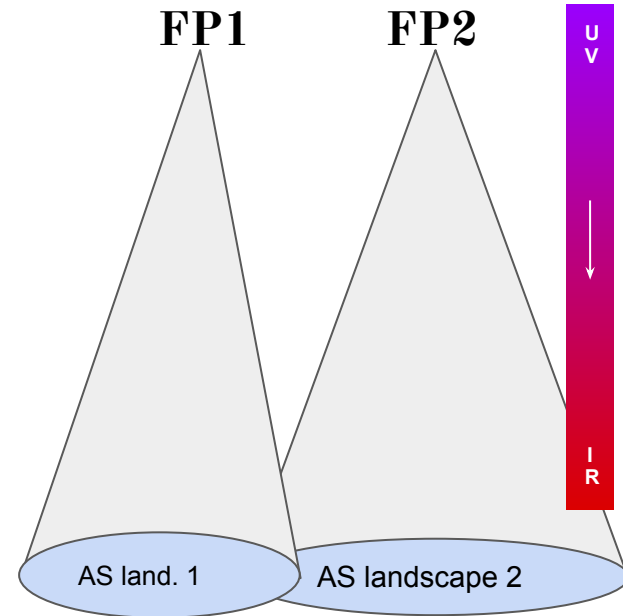
- **Two UV fixed points:**

FP1: one relevant direction (most predictive!)

⇒ once the QG scale is fixed, this is a zero-parameter theory = 1 point in the space of dimensionless Wilson coefficients

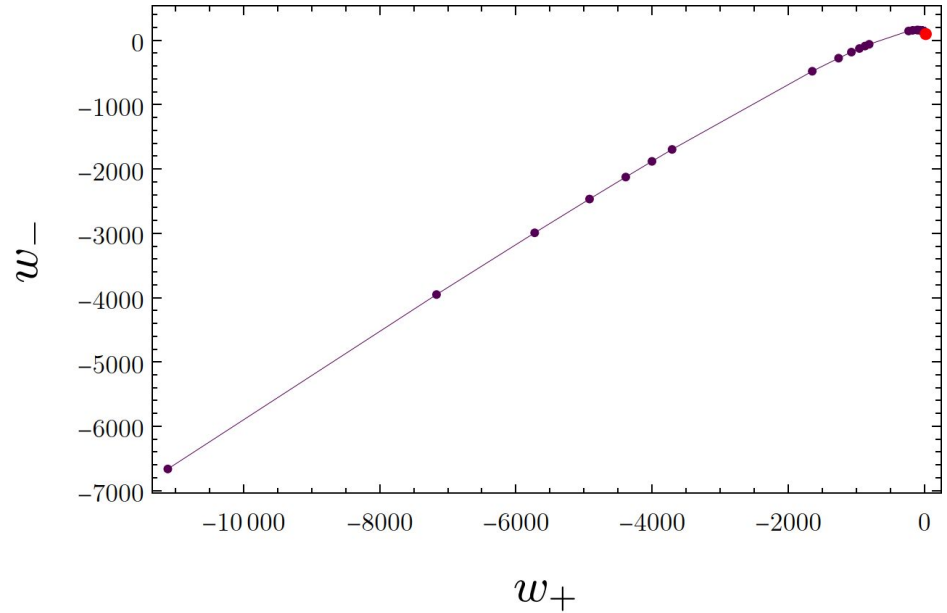
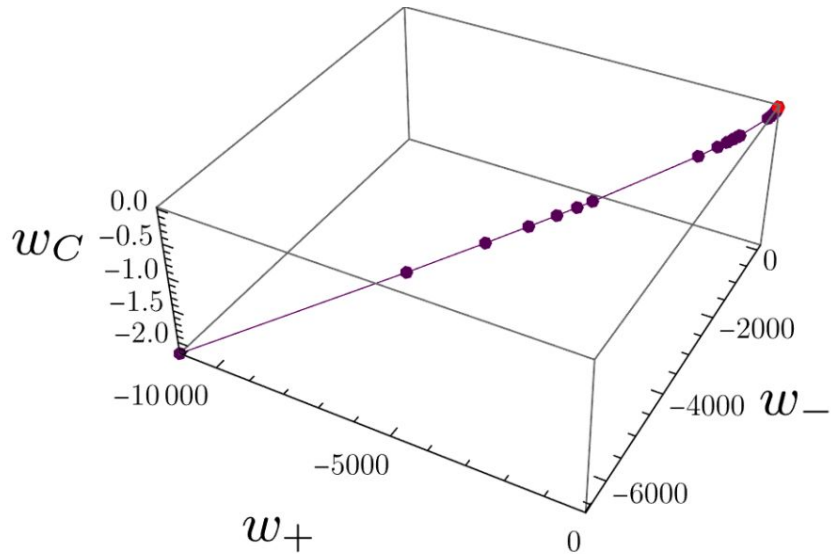
FP2: two relevant directions

⇒ effective action parametrized by 1 dimensionless parameter (line of EFTs)



Asymptotic Safety Landscapes

[Knorr, AP, 2405.08860]

