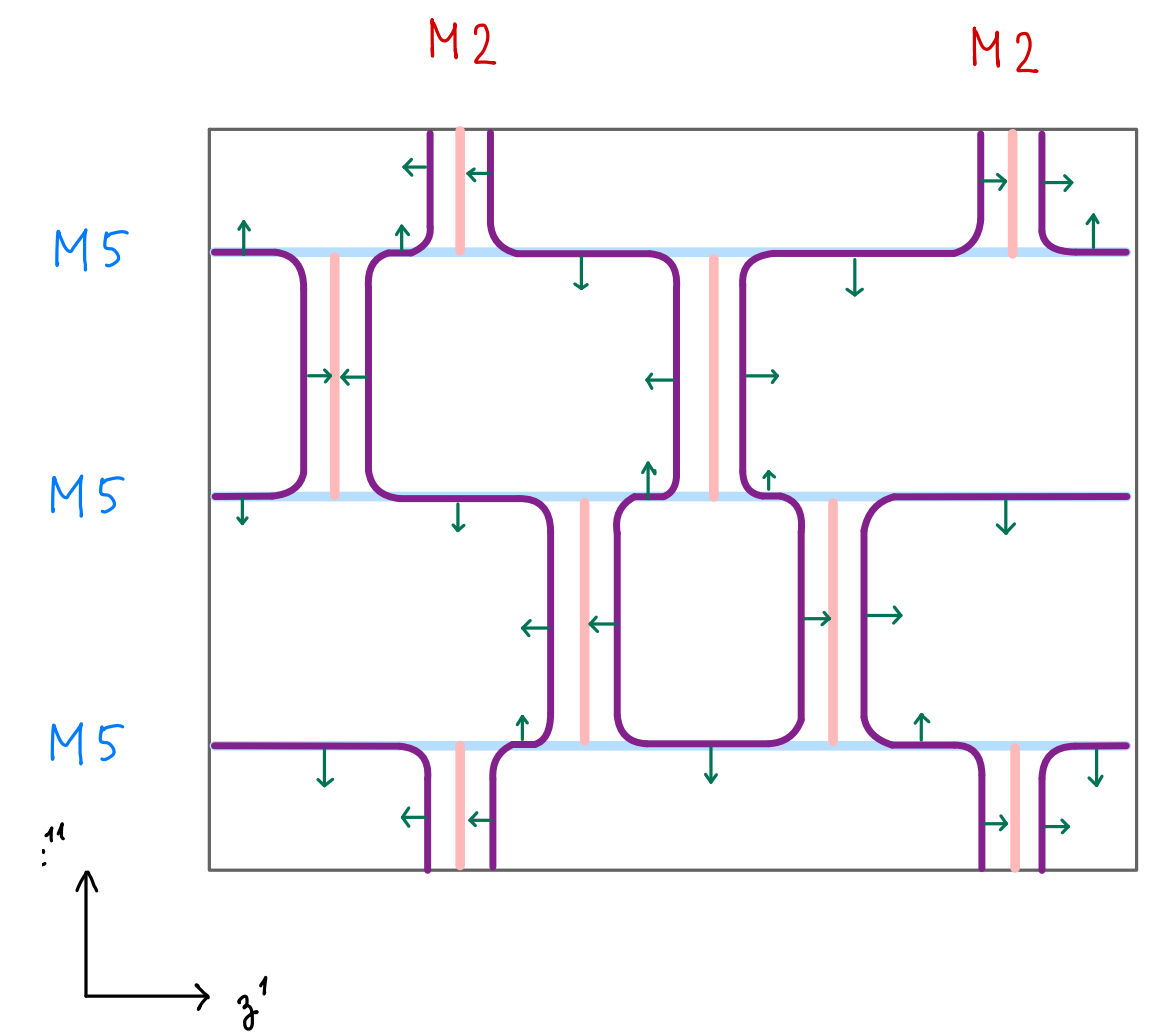
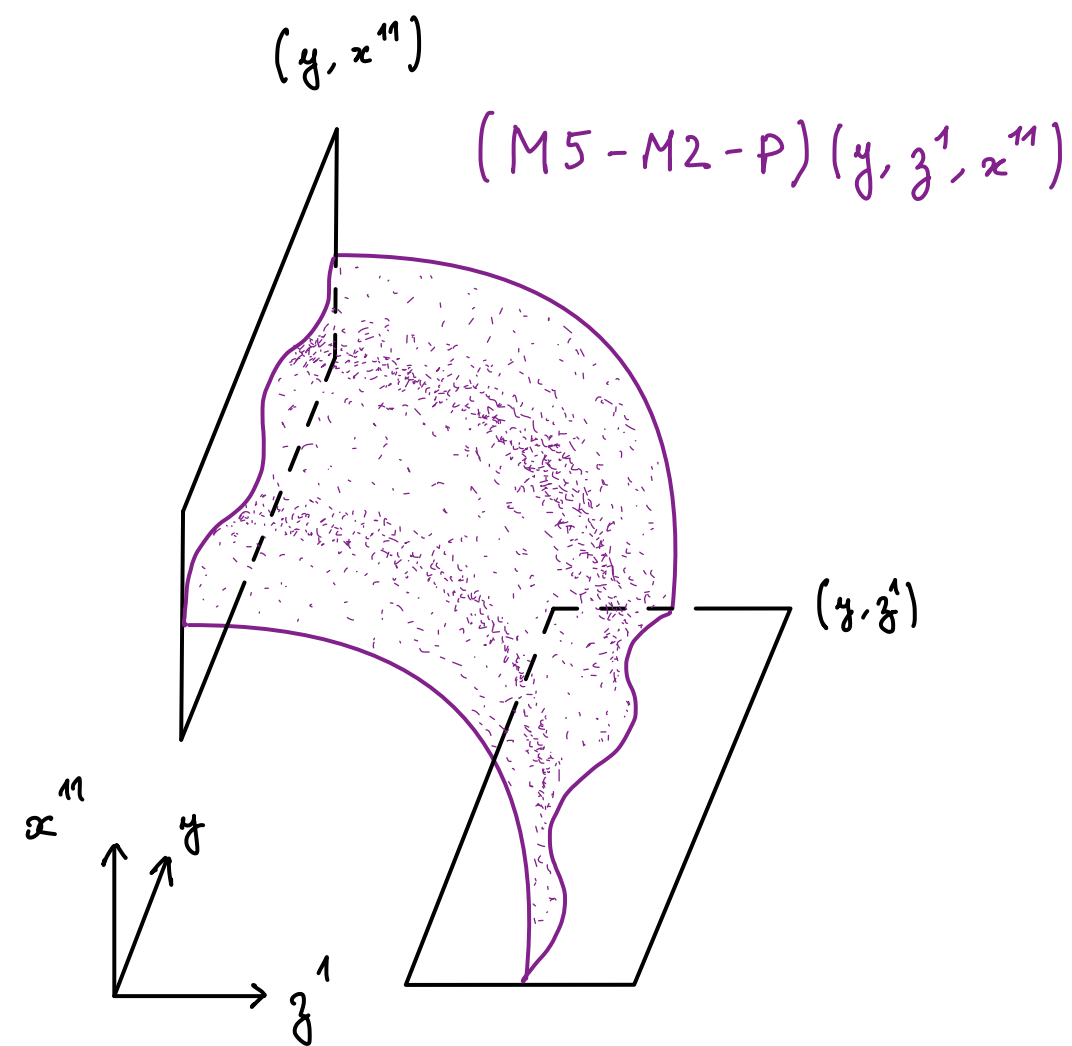


Shapes of M-theory black-hole microstates

Holography and the Swampland,
Corfu

Yixuan Li

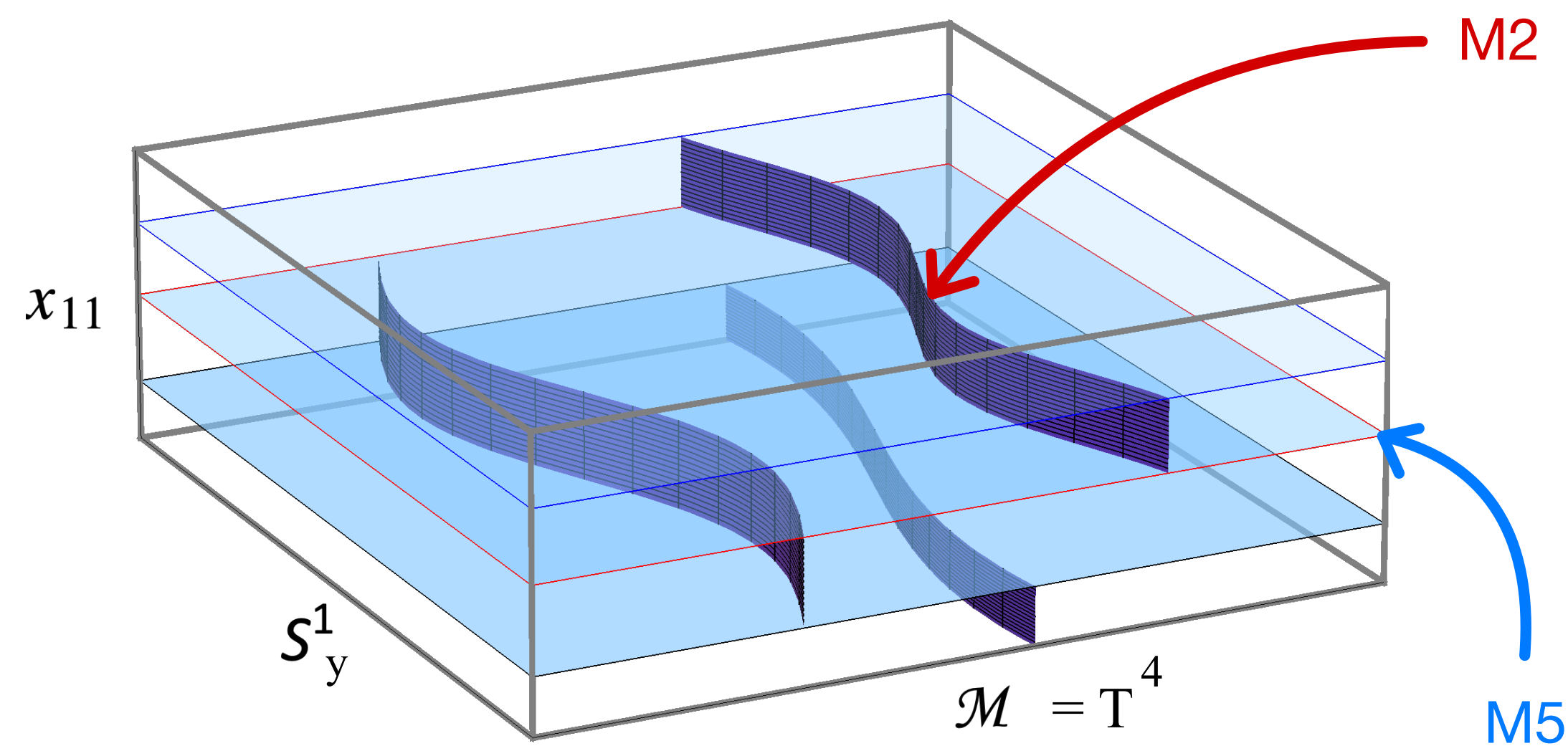
MPI Munich
& IPhT Saclay



Based on [22xx.xxxxx] with I. Bena, A. Houppe and D. Toulikas
and [2202.08844] with I. Bena, N. Ceplak, S. Hampton, D. Toulikas and N. Warner

September 8th, 2022

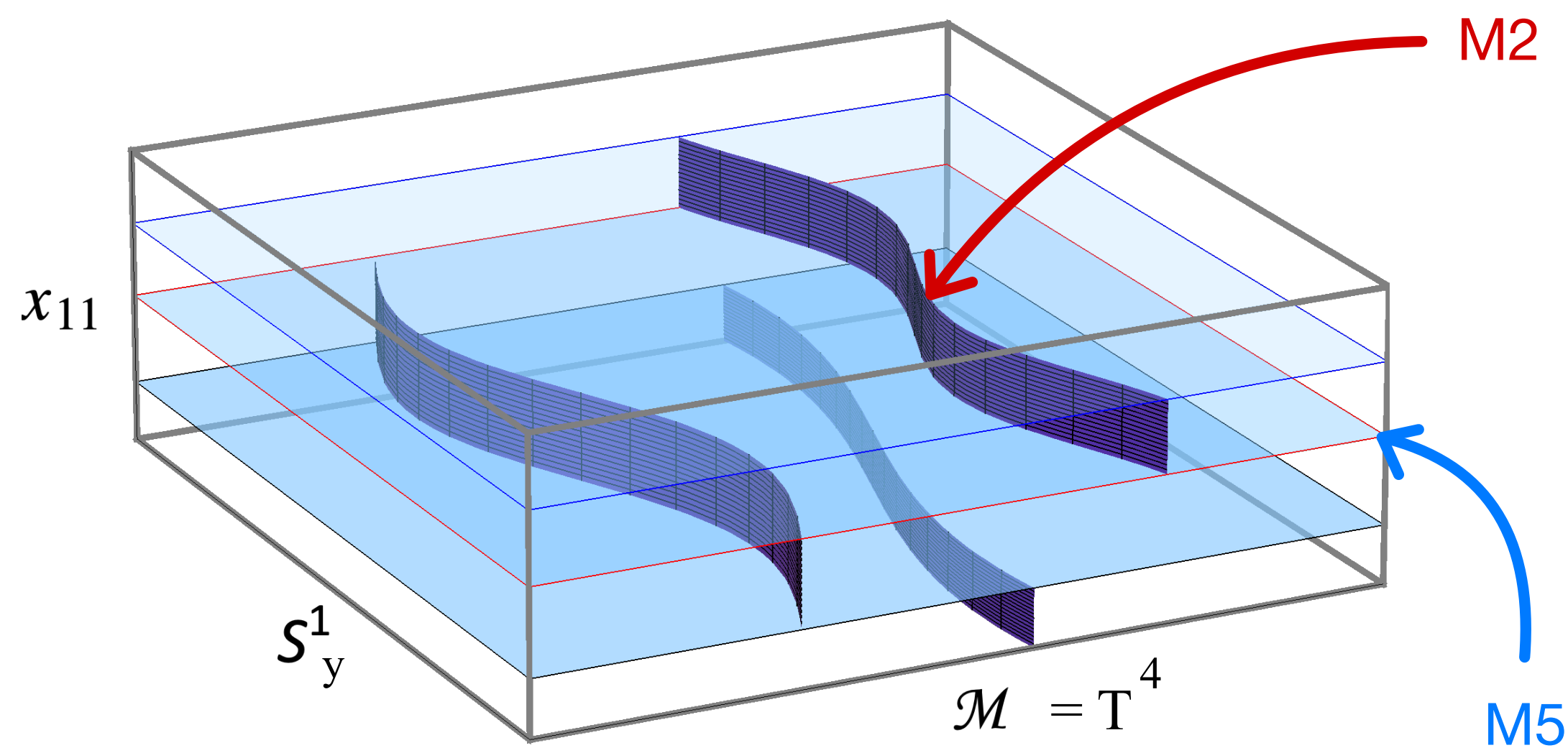
What this talk is about



- M5-M2(-P) black hole: The microstates that are made of **fractionated M2 branes** account for the entropy.
- We found: They can transition into microstates with **16 local supersymmetries**.

« Dijkgraaf-Verlinde-Verlinde microstates »

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« Dijkgraaf-Verlinde-Verlinde microstates »

- M5-M2(-P) black hole: The microstates that are made of **fractionated M2 branes** account for the entropy.
- We found: They can transition into microstates with **16 local supersymmetries**.
Microstates with **16 local susys** account for the black-hole entropy!
- We expect their backreaction to be horizonless microstates.

Outline

1. Local supersymmetries, bound states and black-hole microstates
2. The new M5-M2-P microstates with 16 local supersymmetries

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1. Local supersymmetries, bound states and black-hole microstates
2. The new M5-M2-P microstates with 16 local supersymmetries

1. a.

Supersymmetries and horizons

The 3-charge black hole and the supertube transition

- Type IIA/IIB: $\mathbb{R}^{4,1} \times S_y^1 \times T^4$
- Take brane system with 3 charges:

D5(y, T^4), D1(y), P(y)

or NS5(y, T^4), F1(y), P(y)

\Rightarrow naively, 1/8-BPS everywhere

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⇒ naively, 1/8-BPS everywhere

⇒ controls form of harmonic functions in metric: $1/r^\#$

⇒ develops horizon in supergravity

$$ds^2 = -\frac{2}{\sqrt{H_1 H_5}} [dt^2 + dy^2 + (H_P - 1)^{-1} (dy - dt)^2] + \sqrt{H_1 H_5} ds_{\mathbb{R}^4}^2 + (H_1 H_5)^{-1/2} ds_{T^4}^2$$

with

$$H_{1,5,P} = 1 + \frac{Q_{1,5,P}}{r^2}.$$

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supergravity

Possible conclusion:

All of the microstates seem to develop the same horizon in supergravity.

Therefore nothing special happens at the scale of the horizon:

The microstates differ at Planck size away from singularity, where supergravity breaks down.

The 3-charge black hole and the supertube transition

- Type IIA/IIB: $\mathbb{R}^{4,1} \times S_y^1 \times T^4$
- Take brane system with 3 charges:

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⇒ naively, 1/8-BPS everywhere

⇒ controls form of harmonic

functions in metric: $1/r^\#$

⇒ develops horizon in
supergravity

- *Supertube transition*: ingredients combine together to form a *bound state* that is locally 1/2-BPS.

