

NATIONAL SCIENCE CENTRE
POLAND

**FACULTY OF
PHYSICS**
UNIVERSITY
OF WARSAW

Muon $g-2$ in SUSY with and without stable neutralinos

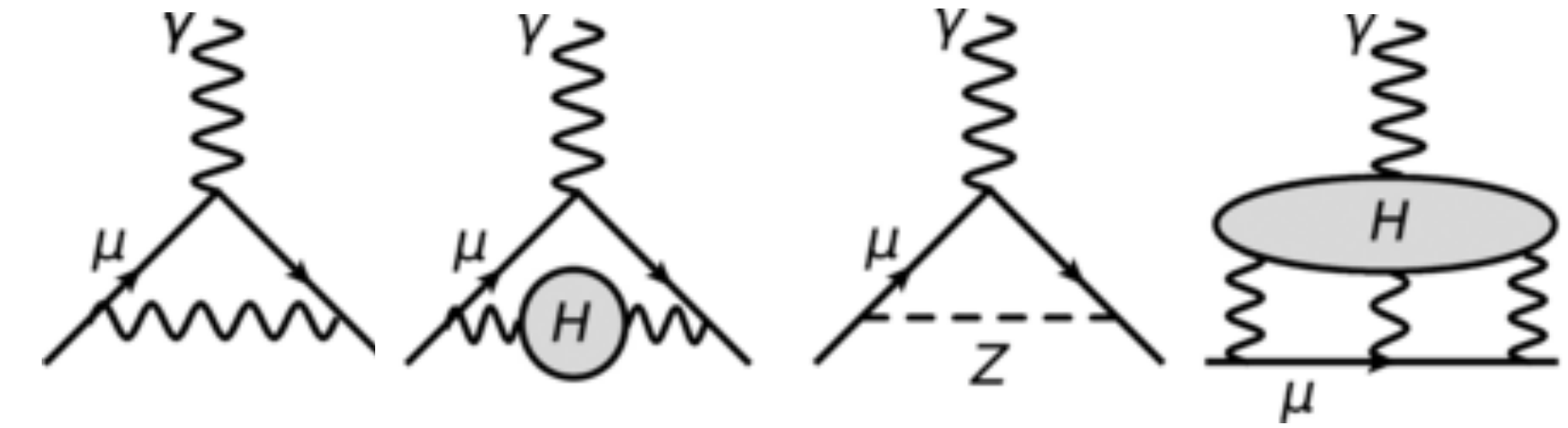
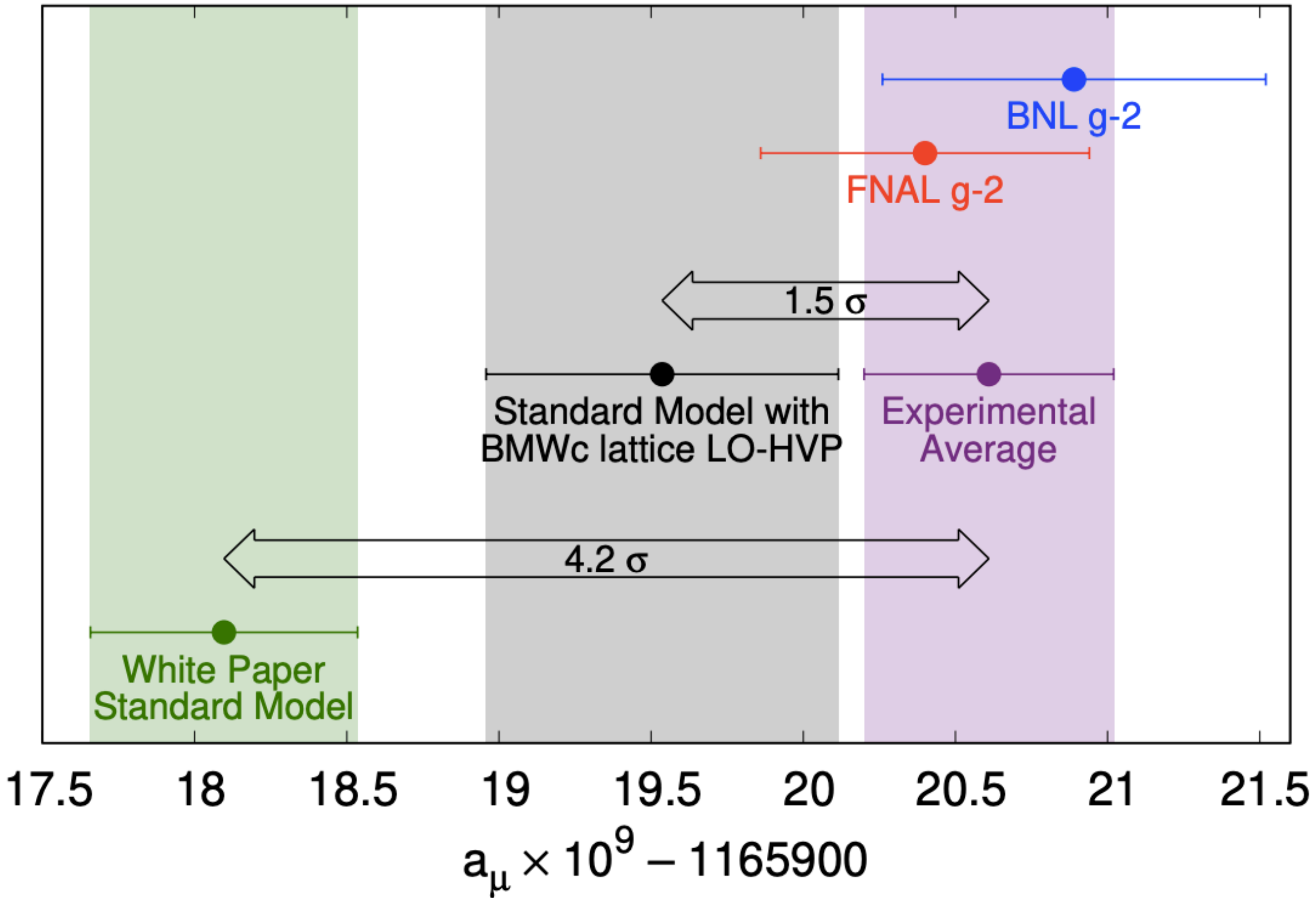
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Based on JHEP 08 (2022) 124; [https://doi.org/10.1007/JHEP08\(2022\)124](https://doi.org/10.1007/JHEP08(2022)124)

R. Masełek Corfu Summer Institute 2022/09/05

$(g-2)_\mu$ anomaly



QED HVP EW HLbL

a_μ^{theo}	=	0.00	1165	91	810	(43)
a_μ^{exp}	=	0.00	1165	92	061	(41)

↑
statistical error dominant

$$a_\mu^{\text{exp}} - a_\mu^{\text{theo}} \simeq (25 \pm 6) \times 10^{-10} \simeq \mathcal{O} \left(\Delta a_\mu^{\text{SM,EW}} \right) \simeq \Delta a_\mu^{\text{BSM}} ?$$

[Muon g-2, Phys. Rev. Lett. 126, 141801]

[T. Aoyama et al., , Phys. Rep. 887, 1 (2020)]

[L. Lellouch, Moriond 2022 EW] 

Motivation

Many BSM scenarios can explain the $(g-2)_\mu$ anomaly

Leptoquarks, Z' , 2HDM, axion, ...

Supersymmetry is particularly motivated, because it offers:

Coupling Unification, Radiative EWSB, Baryogenesis, DM, ...

However, simple SUSY scenarios are heavily constrained by existing experimental results...

Which SUSY scenarios are phenomenologically viable?

Can phenomenologically
viable SUSY explain $(g-2)_\mu$?

MSSM

stable $\tilde{\chi}_1^0$

Can phenomenologically
viable SUSY explain $(g-2)_\mu$?

DM constraints

MSSM unstable $\tilde{\chi}_1^0$ stable $\tilde{\chi}_1^0$

Can phenomenologically
viable SUSY explain $(g-2)_\mu$?

RPV DM constraints GMSB

Muon g-2

ATLAS/CMS

MSSM unstable $\tilde{\chi}_1^0$ stable $\tilde{\chi}_1^0$

Can phenomenologically
viable SUSY explain $(g-2)_\mu$?

RPV DM constraints GMSB

XENON1T/PANDA/LZ/ARGO ...

(g-2)_μ viable parameters

Muon g-2

ATLAS/CMS

MSSM unstable $\tilde{\chi}_1^0$ stable $\tilde{\chi}_1^0$

Can phenomenologically viable SUSY explain (g-2)_μ?