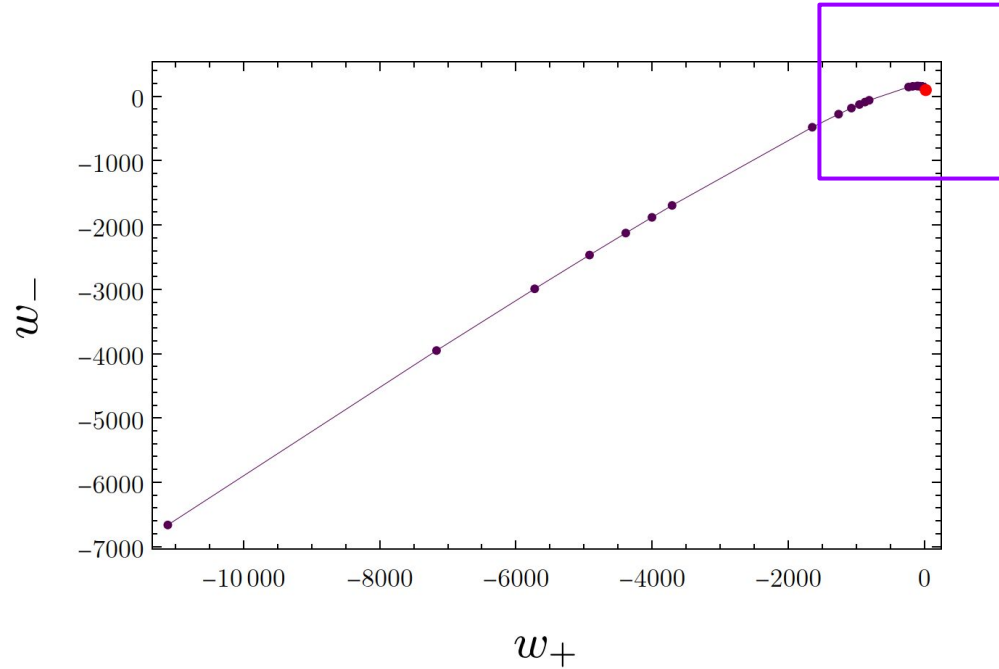


AS landscape from FP1: 1 single point

AS landscape from FP2: almost straight line

Asymptotic Safety Landscapes

[Knorr, AP, 2405.08860]



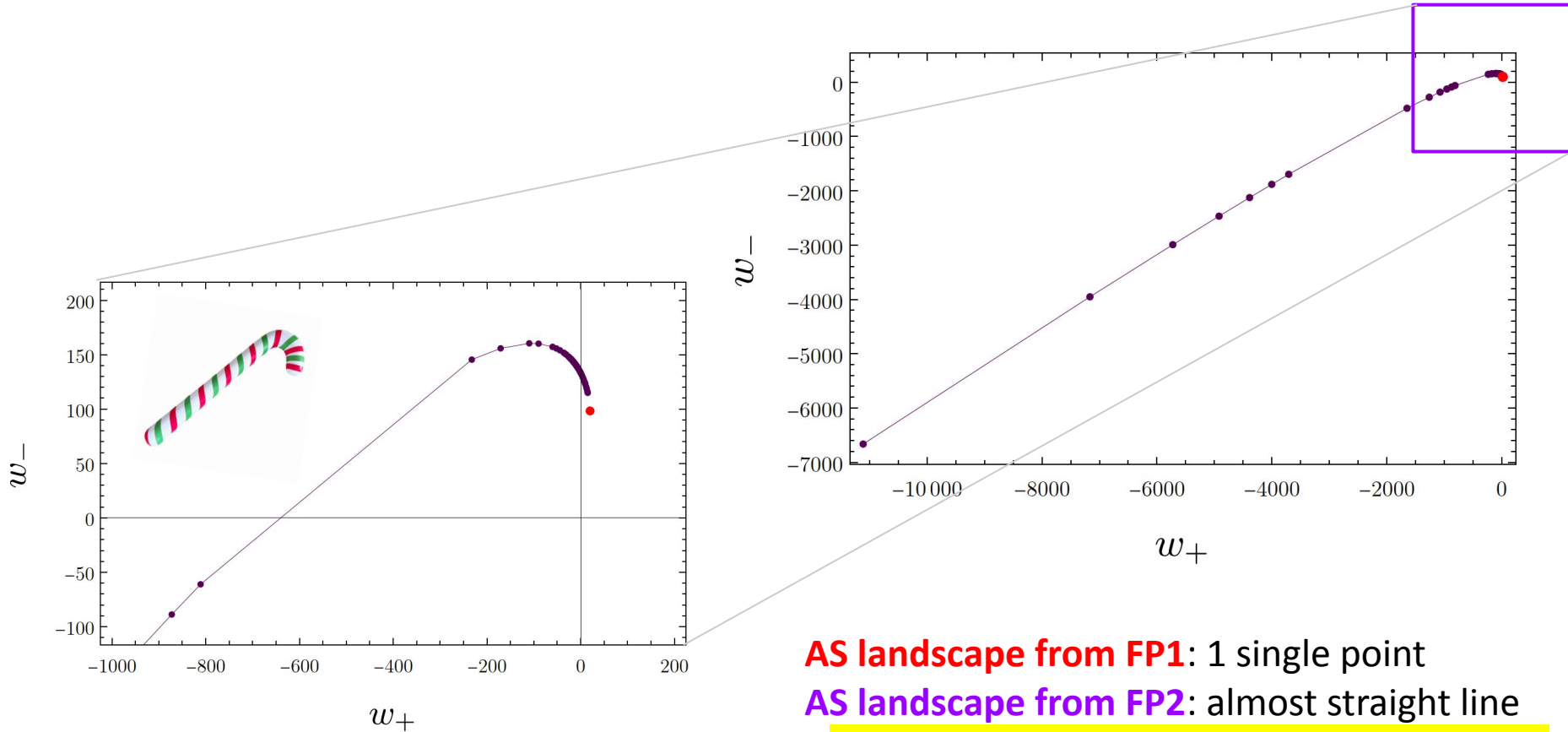
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+ small "candy cane" regime which connects the two