Local VS global supersymmetries

- The presence of fundamental objects halves the supersymmetries of ST vacua:

$$\Pi \epsilon \equiv \frac{1}{2}(1 + P) \epsilon = 0$$

- Generically, the number of constraints Π_i add up. But when the objects form a **bound state**:

$$\hat{\Pi} \epsilon \equiv \frac{1}{2} (1 + \alpha_1 P_1 + \dots + \alpha_n P_n) \epsilon = 0$$

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- The α_i are not unique, can depend on *internal dimensions* x of bound state

$$\hat{\Pi}(x) \epsilon(x) = 0$$

→ *local supersymmetry*

- While for *global supersymmetry*:

$$\forall x, \quad \hat{\Pi}(x) \epsilon = 0.$$

Rewrite projector as:

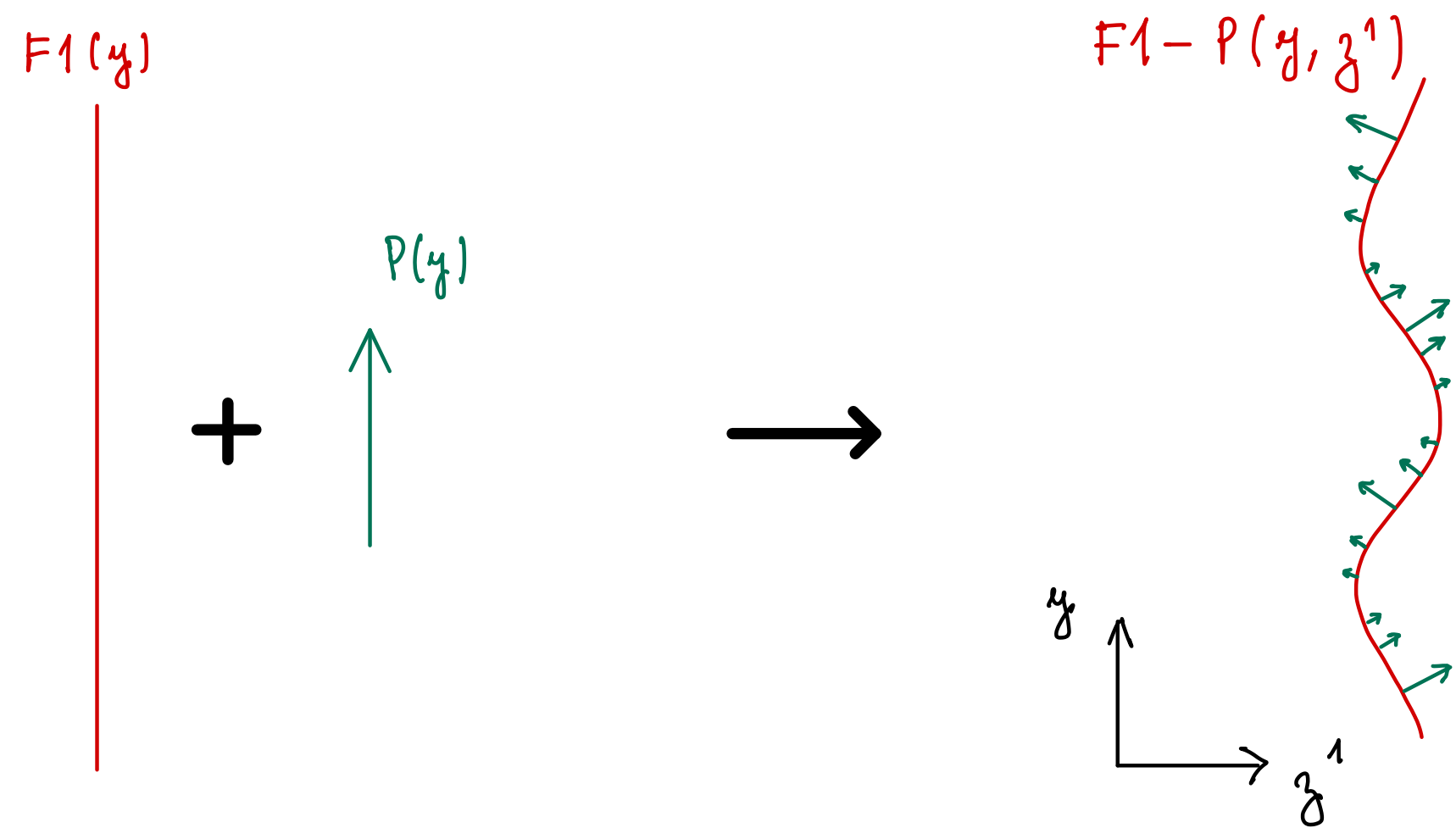
$$\hat{\Pi}(x) = F_1(x) \Pi_1 + \dots + F_k(x) \Pi_k$$

and the global ϵ verifies

$$\Pi_1 \epsilon = \dots = \Pi_k \epsilon = 0$$

Supertube transition: example 1

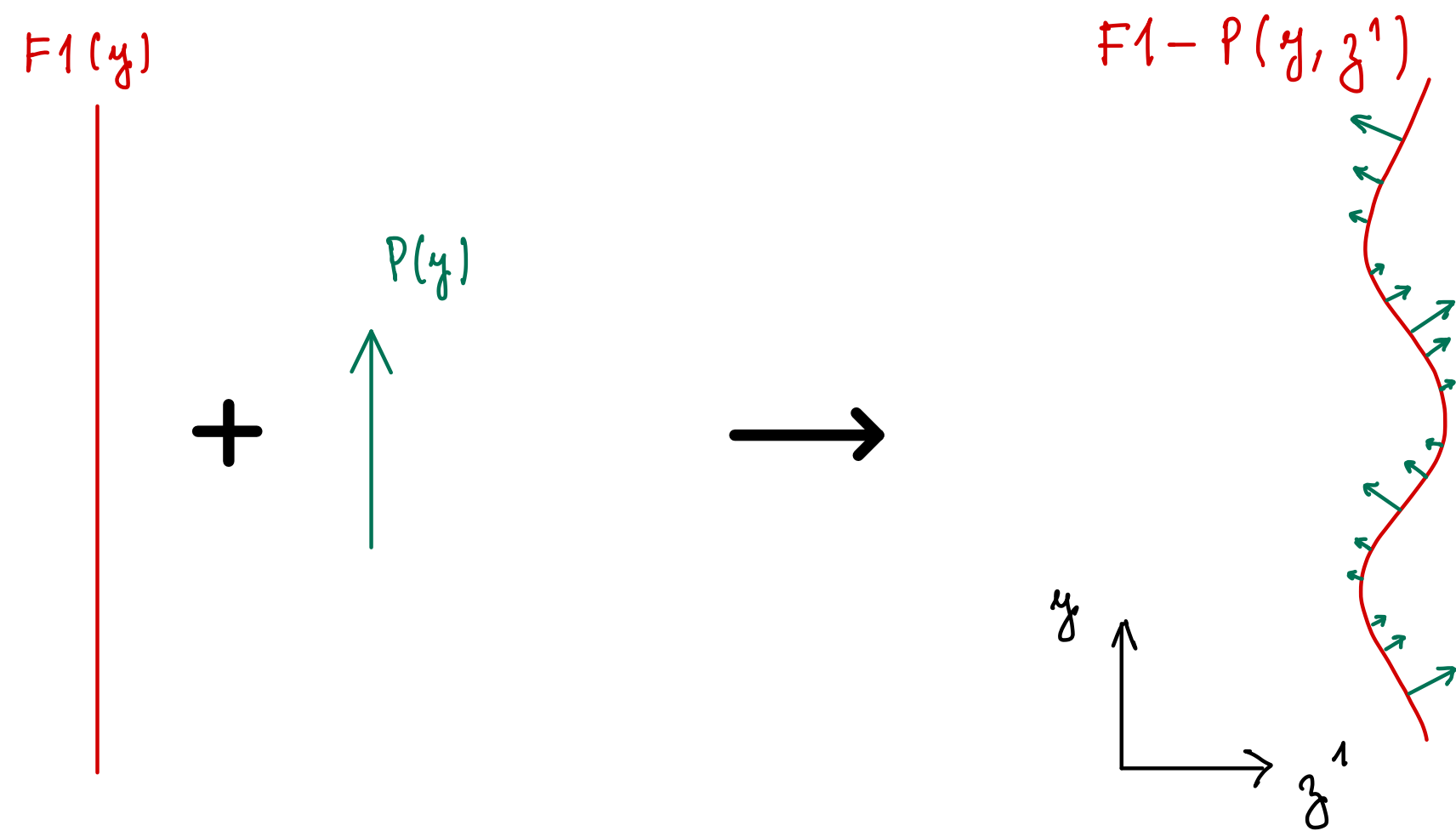
- One can make a bound state out of $F1(y)$ and $P(y)$ by giving a profile to the $F1$:



- $F1(y), P(y) \longrightarrow F1(z), P(z)$ dipoles

Supertube transition: example 1

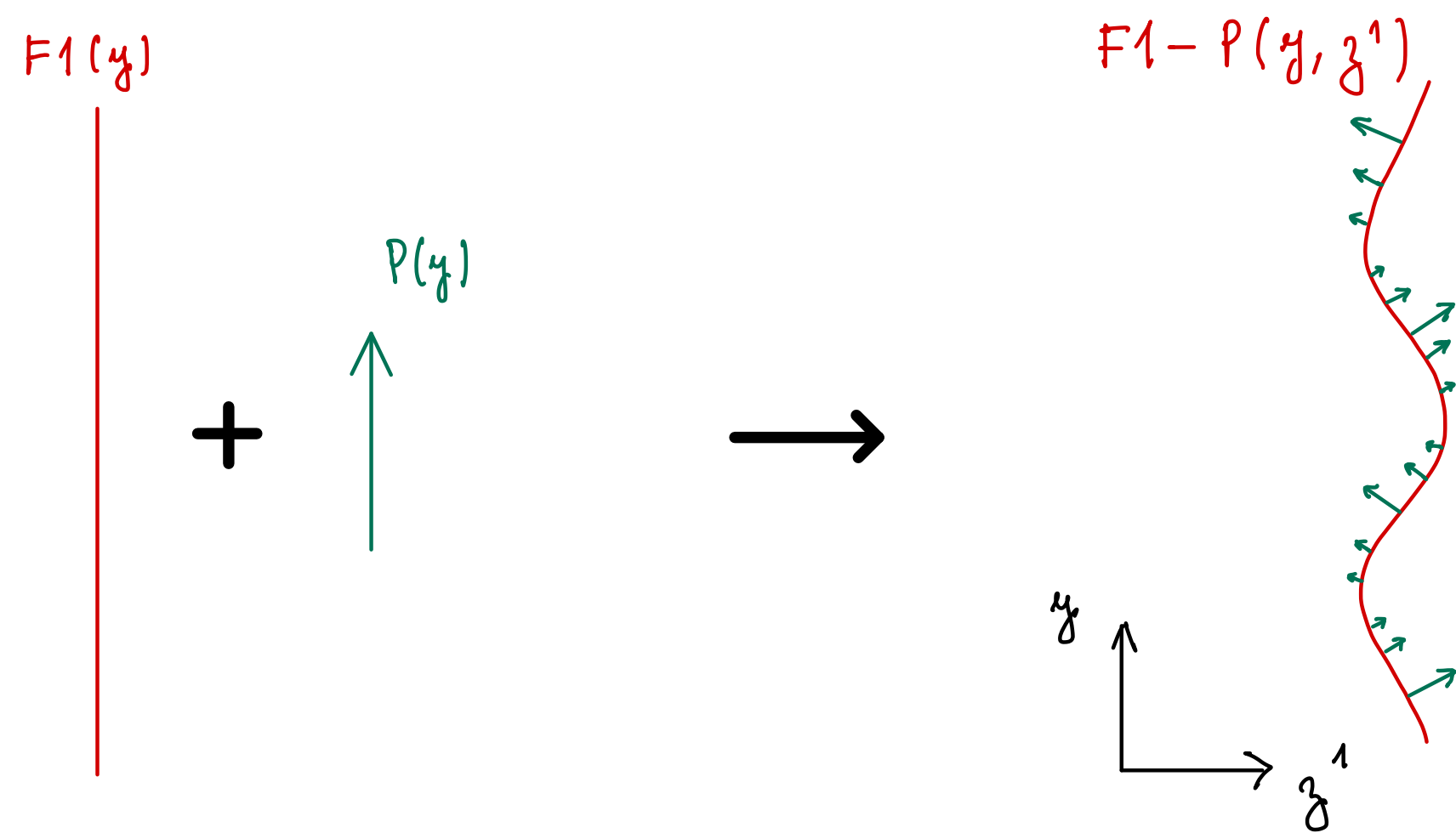
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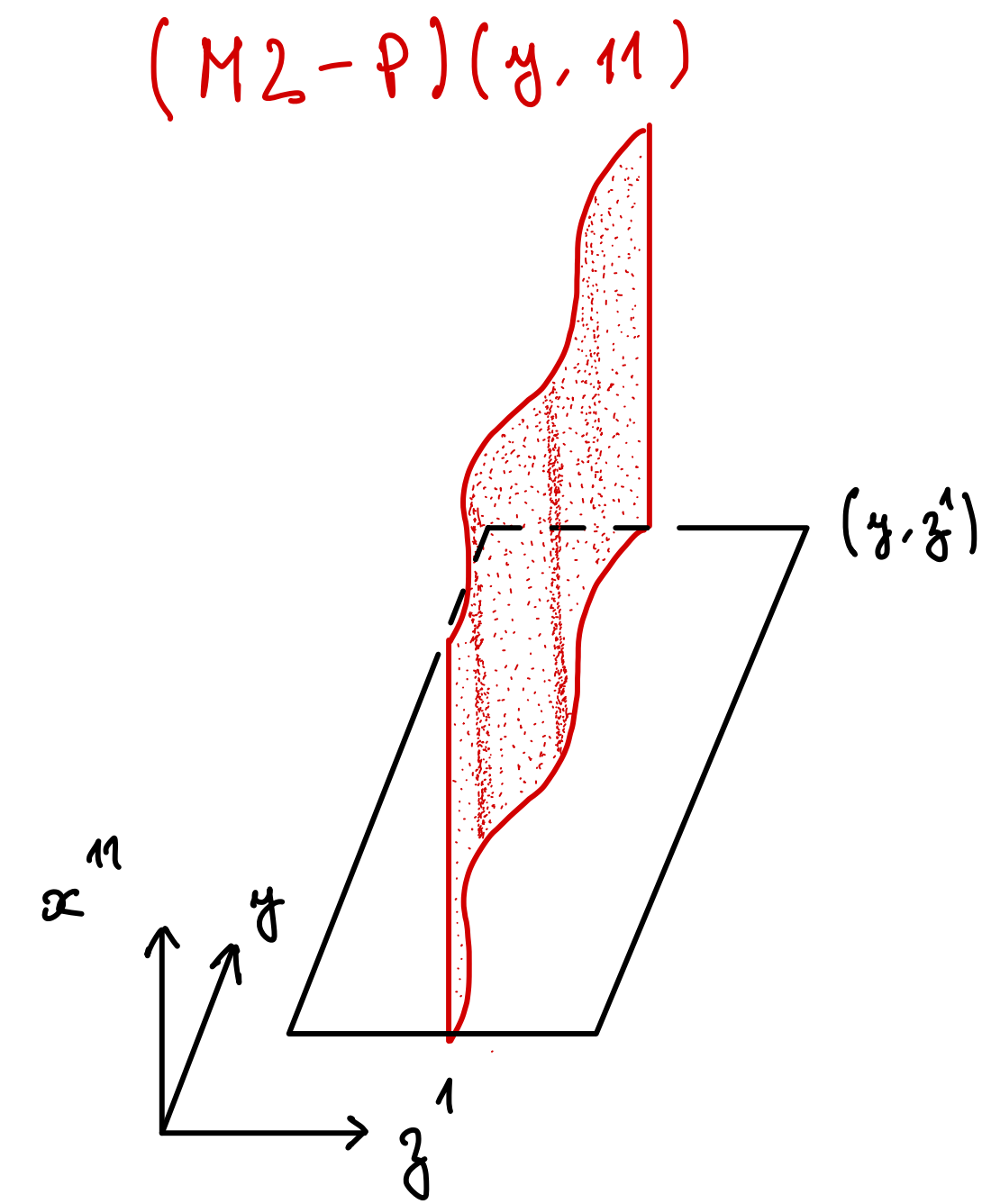
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- From M-theory:

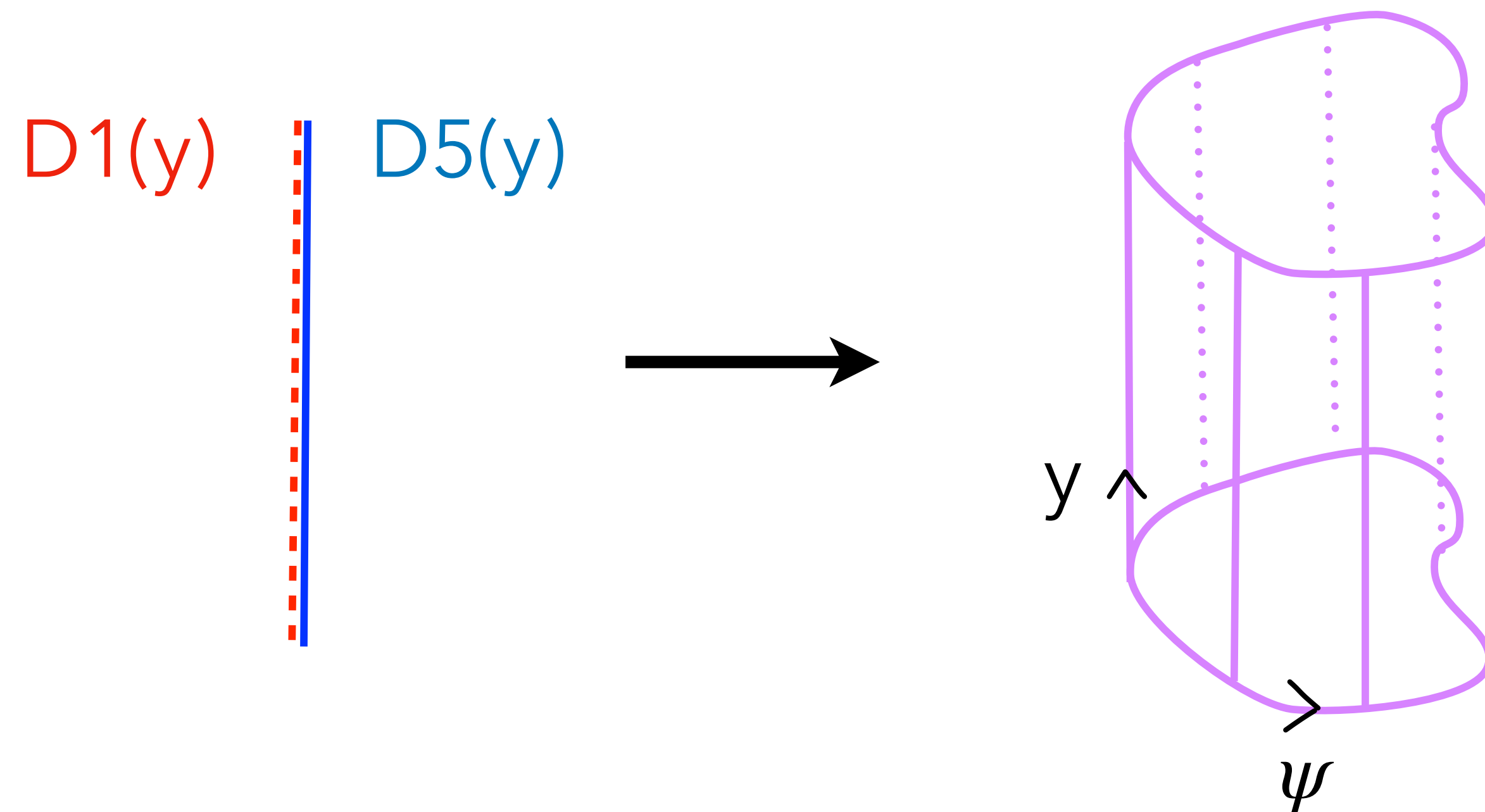


1. b.