RPV DM constraints GMSB

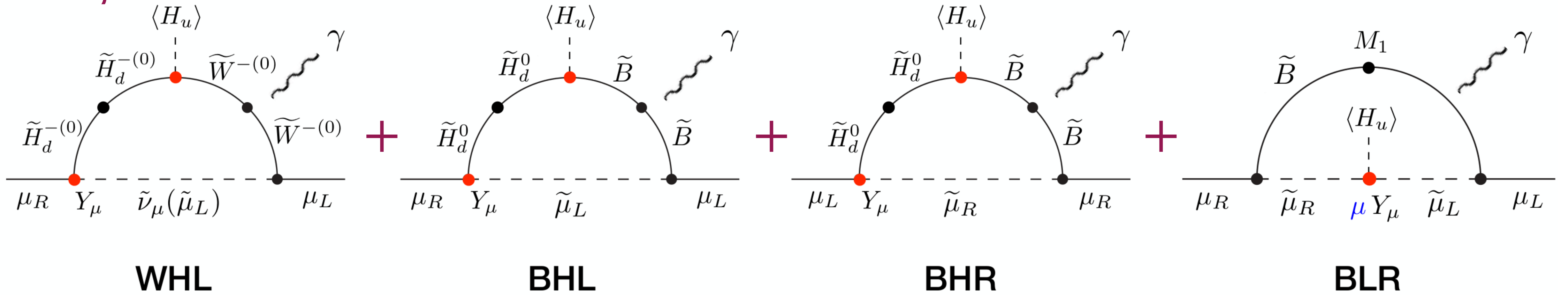
XENON1T/PANDA/LZ/ARGO ...

2D parameter planes

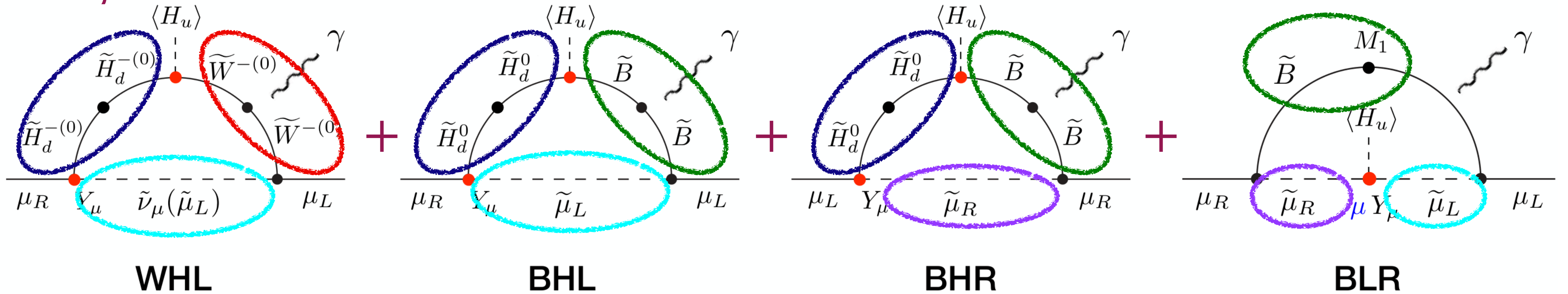


$(g-2)_\mu$ in SUSY

$$\Delta a_{\mu}^{\text{SUSY}} \simeq$$



$$\Delta a_\mu^{\text{SUSY}} \simeq$$



M_1 : Bino mass

$m_{\tilde{l}_R}$: right-handed slepton mass

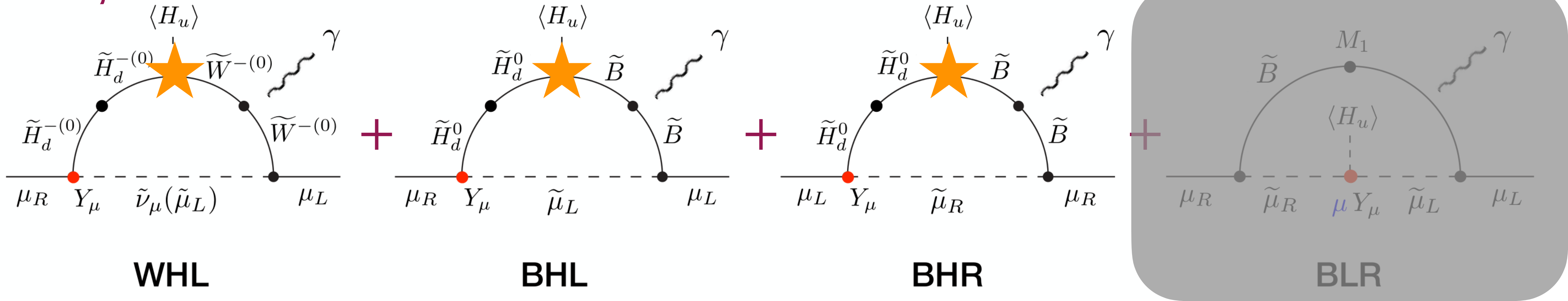
M_2 : Wino mass

$m_{\tilde{l}_L}$: left-handed slepton mass

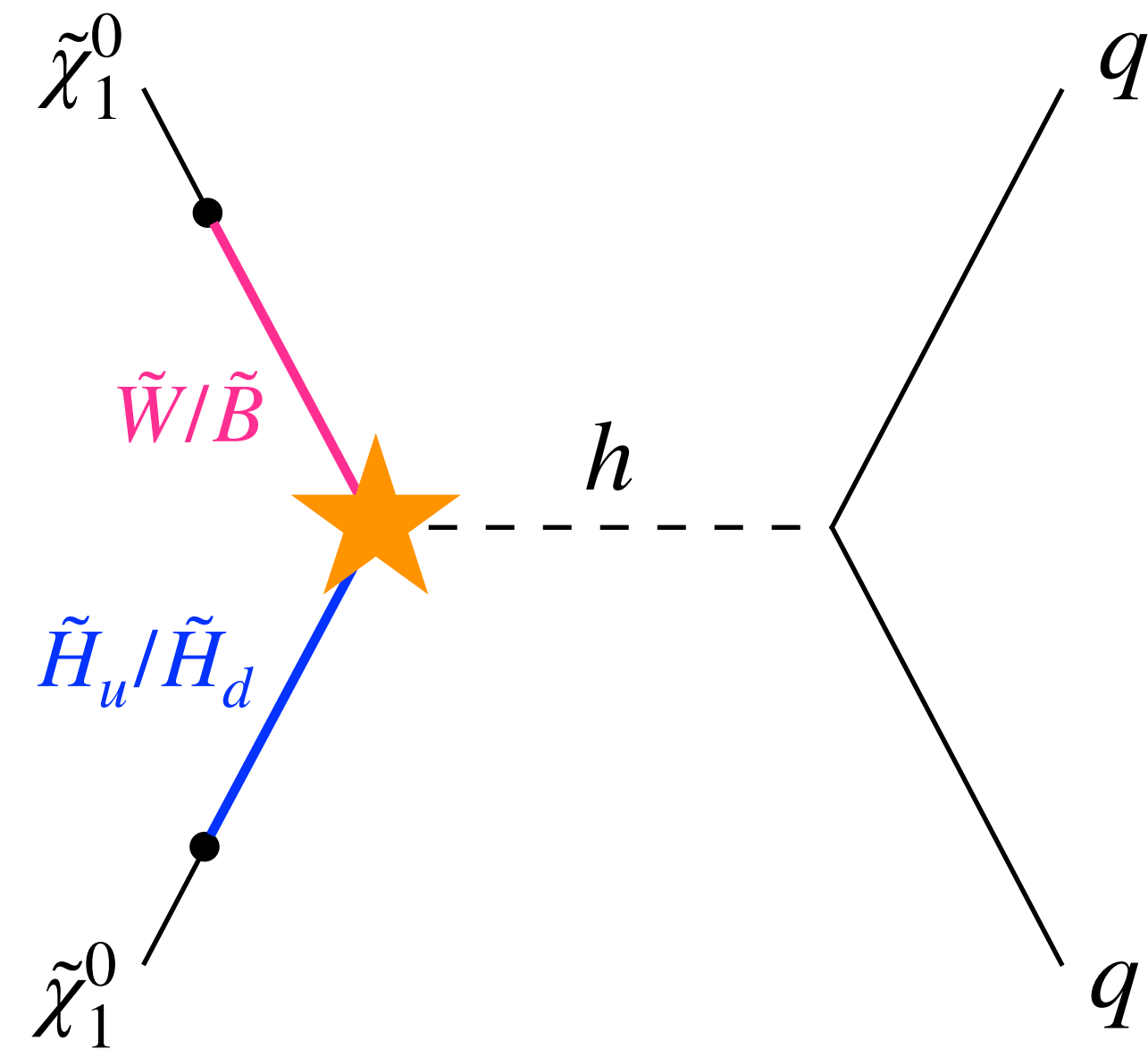
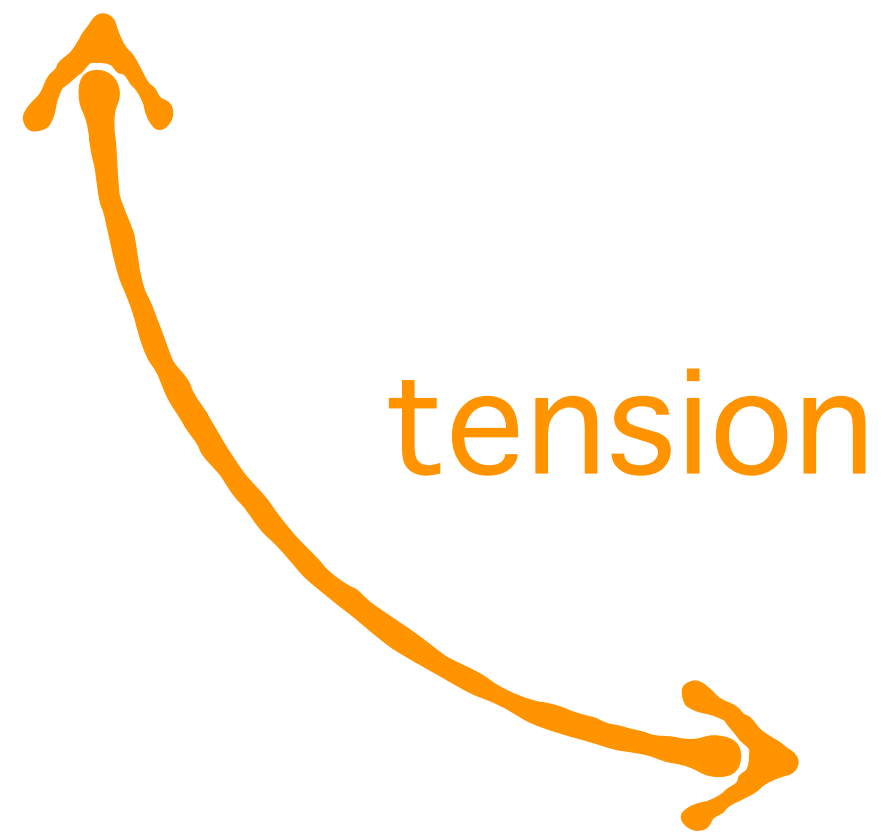
μ : Higgsino mass

