

Cosmology of String Theory: Inflation and Beyond

F. Quevedo, Cambridge. UNIVERSENET 2007. Mytilene

OUTLINE

- String Theory and 4D Inflation

FQ/hepth/0210292

- Moduli Stabilization and the String Landscape
(KKLT and LARGE volume scenarios)

- Inflation and Moduli Stabilization (open string vs closed string inflaton).

C. P. Burgess
0708.2865 [hep-th]

- After Inflation

MOTIVATION

- Inflation: very successful but is only ad-hoc scenario in search of a theory
- String theory: fundamental theory but lacks experimental tests.
- Is it possible to ‘derive’ inflation from string theory?

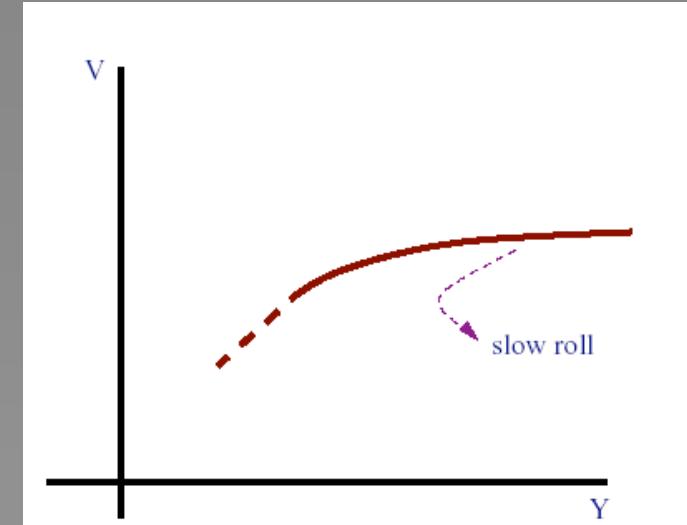
- Need to compute scalar potential from String theory satisfying slow-roll conditions:

$$\epsilon \equiv \frac{M_{Planck}^2}{2} \left(\frac{V'}{V} \right)^2 \ll 1 ,$$

$$\eta \equiv M_{Planck}^2 \frac{V''}{V} \ll 1 .$$

Number of e-folds $N > 60$

$$N(t) \equiv \int_{t_{init}}^{t_{end}} H(t') dt' = \int_{\psi_{init}}^{\psi_{end}} \frac{H}{\dot{\psi}} d\psi = \frac{1}{M_{Planck}^2} \int_{\psi_{end}}^{\psi_{init}} \frac{V}{V'} d\psi .$$



Density perturbations

$$\delta_H = \frac{2}{5} \mathcal{P}_{\mathcal{R}}^{1/2} = \frac{1}{5\pi\sqrt{3}} \frac{V^{3/2}}{M_p^3 V'} = 1.91 \times 10^{-5} ,$$

$$n - 1 = \frac{\partial \ln \mathcal{P}_{\mathcal{R}}}{\partial \ln k} \simeq 2\eta - 6\epsilon , \quad \frac{dn}{d \ln k} \simeq 24\epsilon^2 - 16\epsilon\eta + 2\xi^2 .$$

$$n_{grav} = \frac{d \ln \mathcal{P}_{grav}(k)}{d \ln k} = -2\epsilon .$$

HISTORY

- $t < 1986$ Calabi-Yau String Compactifications: Many free moduli (size and shape of extra dimensions) from g_{mn} , B_{mn} , φ , A_m^l

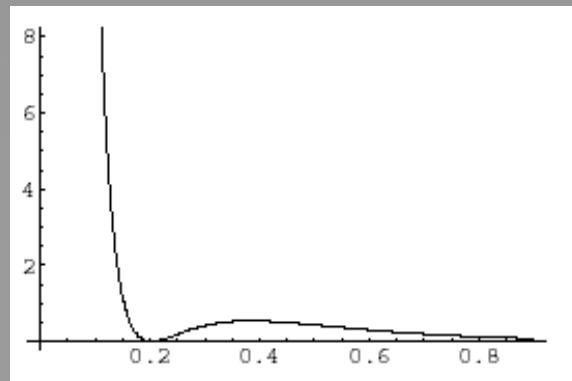
Candelas et al.

Dilaton S,
Kähler T
Complex structure U
Wilson lines W

- $1986 < t < 1991$ Geometric moduli: candidate for inflaton fields. But no potentials ($V=0$).

Binetruy-Gaillard, Banks et al

- Or V too steep:



Brustein-Steinhardt

New Problems:

- **Overshooting**

(natural to end up in runaway)

Brustein-Steinhardt

- **Cosmological Moduli Problem**

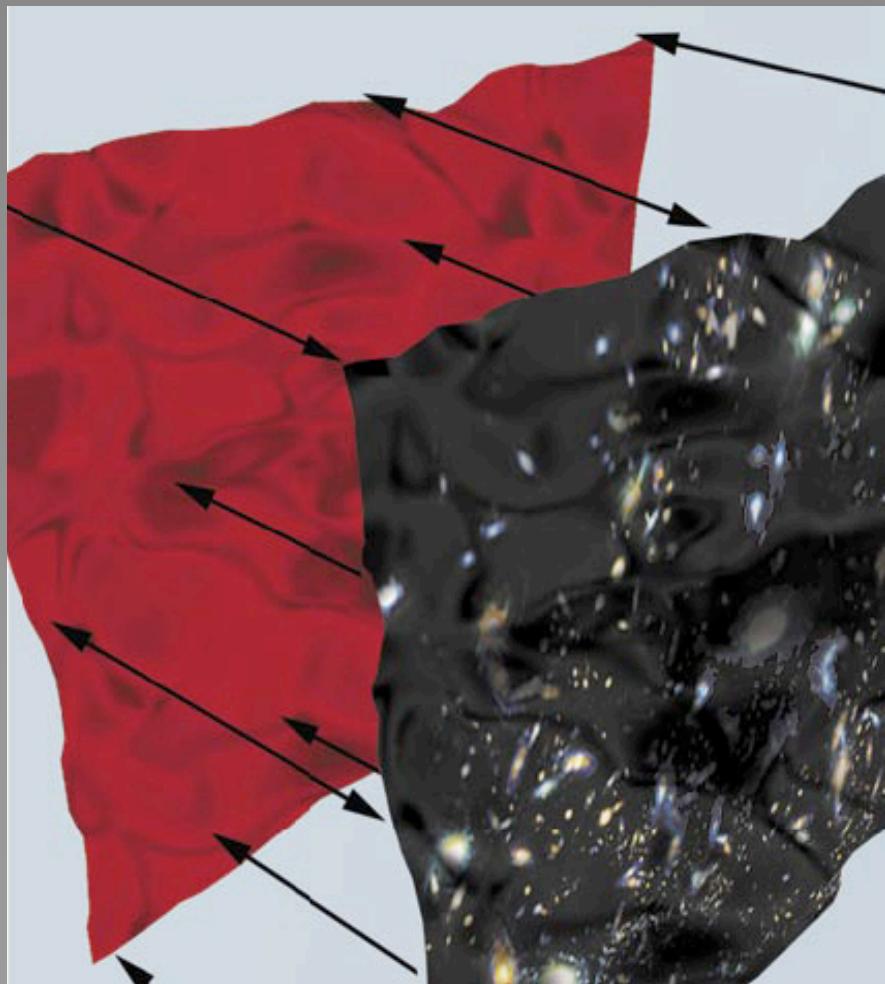
(moduli overclose the universe or ruin
nucleosynthesis)

Coughlan et al. 82

Banks et al. 94

De Carlos et al. 93

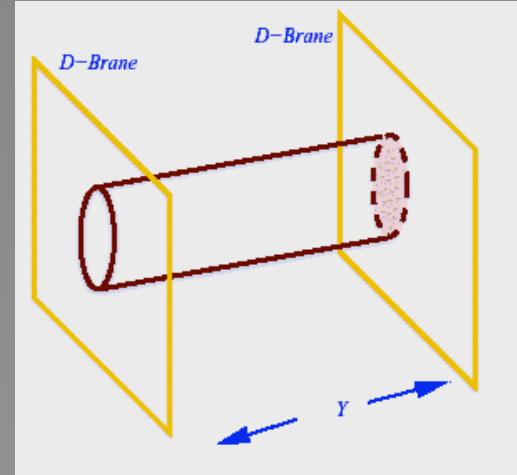
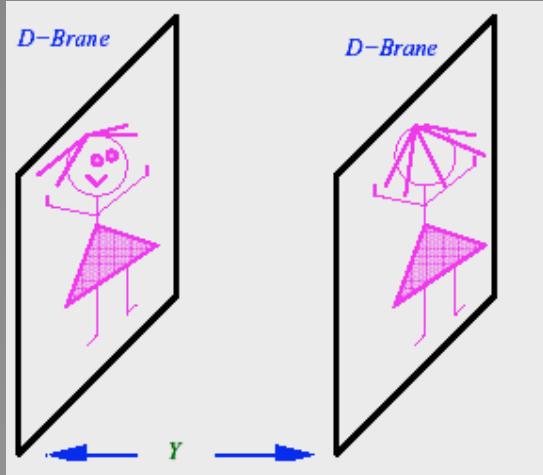
(t>1995) More moduli!



Open string moduli:
Brane separation
Also Wilson Lines

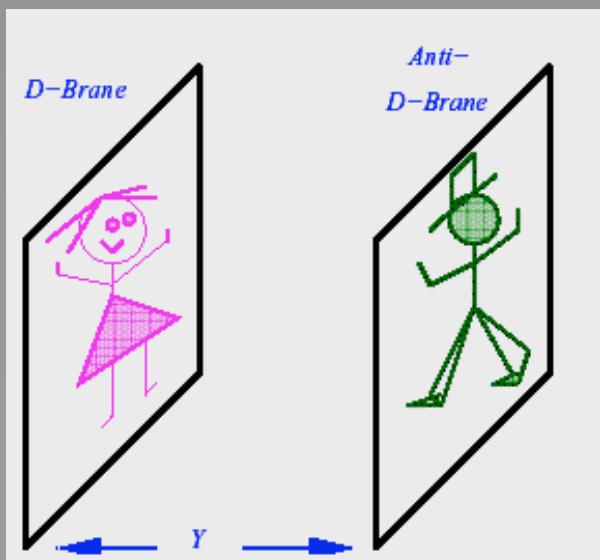
See Avgoustidis talk

- t=199 : D-brane inflation. But $V=0$ or non-calculable.



Dvali-Tye

- t=2001 Brane/Antibrane inflation:



Burgess et al., Dvali et al

$$V(Y) = A - \frac{B}{Y^{d_{\perp}-2}},$$

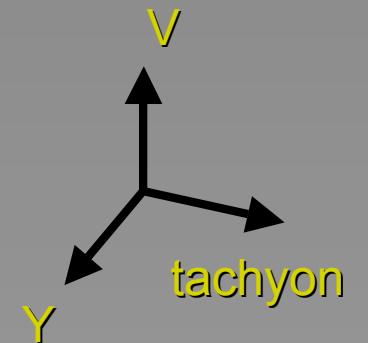
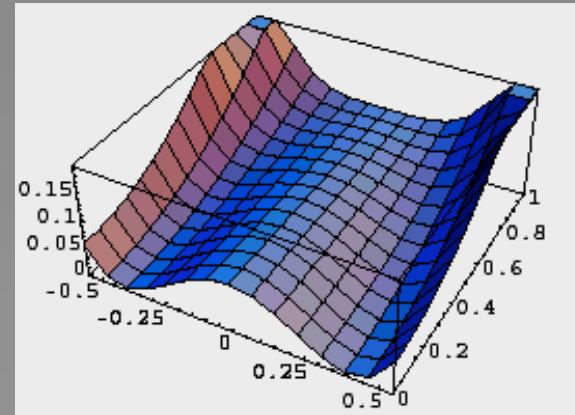
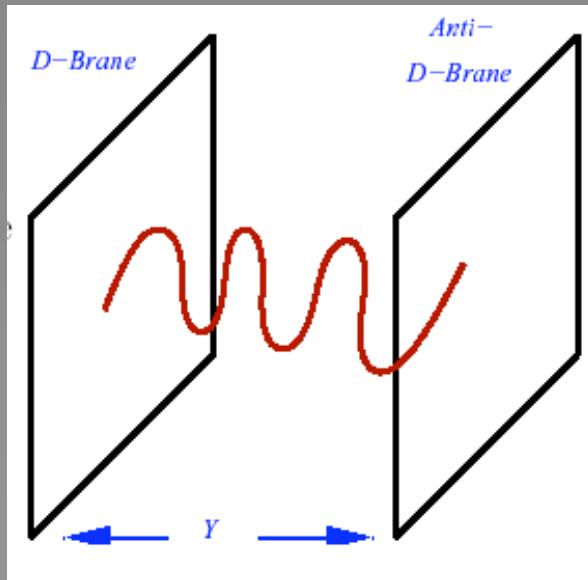
$$A \equiv 2T_p V_{||} = \frac{2e^{\varphi}}{(M_s r_{\perp})^{d_{\perp}}} M_s^2 M_{Planck}^2,$$

$$B \equiv \frac{\beta e^{2\varphi}}{M_s^8} T_p^2 V_{||} = \frac{\beta e^{\varphi} M_{Planck}^2}{M_s^{2(d_{\perp}-2)} r_{\perp}^{d_{\perp}}}.$$

Generically no slow roll
but...