Dealing with horizons: The old way

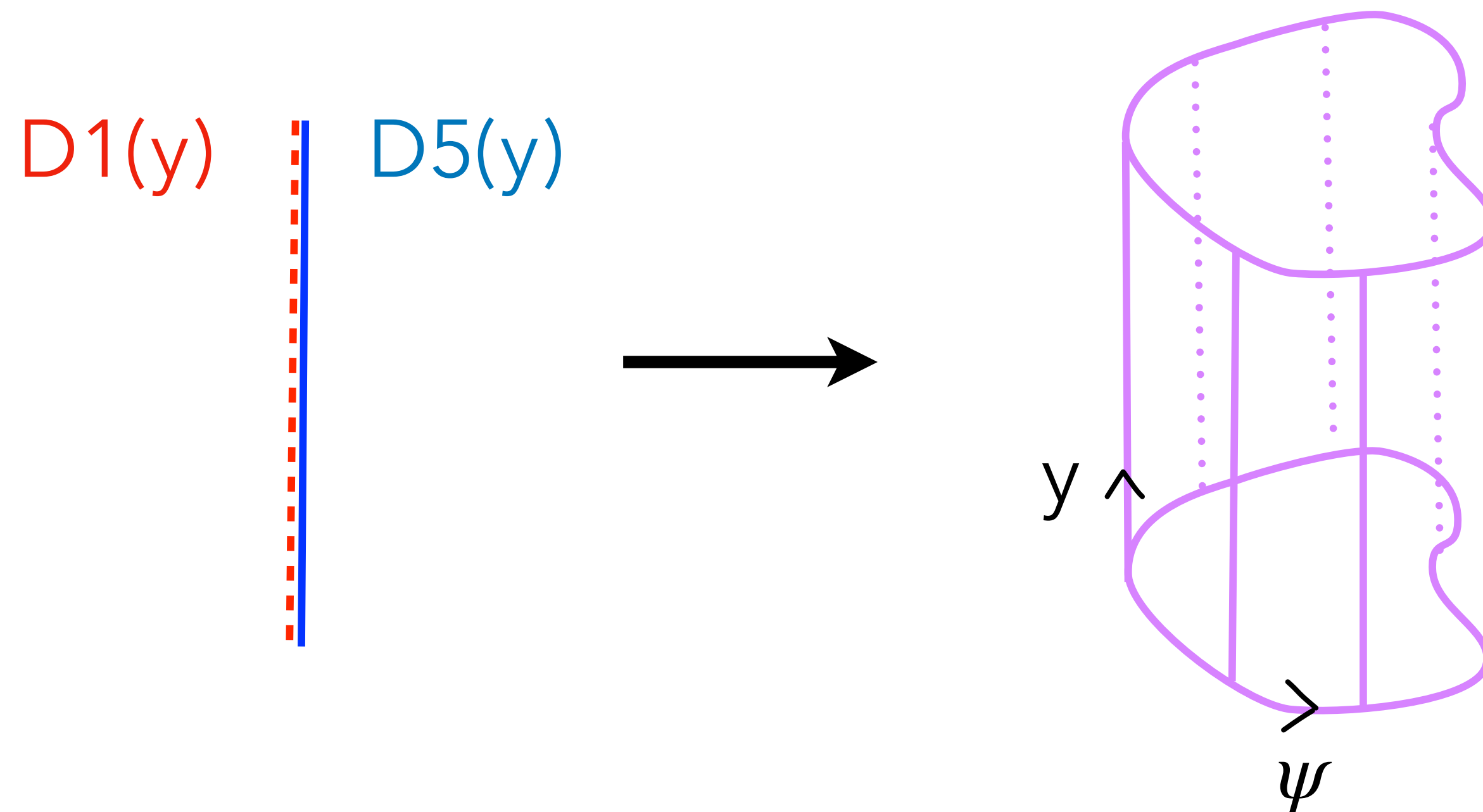
Supertube transition of D1-D5

- $D1(y), D5(y1234) \longrightarrow KKM(1234 \psi, y), P(\psi)$ dipoles
 - The D1-D5 brane system *gains* a dimension through the KKM



Supertube transition of D1-D5

- $D1(y), D5(y1234) \longrightarrow \text{KKM}(1234 \psi, y), P(\psi)$ dipoles
 - The D1-D5 brane system *gains* a dimension through the KKM
 - The (angular) momentum $P(\psi)$ or $J(\psi)$ stabilises the size of the supertube.

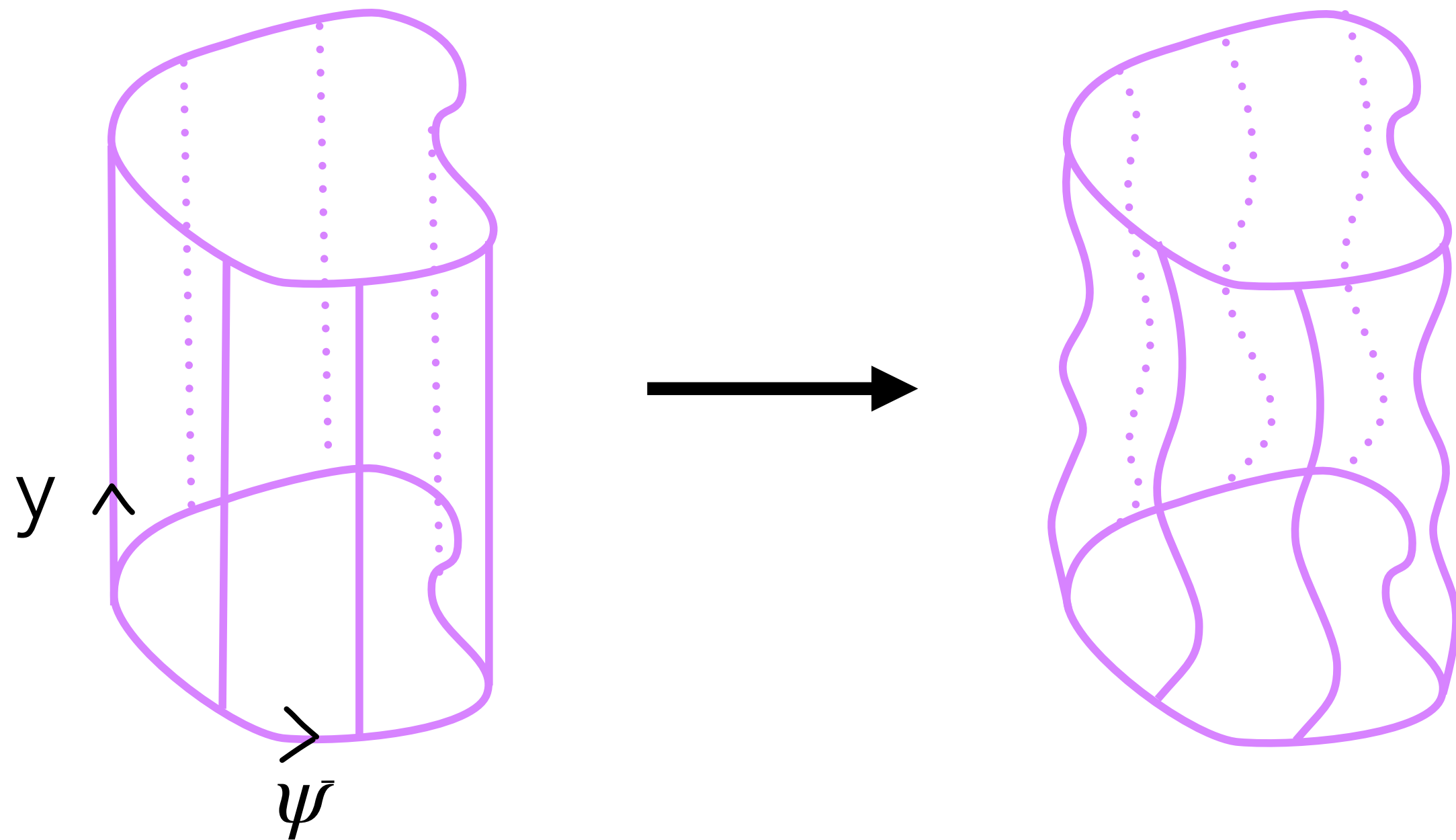


- The bound state is globally 1/4-BPS, but **locally 1/2-BPS**

Supertube transition of D1-D5-P

- How to add momentum on D1-D5 supertube?

→ Add shape modes on the KKM in \mathbb{R}^4 .

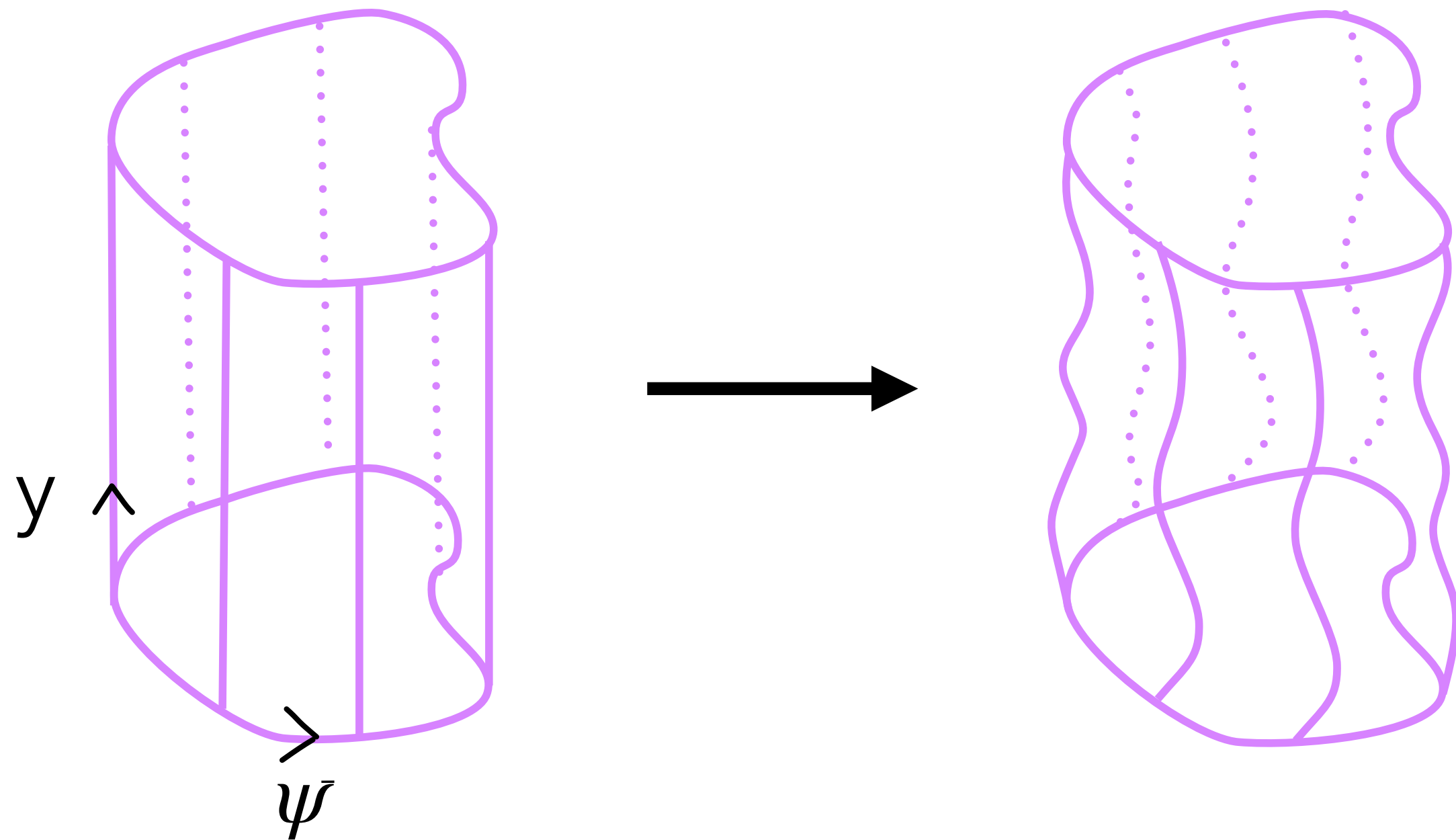


⇒ momentum Q_P along y .

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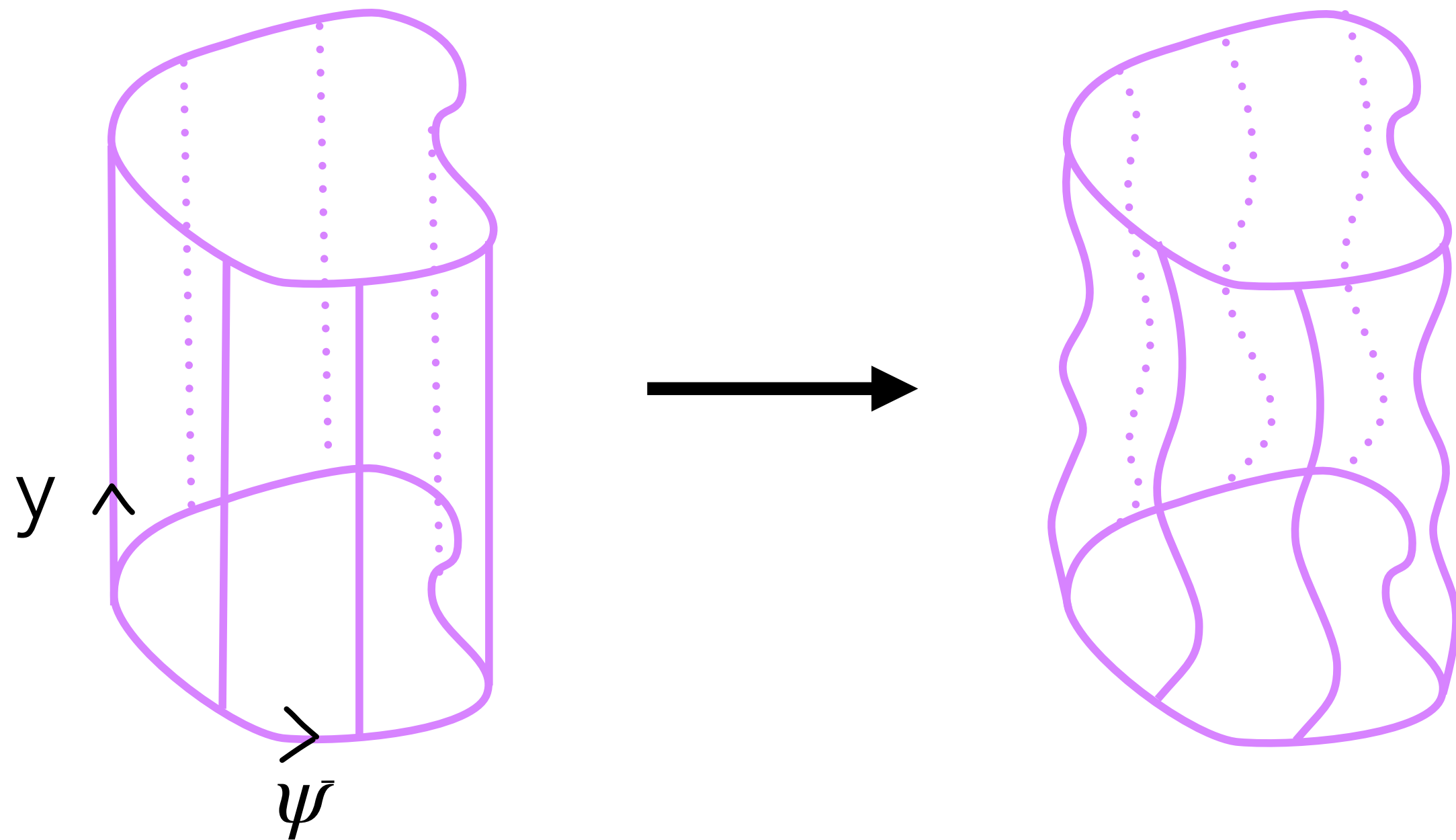
⇒ momentum Q_P along y .

- The bound state is globally 1/8-BPS (like the black hole), but **locally 1/2-BPS**

Supertube transition of D1-D5-P

- How to add momentum on D1-D5 supertube?

→ Add shape modes on the KKM in \mathbb{R}^4 .



⇒ momentum Q_P along y .

- The bound state is globally 1/8-BPS (like the black hole), but **locally 1/2-BPS**
- Different *shape modes* give different **microstates**
- Their backreaction are the **« superstrata »**

[Bena, de Boer, Shigemori, Warner '11]

Superstrata and their limits

- *Superstrata* have been constructed in supergravity: horizonless

[Bena, Giusto, Martinec, Russo, Shigemori, Turton, Warner '16]

- Part of the

Fuzzball hypothesis:

Individual black-hole microstates differ from themselves and from the BH solution at the horizon scale.

Superstrata and their limits

- *Superstrata* have been constructed in supergravity: horizonless

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- Part of the

Fuzzball hypothesis:

Individual black-hole microstates differ from themselves and from the BH solution at the horizon scale.