$$\tan \beta \equiv \langle H_u \rangle / \langle H_d \rangle$$

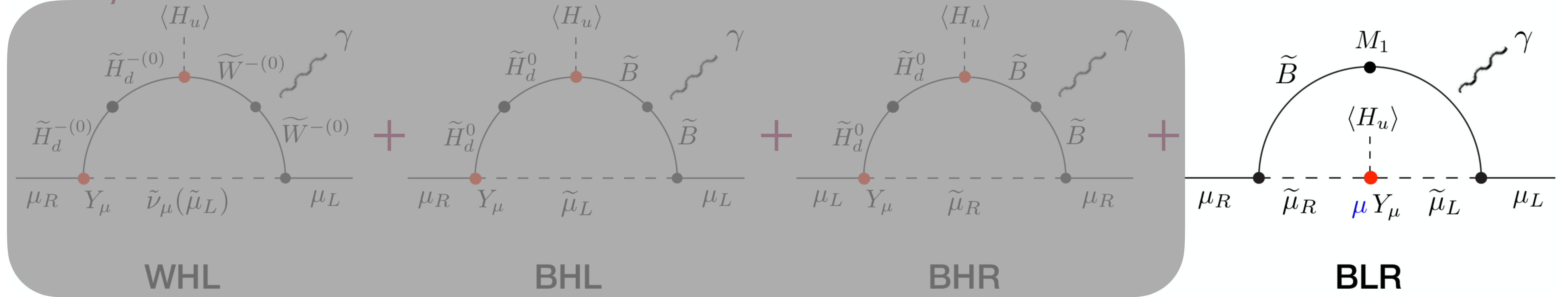
$$\Delta a_\mu^{\text{SUSY}} \simeq$$



Large gaugino-Higgsino mixing leads to a large cross-section for **DM Direct Detection**



$$\Delta a_\mu^{\text{SUSY}} \simeq$$



Bino has very small annihilation cross-section

⊗ overproduction of Bino-like neutralinos in the early Universe: $\Omega_{\tilde{\chi}_1^0} < \Omega_{\text{DM}}$

⊗ slepton-coannihilation needed: $m_{\tilde{l}} \sim m_{\tilde{B}}$

Large off diagonal term in stau mass matrix:

⊗ charge breaking vacuum: $m_{\tilde{\tau}_1}^2 > 0$

⊗ LEP bound: $m_{\tilde{\tau}_1} > 81.9 \text{ GeV}$

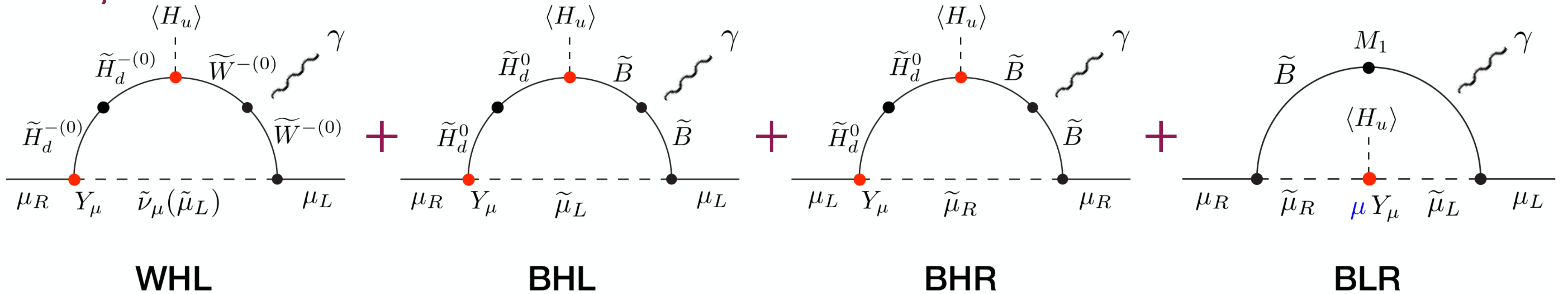
⊗ stau LSP: $m_{\tilde{\tau}_1} > m_{\tilde{\chi}_1^0}$

⊗ vacuum (meta-)stability

$$M_{\tilde{\tau}}^2 \sim \begin{pmatrix} m_{\tilde{\tau}_R}^2 & Y_\tau \mu \langle H_u \rangle \\ Y_\tau \mu \langle H_u \rangle & m_{\tilde{\tau}_L}^2 \end{pmatrix}$$



$$\Delta a_\mu^{\text{SUSY}} \simeq$$



$(g-2)_\mu$ in MSSM has a tension with:

- ⊗ DM Direct Detection
- ⊗ (Bino-like) DM overproduction
- ⊗ lepton + large ETmiss @ LHC
- ⊗ Vacuum stability (for BLR)



consequence of **stable neutralino**

What changes if neutralino is unstable?

R-parity violation scenario

$$W_{\text{RPV}} = \lambda''_{ijk} U_i^c D_j^c D_k^c + \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \kappa_i L_i H_u$$