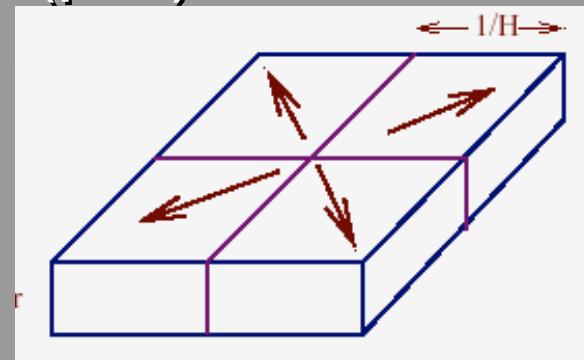
End of inflation: Open string tachyon

Burgess
et al.



Tachyon complex \rightarrow topological defects
D (p-2) branes \rightarrow cosmic strings !

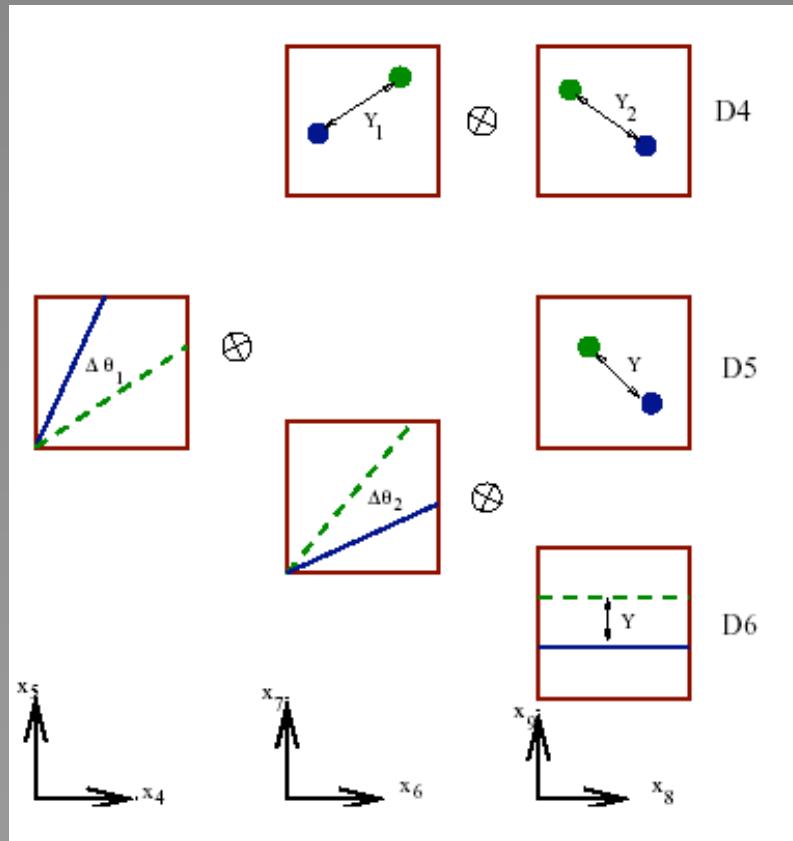
Sen, Burgess
et al.



Tye et al.
Copeland et al.

Intersecting Brane Inflation

Garcia-Bellido et al.
Gomez-Reino, Zavala



Y : Inflaton

End of inflation: tachyon!!

Also: D3-D7 inflation

Kallosh et al.

Wilson Line Inflation

Avgoustidis-Cremades-FQ

T-Duality:

D_p-Branes \longleftrightarrow D(p+1)-Branes

Brane Separation \longleftrightarrow Wilson Lines

Angles \longleftrightarrow Magnetic Fluxes

Brane inflation \longleftrightarrow Wilson Line Inflation

Moduli Stabilisation and Supersymmetry Breaking

The Problem

- String/M-Theory unique but has many solutions or vacua.
- Degeneracy : Discrete + Continuous (SUSY) .
- Outstanding Problems:

SUSY breaking + Vacuum degeneracy.

History

- $t < 1986$ Calabi-Yau String Compactifications: Many free moduli (size and shape of extra dimensions)

CHSW

Dilaton S, Kähler T
Complex structure U
Wilson Lines W

- $1986 < t < 1991$ Gaugino condensation and I-duality

DIN, DRSW, K, FILQ, FMTV

Fix S and one T

- $1991 < t < 2002$ More moduli! (D-brane positions)
- $t > 2002$ GKP/ KKLT : Fluxes fix moduli

...GKP, KKLT, ...

KKLT Scenario

...GKP, KKLT, ...

Type IIB String on Calabi-Yau orientifold

Turn on Fluxes

$$\int_a F_3 = n_a \quad \int_b H_3 = m_b$$

Size of cycle $a = U_a$

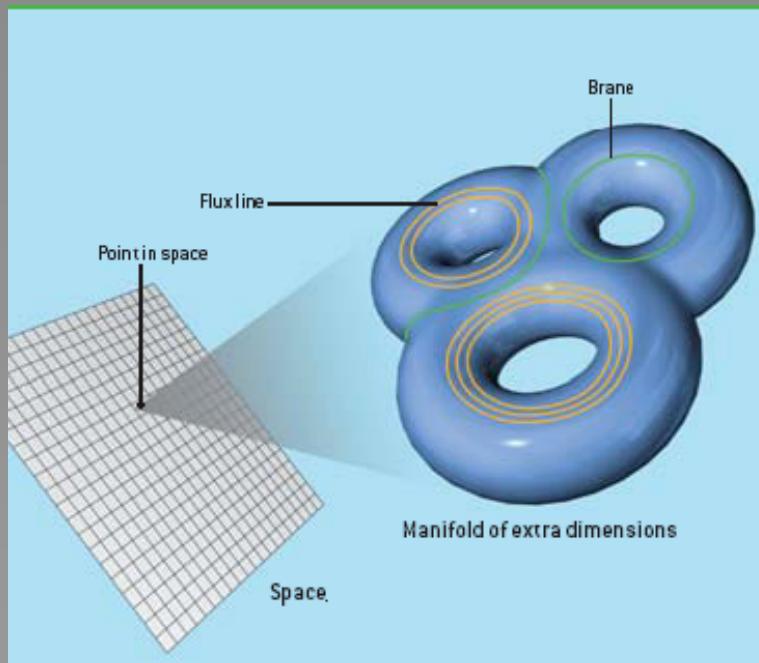
Superpotential $W = \int G_3 \wedge \Omega, \quad G_3 = F_3 - iS H_3$

Scalar Potential: $V = e^K |D_a W|^2$

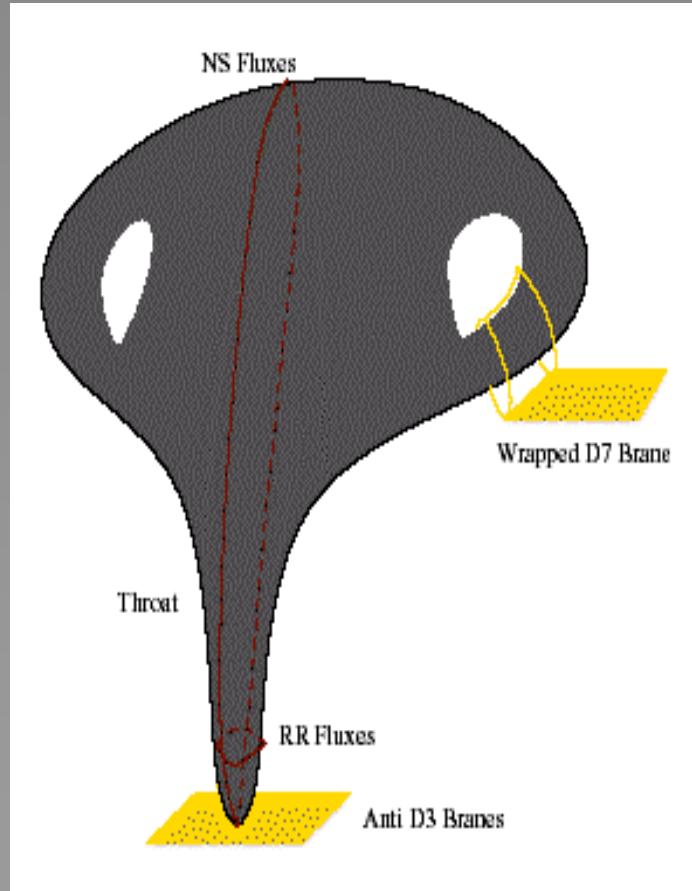
Minimum $D_a W = 0$ Fixes U_a and S
T moduli unfixed: No-Scale models

GKP

4D Compactifications



- To fix Kähler moduli: Non-perturbative D7 effects



Fluxes Non-perturbative

$$W = W_0 + \sum_i A_i e^{-a_i T_i},$$

Volume

$$\mathcal{K} = -2 \log |\mathcal{V}|$$

SUSY AdS minimum

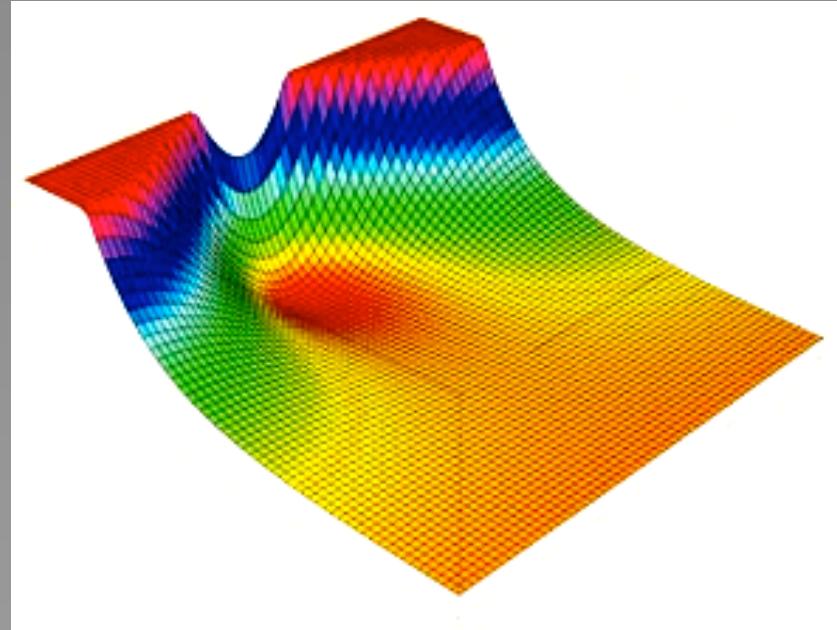
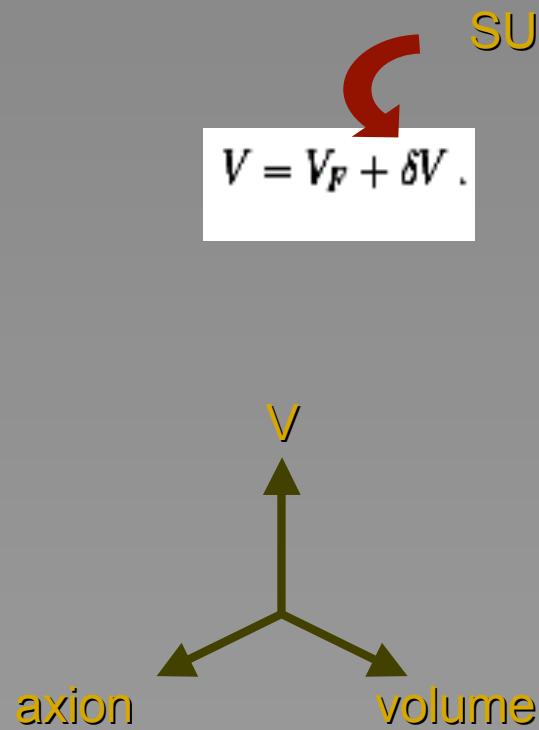
$$V = e^{\mathcal{K}} [G^{ij} D_i W \bar{D}_j \bar{W} - 3|W|^2],$$

$$D_i W \equiv \frac{\partial W}{\partial T_i} + W \frac{\partial \mathcal{K}}{\partial T_i} = 0.$$