Drawbacks:

$$1. S \sim \sqrt{N_1 N_5} N_P^{1/4} \ll \sqrt{N_1 N_5 N_P}$$

[Shigemori '19]

2. Have a non-vanishing angular momentum in \mathbb{R}^4
 \Rightarrow are atypical
 \uparrow are not *exactly spherically symmetric*

See also [Lin, Maldacena, Rozenberg, Shan '22]

Outline

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2. The new M5-M2-P microstates with 16 local supersymmetries

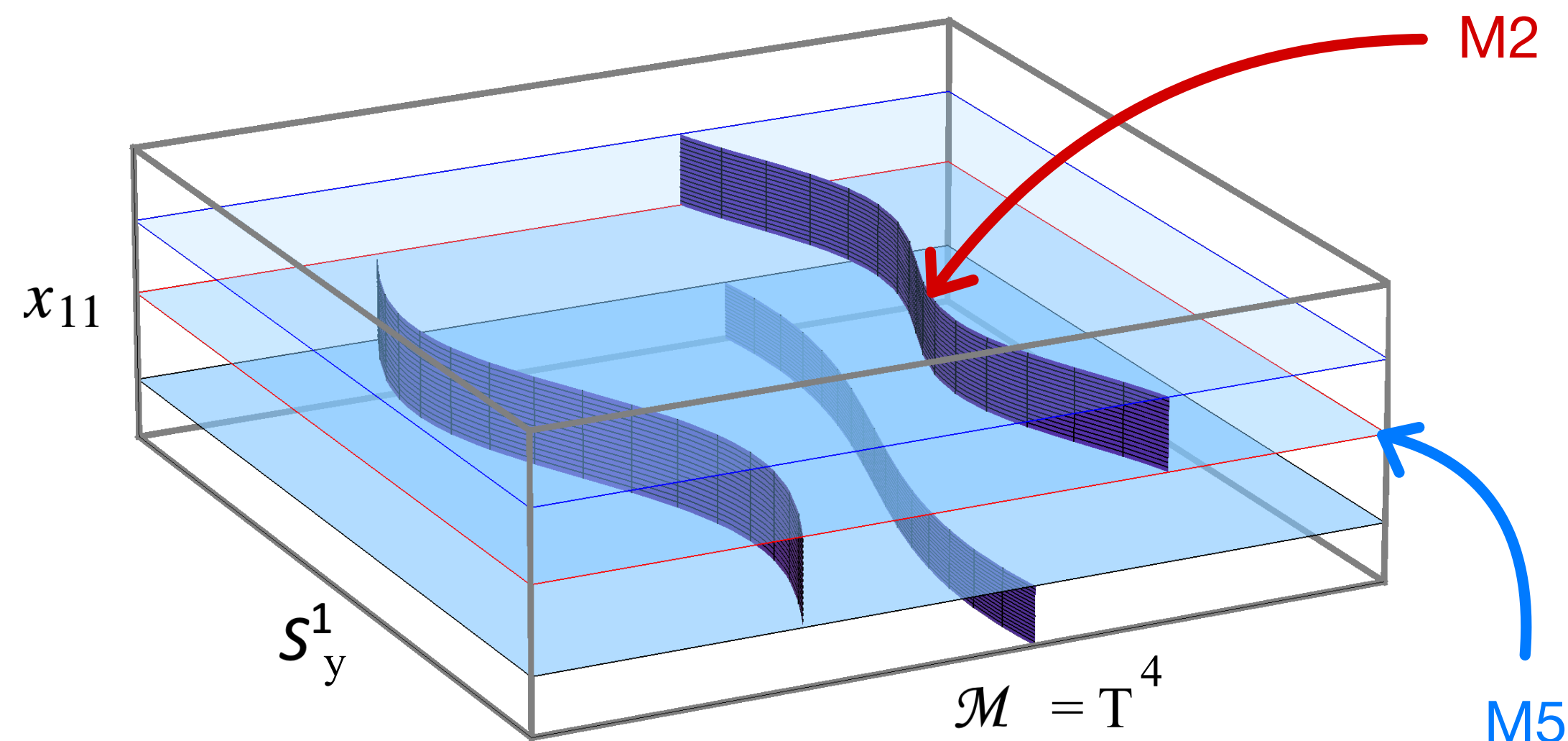
2. a.

Dealing with horizons: A new hope

Taking the problem from the other side

- For the NS5-F1-P black hole (IIA), we know where the entropy is coming from: *little strings / fractionated (M2) branes*

See e.g. [Martinec, Massai, Turton '19]



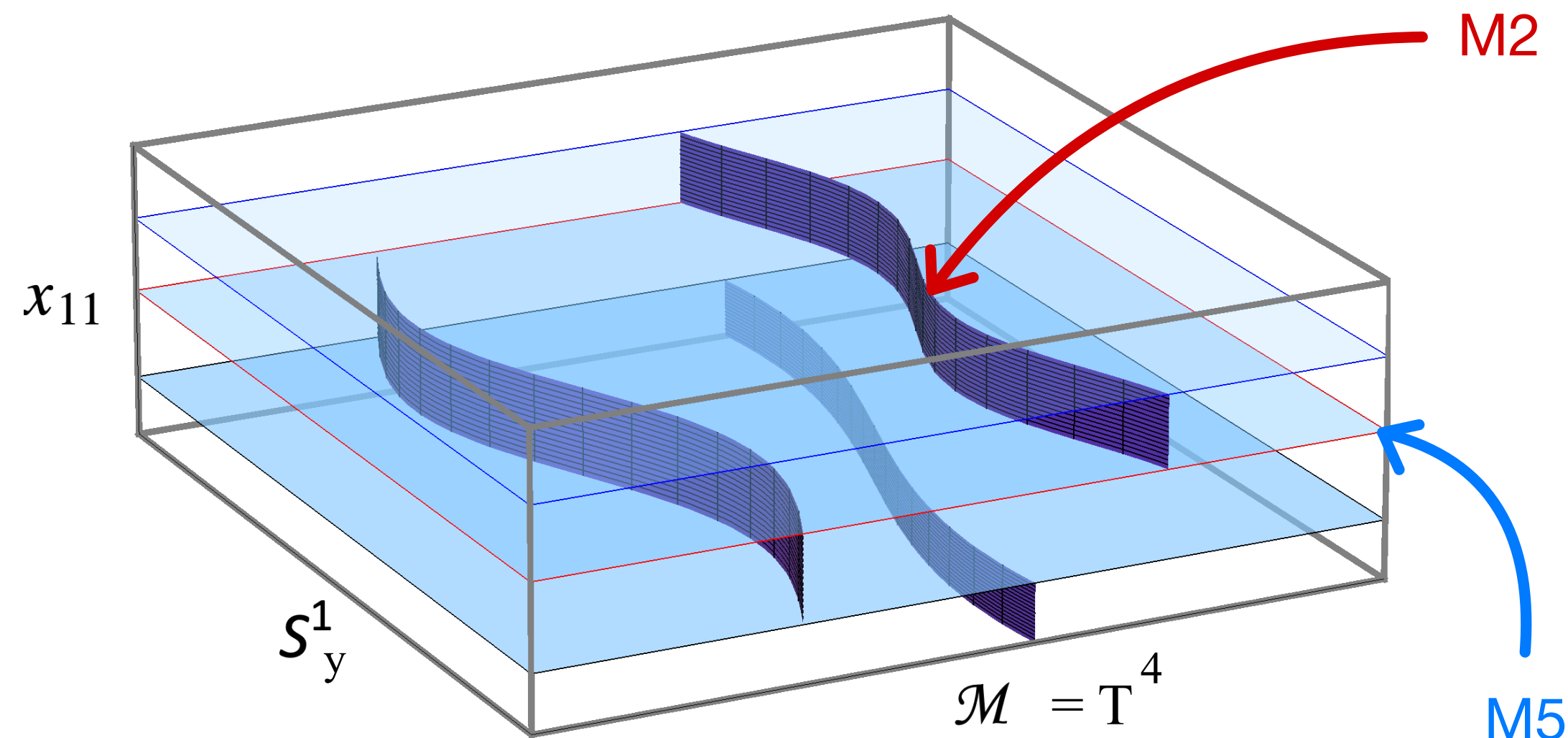
- The momentum is carried by the fractionated M2's through their motion in the T^4
→ *reproduce entropy.*

« Dijkgraaf-Verlinde-Verlinde
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« Dijkgraaf-Verlinde-Verlinde
microstates »

- The momentum is carried by the fractionated M2's through their motion in the T^4
→ *reproduce entropy.*
- The brane system is point-like in the non-compact spatial dimensions
→ *exact spherical symmetry.*

Our results

[Bena, Houppe, YL, Toulukas, to appear]

- We found the **supertube transition** of the Dijkgraaf-Verlinde-Verlinde (DVV) microstates.

Our results

[Bena, Houppe, YL, Toulukas, to appear]

- We found the **supertube transition** of the Dijkgraaf-Verlinde-Verlinde (DVV) microstates.
- We found the *supersymmetric projector*
 - preserving the supersymmetries of **NS5(y, T⁴), F1(y), P(y)** (IIA)
 - corresponding to a **locally 1/2-BPS (16 supersymmetries)** object:

$$\Pi_{\text{NS5-F1-P}} = \frac{1}{2} \left[1 + a^2 P_{\text{NS5}(y1234)}^{\text{IIA}} + b^2 P_{\text{F1}(y)} + c^2 P_{\text{P}(y)} \right. \\ \left. + ab \left(P_{\text{D4}(y234)} - P_{\text{D2}(y1)} \right) + bc \left(P_{\text{P}(1)} - P_{\text{F1}(1)} \right) + ca \left(P_{\text{D4}(1234)} - P_{\text{D0}} \right) \right].$$

First look at the projector

$$\Pi_{\text{NS5-F1-P}} = \frac{1}{2} \left[1 + a^2 P_{\text{NS5}(y1234)}^{\text{IIA}} + b^2 P_{\text{F1}(y)} + c^2 P_{\text{P}(y)} \right. \\ \left. + ab \left(P_{\text{D4}(y234)} - P_{\text{D2}(y1)} \right) + bc \left(P_{\text{P}(1)} - P_{\text{F1}(1)} \right) + ca \left(P_{\text{D4}(1234)} - P_{\text{D0}} \right) \right].$$

$$a^2 + b^2 + c^2 = 1$$

$$\begin{aligned} P_{\text{P}} &= \Gamma^{01} \\ P_{\text{NS5}}^{\text{IIA}} &= \Gamma^{012345} \\ P_{\text{KKM}(12345;6)}^{\text{IIA}} &= \Gamma^{012345} \sigma_3 = \Gamma^{6789} \\ P_{\text{D0}} &= \Gamma^0 i \sigma_2 \\ P_{\text{D2}} &= \Gamma^{012} \sigma_1 \\ P_{\text{D4}} &= \Gamma^{01234} i \sigma_2 \\ P_{\text{D6}} &= \Gamma^{0123456} \sigma_1 \end{aligned}$$

$$\begin{aligned} P_{\text{F1}} &= \Gamma^{01} \sigma_3 \\ P_{\text{NS5}}^{\text{IIB}} &= \Gamma^{012345} \sigma_3 \\ P_{\text{KKM}(12345;6)}^{\text{IIB}} &= \Gamma^{012345} = \Gamma^{6789} \\ P_{\text{D1}} &= \Gamma^{01} \sigma_1 \\ P_{\text{D3}} &= \Gamma^{0123} i \sigma_2 \\ P_{\text{D5}} &= \Gamma^{012345} \sigma_1 \end{aligned}$$

2. b.

*Supertube transitions between 2 ingredients
out of NS5, F1 and P*

Glueing F1 and P

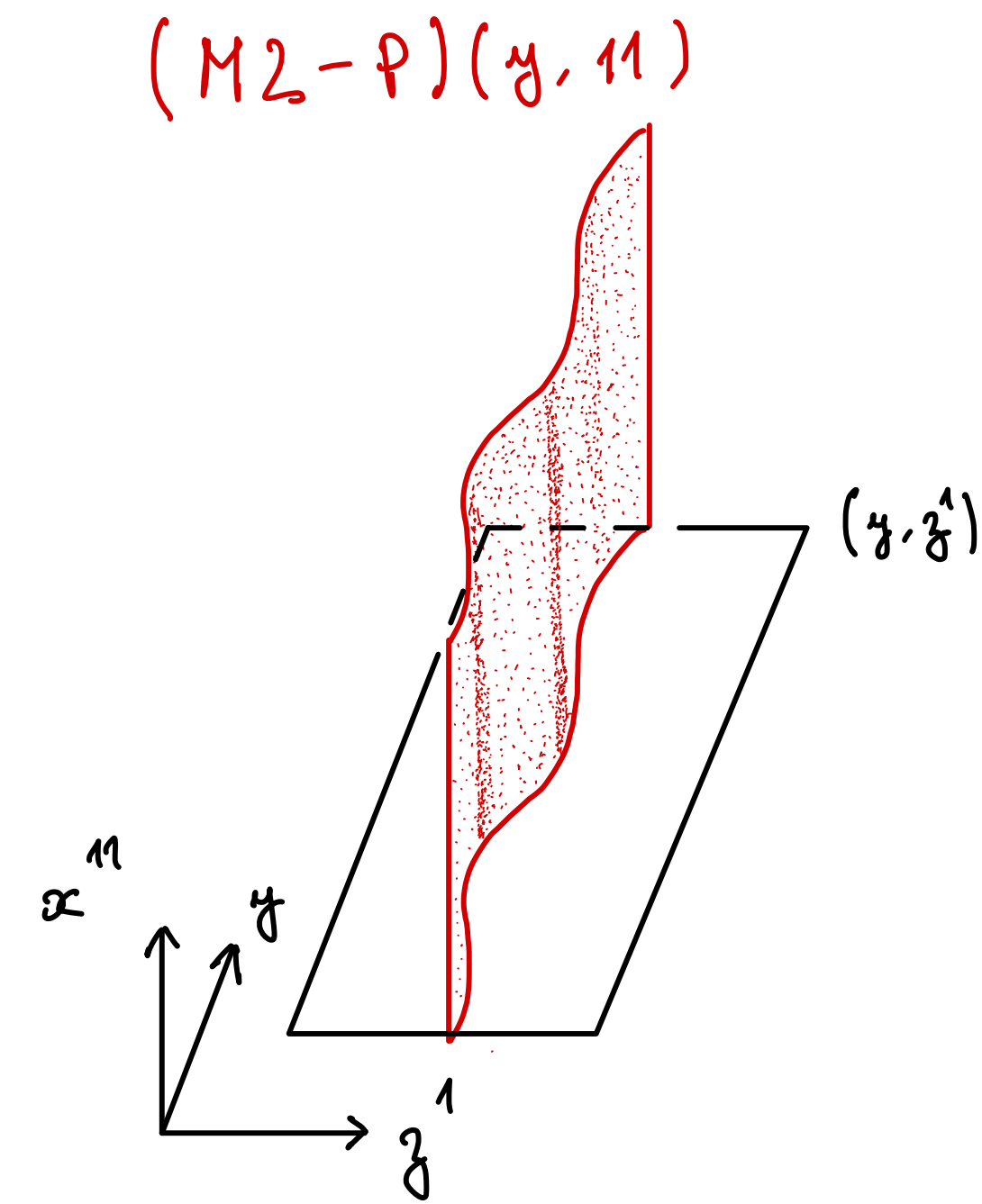
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- Put $a = 0$
- $\text{F1}(y), \text{P}(y) \longrightarrow \text{F1}(z), \text{P}(z)$ dipoles

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- Put $a = 0$
- $\text{F1}(y), \text{P}(y) \longrightarrow \text{F1}(z), \text{P}(z)$ dipoles
- Corresponds to a **M2-brane** carrying momentum along y by moving in T^4 .
- $b = \cos \alpha, \quad c = \sin \alpha$
- Brane system is point-like in \mathbb{R}^4 .



Glueing NS5 and P

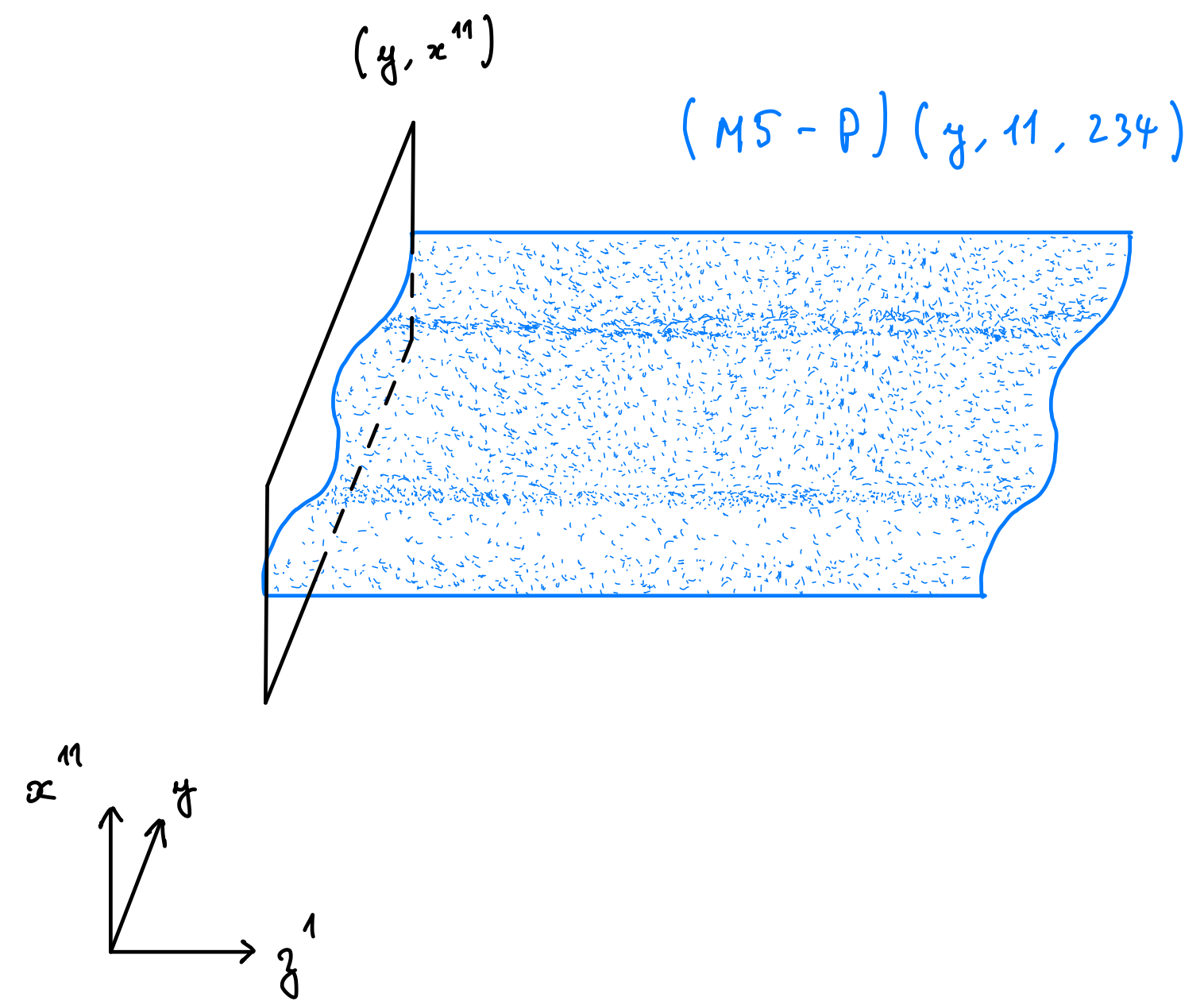
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Glueing NS5 and P

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- Corresponds to a **M5-brane** carrying momentum along y by moving in x^{11} .
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Glueing NS5 and F1

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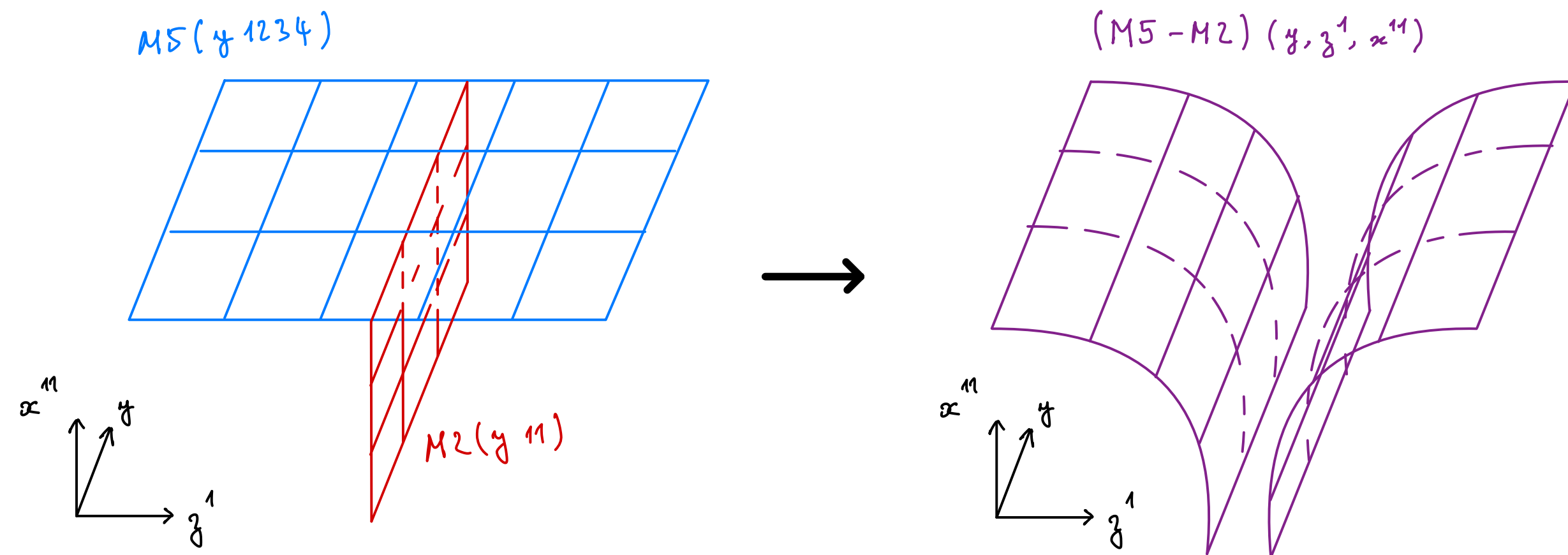
- Put $c = 0$
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- Put $c = 0$
- $\text{NS5}(y, T^4), \text{F1}(y) \longrightarrow \text{local D4}(y234), \text{D2}(y1)$
- ROUGH ANGLES between $\text{M5}'\text{s}$ and $\text{M2}'\text{s}$ become *smooth*:

\longrightarrow new brane system looks like a *furrow* along y .



