# CONTRIBUTION OF SCALAR DIQUARKS TO THE $\Delta I=1 / 2$ RULE 

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#### Abstract

One of the novel features of the superstring inspired models is the possible appearance of colour triplet particles with diquark couplings They can mediate hadronic decays of baryons and mesons We investigate their contribution to the $\Delta l=1 / 2$ rule through the operator product expansion


The superstring theory based on the $\mathrm{E}_{8} \times \mathrm{E}_{8}^{\prime}$ group in ten dimensions [1,2] seems to be the most promising candidate for a unified theory of all fundamental forces Compactification on a Kahler manifold with $\operatorname{SU}(3)$ holonomy leads to an $N=1$ supergravity theory, while an $\mathrm{E}_{6} \times \mathrm{SU}(3)_{\mathrm{H}}$ group emerges [3] Further breaking of $\mathrm{E}_{6}$ by the Hosotanı mechanısm [4] implies a low-energy gauge group of rank five or six which contains the standard $\operatorname{SU}(3) \times \operatorname{SU}(2) \times \mathrm{U}(1)$ group of electroweak and strong interactions [5,6] In the recent literature [7], much effort has been made in order to investigate all possible residual gauge groups contaınıng $\operatorname{SU}(3) \times \operatorname{SU}(2) \times \mathrm{U}(1)$ However, since there are a lot of phenomenological constraints, the construction of an acceptable low-energy model is not an easy task Several problems have already been discussed in the context of superstring-inspired models, 1 e , neutrino masses [8], flavour changing interactions [9], proton decay [10], additional neutral gauge bosons [11], etc
In this letter we are going to discuss the contribution to the $\Delta I=1 / 2$ rule in non-leptonic decays of mesons and baryons from interactions involving the new scalar quarks $D$ and $D^{c}$ which are found in the 27 -dimensional representation of $\mathrm{E}_{6}$ According to the conventional assignment we get

[^0]\[

$$
\begin{aligned}
\{27\} & =\left(\mathrm{u}, \mathrm{~d}, \mathrm{u}^{\mathrm{c}}, \mathrm{e}^{\mathrm{c}}\right)+\left(\mathrm{d}^{\mathrm{c}}, \mathrm{v}_{\mathrm{e}}, \mathrm{e}\right)+\mathrm{v}^{\mathrm{c}}
\end{aligned}
$$
\]

If we restrict ourselves to the rank-five group, the $D$ and $\mathrm{D}^{c}$ fields have the following quantum numbers under $\operatorname{SU}(3) \times \operatorname{SU}(2) \times U(1) \times U(1)$, which is the minimal group containing the standard group
$\mathrm{D}=(3,1,-1 / 3,-2 / 3)$,
$D^{c}=(\overline{3}, 1,1 / 3,-1 / 6)$
The most general superpotential coming from the trilinear couplings $27^{3}$ is [9]

$$
\begin{equation*}
W=W_{0}+W_{1}+W_{2}+W_{3}, \tag{2}
\end{equation*}
$$

where

$$
\begin{align*}
W_{0} & =\lambda_{\mathrm{L}} \overline{\mathrm{H}} \mathrm{~L}^{\mathrm{c}}+\lambda_{\mathrm{u}} \mathrm{HQu}^{\mathrm{c}}+\lambda_{\mathrm{d}} \overline{\mathrm{H} Q \mathrm{~d}^{c}} \\
& +\lambda_{\mathrm{N}} \mathrm{H} \overline{\mathrm{H}} \mathrm{~N}+\lambda_{\nu} \mathrm{HLV}^{\mathrm{c}}+\lambda_{\mathrm{D}} \mathrm{DD}^{\mathrm{c}} \mathrm{~N}, \tag{3a}
\end{align*}
$$

$W_{1}=\lambda_{1} \mathrm{DQQ}+\lambda_{1} \mathrm{D}^{\mathrm{c}} \mathbf{u}^{\mathrm{c}} \mathrm{d}^{\mathrm{c}}$,
$W_{2}=\lambda_{2} \mathrm{D}^{c} \mathrm{LQ}+\lambda_{2}^{\prime} \mathrm{Du}^{\mathrm{c}} \mathrm{e}^{\mathrm{c}}$,
$W_{3}=\lambda_{3} D^{c} v^{c}$
A detailed analysis of the above superpotential has been done elsewhere [9] Here we just recall that in order to avoid several drawbacks, like fast proton decay, flavour-changing neutral currents, weak universality, $W_{1}, W_{2}$ and $W_{3}$ cannot coexist in the
superpotential In fact, the above terms could be forbidden from the superpotential either by topological properties or by imposing discrete symmetries Here we are interested in the phenomenological implications of the $W_{1}$ term which gives rise to non-leptonic decays of mesons and baryons involving the D and $\mathrm{D}^{\mathrm{c}}$ scalar quarks