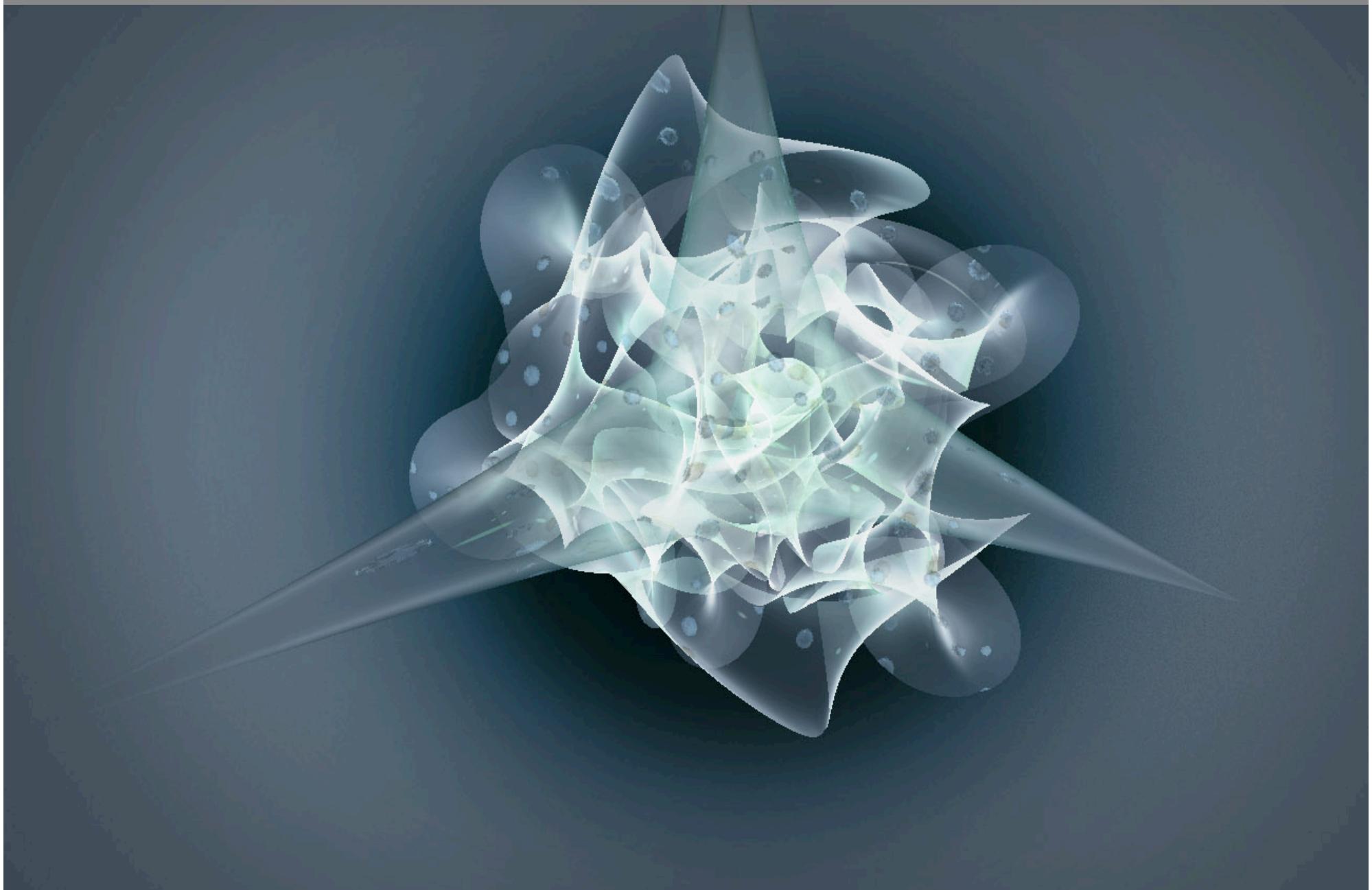
$$(W_0 \ll 1)$$

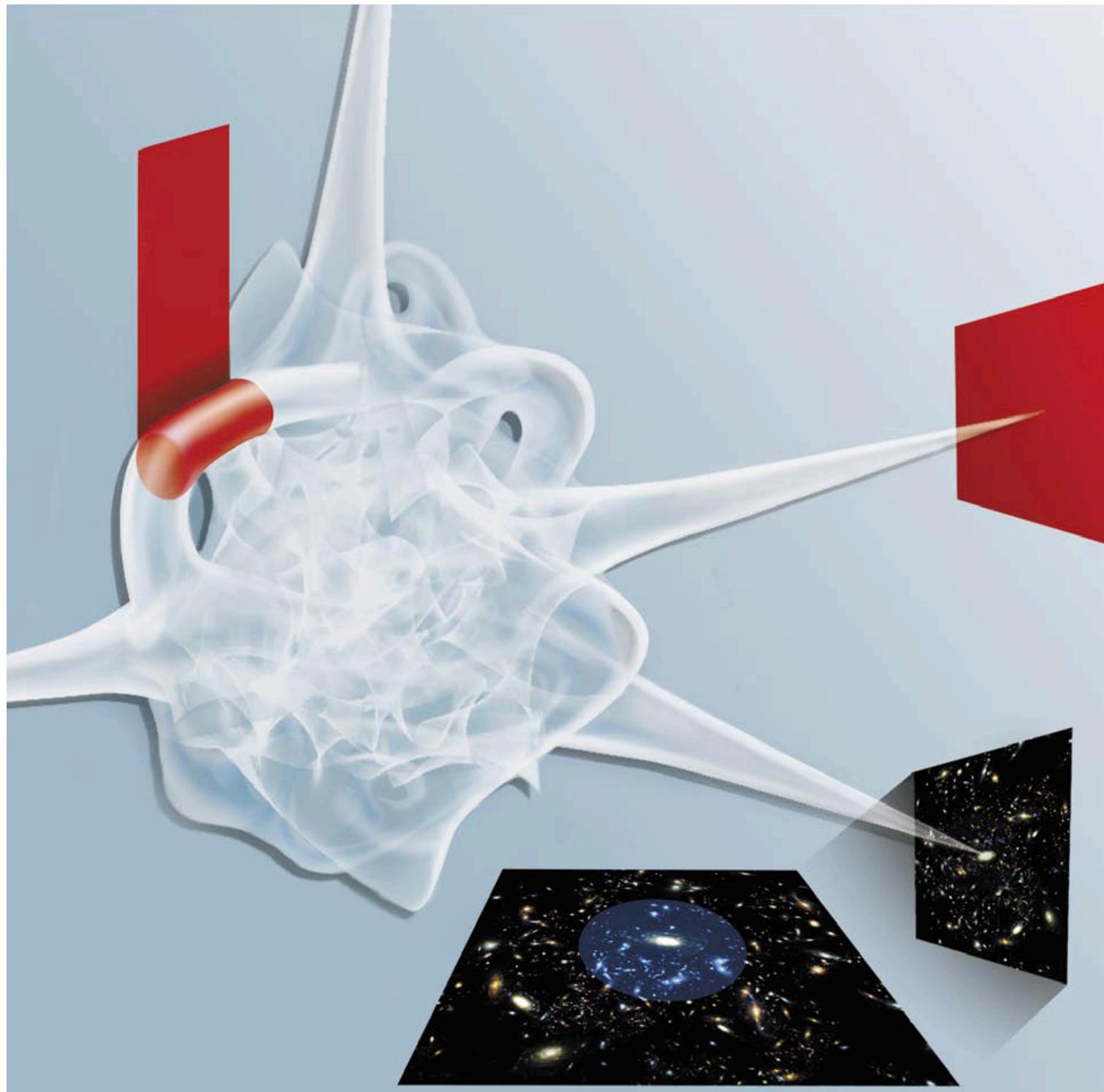
- Lifting to de Sitter (add anti D3 branes, D-terms, etc.)

KKLT, BKQ, SS



ALL MODULI STABILISED !





**Universe
D3 Brane
or
D7 Brane**

Exponentially Large Volumes

Argument:

- In general:

$$\begin{aligned}\mathcal{K} &= \mathcal{K}_0 + \mathcal{K}_p + \mathcal{K}_{np} \approx \mathcal{K}_0 + J, \\ W &= W_0 + W_{np} \approx W_0 + \Omega,\end{aligned}$$

- Then:

$$V = V_0 + V_J + V_\Omega + \dots,$$

$$V_0 \sim W_0^2, \quad V_J \sim JW_0^2, \quad V_\Omega \sim \Omega^2 + W_0\Omega,$$

- Usually V_0 dominates but $V_0=0$
(no-scale $G_{i\bar{k}}^{-1}\mathcal{K}_i\mathcal{K}_{\bar{k}} = 3$)
- Dominant term is V_J unless
 $W_0 \ll 1$ (KKLT)

Exponentially Large Volumes

BBCQ, CQS

- Perturbative corrections to K
- At least two Kähler moduli ($h_{21} > h_{11} > 1$) Example :

$$\mathbb{P}^4_{[1,1,1,6,9]},$$

$$\mathcal{K} = -2 \ln \left(\frac{1}{9\sqrt{2}} \left(\tau_b^{3/2} - \tau_s^{3/2} \right) + \frac{\xi}{2g_s^{3/2}} \right)$$

$$W = W_0 + A_s e^{-a_s T_s}.$$

Non SUSY AdS

$$V = \sum_{\Phi=S,U} \frac{\hat{K}^{\Phi\bar{\Phi}} D_\Phi W \bar{D}_{\bar{\Phi}} \bar{W}}{\mathcal{V}^2} + \frac{\lambda(a_s A_s)^2 \sqrt{\tau_s} e^{-2a_s \tau_s}}{\mathcal{V}} - \frac{\mu W_0 a_s A_s \tau_s e^{-a_s \tau_s}}{\mathcal{V}^2} + \frac{\nu \xi |W_0|^2}{g_s^{3/2} \mathcal{V}^3}$$

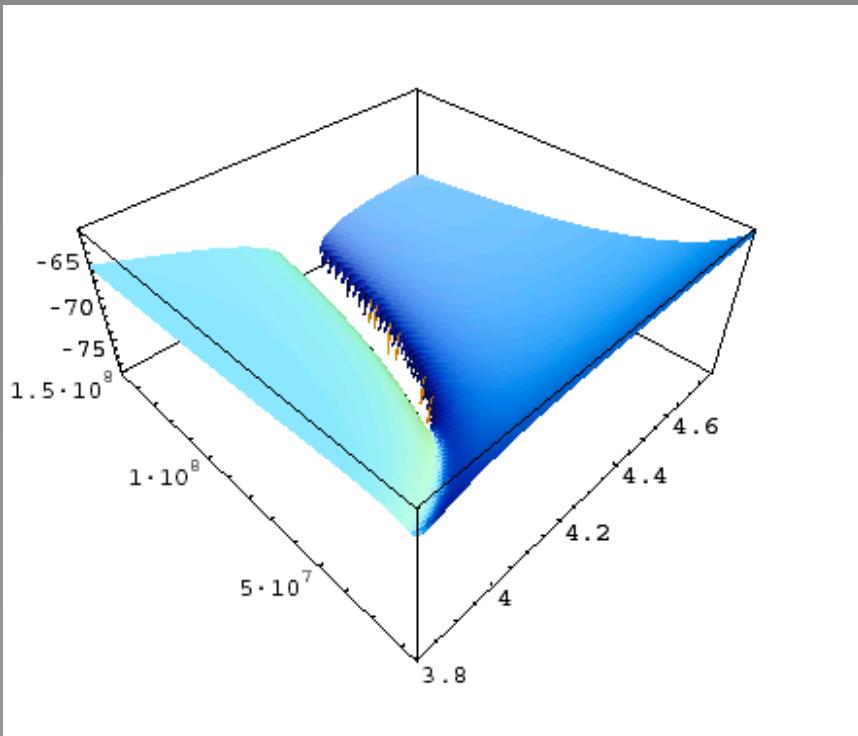
$\mathcal{V} \sim e^{a_s \tau_s} \gg 1$ with $\tau_s \sim \frac{\xi^{2/3}}{g_s}$.

| Scale | \mathcal{V}_s | $g_s N$ | N if $g_s = 0.1$ |
|--------------|----------------------|---------|--------------------|
| GUT | 4600 | 2.25 | 22 |
| Intermediate | 4.6×10^9 | 0.85 | 9 |
| TeV | 4.6×10^{27} | 0.30 | 3 |