\uparrow This M5-M2 furrow is dual to a D4-F1 Callan-Maldacena spike

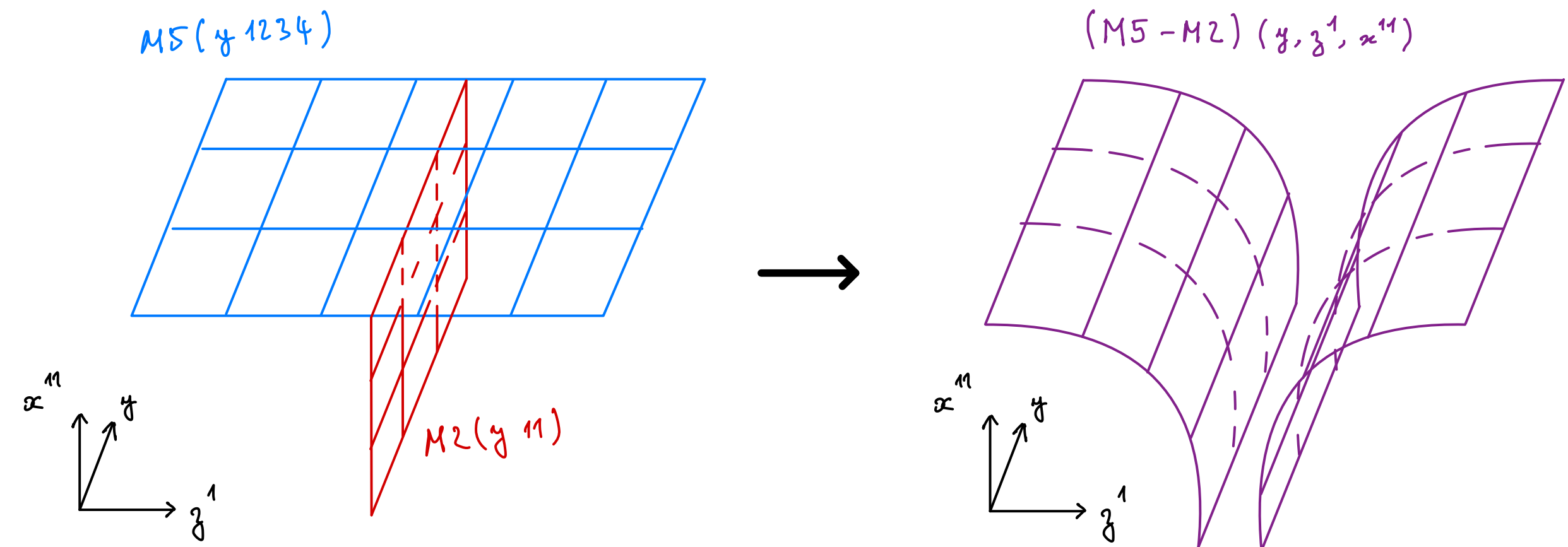
Glueing NS5 and F1

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- The **furrow** interpolates between **M5** and **M2**:

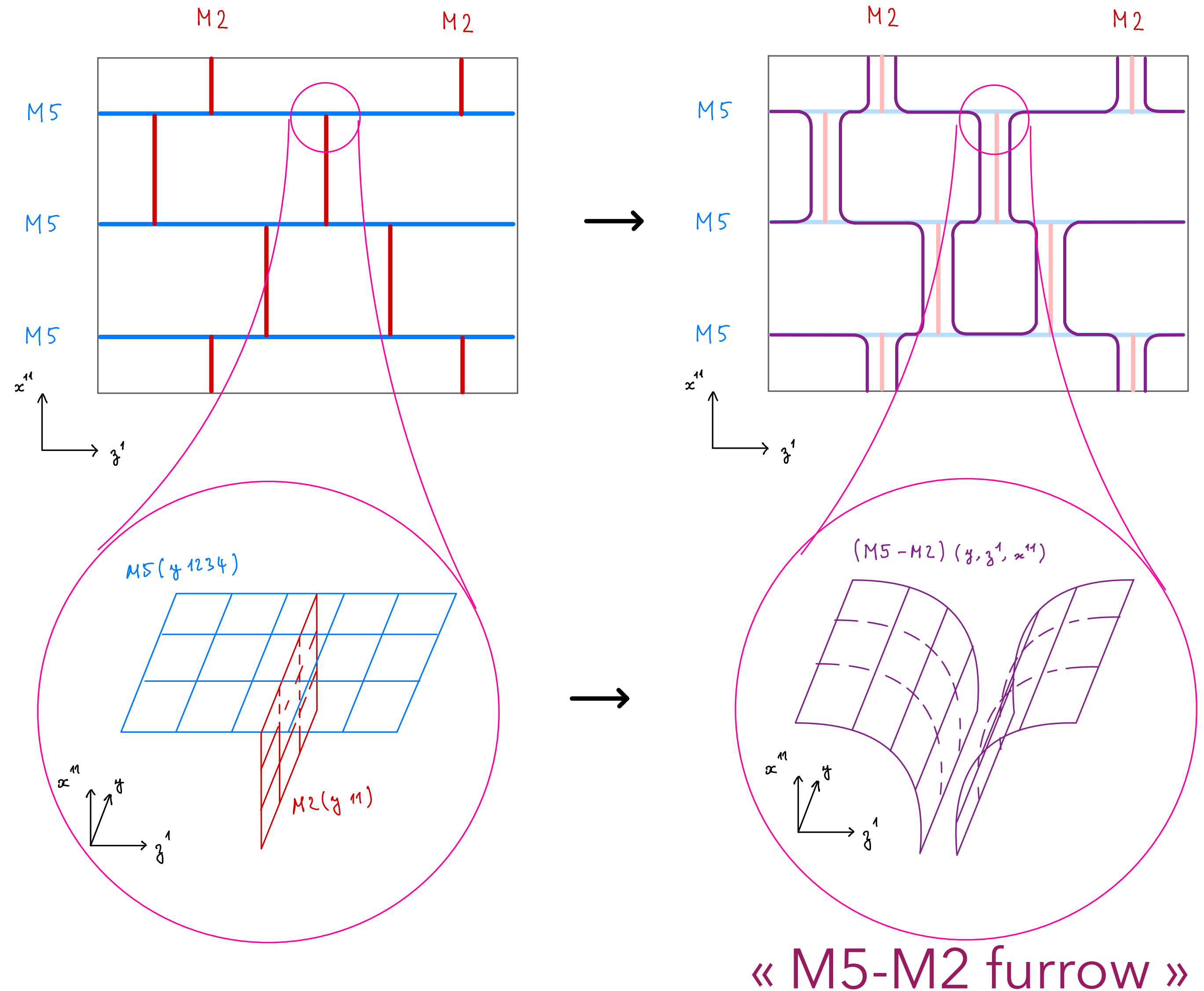
$$a = \cos \beta, \quad b = \sin \beta$$

⇒ The orientation of a local piece of the furrow determines the ratio between **M5** and **M2** charges.



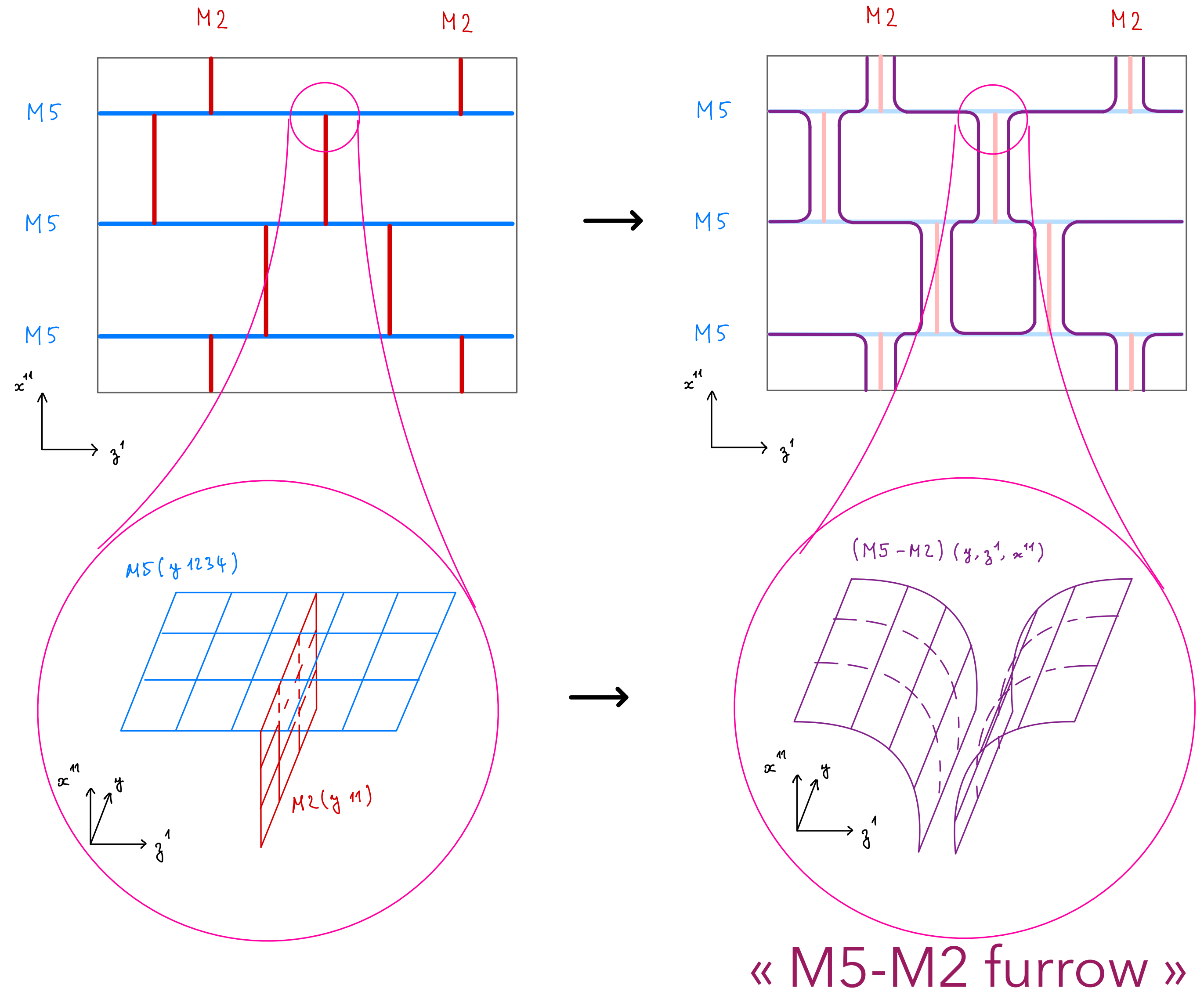
Transition of a M5-M2 black-hole microstate

- Joining 2 furrows make a **tunnel** between two M5's
- Local transition \Rightarrow a M5-M2 black-hole microstate will transition into a « **labyrinth** » ...