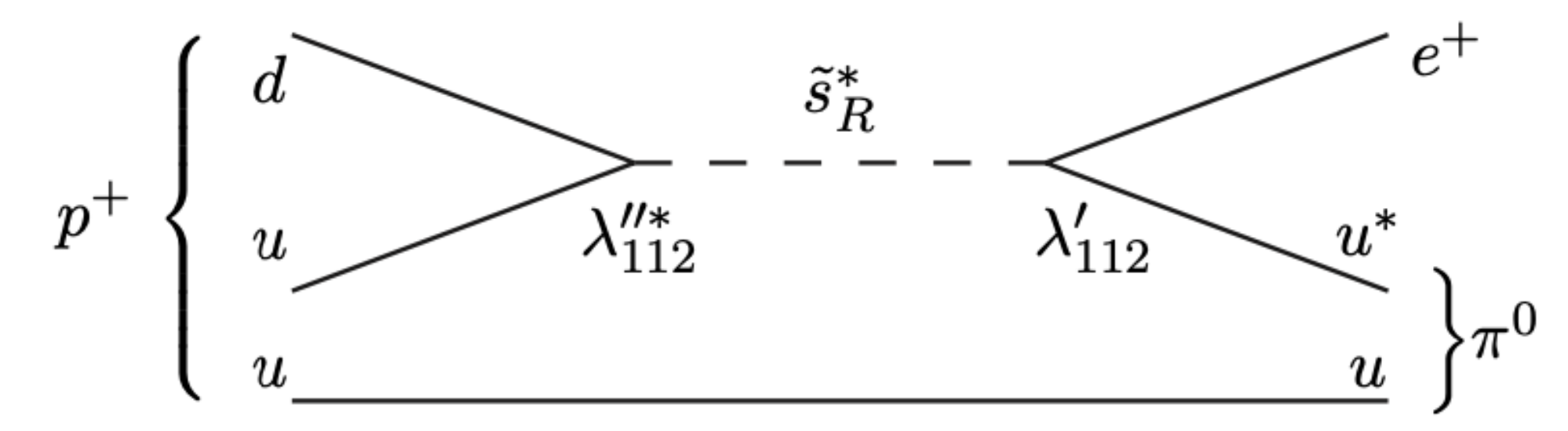
B L L L

⊗ Simultaneous violation of both **B** and **L** leads to a rapid proton decay

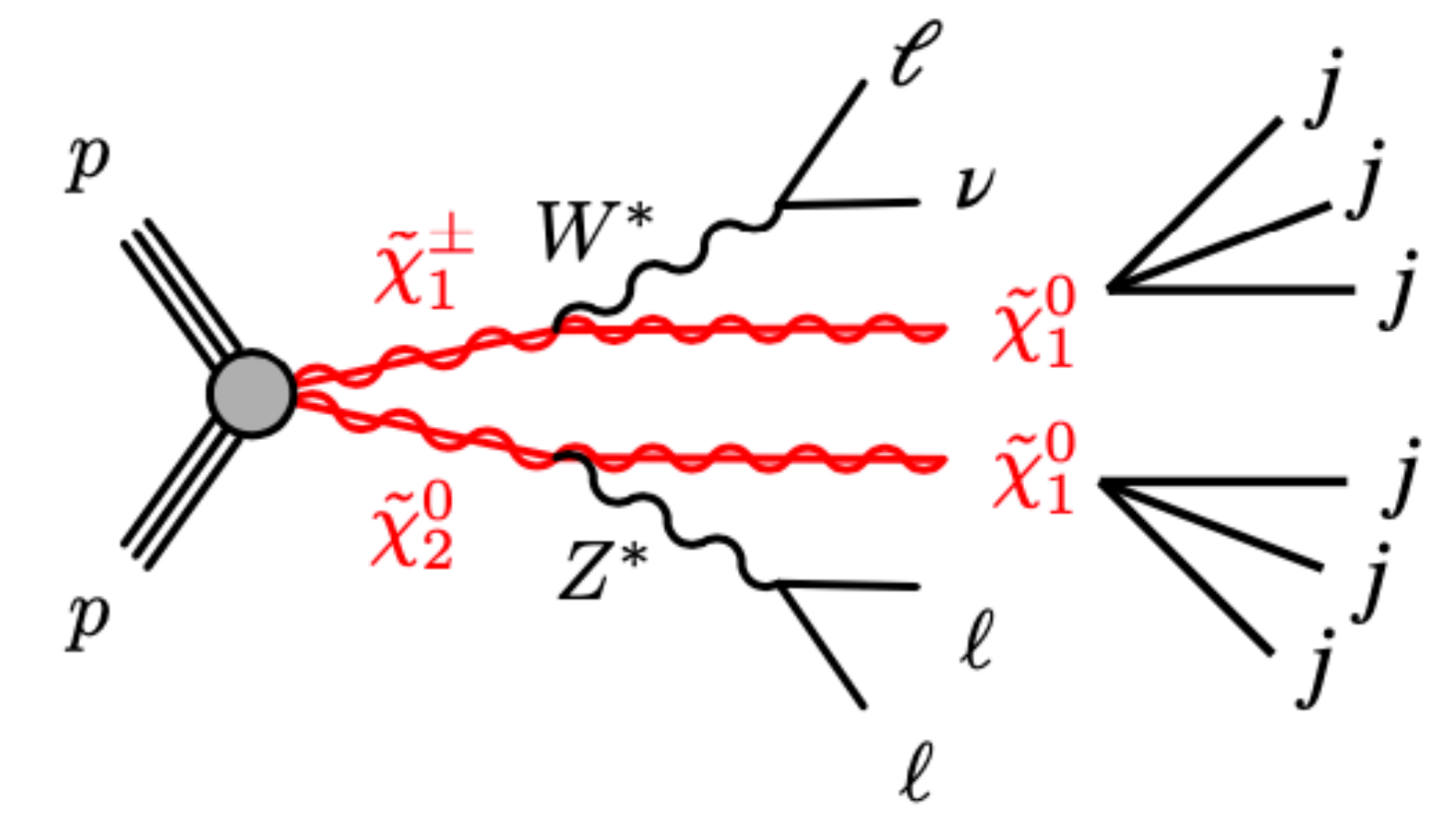
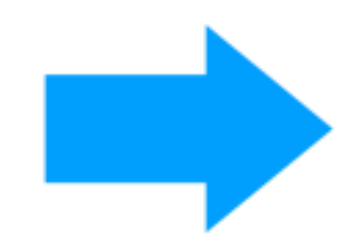
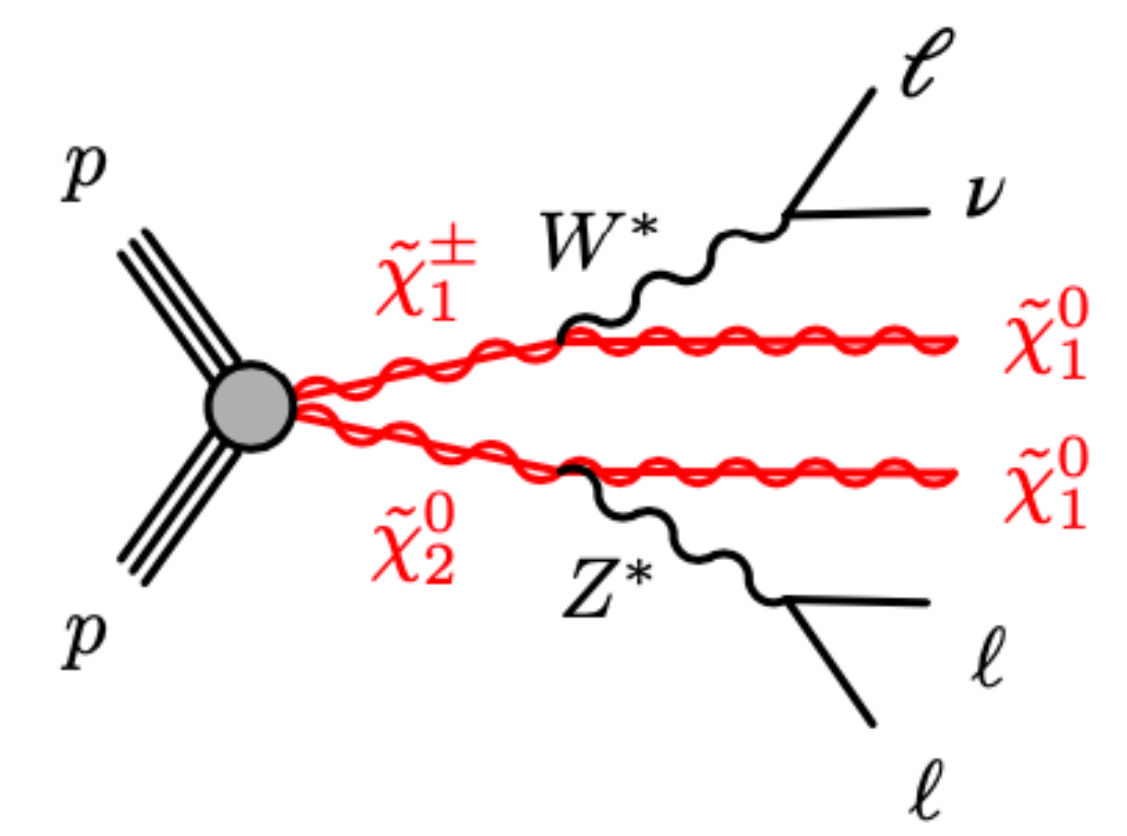
⊗ We introduce only UDD operator with $\lambda''_{112} \neq 0$

⊗ $(g-2)_\mu$ doesn't change wrt. MSSM

⊗ Neutralino LSP decays to 3 (anti)quarks



neutralino LSP



RPV (UDD-type)