Asymptotic Safety Landscapes

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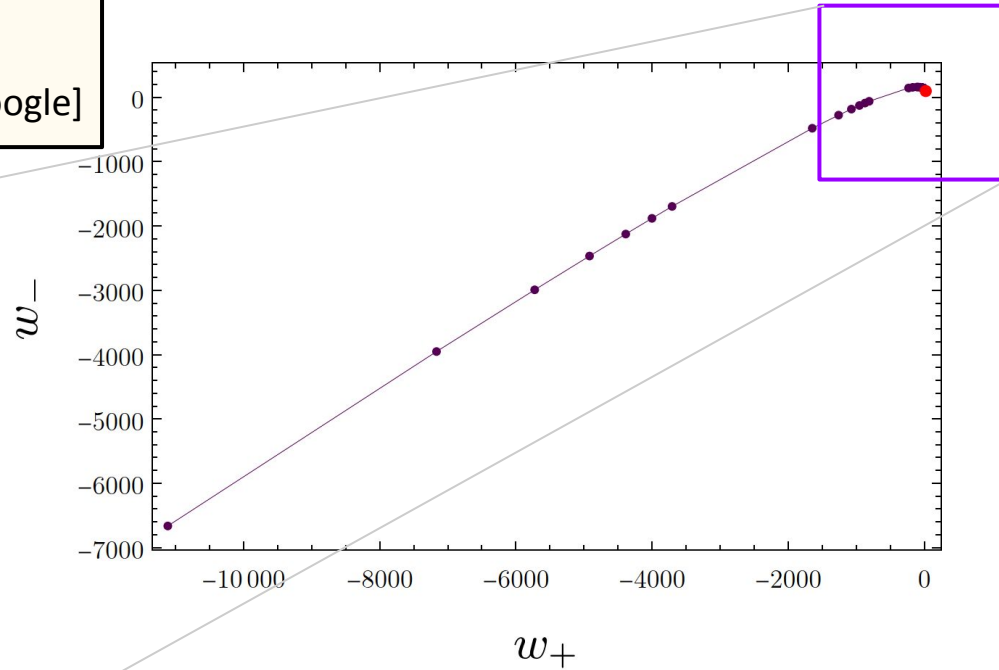
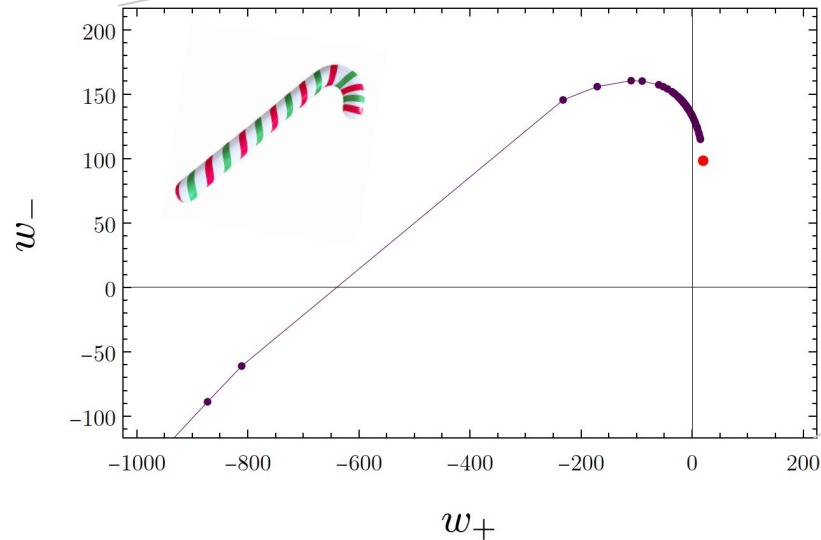
Asymptotic Safety Landscapes

[Knorr, AP, 2405.08860]

Some important nomenclature...

"The curved part of the candy cane is called the **warble**, and the straight part is called the **strabe**."