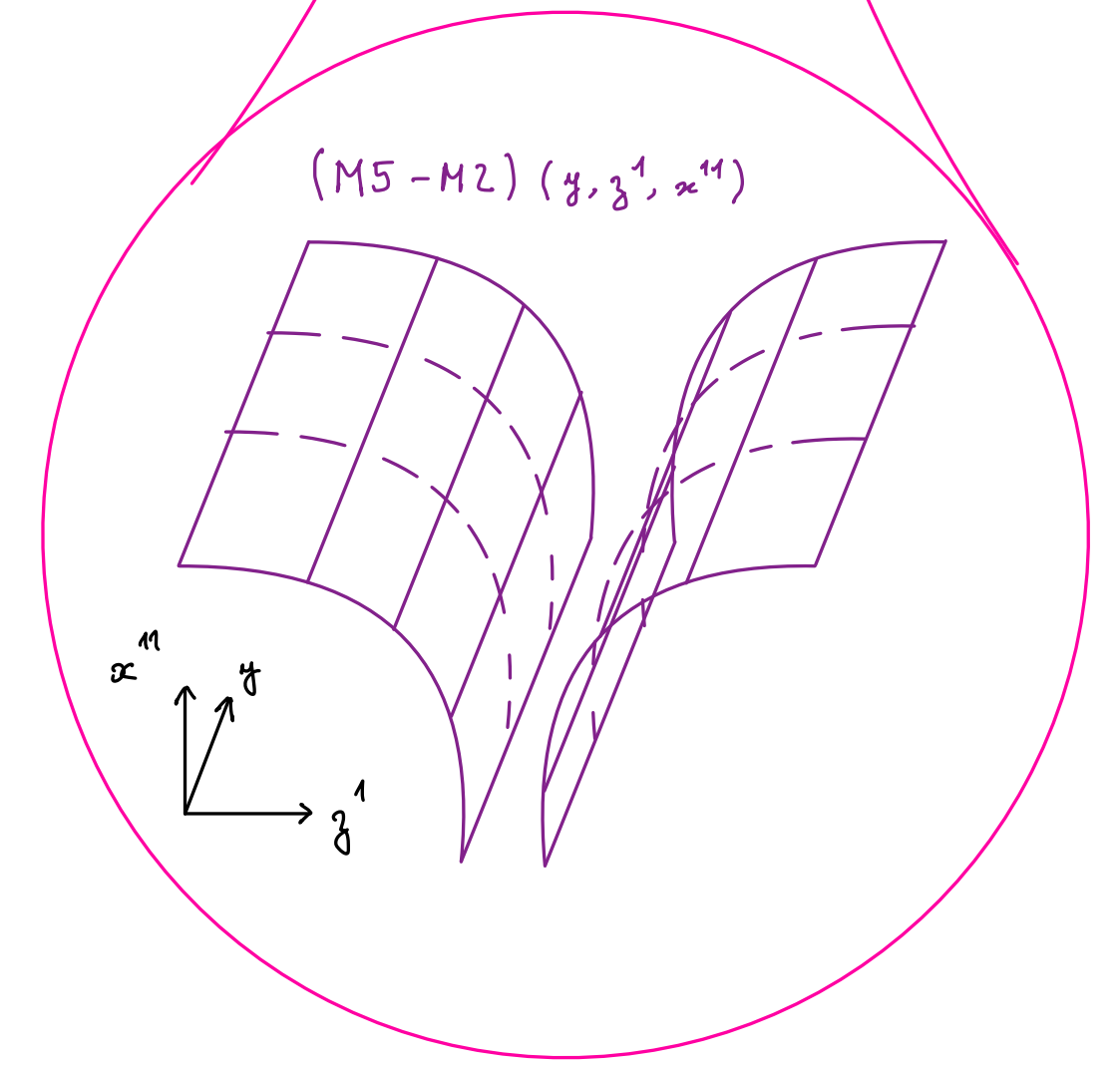
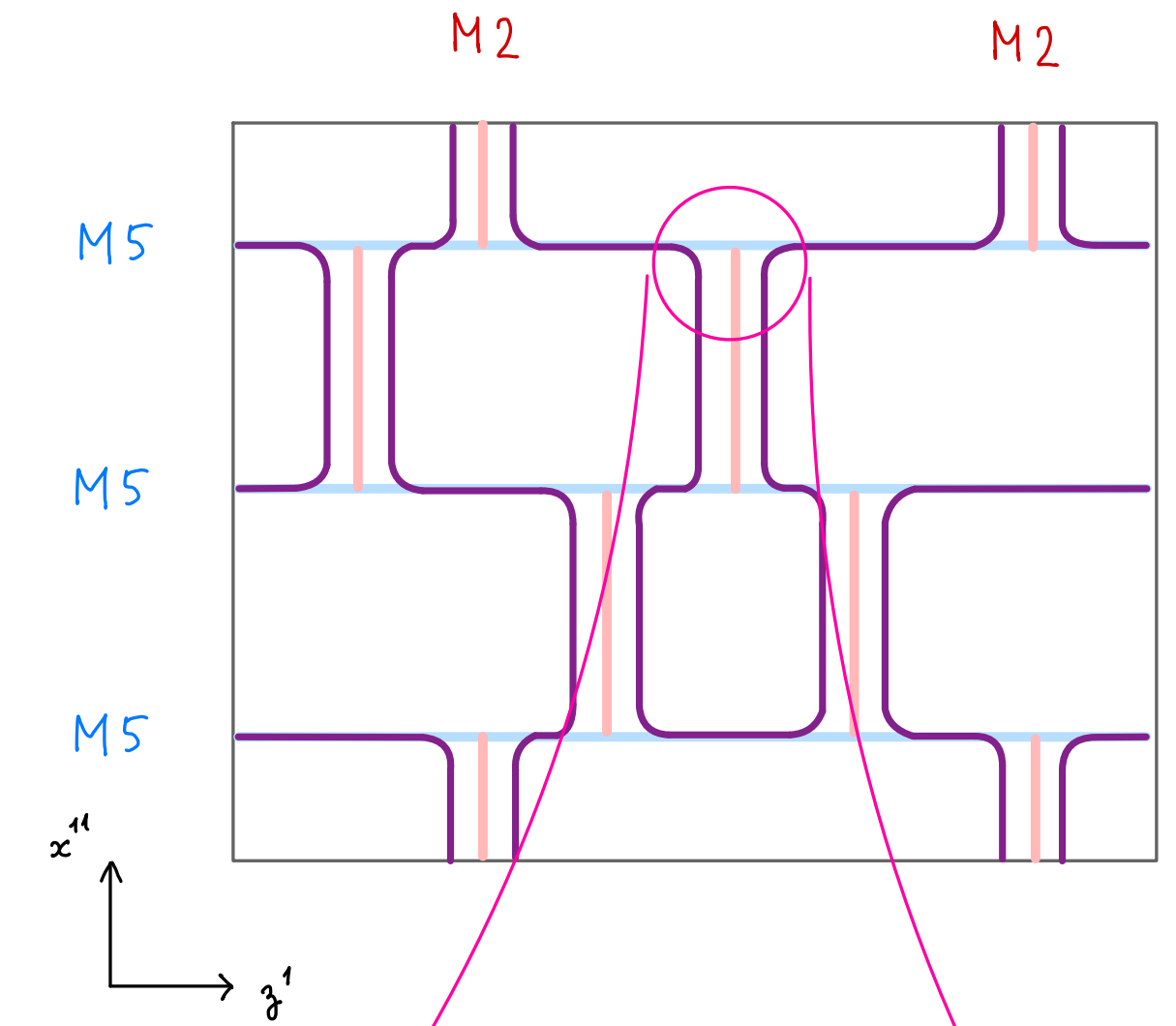
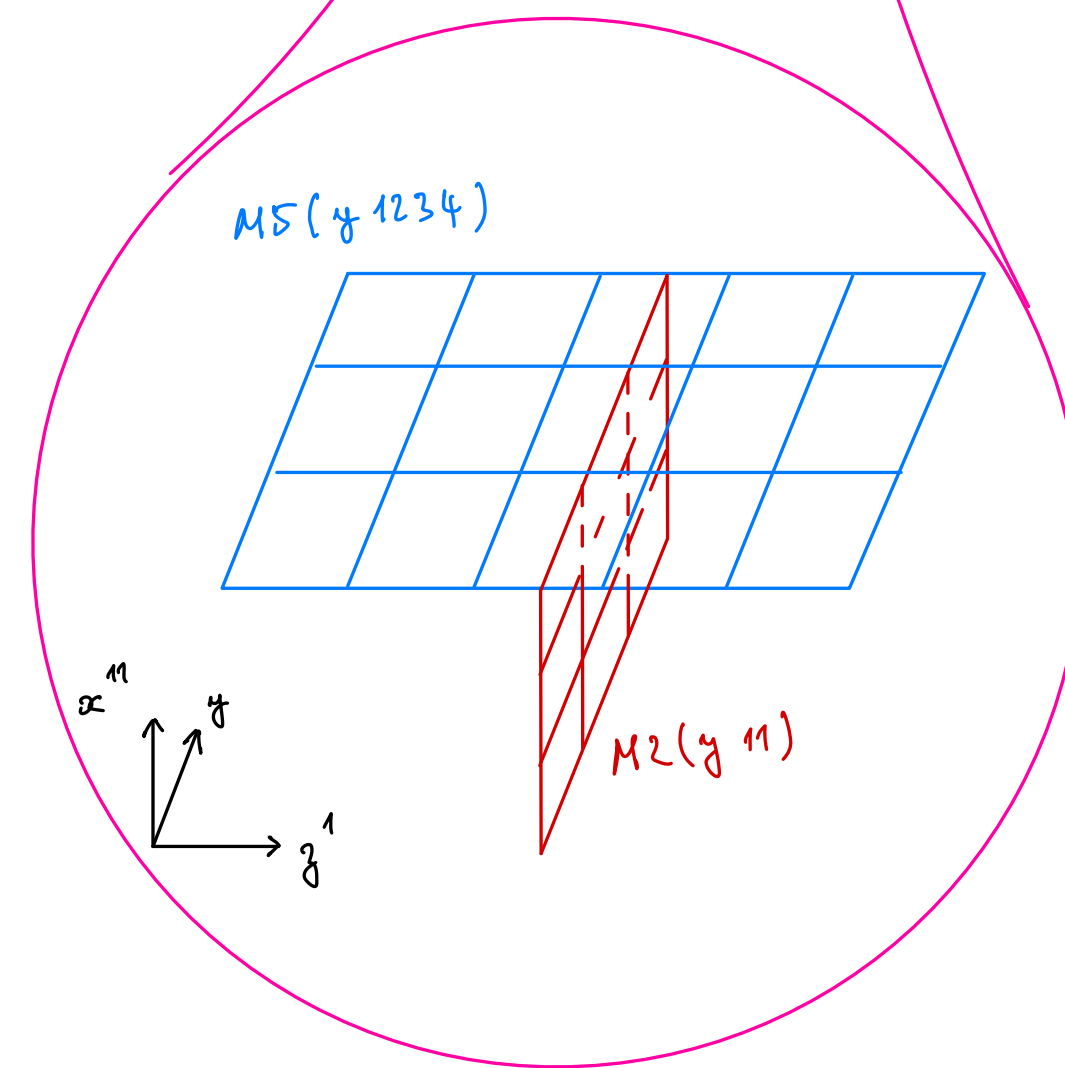
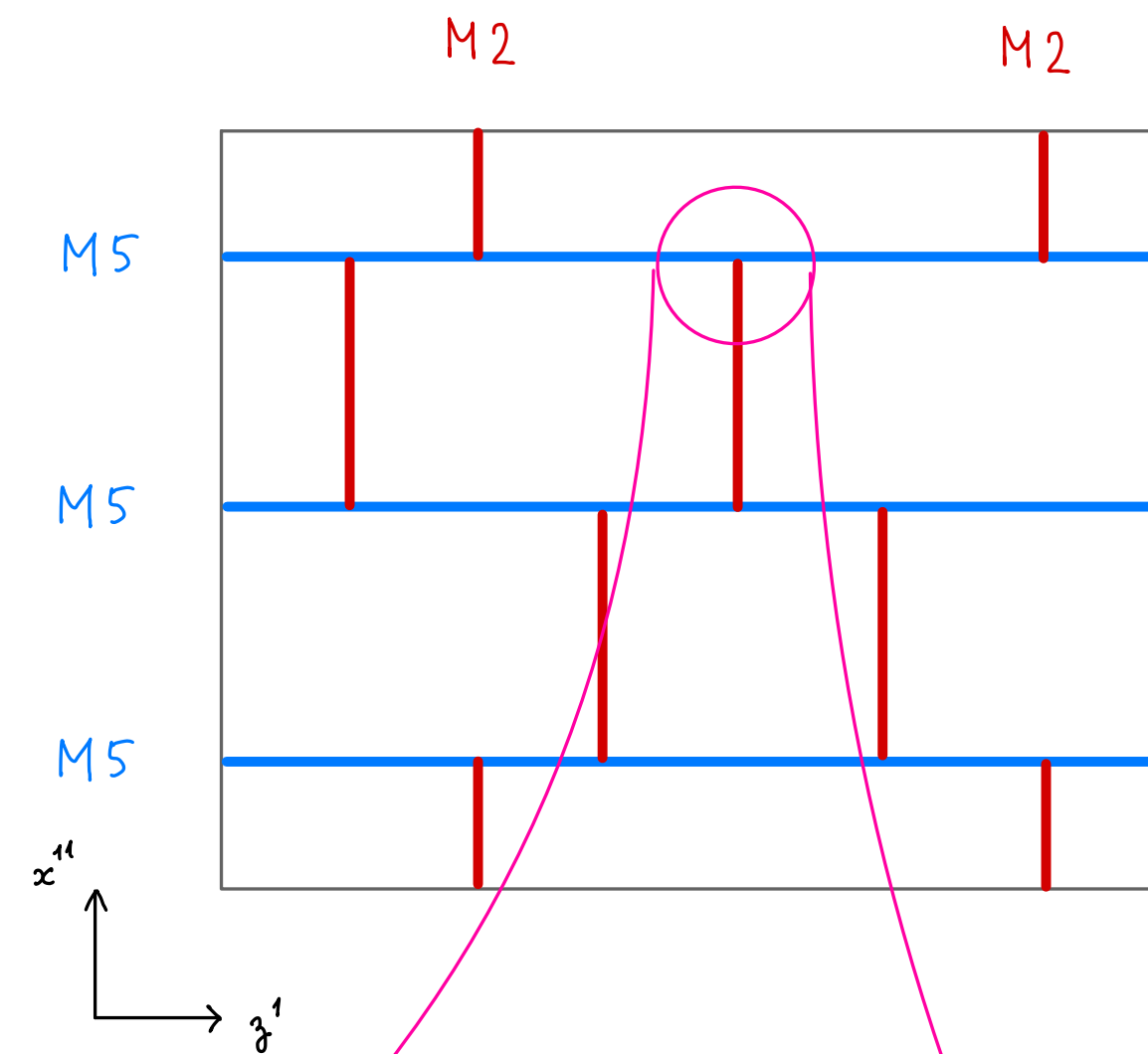
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- ... which is actually multiple layers of multiple tunnels/columns



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 - Local transition \Rightarrow a M5-M2 black-hole microstate will transition into a « **labyrinth** » ...
- ... which is actually multiple layers of multiple tunnels/columns
- \rightarrow « **Multi-storey Greek temple** »



« **M5-M2 furrow** »

2. c.

*Supertube transition of three-charge black-hole
microstates*

Glueing NS5, F1 and P

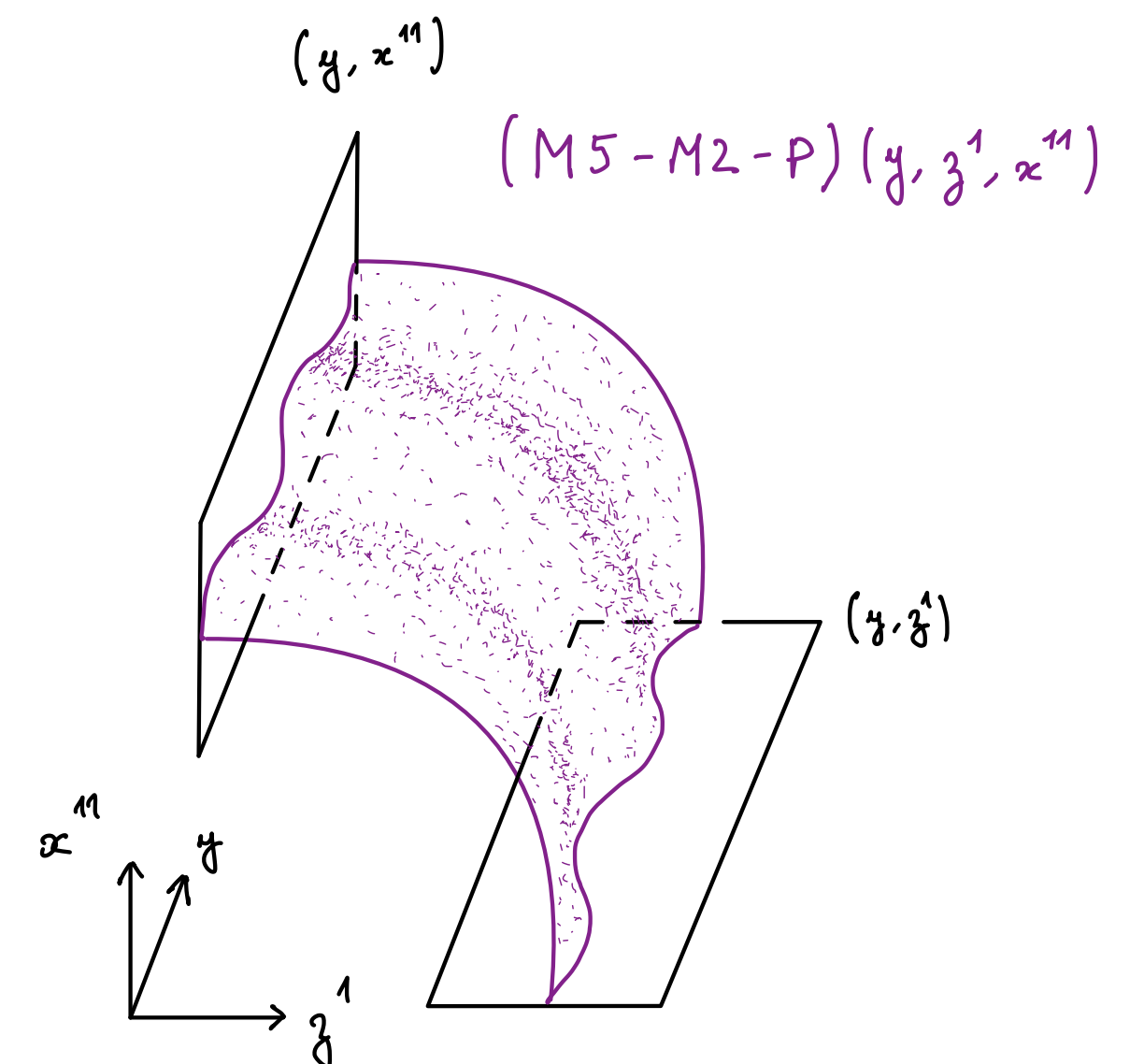
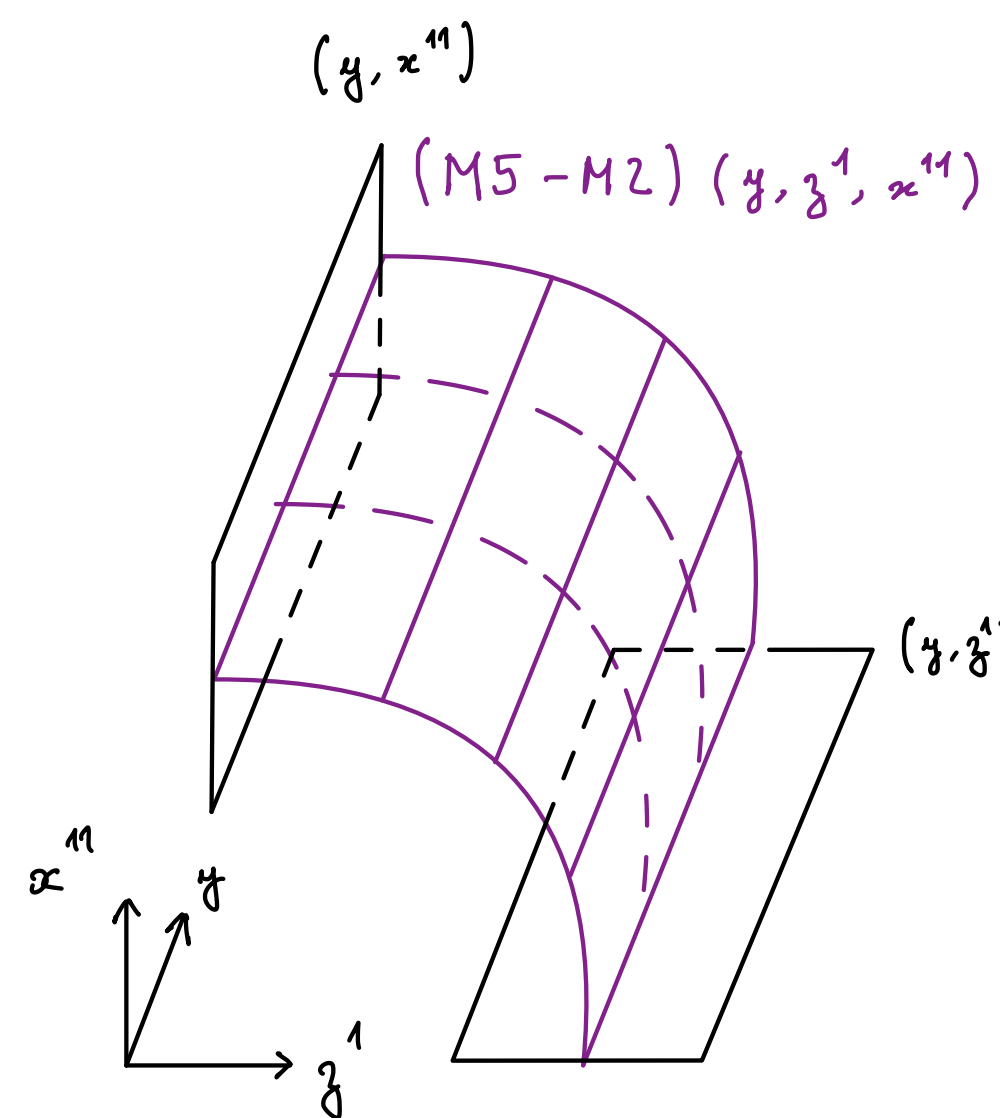
$$\Pi_{\text{NS5-F1-P}} = \frac{1}{2} \left[1 + a^2 P_{\text{NS5}(y1234)}^{\text{IIA}} + b^2 P_{\text{F1}(y)} + c^2 P_{\text{P}(y)} \right. \\ \left. + ab \left(P_{\text{D4}(y234)} - P_{\text{D2}(y1)} \right) + bc \left(P_{\text{P}(1)} - P_{\text{F1}(1)} \right) + ca \left(P_{\text{D4}(1234)} - P_{\text{D0}} \right) \right].$$