Our approach to the $\Delta I=1 / 2$ rule will be through the operator product expansion (OPE) [12] Our aim is to check if the inclusion of $D$ and $D^{c}$ scalars can change the known picture [13] we get from the QCD corrections to the relevant operators The Penguin diagram has been discussed elsewhere [14] (though without inclusion of QCD corrections), therefore we restrict ourselves to the operators $O_{1}$ and $O_{2}$ appearing in the effective hamiltonian $H_{\mathrm{w}}$
$O_{1}=\left(\bar{u}_{\mathrm{L}} \gamma^{\mu} \mathrm{s}_{\mathrm{L}}\right)\left(\overline{\mathrm{d}}_{\mathrm{L}} \gamma_{\mu} \mathrm{u}_{\mathrm{L}}\right)$,
$O_{2}=\left(\overline{\mathrm{u}}_{\mathrm{L}} \gamma^{\mu} t^{a} \mathrm{~s}_{\mathrm{L}}\right)\left(\overline{\mathrm{d}}_{\mathrm{L}} \gamma_{\mu} t^{a} \mathrm{u}_{\mathrm{L}}\right)$,
where the $t^{a}$ are the $\operatorname{SU}(3)$ matrices ( $a=1, \quad, 8$ ) The above operators mix under renormalization, giving as eigenvectors, after diagonalization
$O_{-}=O_{1}-3 O_{2}, \quad O_{+}=O_{1}+\frac{3}{2} O_{2}$
The first one has $\Delta I=1 / 2$ while the second has $\Delta I=1 / 2$ and $3 / 2$ The leading logarithmic approximation gives an enhancement factor to the first
$a_{-}=\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{w}}\right)\right]^{4 / h}$,
where $\alpha_{s}$ is the running coupling constant of QCD
$\alpha_{\mathrm{s}}(Q)=2 \pi / b \ln (Q / A)$,
$\mu$ is the characteristic hadronic scale, $M_{\mathrm{w}}$ is the Wboson mass and $b=11-\frac{2}{3} \cdot$ (\# flavours) is the $\mathrm{O}\left(g^{3}\right)$ term in the QCD $\beta$-function The second operator gets a suppression factor
$a_{+}=\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{w}}\right)\right]^{-2 / b}$
Therefore the enhancement of $O_{-}$relative to $O_{+}$is

$$
\begin{align*}
& F_{\mathrm{W}} \equiv a_{-} / a_{+}=\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{w}}\right)\right]^{6 / b} \simeq 5 \\
&\left(\mu=140 \mathrm{MeV}, N_{\mathrm{f}}=4 \text { and } A=70 \mathrm{MeV}\right), \tag{8}
\end{align*}
$$

not enough to explain the experımental value ( $\sim 20$ )
Now, how is this picture modified with the inclusion of D-scalars? These new particles can mediate only $\Delta I=1 / 2$ decays Therefore we expect no new


Fig $1 \mathrm{D}\left(\mathrm{D}^{\mathrm{c}}\right)$ mediated $\Delta S=1$ transition
operators to appear in the effective hamiltonian The only thing we have to calculate is the zeroth order coefficient of the new contribution to the $O_{-}$ operator

Let us assume for the moment that there is no mixing between D and $\mathrm{D}^{c}$ The coefficient to the operator $O_{-}$is evaluated through the diagram of fig 1 This diagram, with the D-scalar gives

$$
\begin{align*}
A_{\mathrm{D}} & =\left(\bar{u}_{\mathrm{L},}^{\mathrm{c}} \mathrm{~S}_{\mathrm{L}}\right)\left(\overline{\mathrm{u}}_{\mathrm{L} /} \mathrm{d}_{\mathrm{L} k}^{\mathrm{c}}\right) \\
& \times \epsilon^{l j m} \epsilon^{l k m}\left(-\lambda_{1}^{2} / M_{\mathrm{D}}^{2}\right)=\left(\lambda_{1}^{2} / M_{\mathrm{D}}^{2}\right) \frac{1}{2} \frac{2}{3}\left(O_{1}-3 O_{2}\right) \\
& =\left(\lambda_{1}^{2} / M_{\mathrm{D}}^{2}\right) \frac{1}{3} O_{-}, \tag{9}
\end{align*}
$$

where $l, j, k$ and $l$ are colour indices and we have used Fierz rearrangements and identities of conjugate spinors Eq (9) shows also explicitly that the D's contribute only to $\Delta I=1 / 2$ transition A factor of 2 must be included in $A_{\mathrm{D}}$ due to the two terms we get from the antisymmetry with respect to $\mathrm{SU}(2)$ indices of the DQQ term,
$A_{\mathrm{D}}=\frac{2}{3}\left(\lambda_{1}^{2} / M_{\mathrm{D}}^{2}\right) O_{-}$
The enhancement factor $F$ becomes

$$
\begin{align*}
F_{\mathrm{D}} & =F_{\mathrm{w}} \\
& +\frac{\frac{2}{3}\left(\lambda_{\mathrm{1}}^{2} / M_{\mathrm{D}}^{2}\right)\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{D}}\right)\right]^{4 / b}}{\sqrt{2} G\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{w}}\right)\right]^{-2 / b}}, \tag{11}
\end{align*}
$$

where we have imposed the strong assumption that the D's couple to the usual quarks through the usual linear combination (KM angles) [14]