No missing energy, but multi-jet

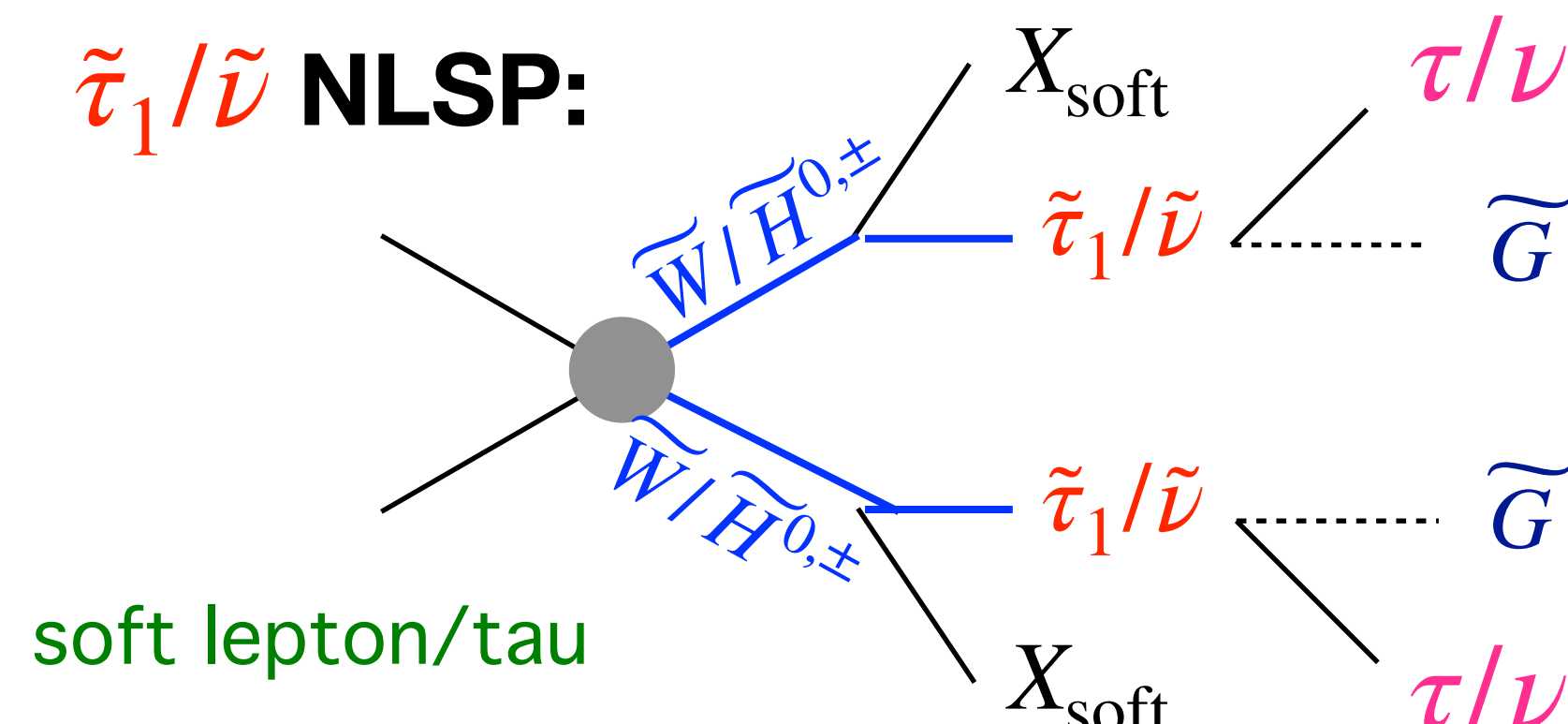
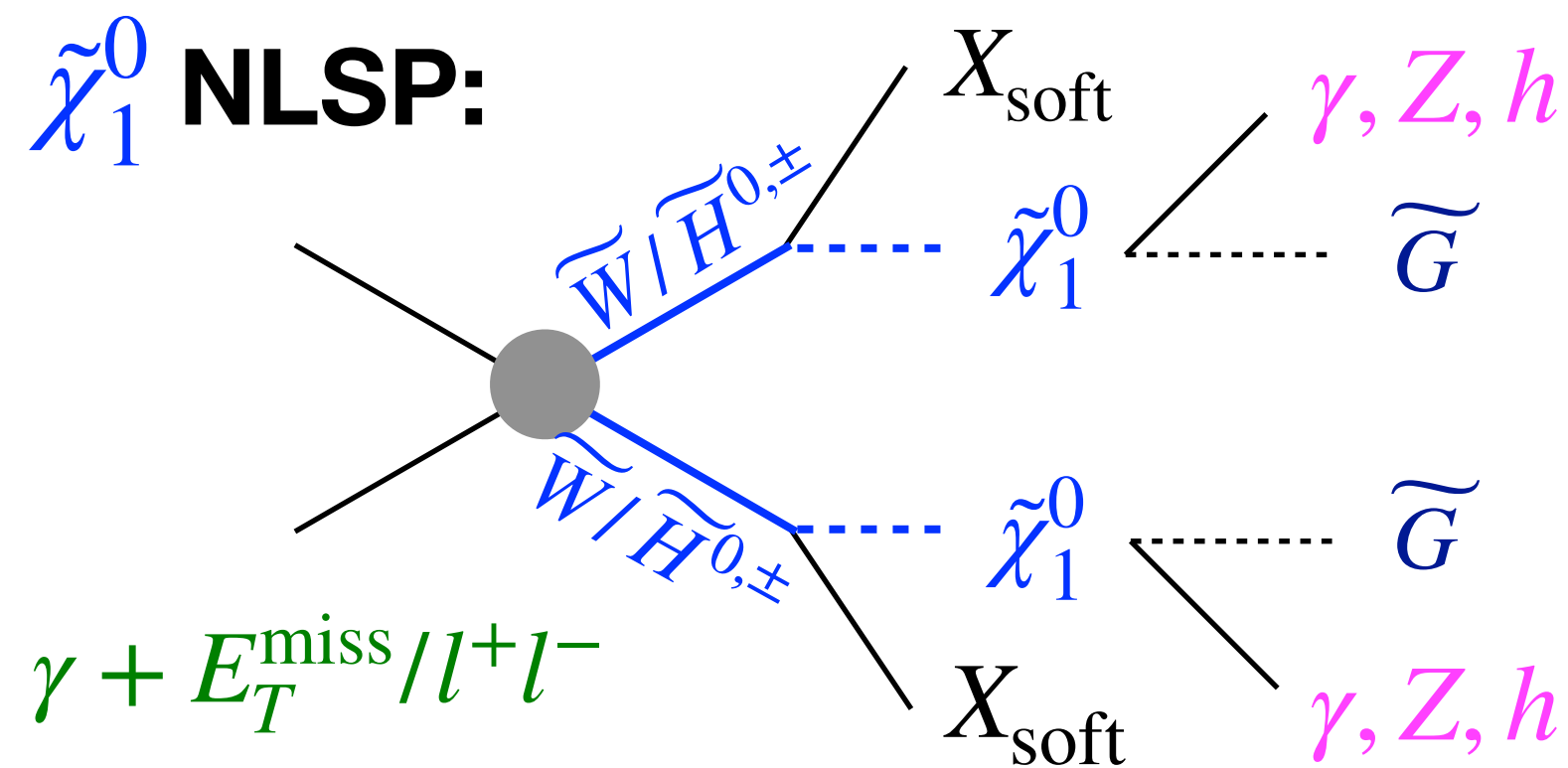
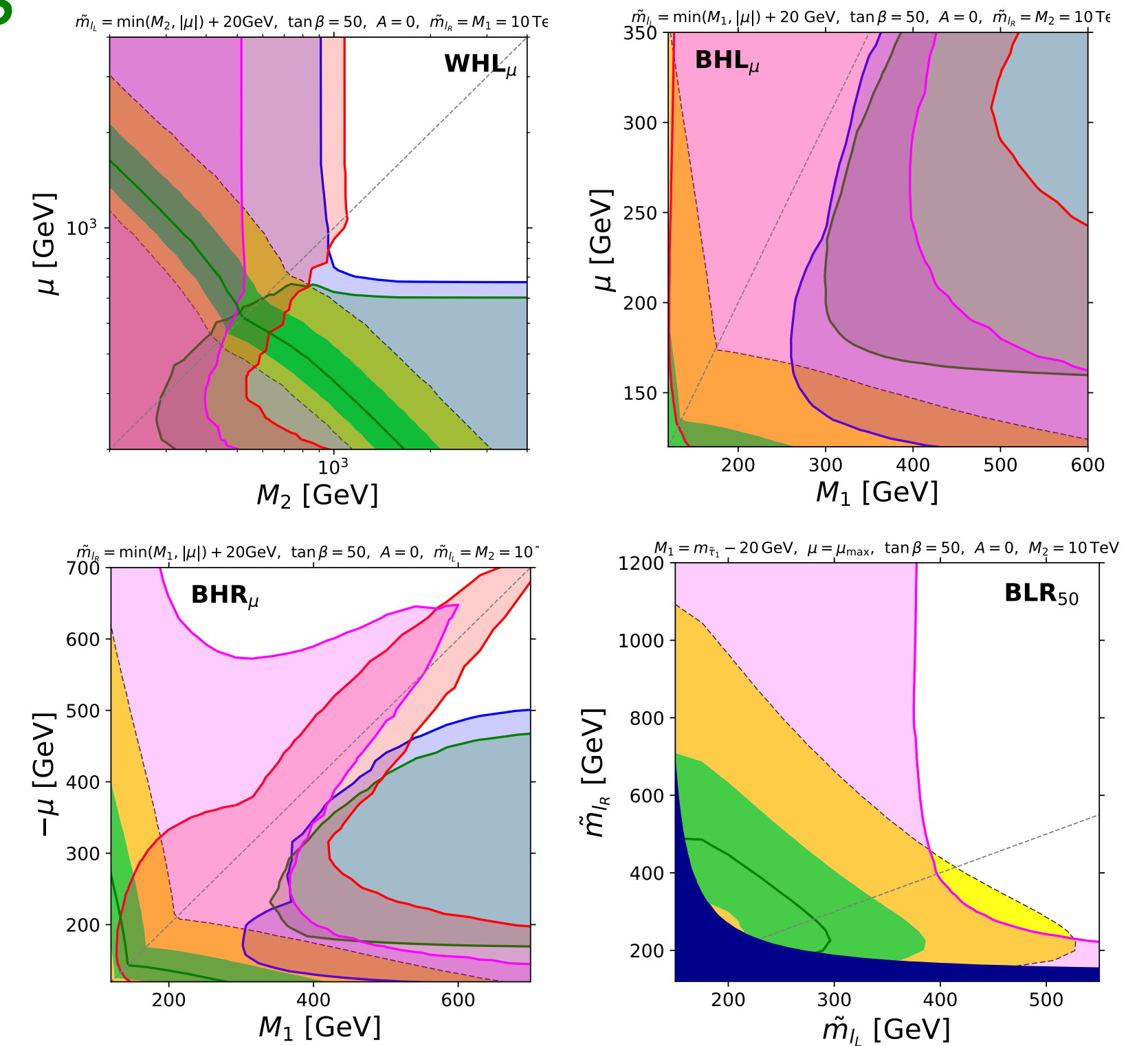
GMSB scenario

In GMSB, light gravitino LSP is motivated by naturalness

⊛ We assume almost massless gravitino LSP ($m_{\tilde{G}} \leq 1$ GeV)

⊛ $(g-2)_\mu$ doesn't change much wrt. MSSM

⊛ If neutralino is NLSP then totally excluded \rightarrow slepton/sneutrino/stau NLSP