- The **M5-M2** furrow carries **momentum** through *ripples* modulated orthogonally to its surface

$$a = \cos \alpha \cos \beta$$

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Glueing NS5, F1 and P

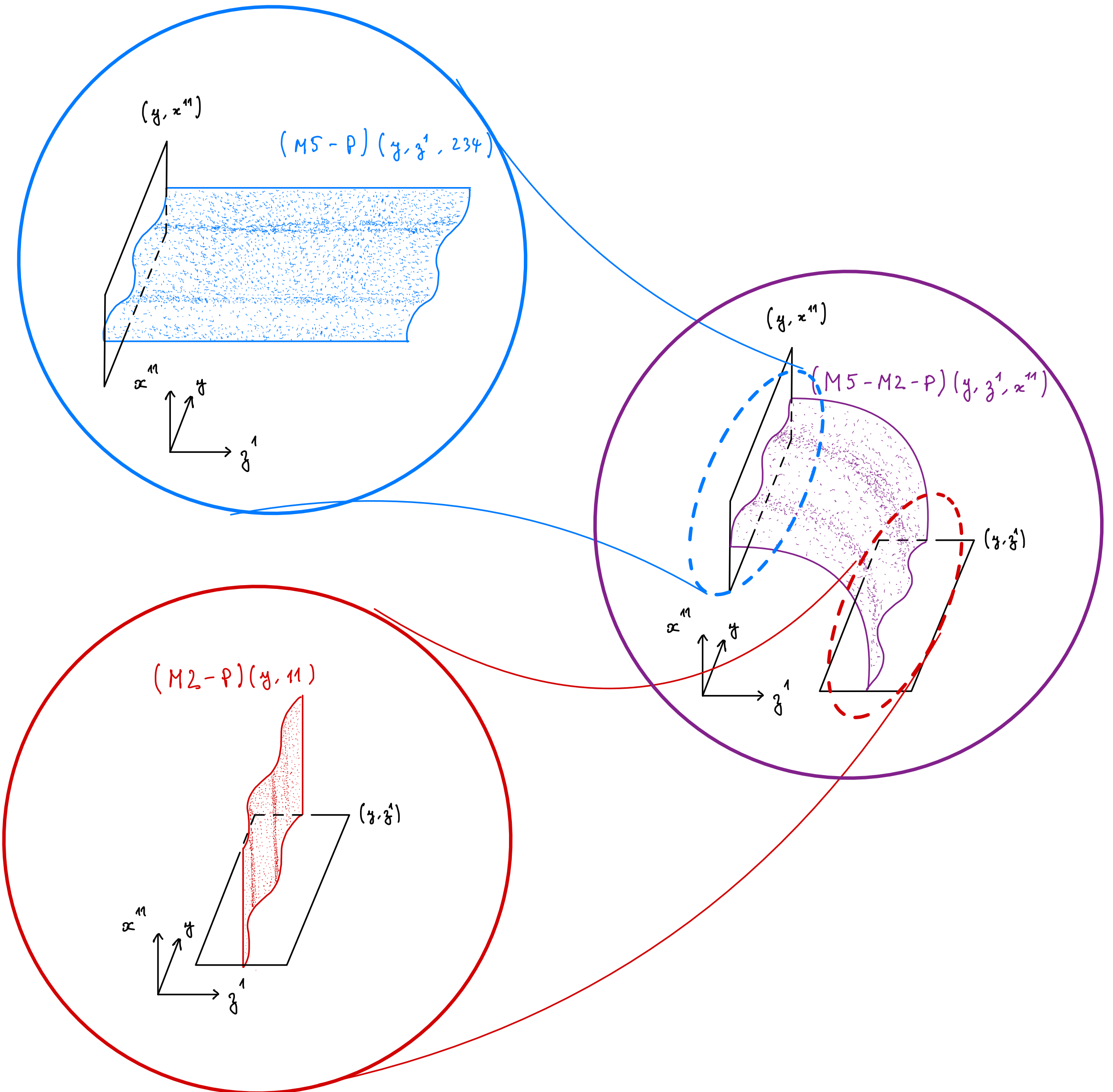
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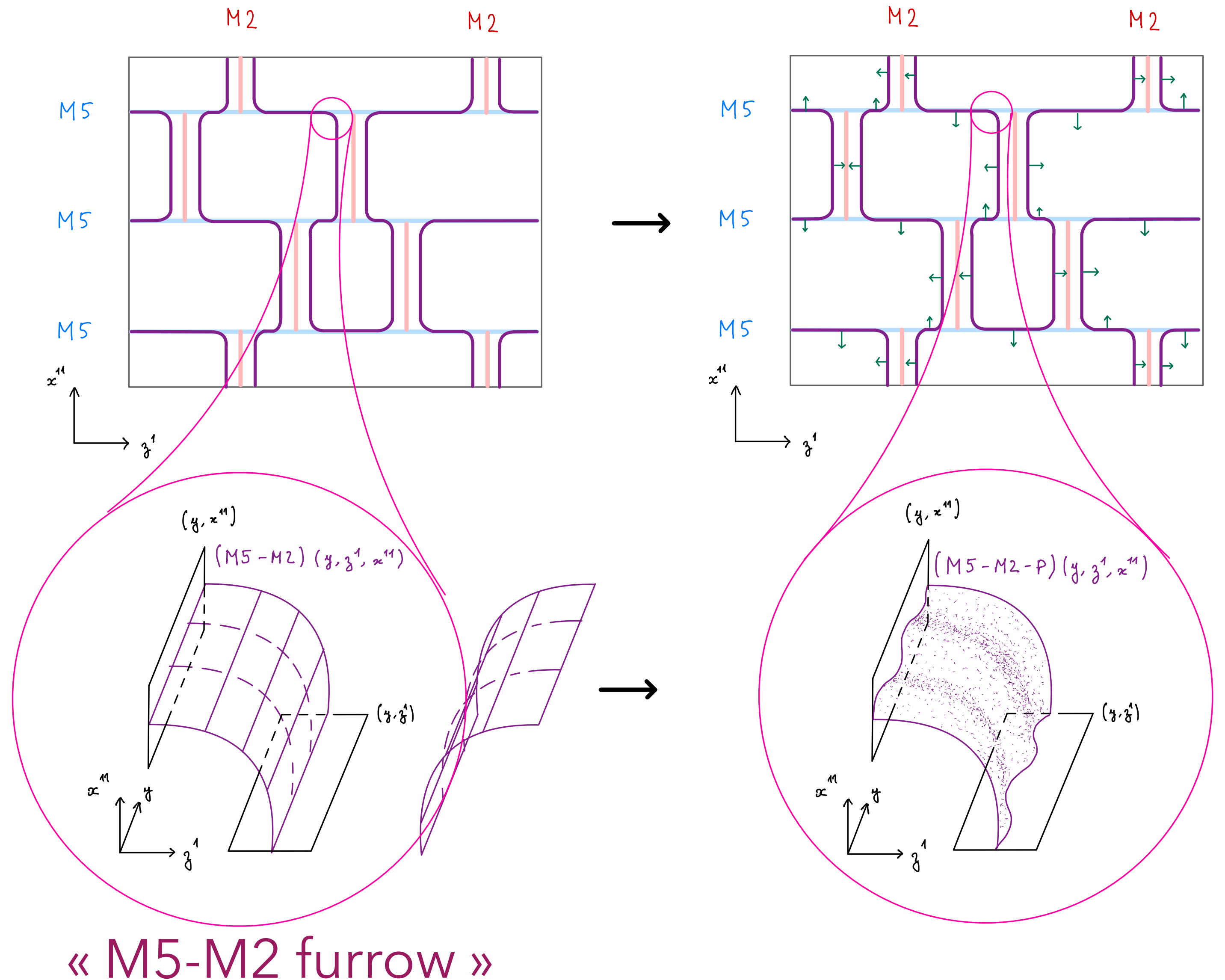
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- β controls the bending angle of the furrow; α controls the angle of ripples orthogonal to the furrow.



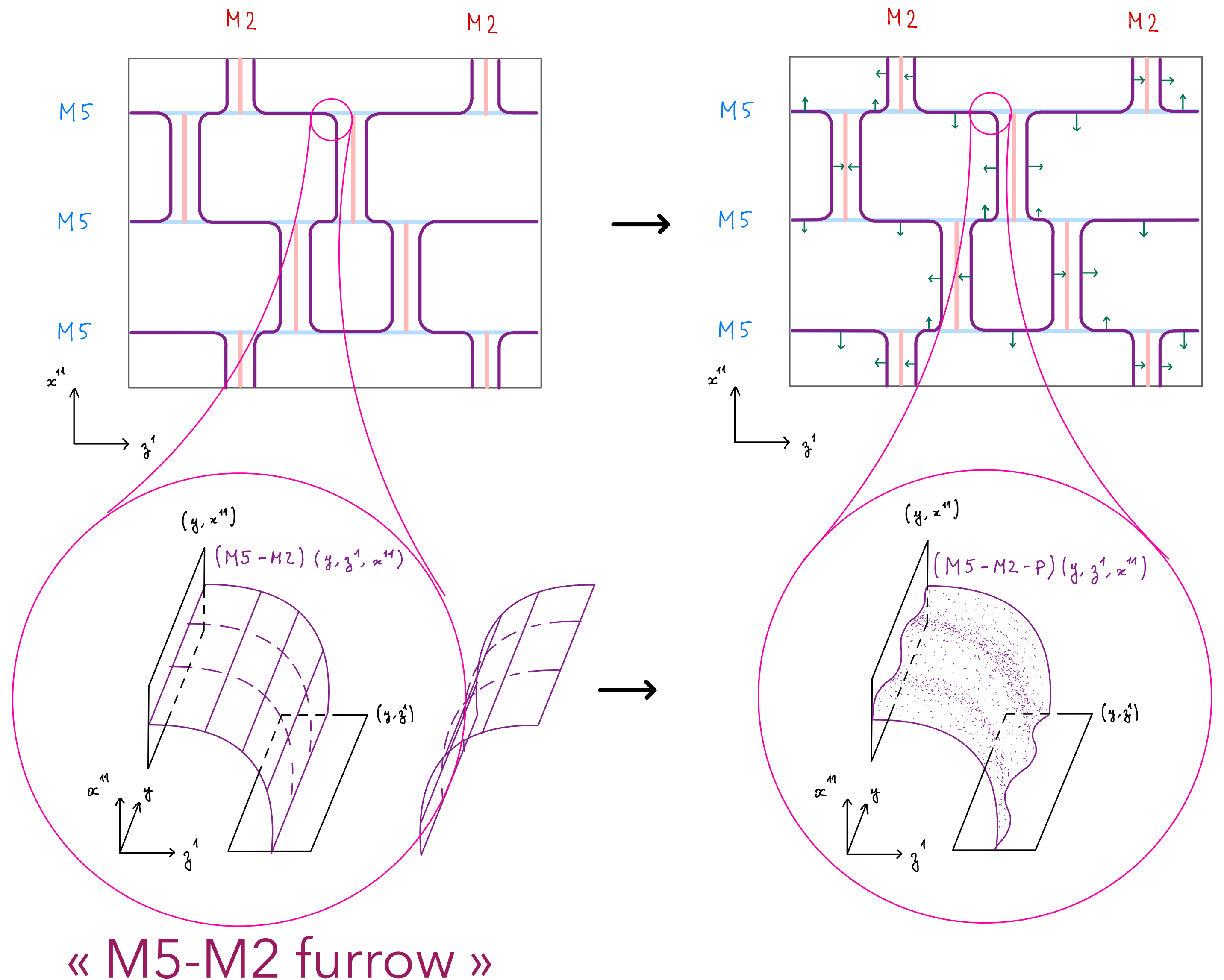
Consequence on a M5-M2-P microstate

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- ⇒ The microstates are ensured to have *exact spherical symmetry*.

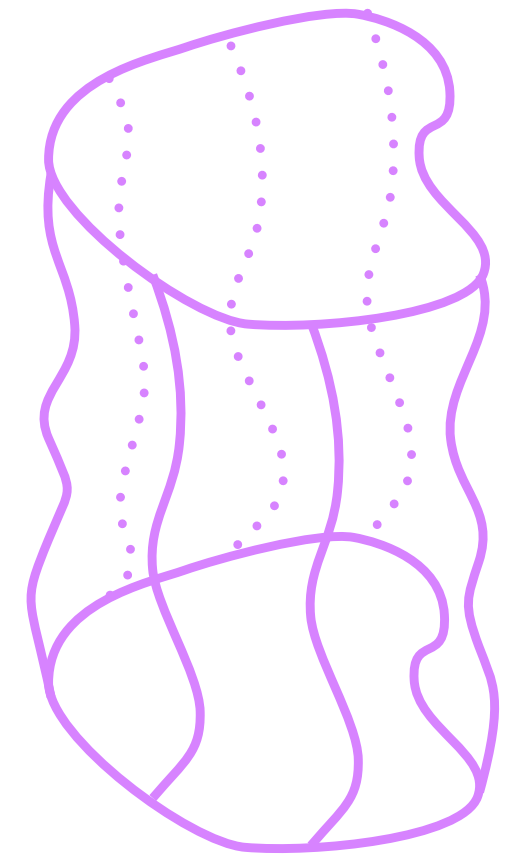


Conclusion

- 1/8-BPS systems have a large moduli space of solutions that have more supersymmetries locally
 - ↑ This is crucial in order to understand the physics of horizons of supersymmetric black-holes

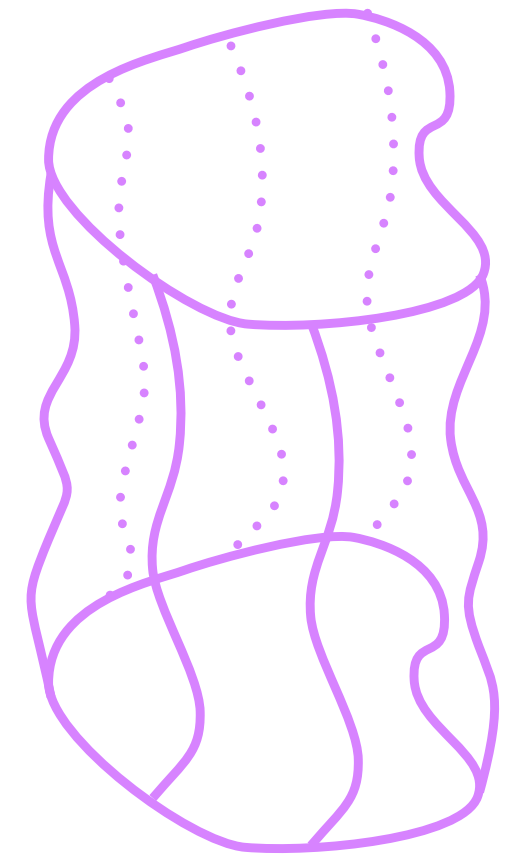
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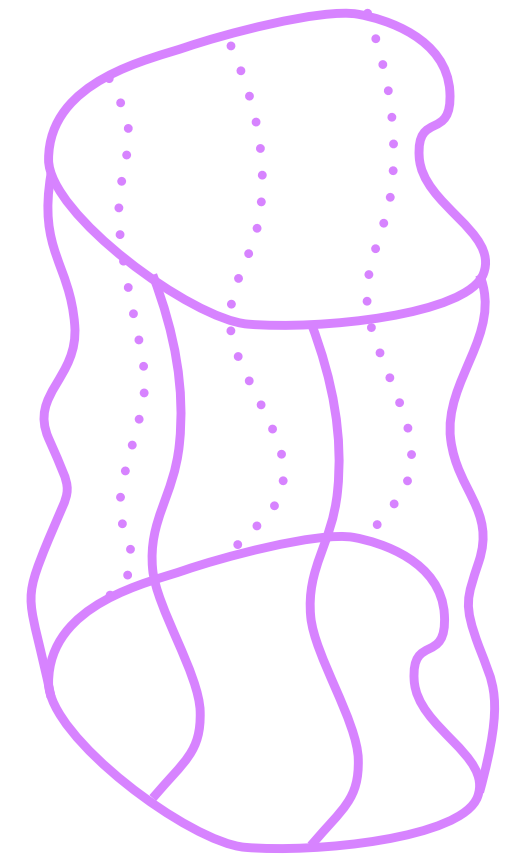
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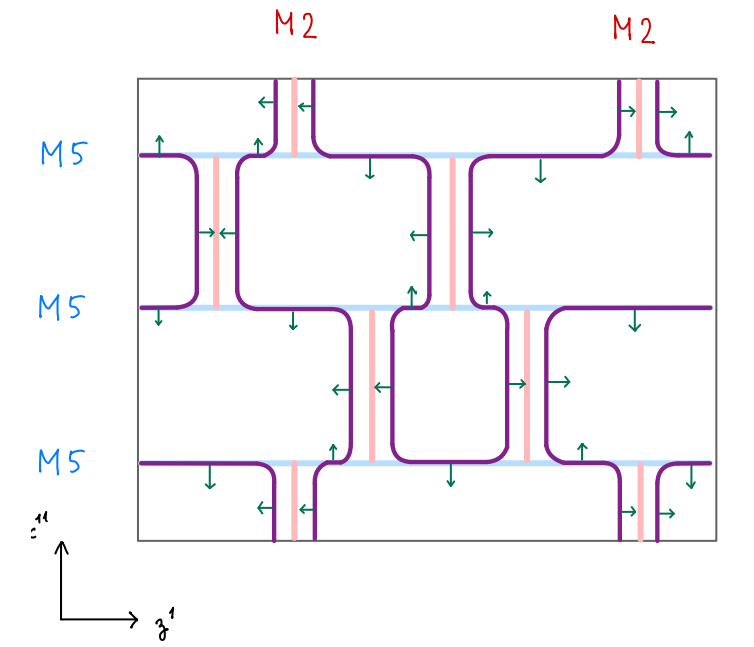
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- New approach: **microstates** can carry momentum by having motion in the *internal dimensions* \Rightarrow exactly spherical symmetry