$W_0 \sim 1-10$

String scale: $M_s^2 = M_p^2/V$

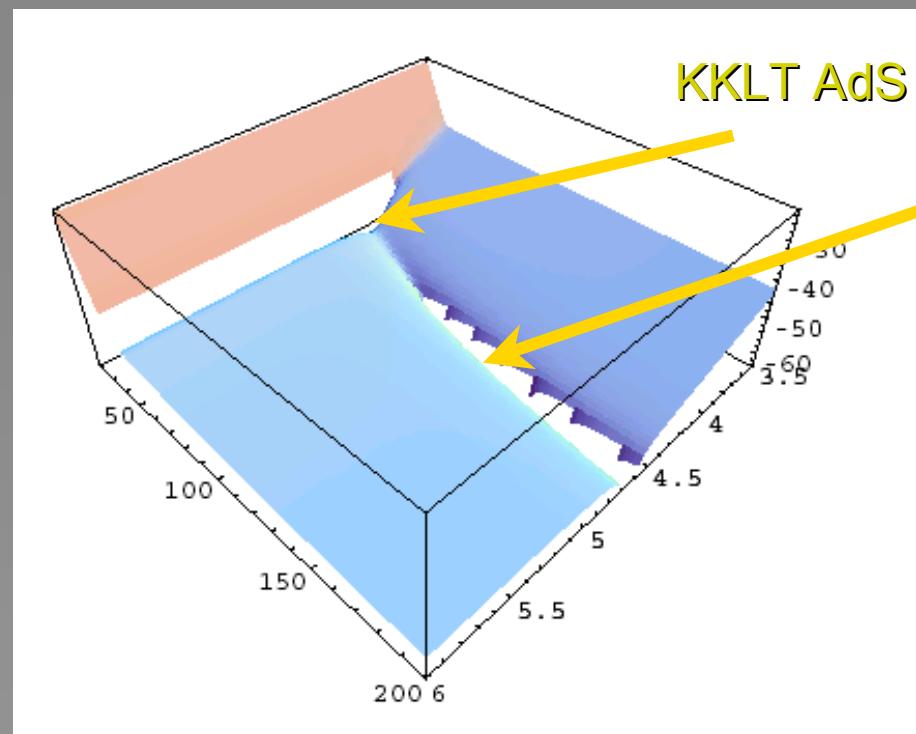
Non SUSY AdS



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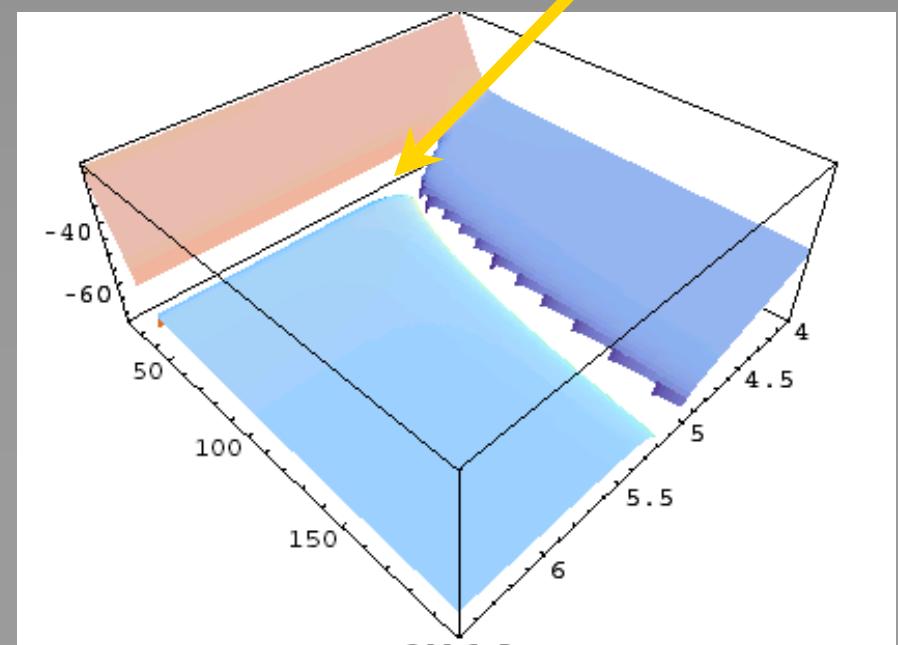
KKLT AdS

Non SUSY AdS

$W_0 \sim 10^{-10}$

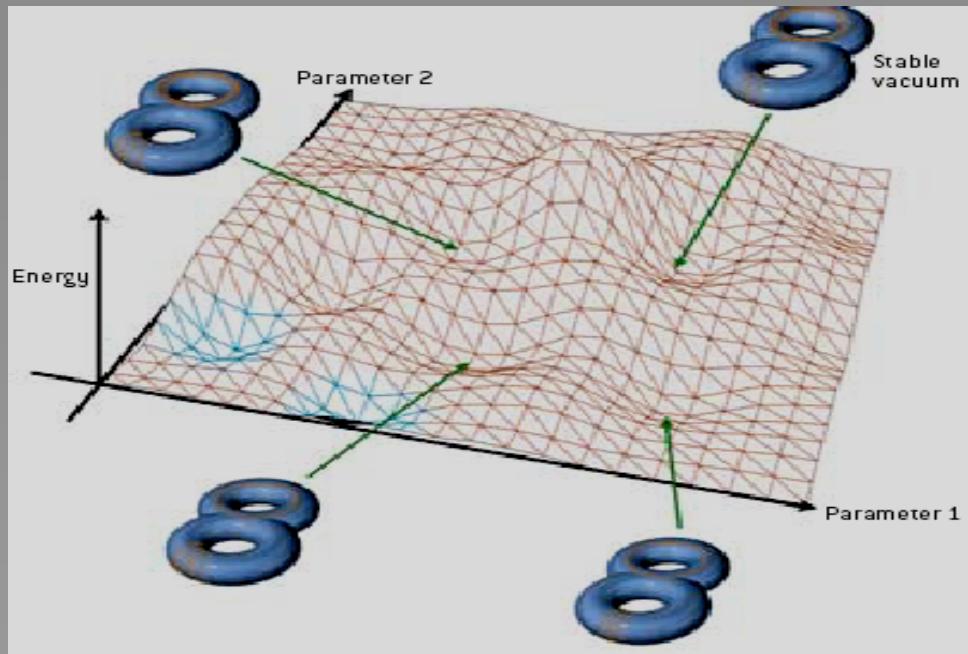
$W_0 < 10^{-11}$

Both minima close



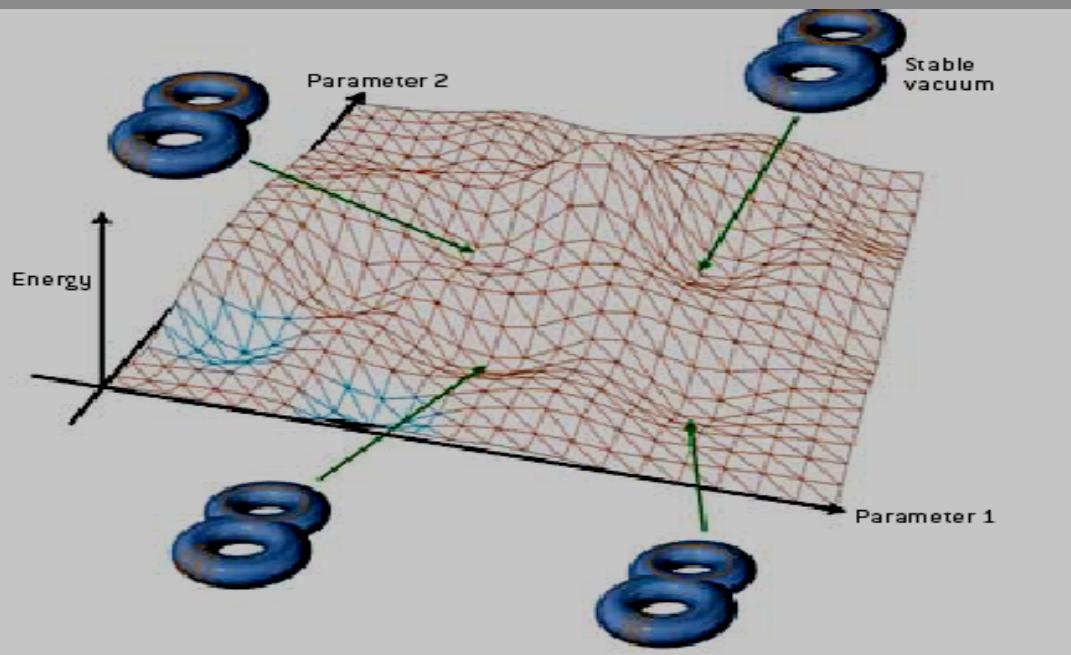
The Landscape

The Landscape



- Huge number of discrete vacua $>10^{500}$
- Statistics [AD, DD, DDF, GKTT,CQ,BGHLW]
- Randall-Sundrum warping from strings! [GKP]
- Non SUSY de Sitter
- Dark energy? [BP]
- SM on D3/D7branes [CG-MQU]
- Soft SUSY breaking?
- Inflation?

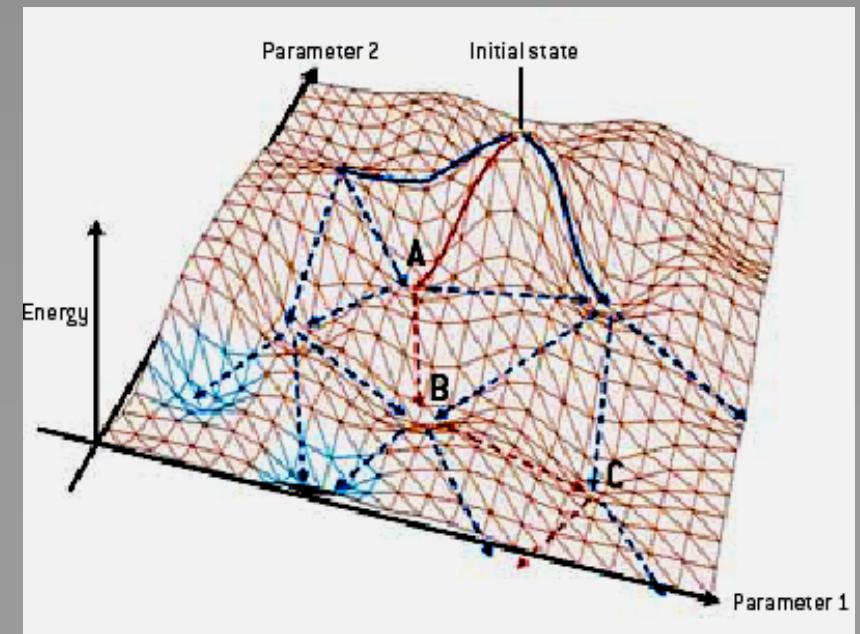
Populating the Landscape



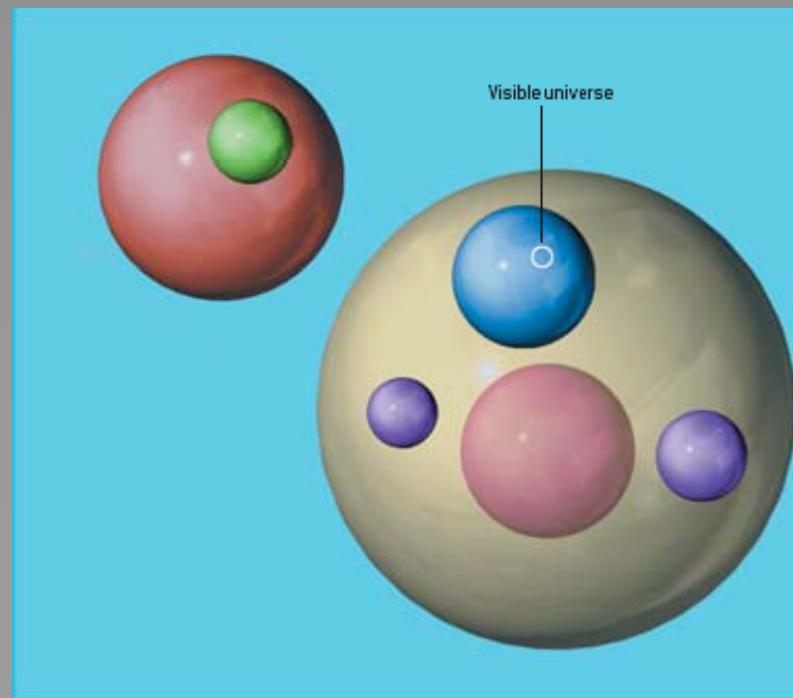
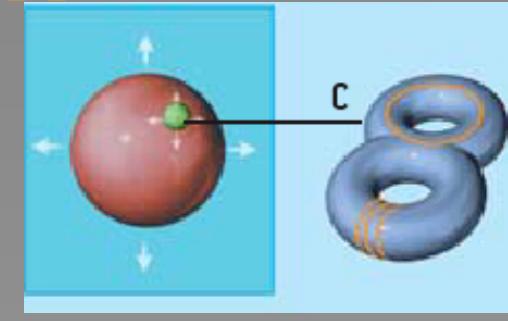
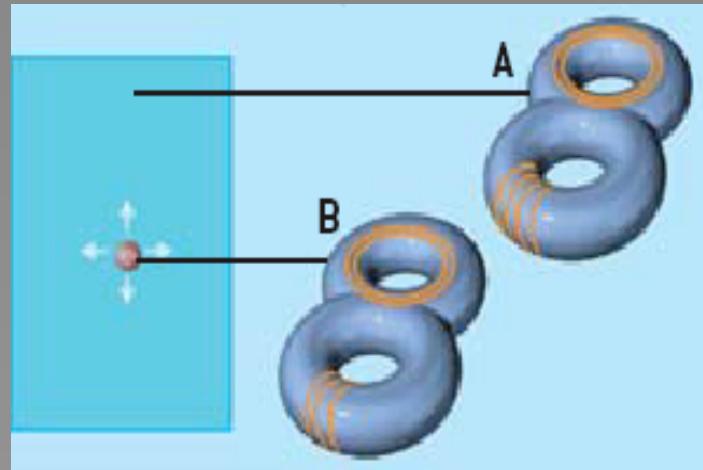
Quantum decay
(tunnel effect)