A scenic landscape of a mountain lake with a reflection of the surrounding mountains and forest. The water is clear and green, reflecting the blue sky and the rugged, rocky peaks of the mountains. The foreground shows large, smooth rocks in the water.

methodology

Morskie Oko, Tatra,
Poland

Analysis

$$M_1, M_2, \mu, m_{\tilde{l}_L}, m_{\tilde{l}_R}, \tan \beta$$

1. Select one of the 4 loop diagrams (WHL, BHL, BHR, BLR)
2. Take 3 relevant masses to be $O(100\text{GeV})$ and other 2 very large
3. Then the diagram dominates $\Delta a_\mu^{\text{SUSY}}$
4. Vary 2 masses and relate/fix the third -> **2D plane scan**

MC
simulations

GM2Calc, CheckMATE2, MicrOmegas ...

constraints

$$a_\mu^{\text{SUSY}}$$

DM abundance

$$\sigma_{\text{SI}}^{\tilde{\chi}_1^0}$$

LHC constraints


List of all recasted LHC analyses

Name	E/TeV	$\mathcal{L}/\text{fb}^{-1}$	Description
atlas_1604_01306	13	3.2	Monophoton
atlas_1605_09318	13	3.3	3 b-jets + 0-1 lepton + MET
atlas_1609_01599	13	36	Monophoton
atlas_1704_03848	13	36	Monophoton
atlas_conf_2015_082	13	3.2	2 leptons (Z) + jets + MET
atlas_conf_2016_013	13	3.2	1 lepton + jets (4 tops, VVL quarks)
atlas_conf_2016_050	13	13.3	1 lepton + (b) jets + MET
atlas_conf_2016_054	13	13.3	1 lepton + (b) jets + MET
atlas_conf_2016_076	13	13.3	2 lepton + jets + MET
atlas_conf_2016_096	13	13.3	Multi-lepton + MET
atlas_conf_2017_060	13	36	Monojet
atlas_conf_2016_066	13	13.3	Photons, jets and MET
atlas_1712_08119	13	36	soft leptons (compressed EWKinos)
atlas_1712_02332	13	36	squarks and gluinos, 0 lepton, 2-6 jets
atlas_1709_04183	13	36	Jets + MET (stops)
atlas_1802_03158	13	36	search for GMSB with photons
atlas_1708_07875	13	36	EWKino search with taus and MET
atlas_1706_03731	13	36	Multilepton + Jets + MET (RPC and RPV)
atlas_1908_08215	13	36	2 leptons + MET (EWKinos)
atlas_1909_08457	13	139	SS lepton + MET (squark, gluino)
atlas_conf_2019_040	13	139	Jets + MET (squark, gluino)
atlas_conf_2019_020	13	139	3 leptons (EWKino)
atlas_1803_02762	13	36	2 or 3 leptons (EWKino)
atlas_conf_2018_041	13	80	Multi-b-jets (stops, sbottoms)
atlas_2101_01629	13	139	1 lepton + jets + MET
atlas_conf_2020_048	13	139	Monojet
atlas_2004_14060	13	139	$t\bar{t}$ + MET
atlas_1908_03122	13	139	Higgs bosons + b-jets + MET
atlas_2103_11684	13	139	4 or more leptons (RPV, GMSB)
atlas_2106_09609	13	139	Multijets + leptons (RPV)
atlas_1911_06660	13	139	Search for Direct Stau Production

Name	E/TeV	$\mathcal{L}/\text{fb}^{-1}$	Description
cms_pas_sus_15_011	13	2.2	2 leptons + jets + MET
cms_sus_16_039	13	35.9	electrowekinos in multilepton final state
cms_sus_16_025	13	12.9	electroweakino and stop compressed spectra
cms_sus_16_048	13	35.9	two soft opposite sign leptons

Name	E/TeV	$\mathcal{L}/\text{fb}^{-1}$	Description
atlas_1308_1841	8	20.3	0 lepton + ≥ 7 jets + MET
atlas_1308_2631	8	20.1	0 leptons + 2 b-jets + MET
atlas_1402_7029	8	20.3	3 leptons + MET (chargino+neutralino)
atlas_1403_4853	8	20.3	2 leptons + MET (direct stop)
atlas_1403_5222	8	20.3	stop production with Z boson and b-jets
atlas_1404_2500	8	20.3	Same sign dilepton or 3 lepton
atlas_1405_7875	8	20.3	0 lepton + 2-6 jets + MET
atlas_1407_0583	8	20.3	ATLAS, 1 lepton + (b-)jets + MET (stop)
atlas_1407_0608	8	20.3	Monojet or charm jet (stop)
atlas_1411_1559	8	20.3	monophoton plus MET
atlas_1501_07110	8	20.3	1 lepton + 125GeV Higgs + MET
atlas_1502_01518	8	20.3	Monojet + MET
atlas_1503_03290	8	20.3	2 leptons + jets + MET
atlas_1506_08616	8	20.3	di-lepton and 2b-jets + lepton
atlas_1507_05493	8	20.3	photonic signatures of gauge-mediated SUSY
atlas_conf_2012_104	8	20.3	1 lepton + ≥ 4 jets + MET
atlas_conf_2013_024	8	20.3	0 leptons + 6 (2 b-)jets + MET
atlas_conf_2013_049	8	20.3	2 leptons + MET
atlas_conf_2013_061	8	20.3	0-1 leptons + ≥ 3 b-jets + MET
atlas_conf_2013_089	8	20.3	2 leptons (razor)
atlas_conf_2015_004	8	20.3	invisible Higgs decay in VBF
atlas_1403_5294	8	20.3	2 leptons + MET, (SUSY electroweak)
atlas_higg_2013_03	8	20.3	2 leptons + MET, (invisible Higgs)
atlas_1502_05686	8	20.3	search for massive sparticles decaying to many jets

Name	E/TeV	$\mathcal{L}/\text{fb}^{-1}$	Description
cms_1303_2985	8	11.7	α_T + b-jets
cms_1408_3583	8	19.7	monojet + MET
cms_1502_06031	8	19.4	2 leptons, jets, MET (only on-Z)
cms_1504_03198	8	19.7	1 lepton, ≥ 3 jets, ≥ 1 b-jet, MET (DM + 2 top)
cms_sus_13_016	8	19.5	OS lepton 3+ b-tags

A wide-angle photograph of a beach at sunset. The sky is a vibrant orange and yellow, with the sun low on the horizon. In the foreground, a yellow fishing boat with a motor and several flags is beached. Another similar boat is visible further down the beach to the left. A few people can be seen walking in the distance. The water is calm with gentle waves. A semi-transparent white box with rounded corners is overlaid in the lower half of the image, containing the word "results" in a dark blue, sans-serif font.

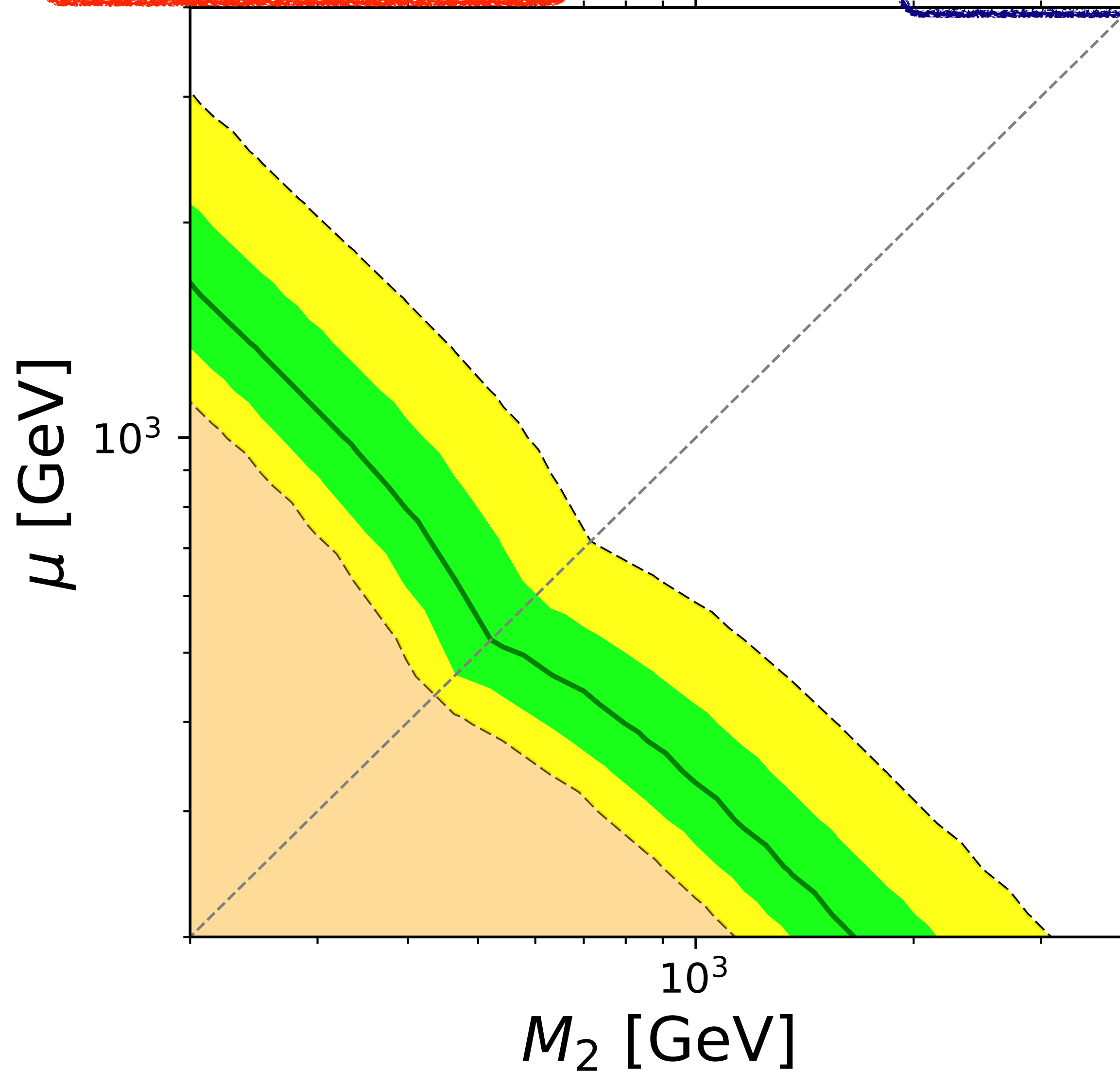
results

Beach in Dębki, Poland

MSSM, WHL_μ

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \quad \tan\beta = 50, \quad A = 0, \quad \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$