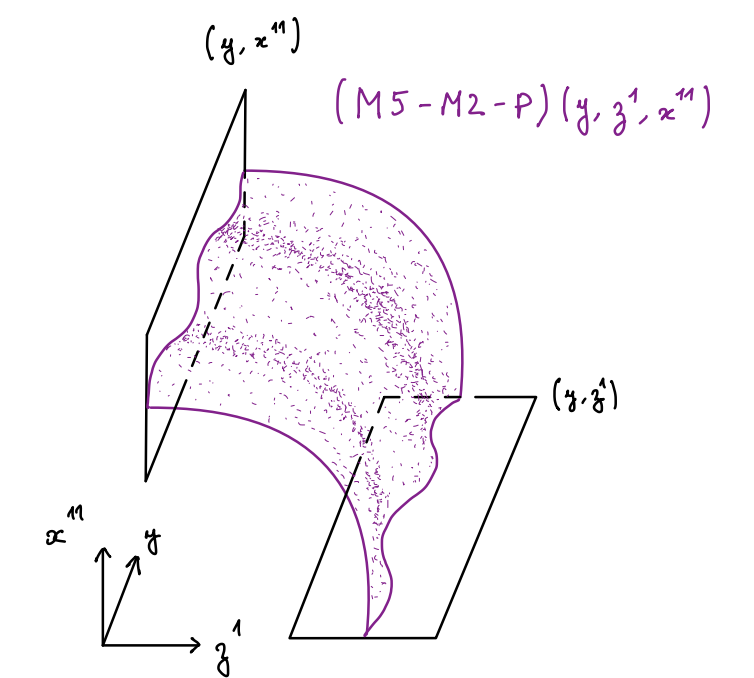
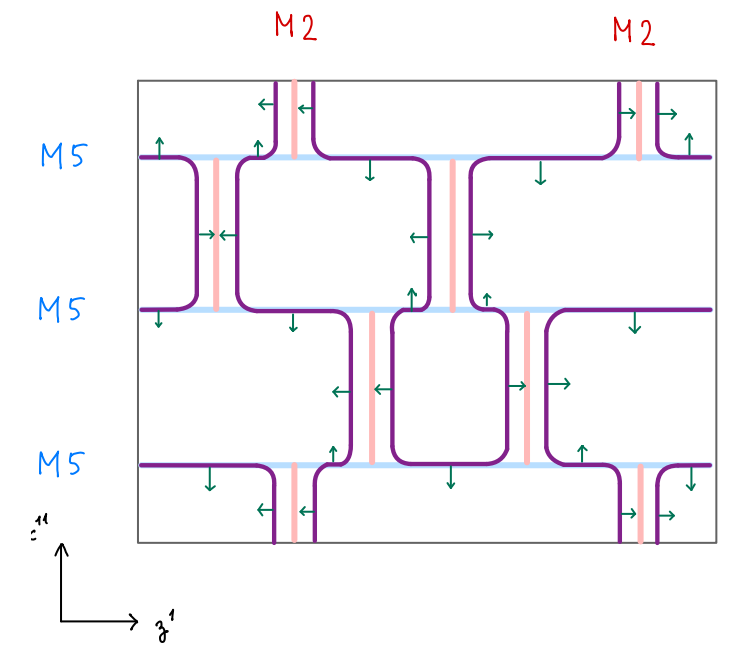
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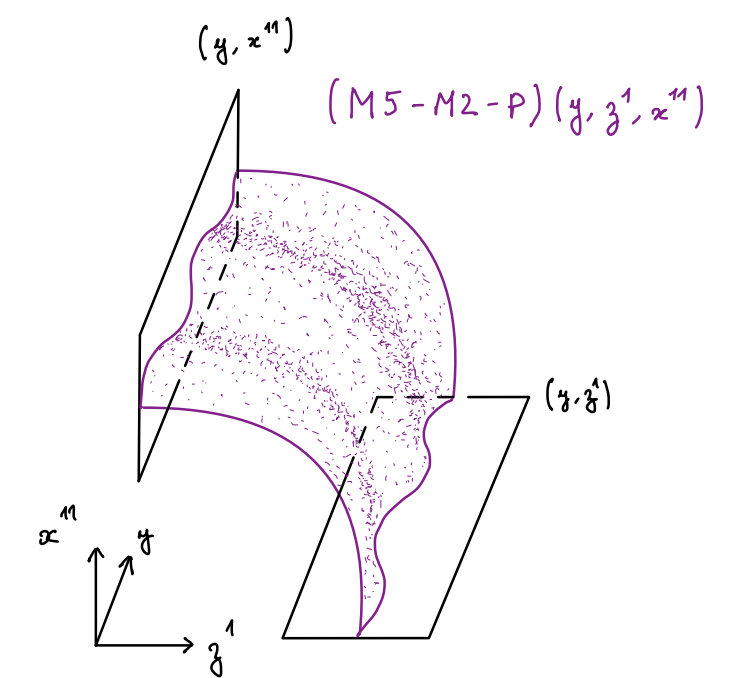
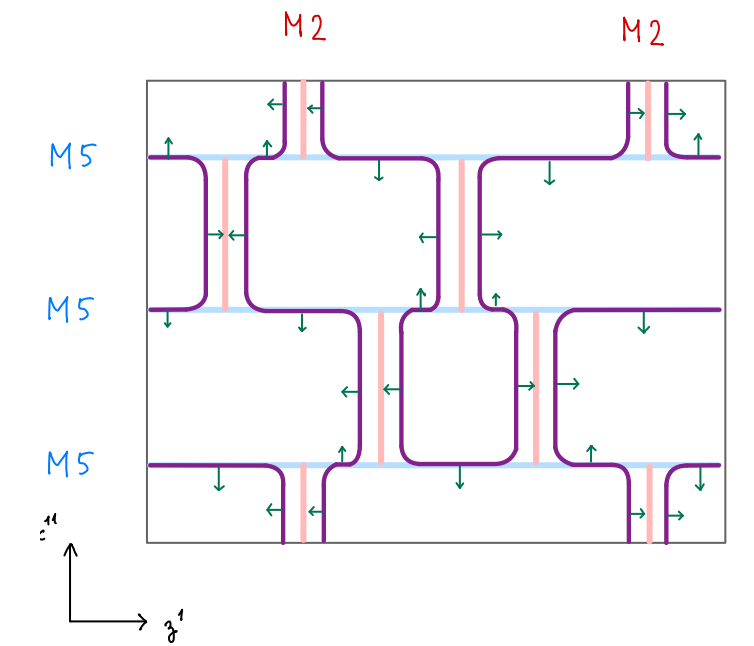
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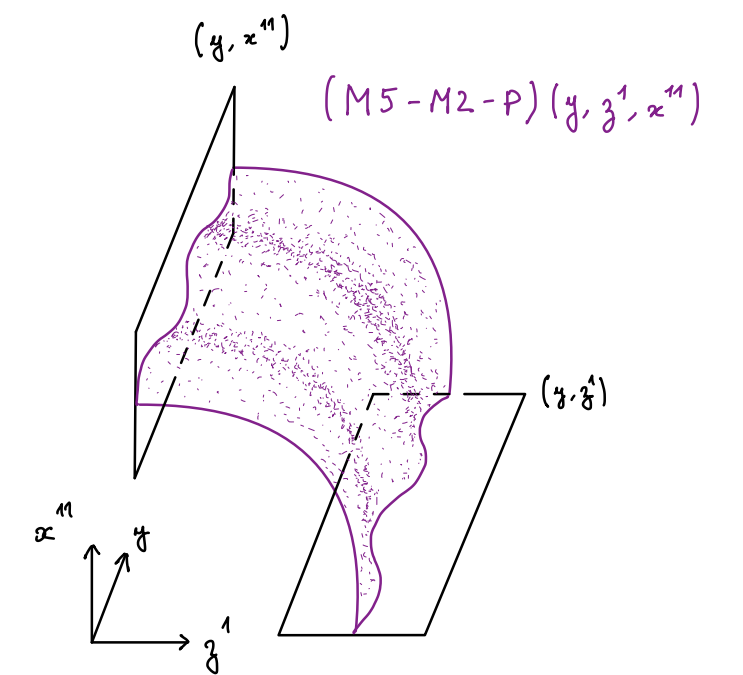
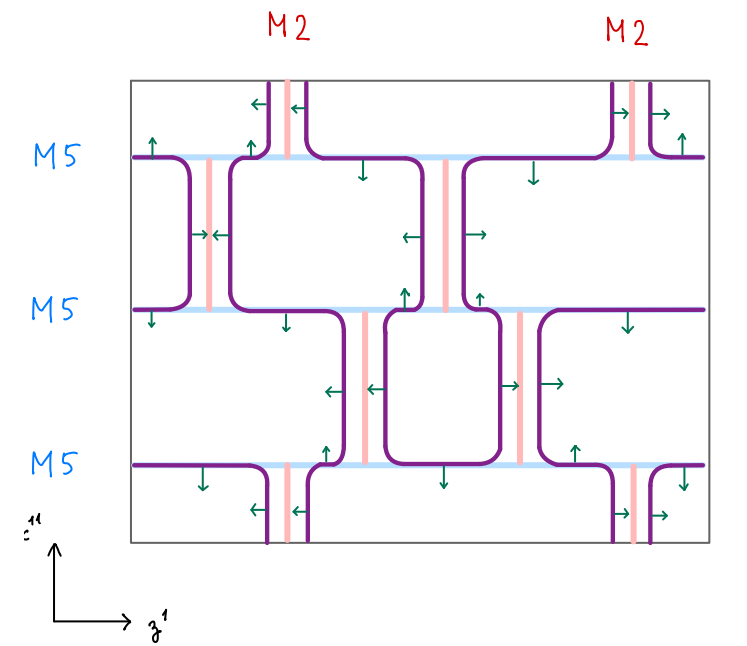
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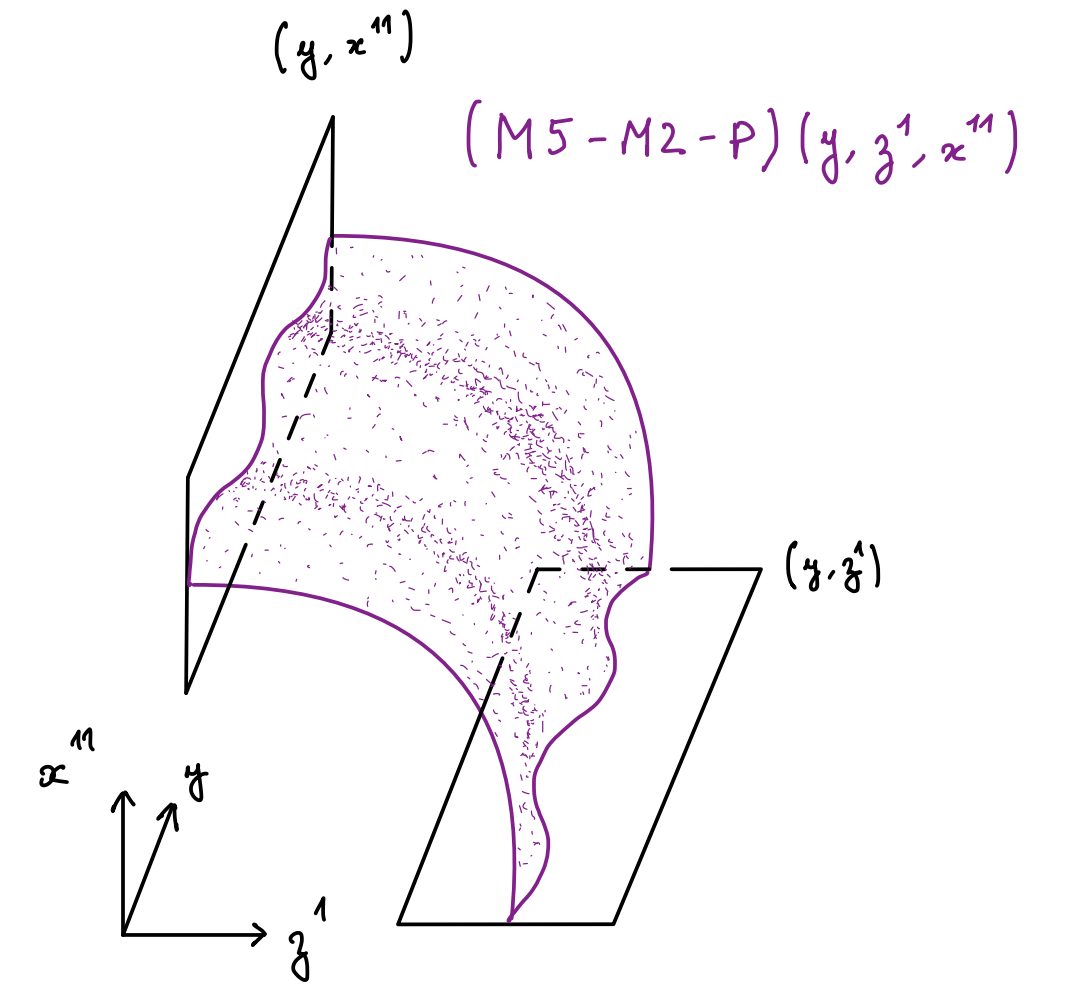
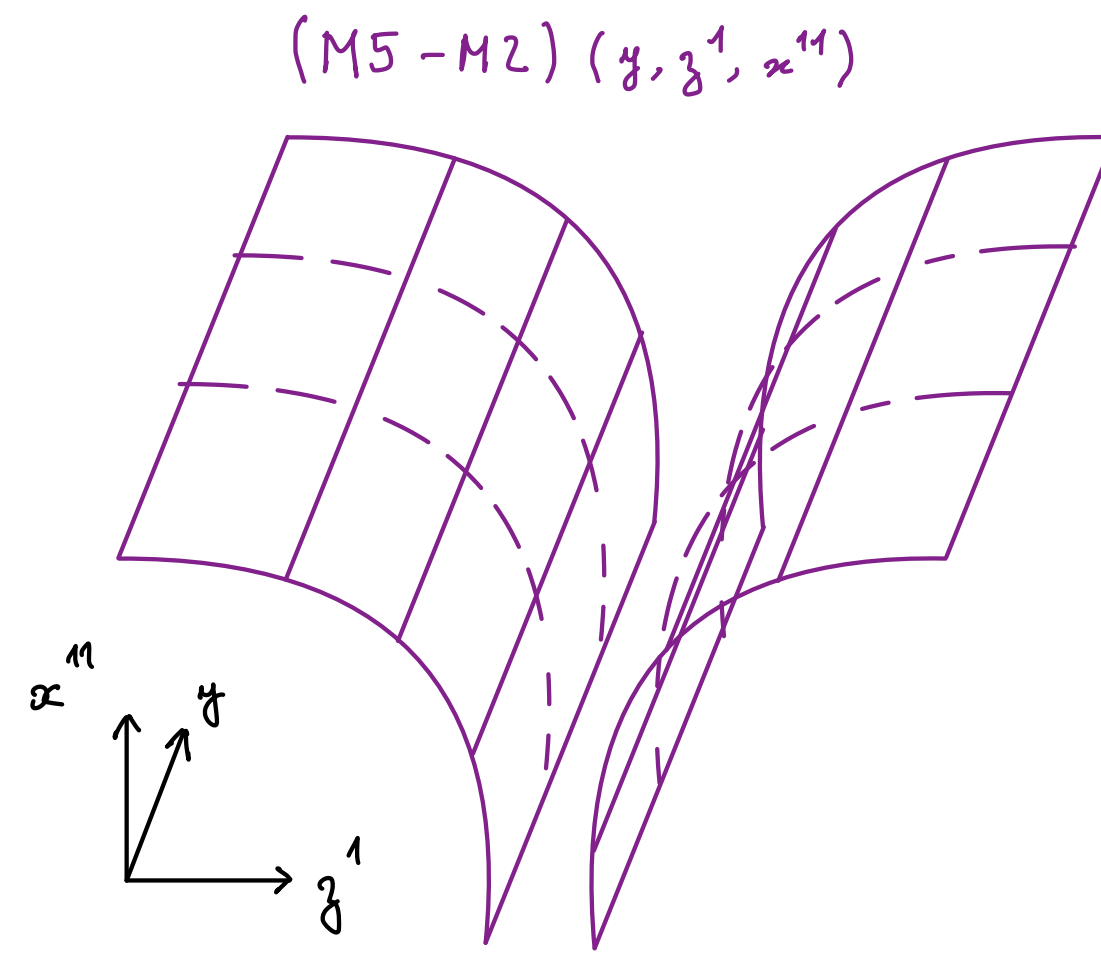
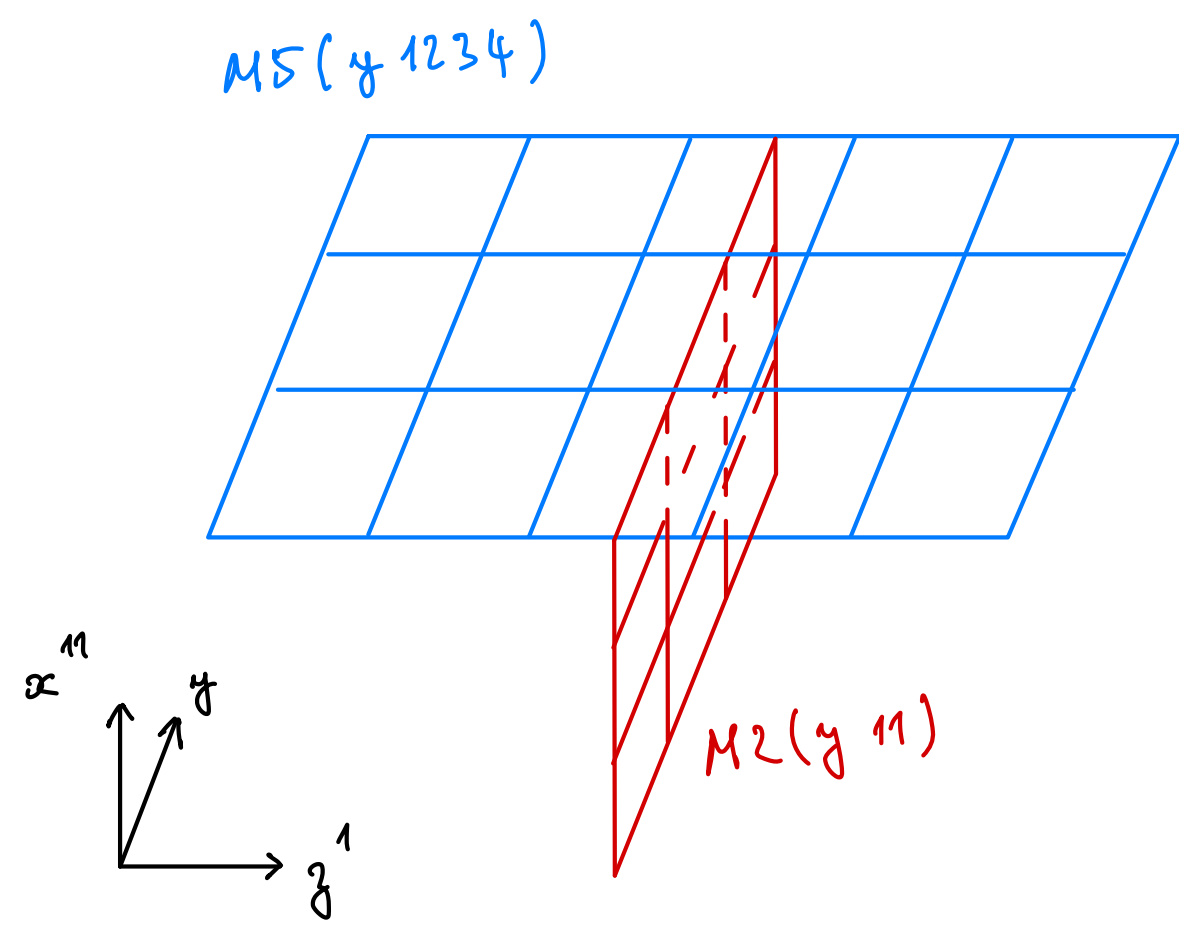
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⇒ support Fuzzball hypothesis for M-theory black-hole microstates
- We have already begun to build the fully-backreacted supergravity solution.





Thank
you

for
your

attention
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