[Google]



- AS landscape from FP1: 1 single point
- AS landscape from FP2: almost straight line + small "candy cane" regime which connects the two

(Some) positivity bounds and the Weak Gravity Conjecture

- **Positivity bounds:**

$$w_+ > w_- , \quad 3w_+ - w_- - 2|w_C| > 0$$

[Carrillo González, de Rham, Jaitly, Pozsgay, Tokareva, '23]

- **Electric WGC in the presence of higher derivatives**

$$3w_+ - w_- + 2w_C > 0$$

[Cheung, Liu, Remmen, '18]

Caveats

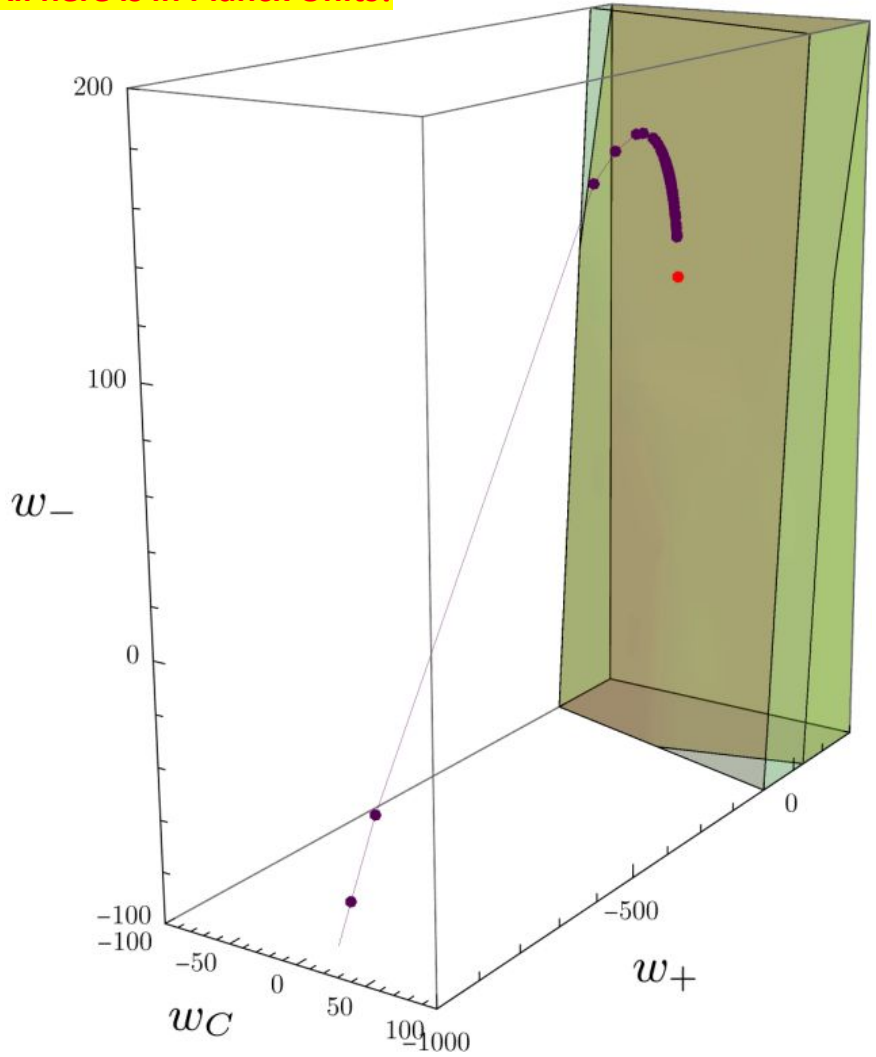
- **CAVEAT:** ambiguity in defining the logs in the presence of massless poles, positivity bounds are typically identified in theories with massive DOF that are integrated out
- **EXPECTATION:** Standard positivity bounds may be violated in the presence of gravity

$$c > 0 \quad \rightarrow \quad c > -\mathcal{O}(1) M^{-2} M_{Pl}^{-2}$$

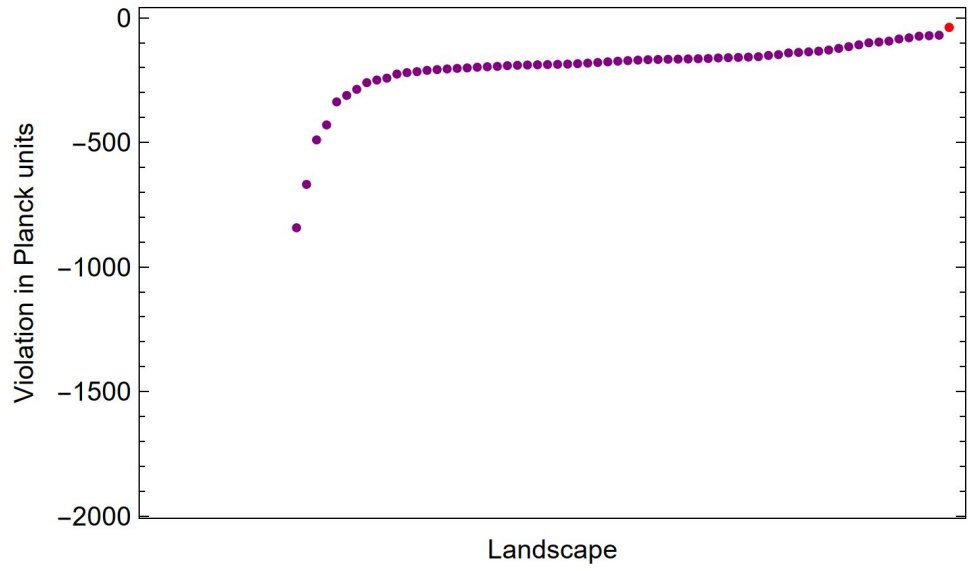
[See talk by Shuang-Yong Zhou]

[Alberte, de Rham, Jaitly, Tolley, '20+'21)]

All here is in Planck Units!