Classical Solutions



Multiverse and Eternal Inflation



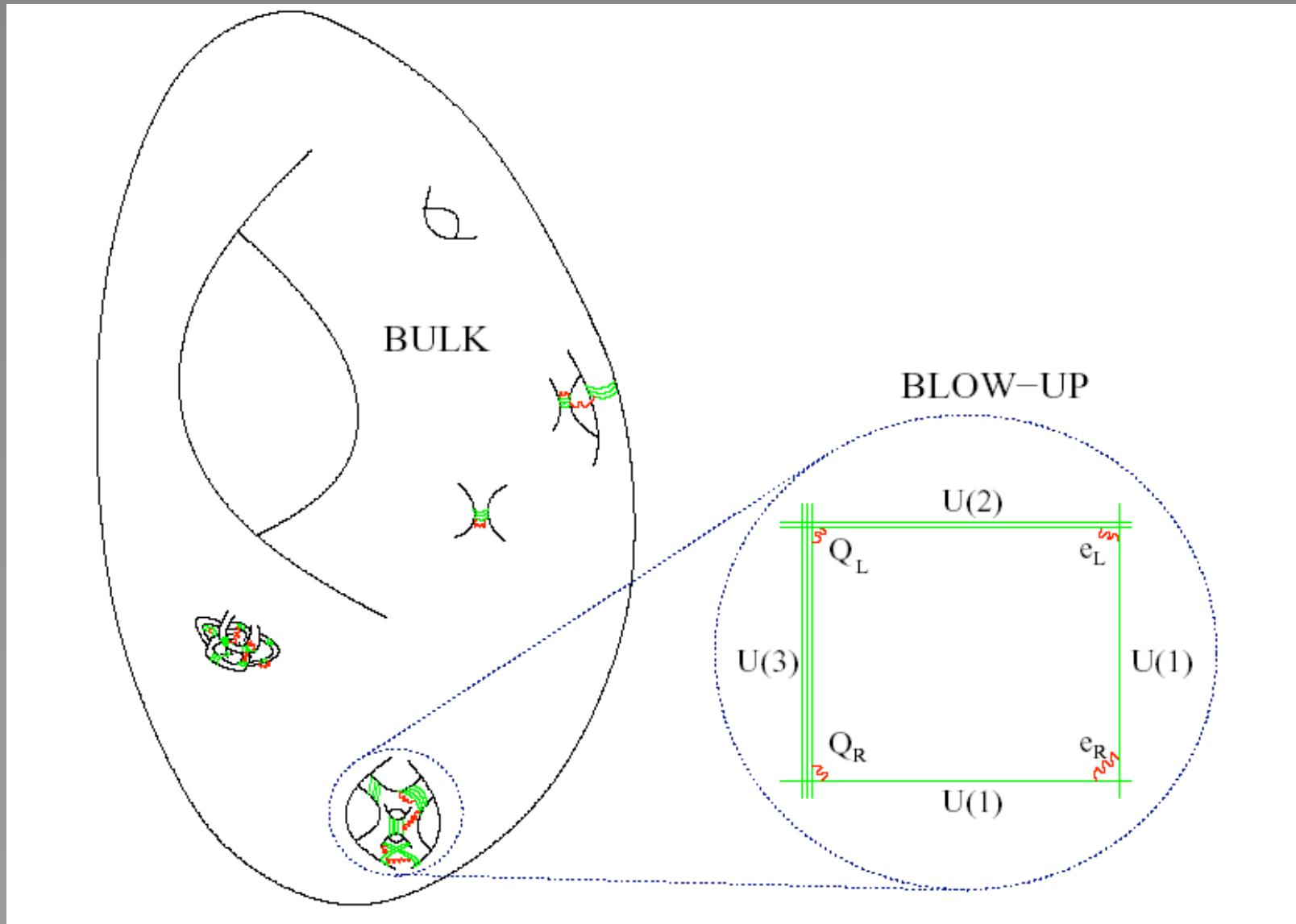
Interesting But...

- This is NOT the slow-roll inflation that we are after.
- Where are we in the landscape?

Modular Model Building

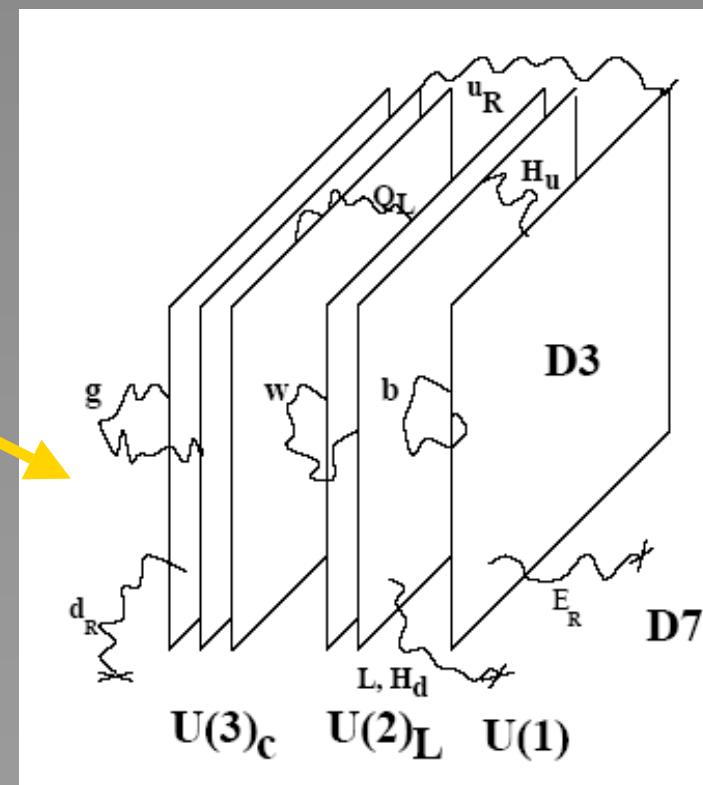
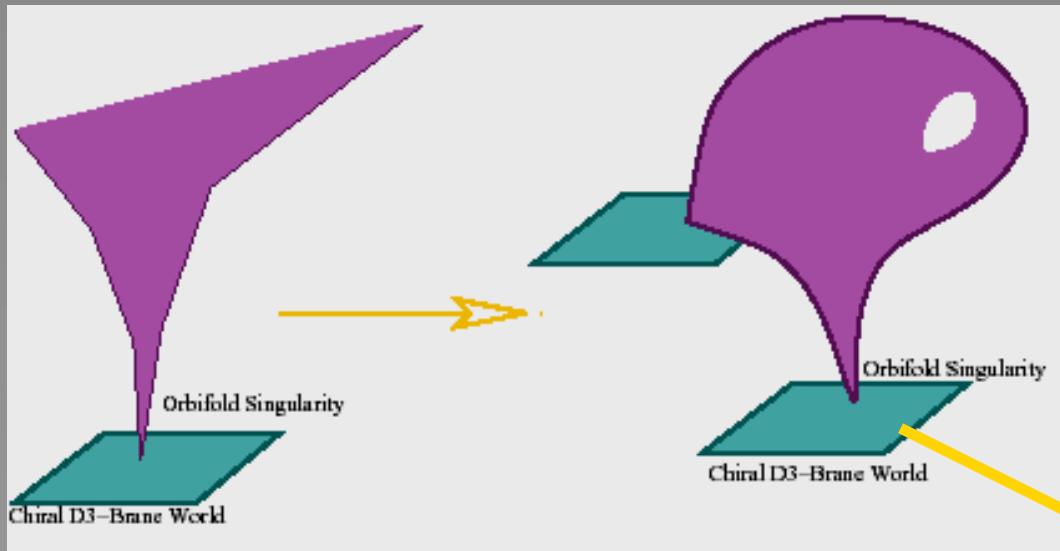
(Bottom up approach)

The Standard Model in the CY



Realistic Models

AIQU, CG-MQU,
H. Verlinde et al.



Bottom-up Approach

Aldazabal,Ibanez, FQ, Uranga 2000

Verlinde,Wijnholt 2006

Local (brane) Properties

- Gauge group
- Chiral spectrum
- Yukawa couplings
- Gauge unification
- Proton stability
- Baryogenesis
- Reheating

Global (bulk) Properties

- Moduli Stabilisation
- SUSY Breaking
- Soft terms
- Cosmological constant
- Inflation

PHENOMENOLOGY

(From Strings to LHC)

(LARGE Volume models)

Standard Model on D7 Branes

- Solve hierarchy problem $M_{\text{string}} = 10^{11} \text{ GeV!}$

$$m_s \sim \frac{M_P}{\sqrt{\mathcal{V}}} , \quad m_{3/2} \sim \frac{M_P}{\mathcal{V}} W_0.$$

- $W_0 \sim 1$ (no fine tuning)
- Kahler potential for *chiral* matter computed

Conlon, Cremades, FQ (2006)

Chiral Matter on D7 Branes

Soft SUSY Breaking terms

$$M_i = \frac{F^s}{2\tau_s},$$

$$m_\alpha = \sqrt{\lambda} M_i,$$

$$A_{\alpha\beta\gamma} = -3\lambda M_i,$$

$$B = -(\lambda + 1) M_i.$$

Simplest case

$\lambda=1/3$

$$m_{soft} = \frac{m_{3/2}}{\ln(M_P/m_{3/2})}.$$

- Universality!
- No extra CP violation!
- $M_i = m_{3/2} / \log (M_P/m_{3/2})$
- String scale 10^{11} GeV
- Solves hierarchy problem!

Stringy source of universality (approximate)

$\Psi \iff$ Kähler moduli,

$\Phi = \Psi_{\text{susy-breaking}} \oplus \chi_{\text{flavour}}$.

$\chi \iff$ Complex structure moduli.

CP Violation

$$\phi_A = \{\arg\left(\frac{A_{\alpha\beta\gamma}}{Y_{\alpha\beta\gamma}}\right)\}, \phi_B = \{\arg B\}, \phi_C = \{\arg(M_a)\}.$$

Physical phases $\phi = \{\phi_A - \phi_C, \phi_B - \phi_C\}$ vanish !

Also: Anomaly mediation suppressed !!!

From Strings to LHC data

CKSAQ 0705.3460[hep-ph],

- Stabilise Moduli
- SUSY broken with hierarchy
- “Realistic” Observable sector
- Soft SUSY Breaking terms@Ms
- RG-Running of Soft terms to TeV (softsusy)
- Event Generators (PYTHIA-Herwig)
- Detector Simulators (PGS, GEANT) 10⁻¹ fb
- Data Analysis and reconstruction (Root) 100⁻¹ fb
- Estimate overall uncertainty

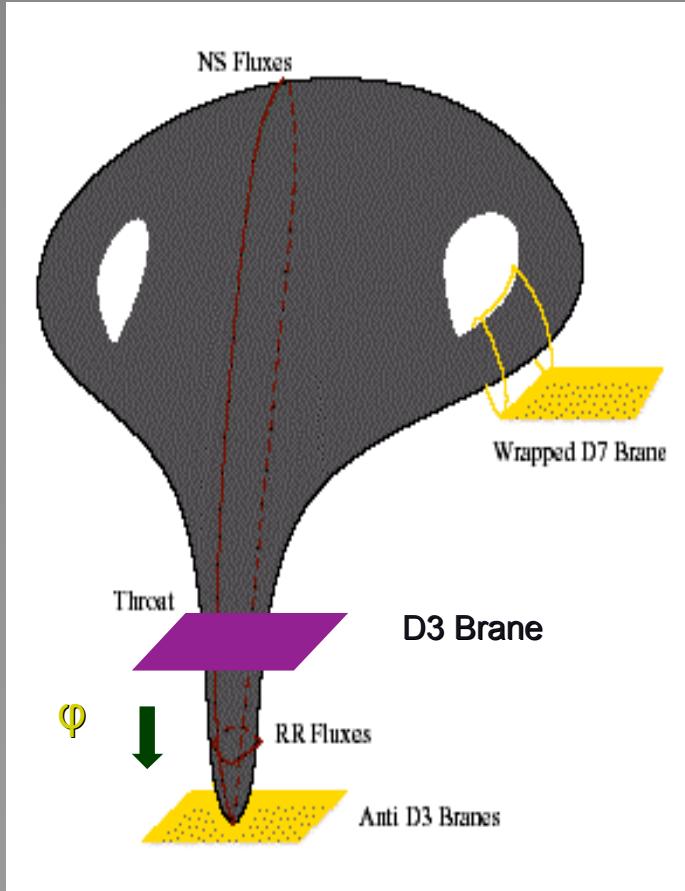
COSMOLOGY

(Inflation, Cosmological moduli
problem, etc.)