compressed
mass spectrum



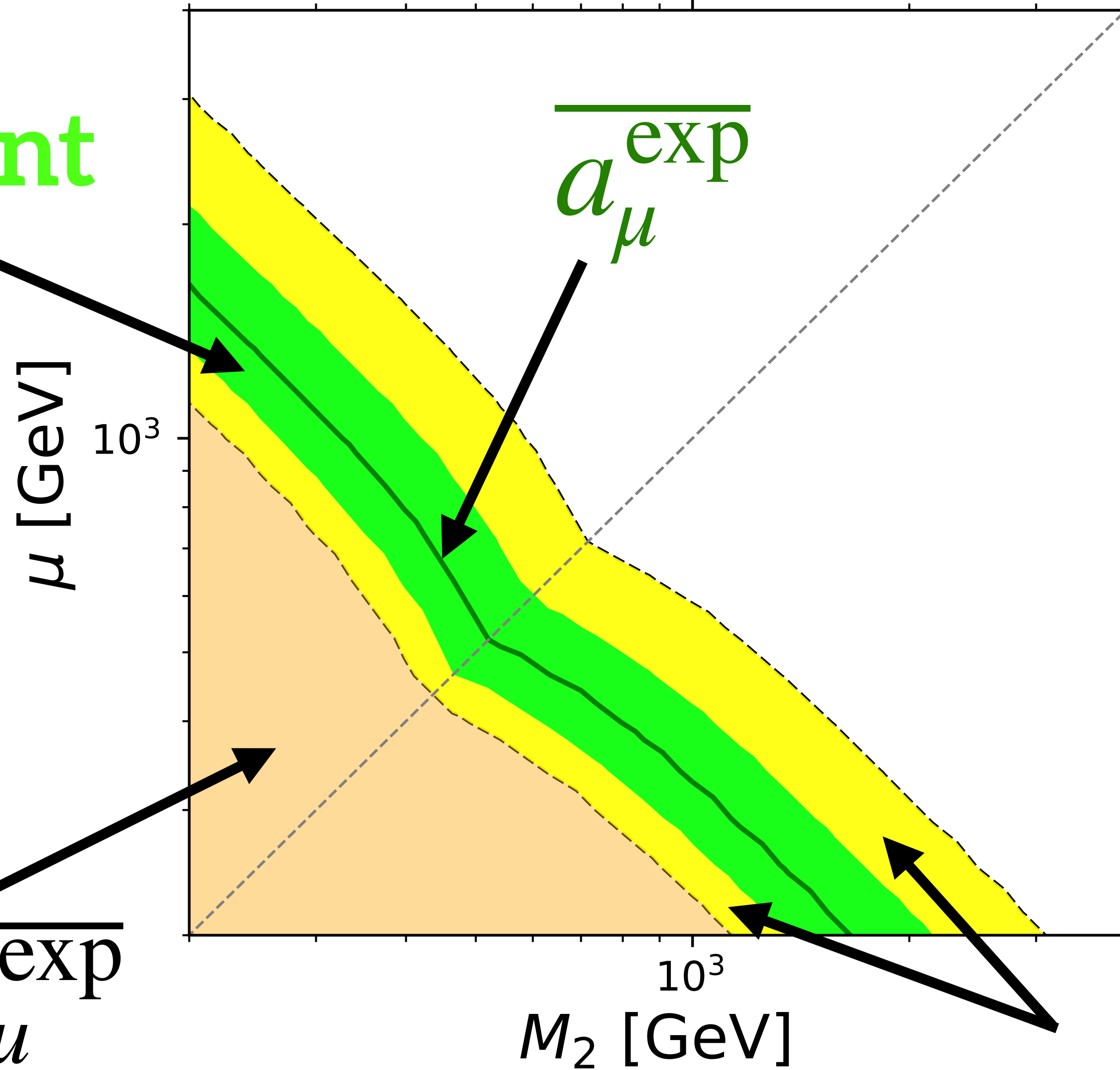
**WHL
dominates**

MSSM, WHL_μ

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \quad \tan\beta = 50, \quad A = 0, \quad \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$

1 σ agreement

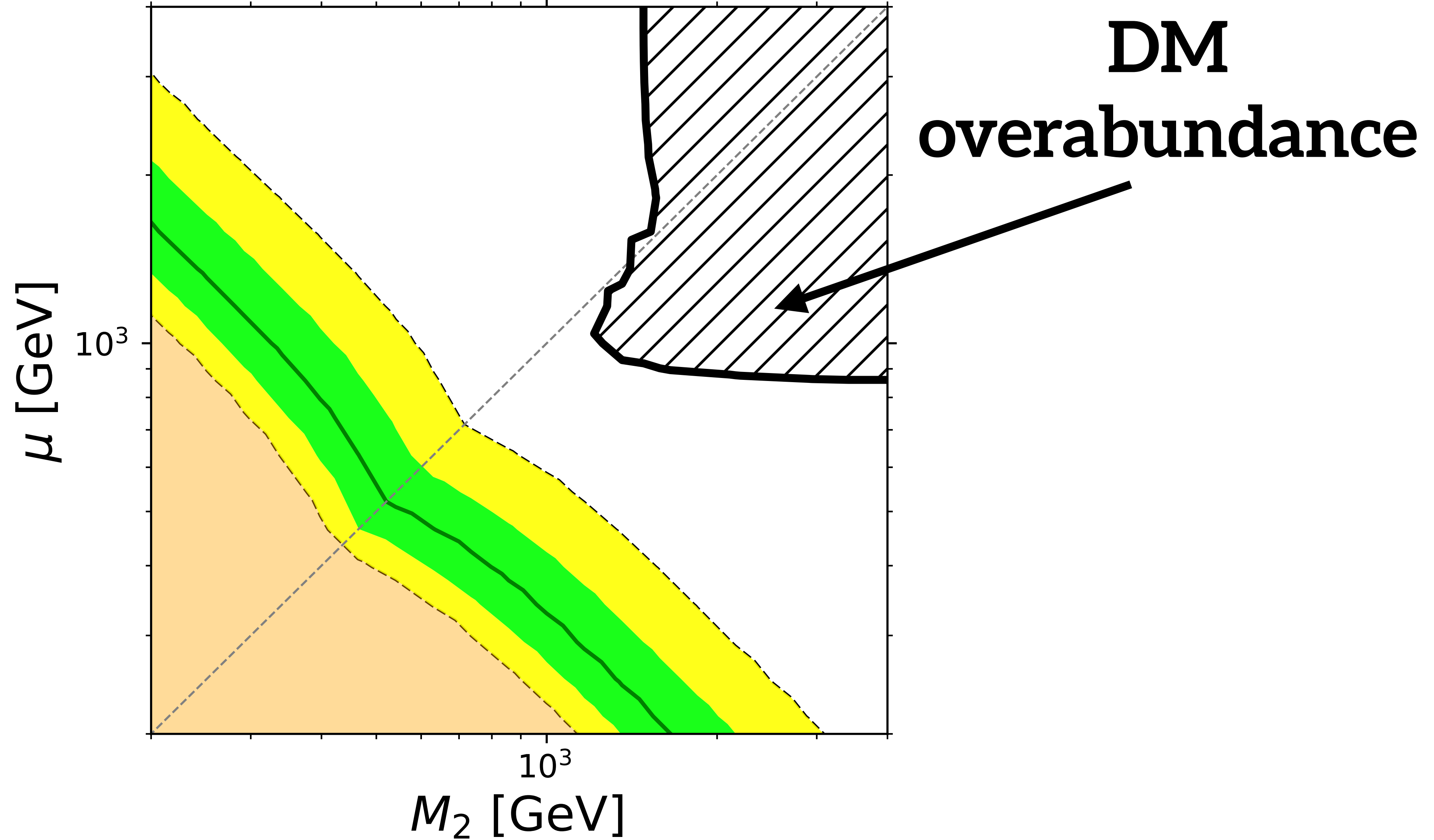
$$a_\mu^{\text{SUSY}} > \overline{a_\mu^{\text{exp}}}$$