[Knorr, AP, 2405.08860]



Planck-scale suppressed violations of WGC and positivity bounds:

- In the “*strabe*” part of the landscape the violation gets larger, in the “*warble*” it is minimized.
- The landscape from the most predictive FP minimizes the violation.

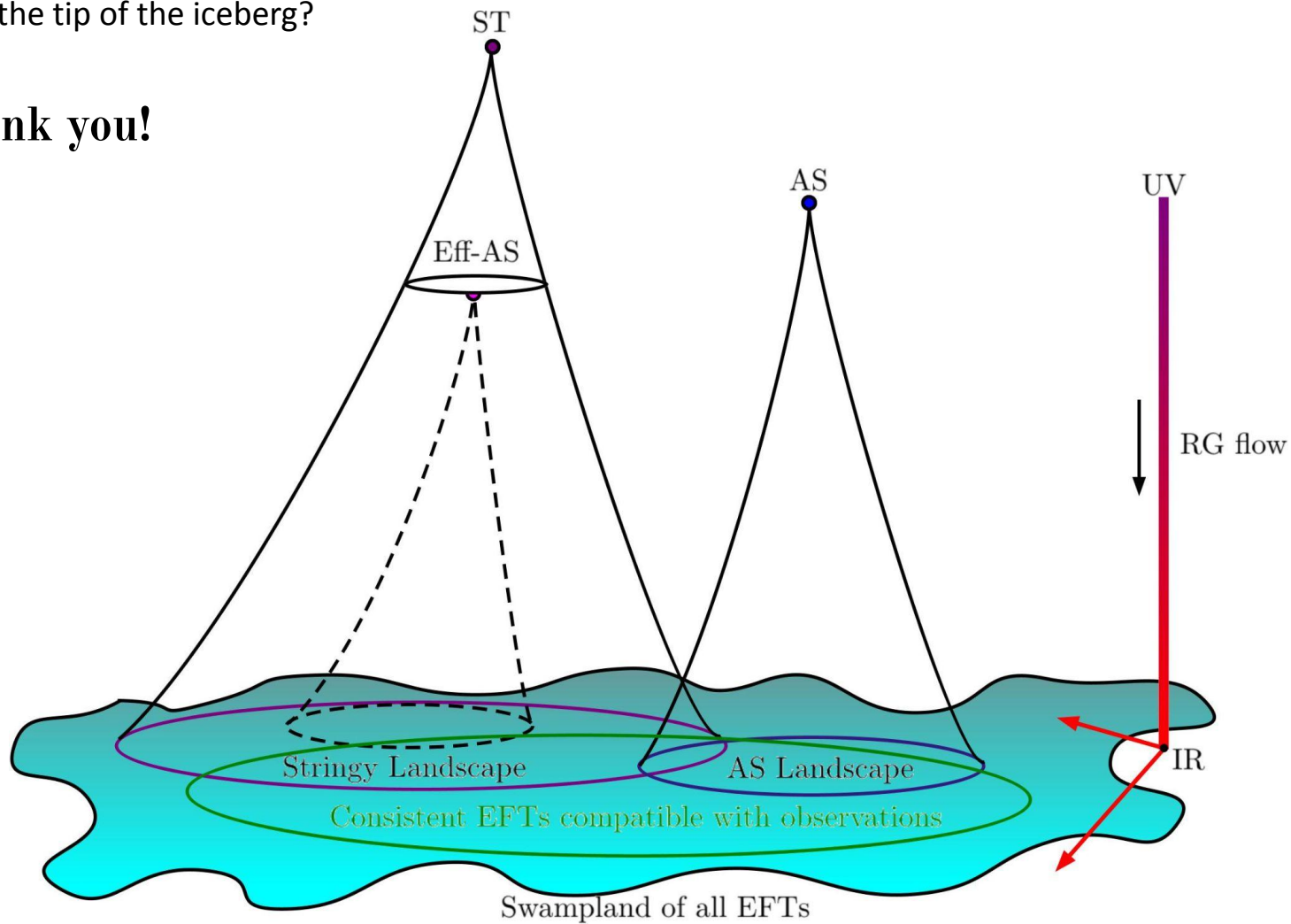
Compatible with expectations/conjectures from EFT in the presence of massless poles:
Alberte, de Rham, Jaitly, Tolley, PRD 102, 125023 (2020)

Summary

- *Computing QG landscapes: “killing N birds with one stone”*
Testing swampland conjectures in other approaches to quantum gravity, e.g., asymptotic safety
Testing consistency of QG predictions (from different approaches): positivity positivity bounds
ST vs AS landscape (vs others?): comparing predictions
String Lamppost Principle: do swampland conjectures identify the string landscape or are more general?
- **Very clear recipe in asymptotic safety:**
 - Start from UV fixed point, integrate the FRG flow down to the IR, identify AS landscape
 - Find intersections: swampland constraints, positivity bounds, observations, other QG landscapes
- **Case study 1: AS landscapes in one-loop quadratic gravity**
Caveats: toy model, not full FRG computation, not all swampland criteria, electromagnetic duality assumed
 - Non-trivial intersection
 - WGC is satisfied, de Sitter and trans-Planckian can be violated
- **Case study 2: AS landscapes in non-perturbative photon-graviton systems**
Caveats: toy model, definitions of Wilson coefficients with logs is ambiguous
 - Planck-scale-suppressed violations of positivity bounds
 - Violation is minimized by the most predictive fixed point / the smaller sub-landscape (one point)
- **Common feature of models 1 and 2: Near-flatness of the AS landscape?**
Coincidence or universal pattern? Implications? Fundamental explanation?