The $\mathrm{D}^{\mathrm{c}}$ scalar induces the same operator but with right-handed currents,
$O^{\mathrm{R}}=O_{1}^{\mathrm{R}}-3 O_{2}^{\mathrm{R}}$
This operator induces $\Delta I=1 / 2$ transitions and we know that, under renormalization, it has the same


Fig 2 The enhancement factor $F_{\mathrm{DD}}$ as a function of the mass $M_{\mathrm{D}}\left(M_{\mathrm{D}}=M_{\mathrm{D}}\right)$, for different values of $\lambda\left(\equiv \lambda_{1}=\lambda_{1}^{\prime}\right)$
behaviour as the left-handed $O_{-}$operator Therefore we get
$F_{\mathrm{DD}}=F_{\mathrm{w}}+F_{\mathrm{D}}$

$$
\begin{equation*}
+\frac{\frac{1}{3}\left(\lambda_{1}^{2} / M_{\mathrm{Dc}}^{2}\right)\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{Dc}}\right)\right]^{4 / b}}{\sqrt{2 G\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{w}}\right)\right]^{-2 / b}}} \tag{12}
\end{equation*}
$$

To have a feeling of the above quantity $F_{\mathrm{D} \mathbf{D}}$, it is natural to put $\lambda_{1}=\lambda_{1}^{\prime}$ and $M_{\mathrm{D}}=M_{\mathrm{D}}$ In fig 2 we plot this quantity as a function of $M_{\mathrm{D}}$, for different values of $\lambda$ We see that even with $\lambda=03$ we must have $M_{\mathrm{D}} \leqslant 150 \mathrm{GeV}$ in order to gain $25 \%$ in enhancement, relative to $F_{\mathrm{w}}$

We know that L-R currents [13], under renormalization, get an enhancement significantly bigger than $\mathrm{L}-\mathrm{L}$ and $\mathrm{R}-\mathrm{R}$ currents The corresponding exponent is $10 / b$ instead of $4 / b$ If we assume $D-D^{c}$ mixing, then an operator with the desired L-R structure will appear in the effective hamiltonian If $\phi$ is the mixing angle, $D_{1}$ and $D_{2}$ the physical states after diagonalization and $\bar{\lambda}=\sqrt{\lambda_{1} \lambda_{i}^{\prime}}$ a mean coupling, the enhancement factor from the L-R operator is
$F_{\mathrm{LR}}=\mid \bar{\lambda}^{2} \sin \phi \cos \phi$

$$
\begin{align*}
& \times\left\{\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{D}_{1}}\right)\right]^{10 / b} / M_{\mathrm{D}_{1}^{2}}\right. \\
& \left.-\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{D}_{2}}\right)\right]^{10 / b} / M_{\mathrm{D}_{2}^{2}}\right\} \\
& \times\left\{\sqrt{2} G\left[\alpha_{\mathrm{s}}(\mu) / \alpha_{\mathrm{s}}\left(M_{\mathrm{w}}\right)\right]^{-2 / b}\right\}^{-1} \mid \tag{13}
\end{align*}
$$



Fig 3 Contours of the enhancement factor $F_{1 \mathrm{R}}$ in the plane of ( $M_{\mathrm{D}_{1}}, M_{\mathrm{D}_{2}}$ ) for different values of the mixing angle $\phi\left(=30^{\circ}, 45^{\circ}\right)$ and $\bar{\lambda}(=01,02,03)$ (a) $F_{\mathrm{LR}}=10$, (b) $F_{\mathrm{LR}}=01$

In fig 3 we show the contour of $F_{\mathrm{LR}}$ in the ( $M_{\mathrm{D}_{1}}, M_{\mathrm{D}_{2}}$ ) plane, and for $\phi=30^{\circ}$ and $45^{\circ}$ Again here we notice that even with $\bar{\lambda}=03$ and maximal mixing ( $\phi=45^{\circ}$ ), one of the $\mathrm{D}_{12}$ must be below 200 GeV in order to have $F_{\mathrm{LR}} \sim 10$ or $F_{\mathrm{LR}} / F_{\mathrm{W}} \sim 20 \%$

In conclusion, treating the D-mediated hadronic decays of mesons and baryons as a short-distance effect, we calculated the contribution of the above D-scalar to the $\Delta I=1 / 2$ rule ${ }^{\# 1}$ We see that we cannot expect any sizeable contribution, which, even in the most favourable case ( $\bar{\lambda}=03$, maximal mixing $\phi=45^{\circ}$ ) does not exceed the (first-order) result from the weak effective hamiltonian by $20 \%$ if $M_{D}=200$ GeV

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\#1 No standard method can be applied to the matrix elements, sunce D-medrated decays are not of the so-called external type quark graphs

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