Brane-Antibrane Inflation

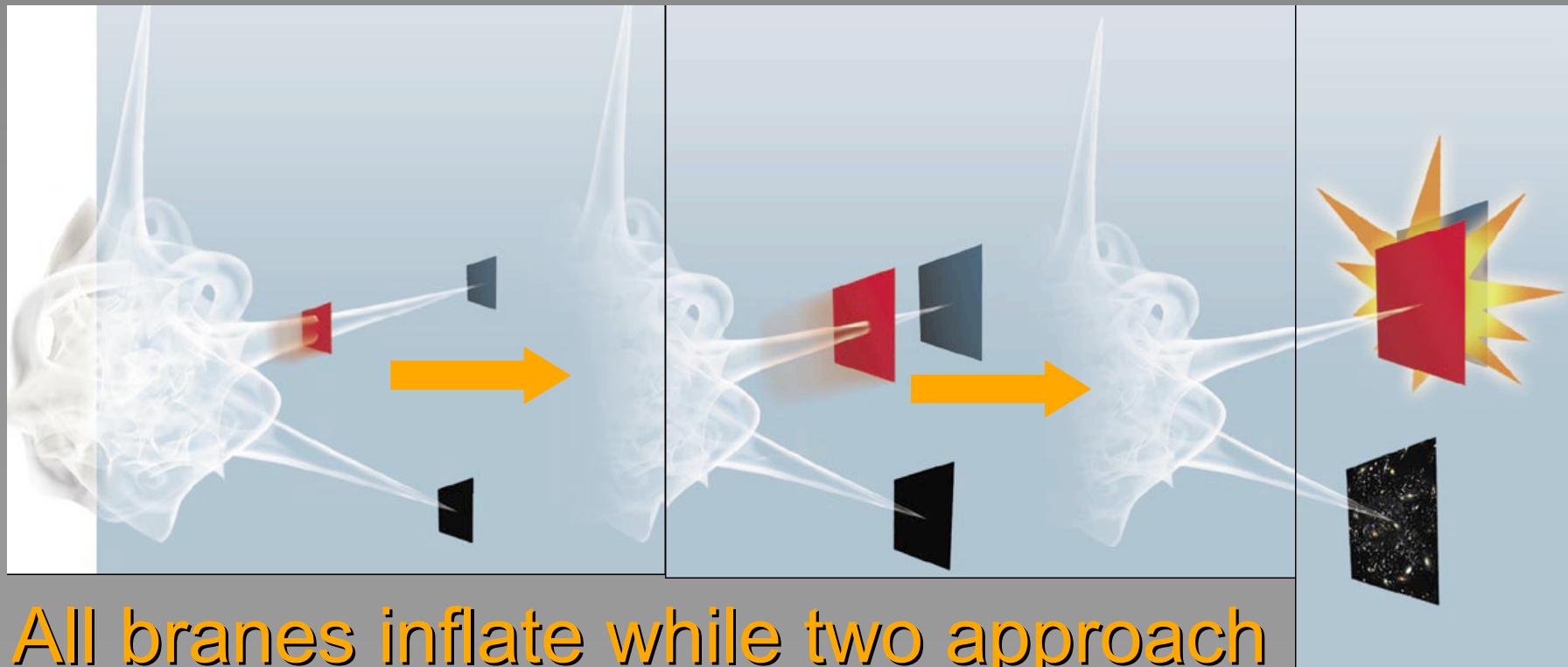
BMNRQZ, DSS

ϕ inflaton field

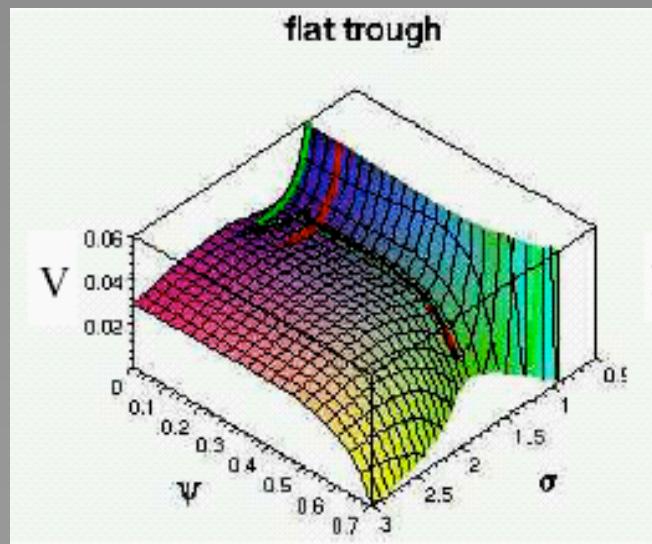


KKLMMT, HKP, KTW,
FT, BCSQ

BRANE - ANTIBRANE INFLATION



Slow-roll (large field) inflation possible.
Need 1/1000 fine tuning of parameters to
get 60-efoldings (η -problem)



$$N \sim 60, \delta_H \sim 10^{-5} \text{ for}$$

$$M_S \sim 10^{15} \text{ GeV}$$

$$n_s \sim 1.05$$

Burgess, Cline,
Stoica, FQ

$$n_s < 1 \text{ (Cline-Stoica)}$$

Needs at least two throats !

Also: D3-D7 on K3xT2 Kallosh et al.

DBI in the sky

Silverstein-Tong, Chen, Tye et al.

Tachyonic Inflation

Sen, Raeymakers, Cremades-Sinha-FQ

$$S = \int d^4x \sqrt{-g} \left(\frac{M_{pl}^2}{2} R - \mathcal{A}V(T) \sqrt{1 + B\partial_\mu T \partial^\mu T} \right) -$$

$$V(T) = \frac{V_0}{\cosh(\frac{T}{\sqrt{2}\alpha'})}.$$

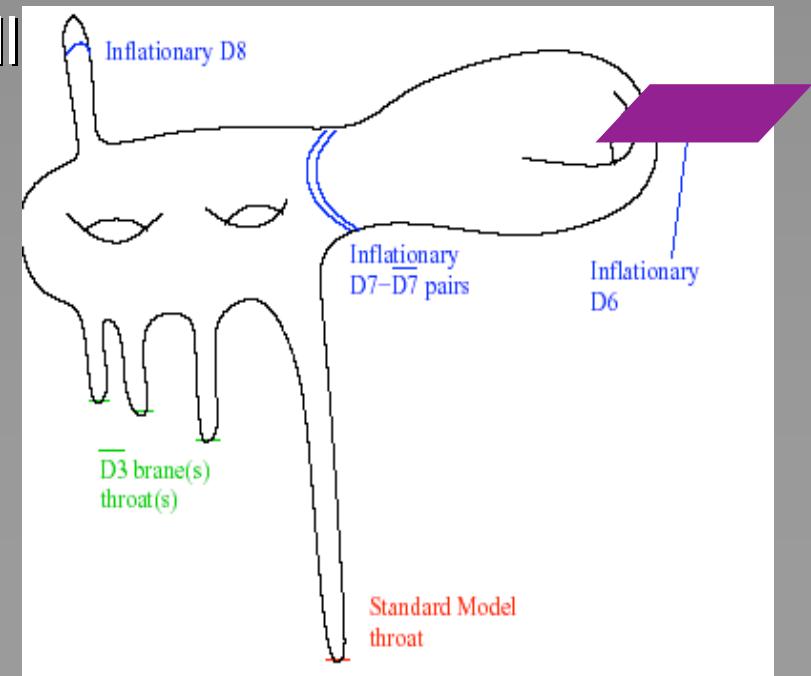
A, B depend on warping (fluxes) and E&M fields on non-BPS brane. If $A, B \sim 1$ no slow-roll

$$\epsilon = \frac{M_{pl}^2}{2AB} \left(\frac{V'^2}{V^3} \right) \ll 1, \quad \eta = \frac{M_{pl}^2}{AB} \left[\frac{V''}{V^2} - \frac{1}{2} \left(\frac{V'^2}{V^3} \right) \right] \ll 1.$$

$$\delta_H = \frac{\sqrt{\mathcal{A}^2 B}}{5\pi\sqrt{3}M_{pl}^3} \frac{V^2}{V'}.$$

AB large \rightarrow slow-roll

No fine-tuning! But need large fluxes



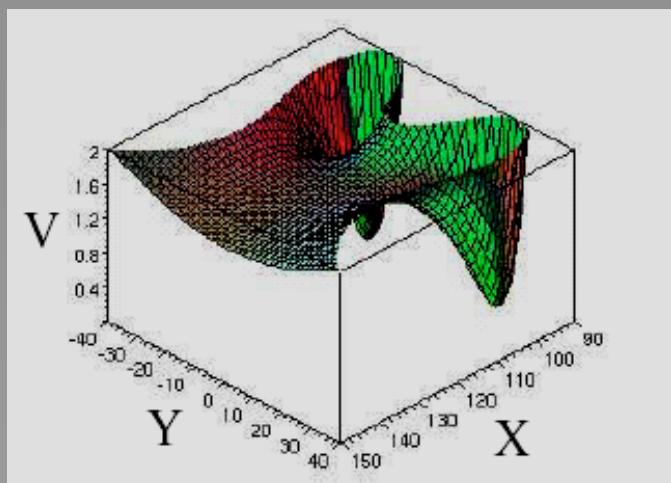
Racetrack Inflation



Blanco-Pillado et al.



Topological eternal inflation !



Also for $W_0=0$ if add matter

$$W = W_0 + A e^{-aT} + B e^{-bT}.$$

$$\epsilon \equiv \frac{M_{pl}^2}{2} \left(\frac{V'}{V} \right)^2 \ll 1$$

$$\eta \equiv M_{pl}^2 \frac{V''}{V} \ll 1.$$

Slow roll if 1/1000 fine tuning,
 $N \sim 60$, $\delta_H \sim 10^{-5}$ for $M_s \sim 10^{15} \text{ GeV}$
 $n_s \sim 0.95$!!

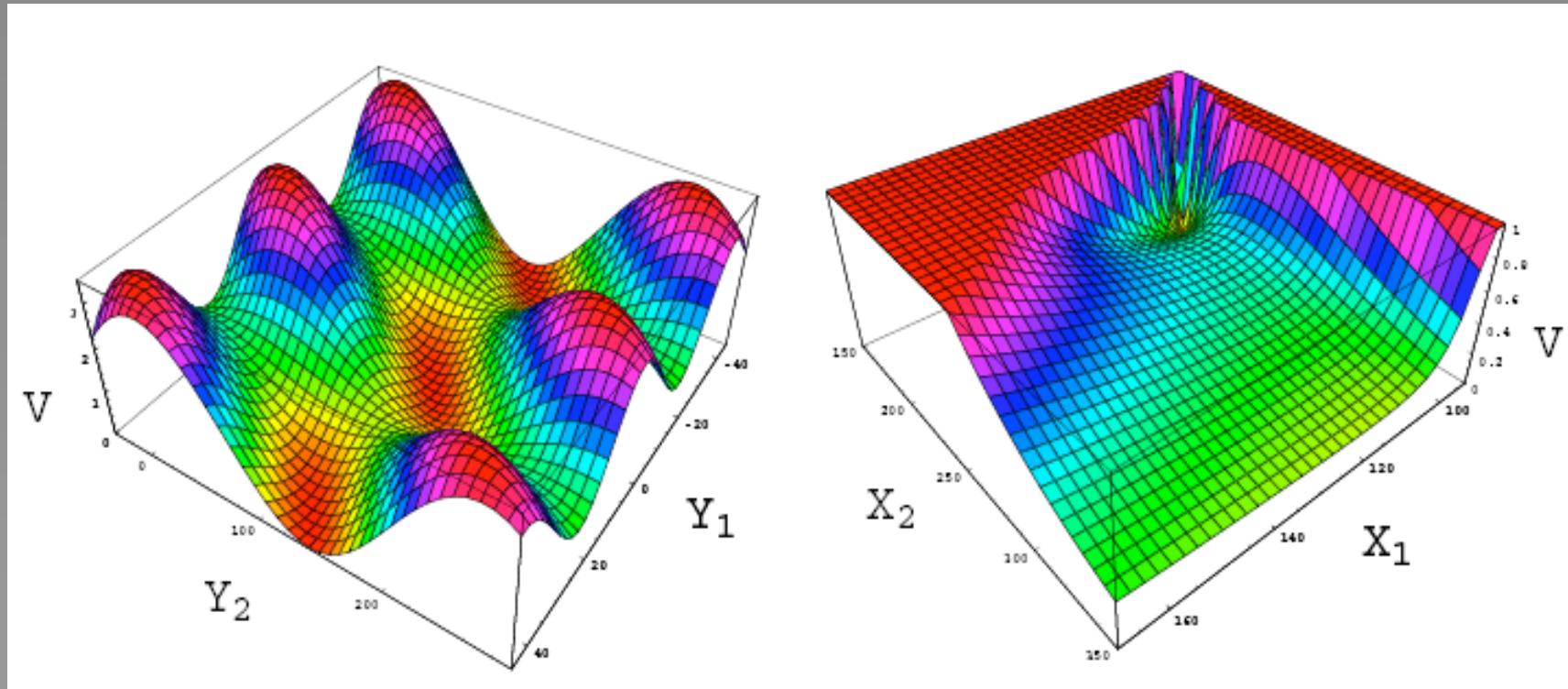
Lalak, Ross, Sarkar

Better Racetrack Inflation

Blanco-Pillado et al.

$$W = W_0 + A e^{-a\tau_1} + B e^{-b\tau_2}$$

Douglas et al.