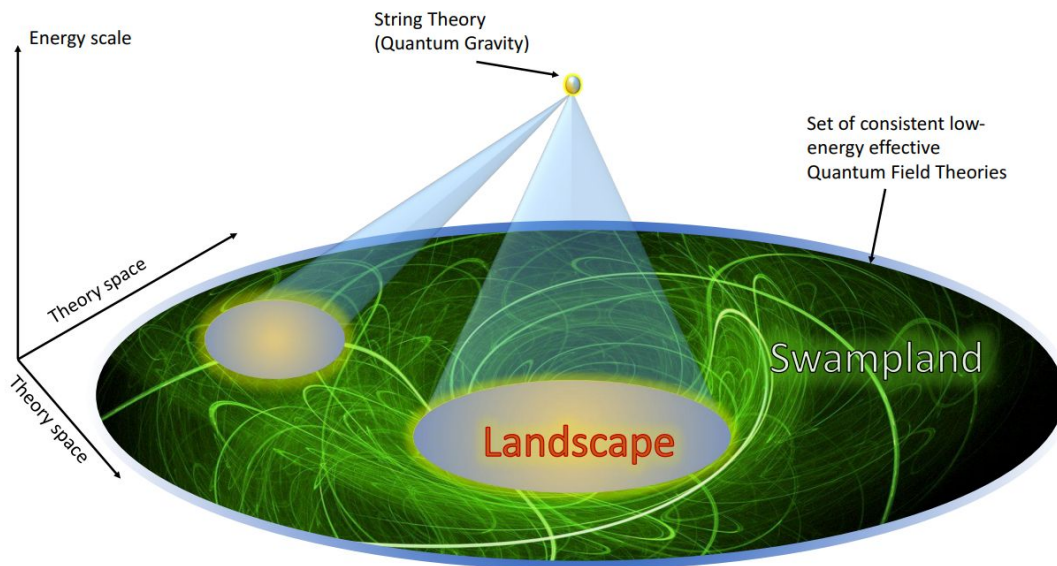
...merely the tip of the iceberg?

Thank you!



One Attempt within String Theory: The Swampland Program

- **What: Swampland Program:** aims at identifying the “string landscape” of EFTs coming from its UV completion
- **How: via Swampland “Criteria”,** tied to string (mostly susy) constructions:
 - Partially inspired by ST (but also from general considerations, e.g., BH physics and cosmology);
 - Tested within string models, no counterexamples

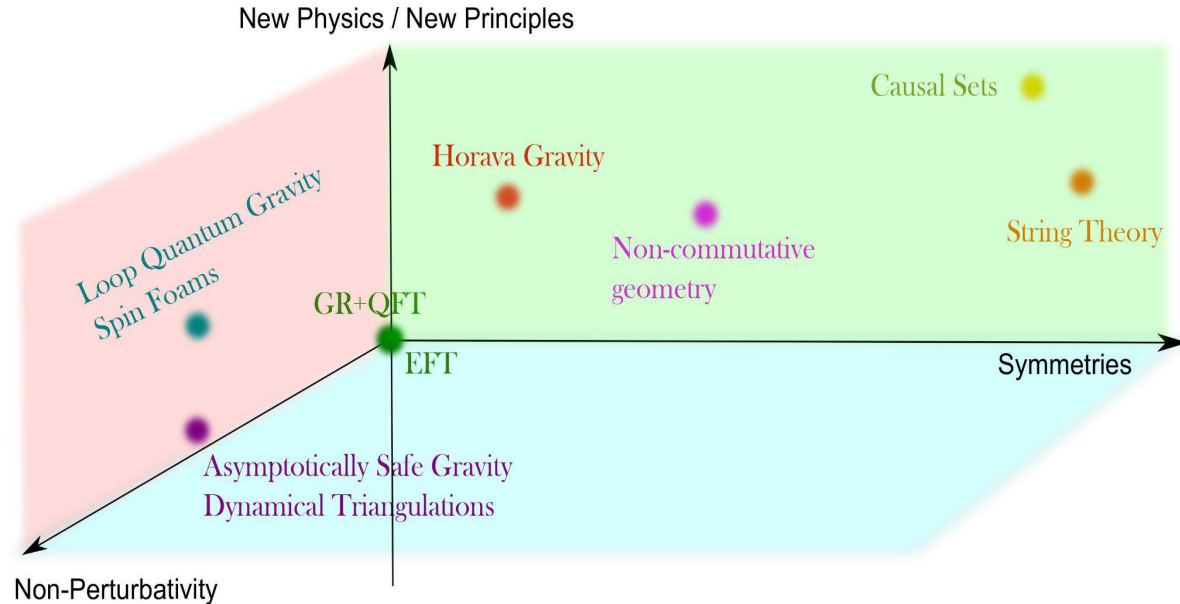


E. Palti (2019)

The realm of Quantum Gravity

Several theories:

- String Theory
- Asymptotically Safe Gravity
- Dynamical Triangulation
- Non-local gravity
- Loop quantum gravity
- Group field theory
- Causal sets
- Horava gravity
- ...

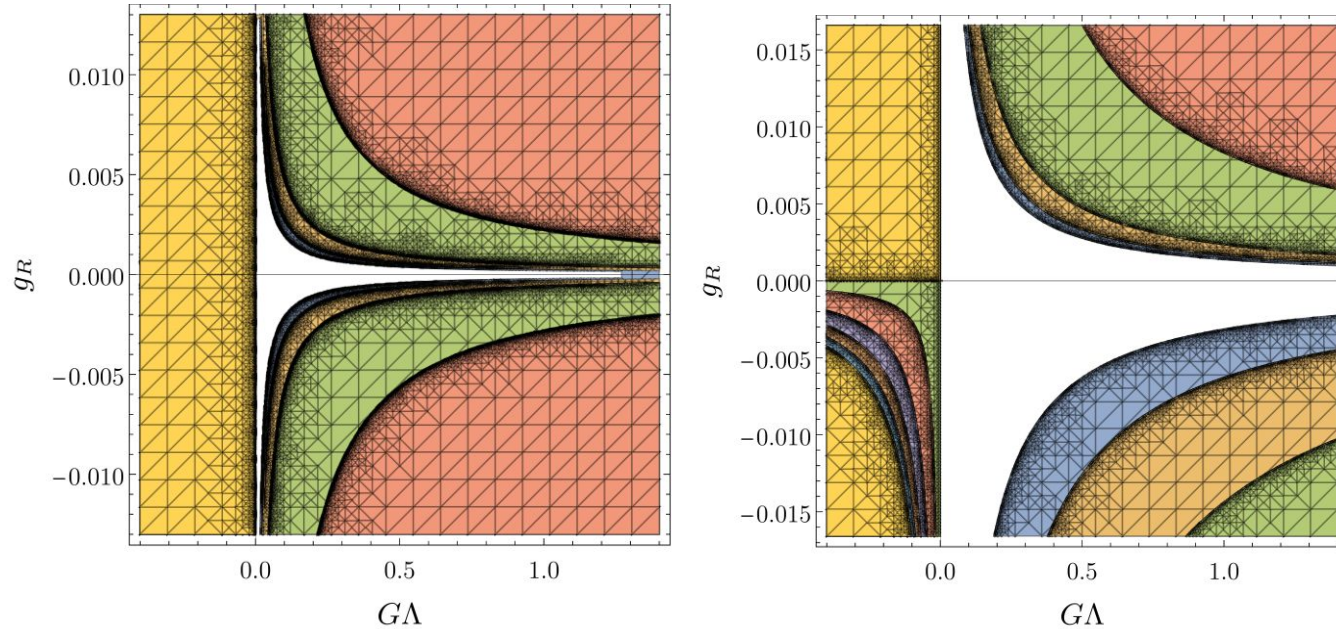


Goals:

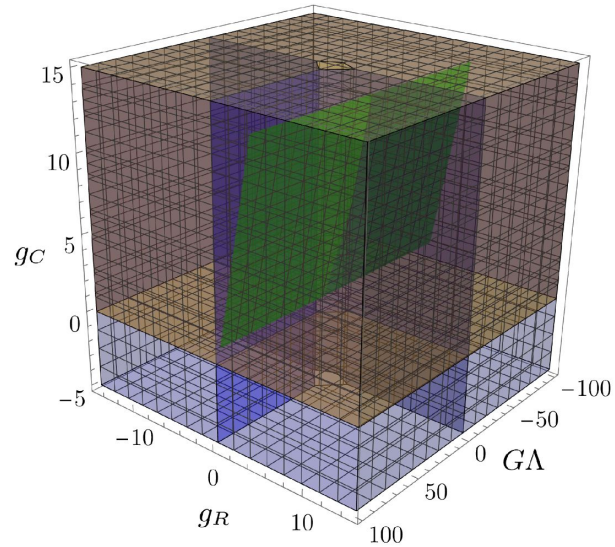
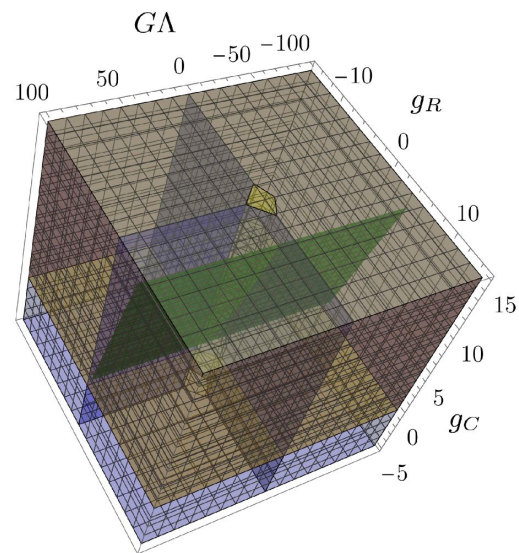
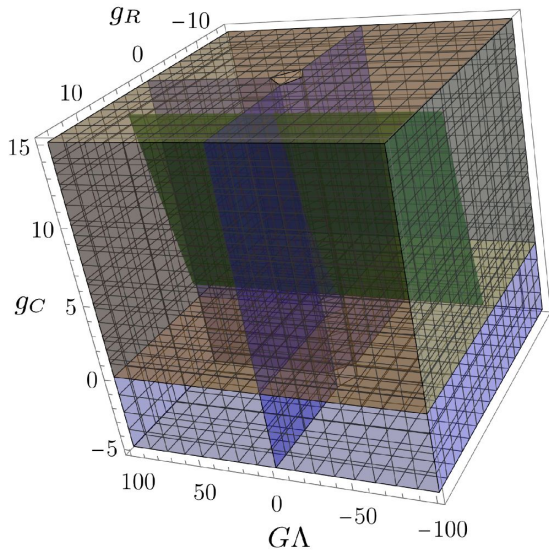
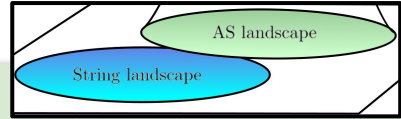
- Consistency: Renormalizability, unitarity, compatibility with large scale physics & observations
- Predictions: quantum cosmology, quantum black holes, scattering amplitudes, grav. Waves
- Comparison between approaches?