Explicitly derived model

Similar physics

Kähler Moduli Inflation

Conlon-FQ

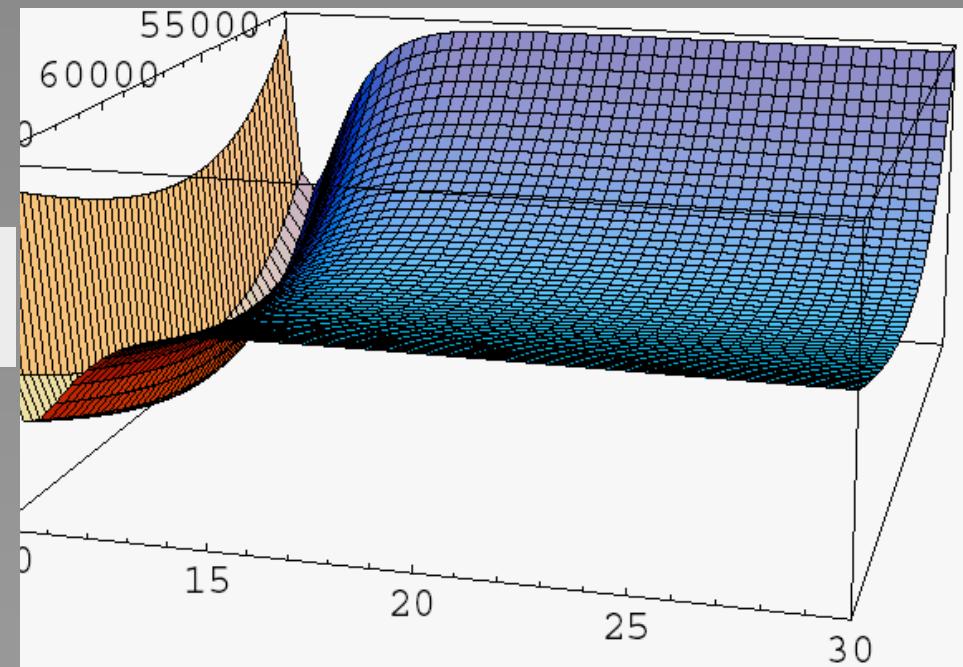
Bond-Kofman-Prokushkin

Calabi-Yau:

$$h_{21} > h_{11} > 2$$

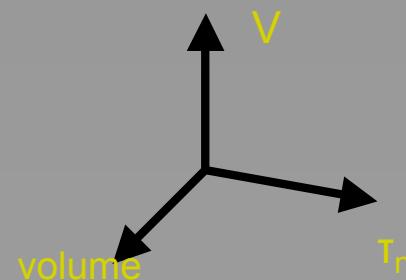
$$V = \sum_i \frac{8(a_i A_i)^2 \sqrt{\tau_i}}{3\mathcal{V} \lambda_i \alpha} e^{-2a_i \tau_i} - \sum_i 4 \frac{a_i A_i}{\mathcal{V}^2} W_0 \tau_i e^{-a_i \tau_i} + \frac{3\xi W_0^2}{4\mathcal{V}^3}.$$

Small field inflation
No fine-tuning!!
 $0.960 < n < 0.967$



GUT scale Ms?,

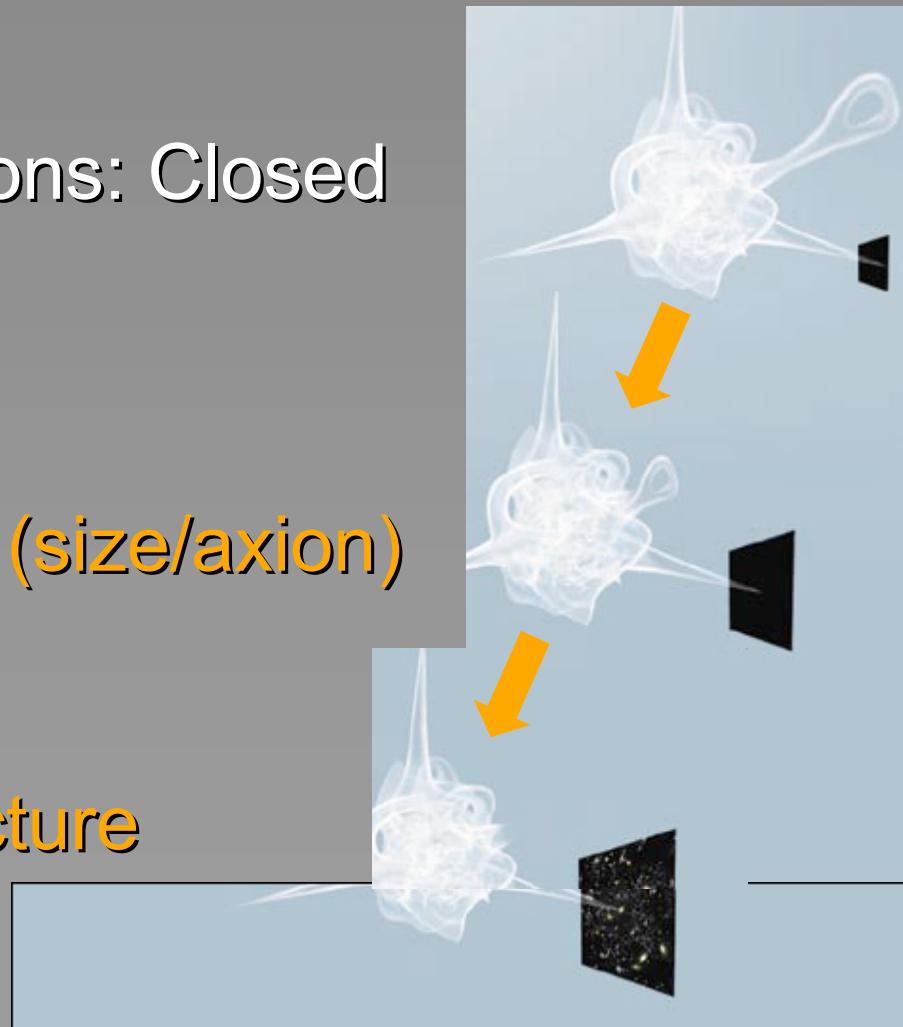
Loops?



MODULI INFLATION

Candidate Inflatons: Closed string modes

- Kahler Moduli (size/axion)
- Complex structure moduli?



Open Questions

- Inflation possible but not generic (fine tuning)
- Initial conditions/Singularity,...
- Non tensor perturbations ($r=s/t \lll 1$)?

Baumann, McCalister

- Tension phenomenology vs cosmology

Gravitino mass 1 TeV /Gravitino mass $\gg 1 \text{ TeV} ??$

Ross, Sarkar

Kallosh-Linde

(string scale 10^{11} GeV / string scale $\sim \text{GUT scale}$)

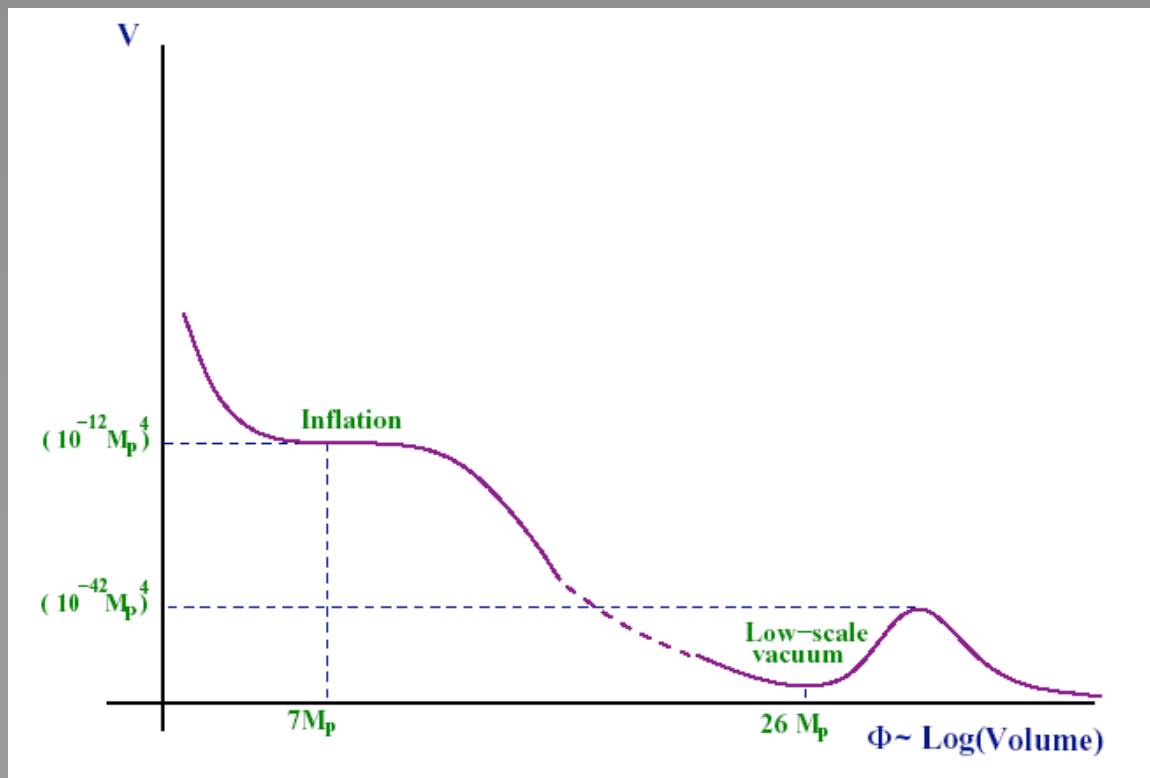
Possible ways out

- Low scale inflation?

German, Ross, Sarkar, ...

- Runaway before reheating?

Conlon et al.



After Inflation

Physics of Moduli Fields

- Dilaton and Complex Structure

Moduli masses:

$$m_{3/2} \sim \frac{M_P}{\mathcal{V}}, \quad m_s \sim \frac{M_P}{\sqrt{\mathcal{V}}}.$$

- Small (heavy) Kahler moduli
- Large (light) Kahler modulus

$$m_{\tau_b} \sim \frac{M_P \ln(M_P/m_{3/2})}{\mathcal{V}}.$$

$$m_{\tau_b} \sim \frac{M_P}{\mathcal{V}^{3/2}} \sim M_P \left(\frac{m_{3/2}}{M_P} \right)^{3/2}.$$

Physical Fields

$$\begin{aligned}\delta\tau_b &= \left(\sqrt{6}\langle\tau_b\rangle^{1/4}\langle\tau_s\rangle^{3/4}(1-2\epsilon)\right) \frac{\Phi}{\sqrt{2}} + \left(\sqrt{\frac{4}{3}}\langle\tau_b\rangle\right) \frac{\chi}{\sqrt{2}} \sim \mathcal{O}(\mathcal{V}^{1/6}) \Phi + \mathcal{O}(\mathcal{V}^{2/3}) \chi \\ \delta\tau_s &= \left(\frac{2\sqrt{6}}{3}\langle\tau_b\rangle^{3/4}\langle\tau_s\rangle^{1/4}\right) \frac{\Phi}{\sqrt{2}} + \left(\frac{\sqrt{3}}{a_s}(1-2\epsilon)\right) \frac{\chi}{\sqrt{2}} \sim \mathcal{O}(\mathcal{V}^{1/2}) \Phi + \mathcal{O}(1) \chi \quad (3.7)\end{aligned}$$

Decay Rates

$$\lambda_{\chi\gamma\gamma} = \frac{\sqrt{6}}{2M_P \ln(M_P/m_{3/2})},$$

$$\lambda_{\Phi\gamma\gamma} \sim \left(\frac{2}{\sqrt{3}} \frac{\langle\tau_b\rangle^{3/4}}{\langle\tau_s\rangle^{3/4} M_P}\right) \sim \frac{\sqrt{\mathcal{V}}}{M_P} \sim \frac{1}{m_s}.$$

$$\delta\mathcal{L}_{\Phi ee} \sim \frac{\sqrt{\mathcal{V}}\chi}{M_P} m_e \bar{e} e \sim \frac{\chi}{m_s} m_e \bar{e} e.$$

$$\delta\mathcal{L}_{\chi ee} \sim \left(1 + \frac{1}{a\langle\tau_s\rangle}\right) \frac{1}{\sqrt{6}} \frac{\chi}{M_P} m_e \bar{e} e.$$

| | Light modulus χ | Heavy Modulus Φ |
|------------------------|--|--|
| Mass | $\sim m_{3/2} \left(\frac{m_{3/2}}{M_P}\right)^{\frac{1}{2}} \sim 2\text{MeV}$ | $2 m_{3/2} \ln(M_P/M_{3/2}) \sim 1200\text{TeV}$ |
| Matter Couplings | M_P^{-1} | m_s^{-1} |
| Decay Modes | | |
| $\gamma\gamma$ | $\text{Br} \sim 0.025, \quad \tau \sim 6.5 \times 10^{25}\text{s}$ | $\tau \sim 10^{-17}\text{s}$ |
| e^+e^- | $\text{Br} \sim 0.975, \quad \tau \sim 1.7 \times 10^{24}\text{s}$ | $\tau \sim 10^{-17}\text{s}$ |
| $\psi_{3/2}\psi_{3/2}$ | inaccessible | $\text{Br} \sim 10^{-30}, \quad \tau \sim 10^{-2}\text{s}$ |

Other Cosmological Implications

J.Conlon, FQ

- Cosmological moduli problem

DCQR, BKN

U,S: trapped at their minimum

T: except for volume, heavy ad decay fast ! (No
CMP nor gravitino overproduction)

Volume: (mass MeV) CMP

- Observational implications of light volume modulus?

Gamma rays, e^+e^-

Solution of CMP?