- Swampland conjectures:

→ De Sitter and trans-Planckian conjectures



$$0 \leq c \leq 3.5, \quad f = 0.1 \text{ (left),} \quad f = 1 \text{ (right)}$$



Green plane:

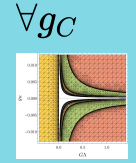
AS landscape [one-loop quadratic approx]

$$EFT_{AS} \approx \{g_R = -0.74655 - \frac{2}{3}\omega_- g_C\} \quad g_C > 0$$

Blue hyperplane:

Stringy “no de Sitter” conjecture

[~ no positive cosmological constant]



Yellow hyperplane:

Weak gravity conjecture

[~ gravity is the weakest force] $g_C > 0$

Within this simple model of AS, and only some swampland conjectures

⇒ non-trivial intersection (partial compatibility?)

[Basile, AP. 2107.06897]

- **Swampland conjectures:**

→ **De Sitter conjecture** [(Obied, Ooguri, Spoyneiko, Vafa, 2018), (Ooguri, Palti, Shiu, Vafa, 2019)]

$$M_{Pl} \|\nabla V\| \geq cV \quad \text{for } \Delta\phi \leq fM_{Pl} \quad f, c \sim \mathcal{O}(1)$$

→ **Trans-Planckian conjecture** [(Bedroya, Vafa, 2020)]

Relevant for early-universe cosmology. Special value of c:

$$c = \frac{2}{\sqrt{(d-1)(d-2)}}$$

In the case of higher-derivative gravity V is the potential of the additional scalar mode in the $F(R)$ part of the action. In our case this is a **Starobinsky-like potential**:

$$V(\phi) = \frac{M_{Pl}^2}{8\pi} e^{-2\sqrt{\frac{2}{3}} \frac{\phi}{M_{Pl}}} \left(\frac{3m^2}{4} \left(e^{\sqrt{\frac{2}{3}} \frac{\phi}{M_{Pl}}} - 1 \right)^2 + \Lambda \right) \quad g_R = - \frac{M_{Pl}^2}{(8\pi) \cdot 12m^2}$$

⇒ Non-trivial bounds for different f and c .

- **AS model**: photon-graviton systems at quadratic order, only **essential couplings** included

[see Knorr's talk!]

$$\mathcal{L} = -\frac{R}{16\pi G_N} + \Theta_E E + \frac{1}{4} F^{\mu\nu} F_{\mu\nu} + G_2 (F^{\mu\nu} F_{\mu\nu})^2 + G_4 F^\mu{}_\nu F^\nu{}_\rho F^\rho{}_\sigma F^\sigma{}_\mu + G_{CFF} C^{\mu\nu\rho\sigma} F_{\mu\nu} F_{\rho\sigma}$$

- Three dimensionless Wilson coefficients (redefined for convenience; only one log-presc. ambiguity)

$$w_+ = \frac{1}{2} \frac{G_2 + G_4}{(16\pi G_N)^2}, \quad w_- = \frac{1}{2} \frac{G_2 - G_4}{(16\pi G_N)^2} + b \ln[16\pi G_N k^2], \quad w_C = \frac{G_{CFF}}{16\pi G_N}$$

- **Two UV fixed points:**

FP1: one relevant direction (most predictive!)

$$g^* = 0.131, \quad g_+^* = 0.351, \quad g_-^* = 3.327, \quad g_{CFF}^* = 0.00375$$

$$\theta_1 = 1.845, \quad \theta_{2,3} = -0.239 \pm 0.0155i, \quad \theta_2 = -0.291$$

FP2: two relevant directions

$$g^* = 0.126, \quad g_+^* = -0.308, \quad g_-^* = 4.001, \quad g_{CFF}^* = -0.00410$$

$$\theta_1 = 1.936, \quad \theta_2 = 0.184, \quad \theta_3 = -0.141, \quad \theta_4 = -0.236$$