Thermal Inflation

Lyth+Stewart (1995)

$$V = V_0 + (T^2 - m_\sigma^2) \sigma^2 + \dots$$

$$\langle \sigma \rangle \equiv M_* \gg m_\sigma.$$

$m_\sigma \sim 1 \text{ TeV}$ and $M_* \sim 10^{11} \text{ GeV}$

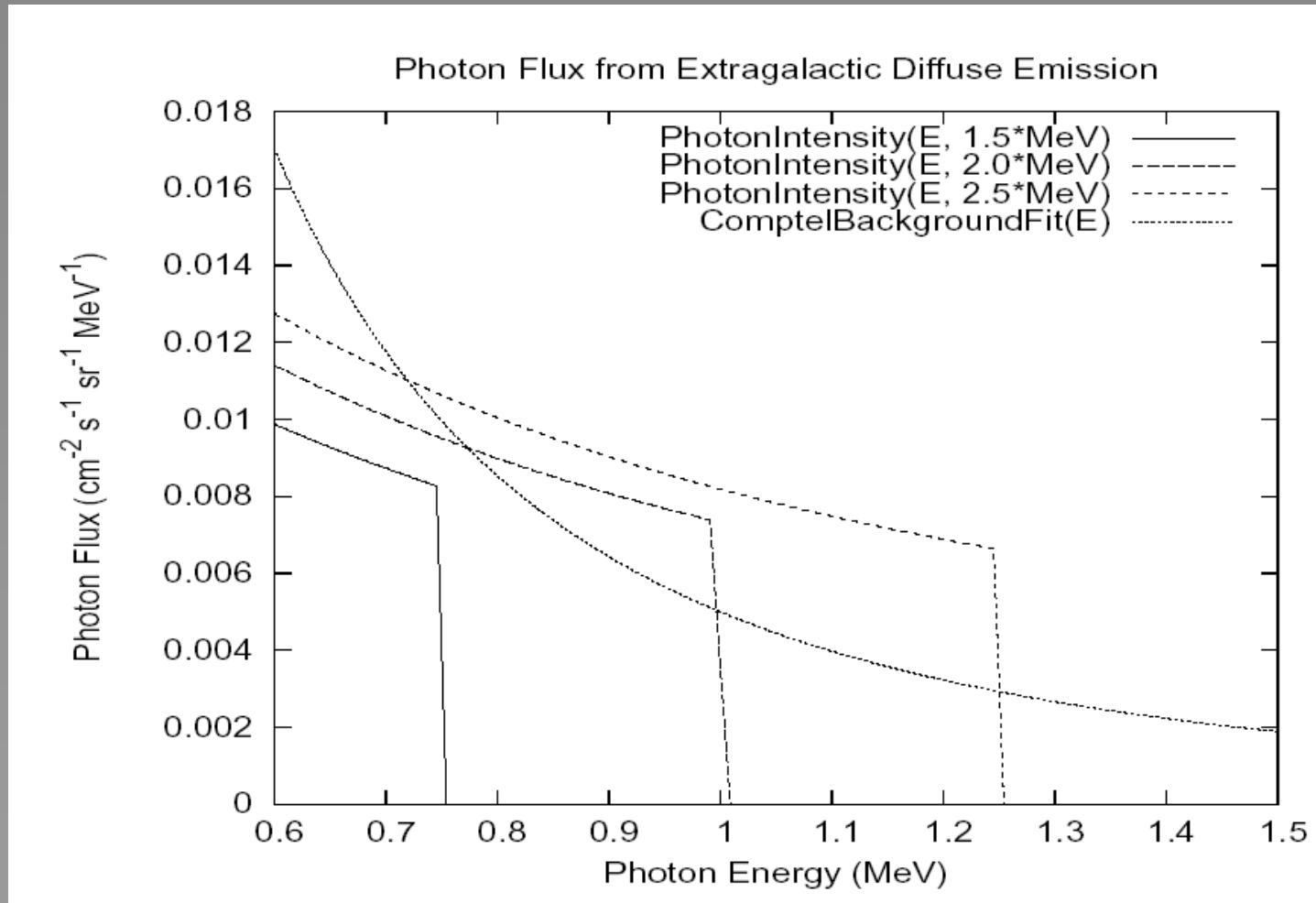
Number of e-folds

$$N \sim \log \left(V_0^{1/4} / T_c \right) \sim \log (M_*/m_\sigma)^{1/2}$$

N~10 dilutes moduli

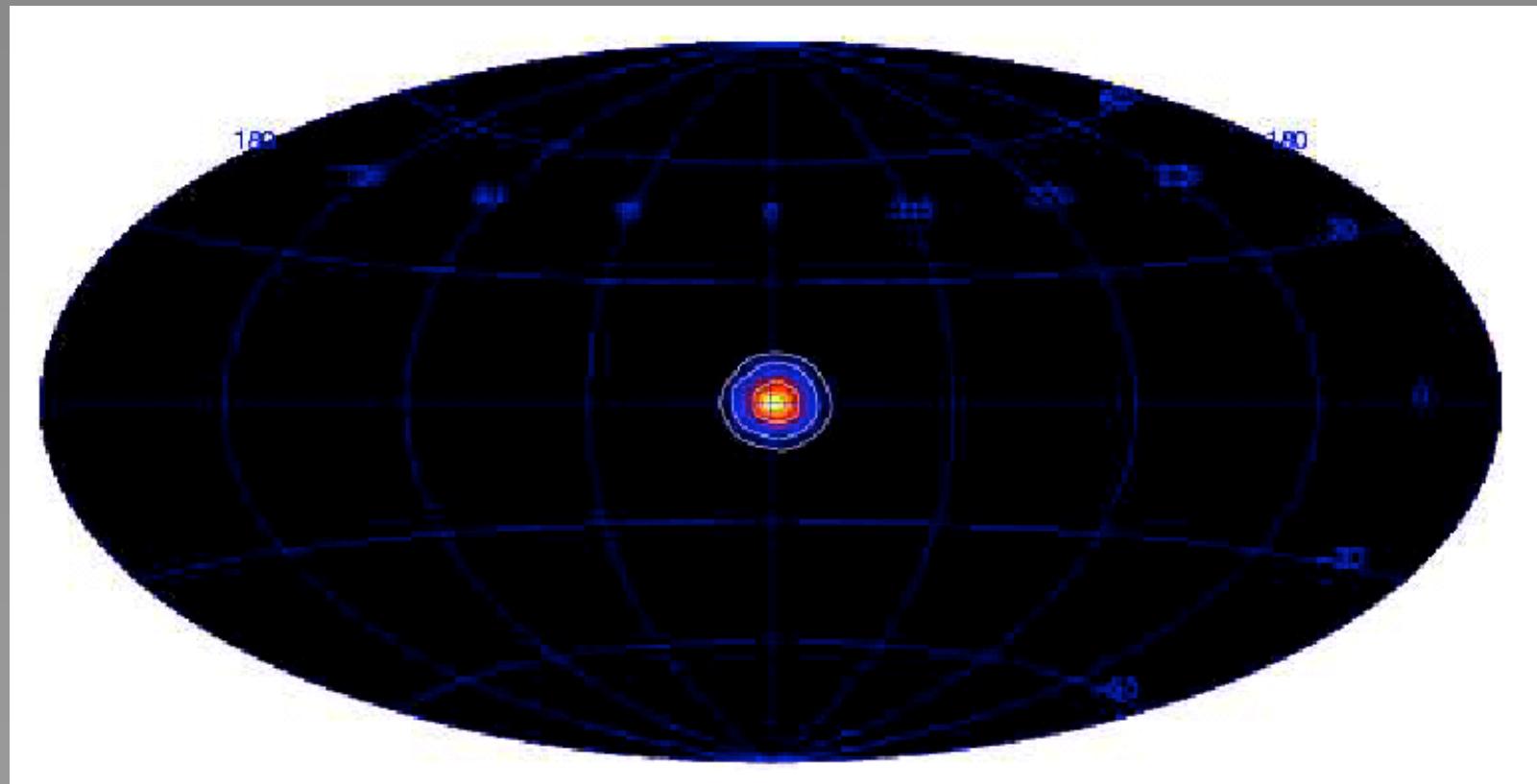
Late time implications:

Diffuse Gamma Ray Background

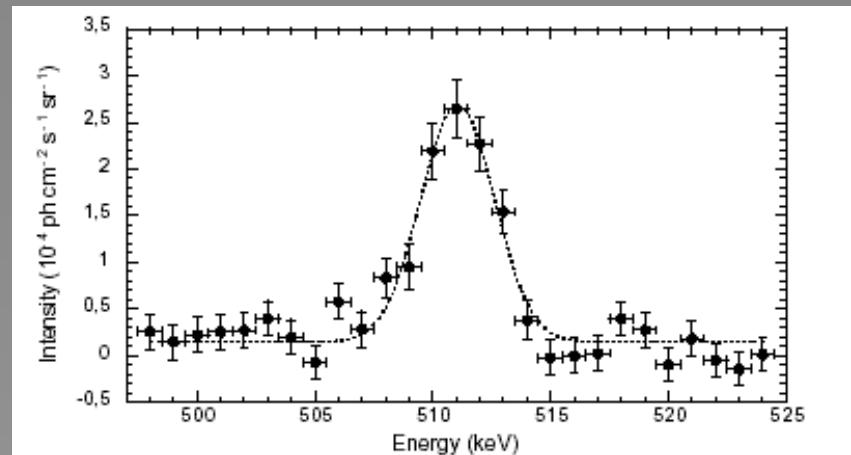


$$\frac{\Omega_\chi}{\Omega_m} \lesssim \left(\frac{1\text{MeV}}{m_\chi} \right)^{3.5}.$$

The 511 keV Line

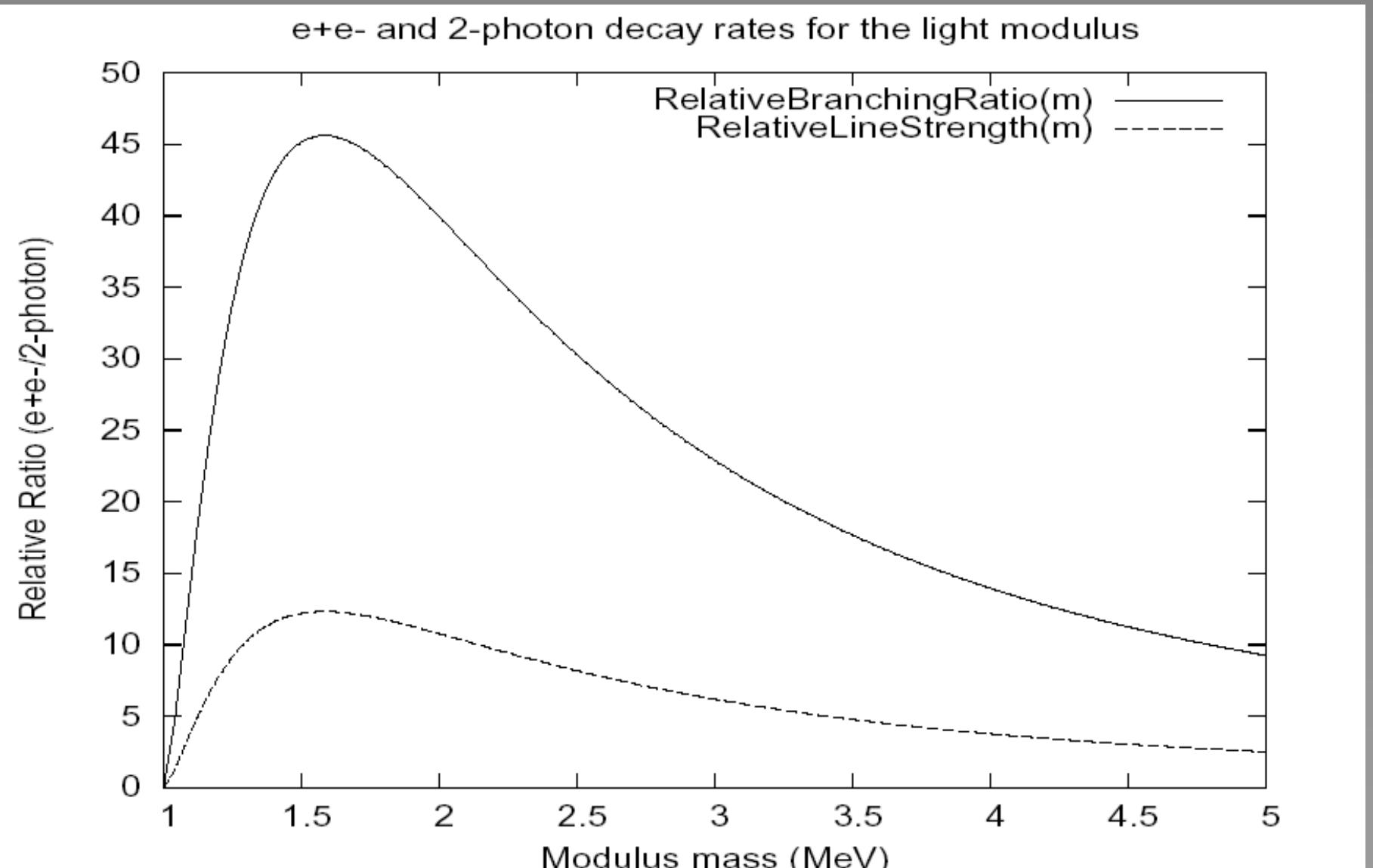


INTEGRAL/ SPI 511 keV line



Light Modulus χ : Dark matter?
Mass 1MeV, coupling to electrons dominant

511 keV from volume modulus decay? (prediction!)



$$\frac{\Omega_\chi}{\Omega_{dm}} \lesssim 10^{-3} \left(\frac{2 \text{ MeV}}{m_\chi} \right)^2.$$

Intensity
INTEGRAL

$\sim 8 \times 10^{-5} \text{ photons cm}^{-2} \text{s}^{-1}$
 $\lesssim 5 \times 10^{-5} \text{ photons cm}^{-2} \text{s}^{-1}$

CONCLUSIONS

- Exciting times for string cosmology/phenomenology!
- Soft terms calculable → rich phenomenology
- Distinctive moduli cosmology
- Concrete models of inflation (**closed vs open string inflaton**)
- Model independent signatures: **cosmic strings, no tensor modes, light modulus** (CMP, 511 keV? Prediction!)
- Many open questions

M_{GUT} vs 10^{11} GeV scales?
Fully realistic model?...

- Alternatives to inflation?