2 σ agreement

MSSM, WHL_μ

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \quad \tan\beta = 50, \quad A = 0, \quad \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$



ATLAS DT

[2201.02472]

$$m_{\chi_1^\pm} - m_{\chi_1^0} \sim \mathcal{O}(100 \text{ MeV})$$

$$c\tau_{\tilde{\chi}_1^\pm} \sim \mathcal{O}(1 \text{ cm})$$

$$\chi_1^\pm \rightarrow \chi_1^0 + X_{\text{soft}}^\pm$$

Wino-like LSP excluded
up to $M_2 \sim 760 \text{ GeV}$

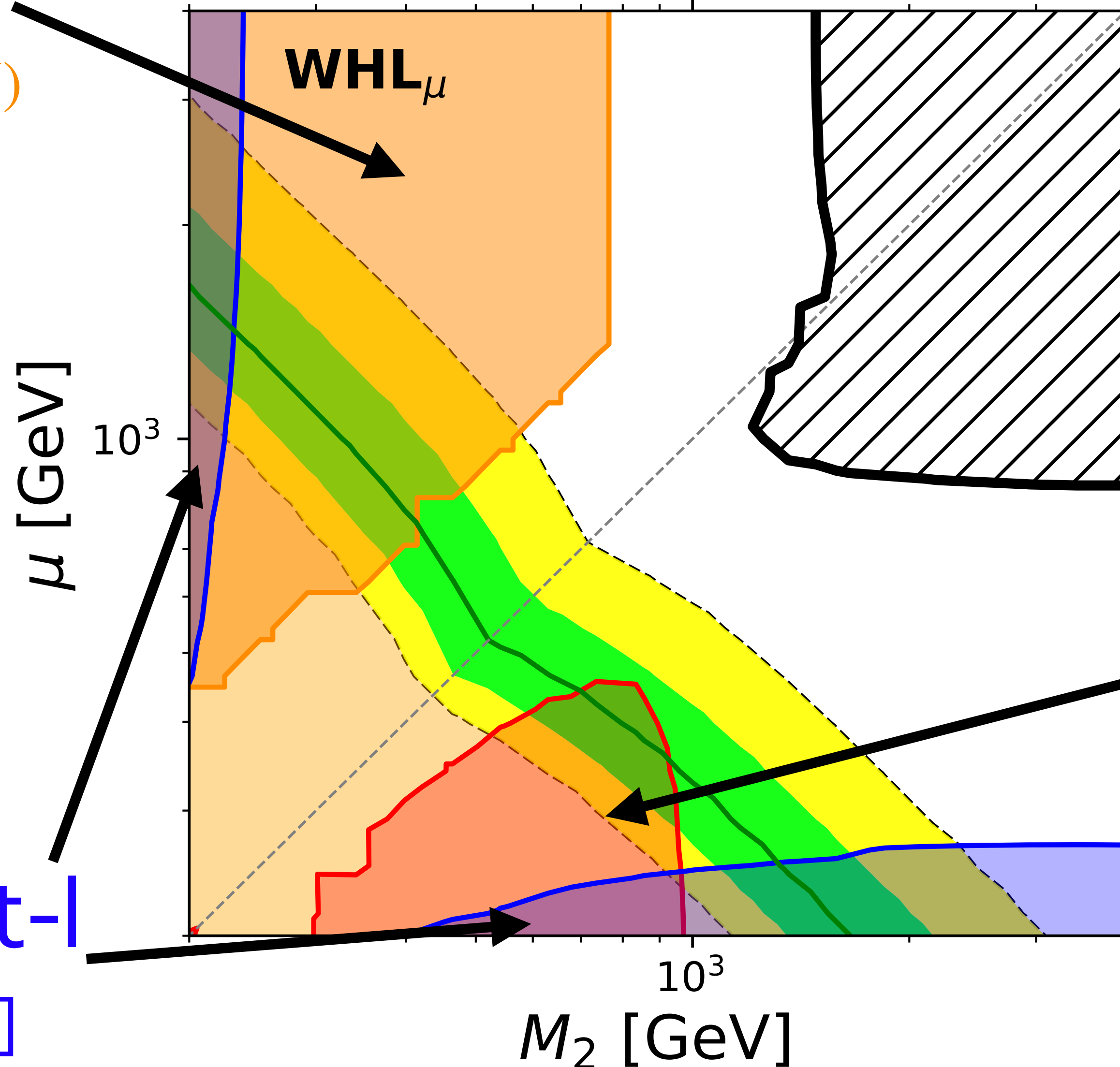
$$\begin{aligned} \tilde{\zeta} \tilde{\zeta}' &\rightarrow (l^+ \tilde{\eta})(l^- \tilde{\eta}') \\ \tilde{\zeta} &\equiv \tilde{l} / \tilde{\nu} \\ \tilde{\eta} &\equiv \tilde{\chi}_1^\pm / \tilde{\chi}_1^0 \end{aligned}$$

ATLAS soft-l

[1911.12606]

MSSM, WHL_μ

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20 \text{ GeV}, \quad \tan\beta = 50, \quad A = 0, \quad \tilde{m}_{l_R} = M_1 = 10 \text{ TeV}$$



$$pp \rightarrow \tilde{W}^{+,0} \tilde{W}^{-,0}$$

$$W^\pm \rightarrow l^\pm \tilde{\nu}$$

$$W^0 \rightarrow l^\pm \tilde{l}^\mp$$

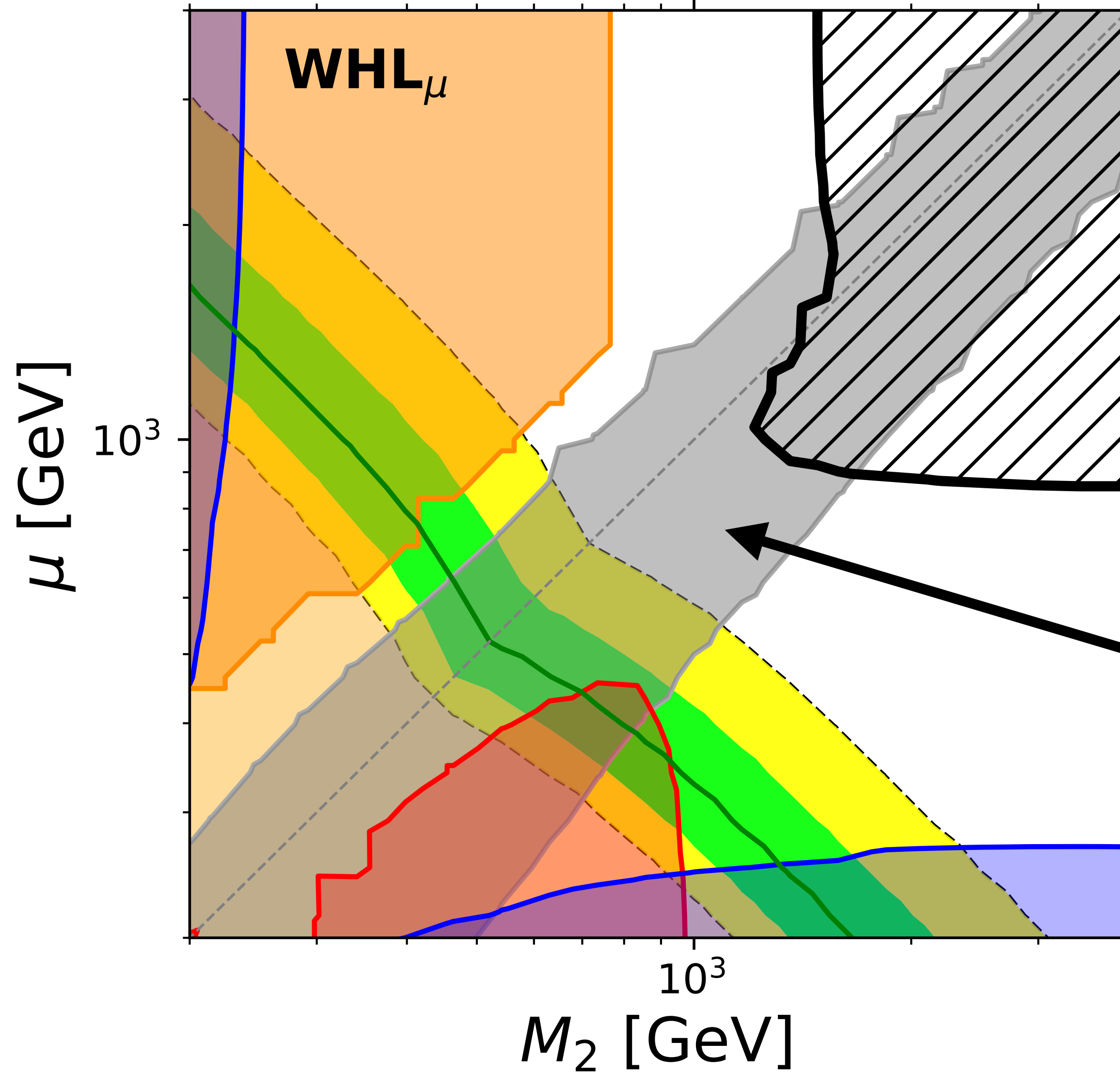
slepton decays to
higgsino LSP
are very soft (20 GeV)

CMS l+l-

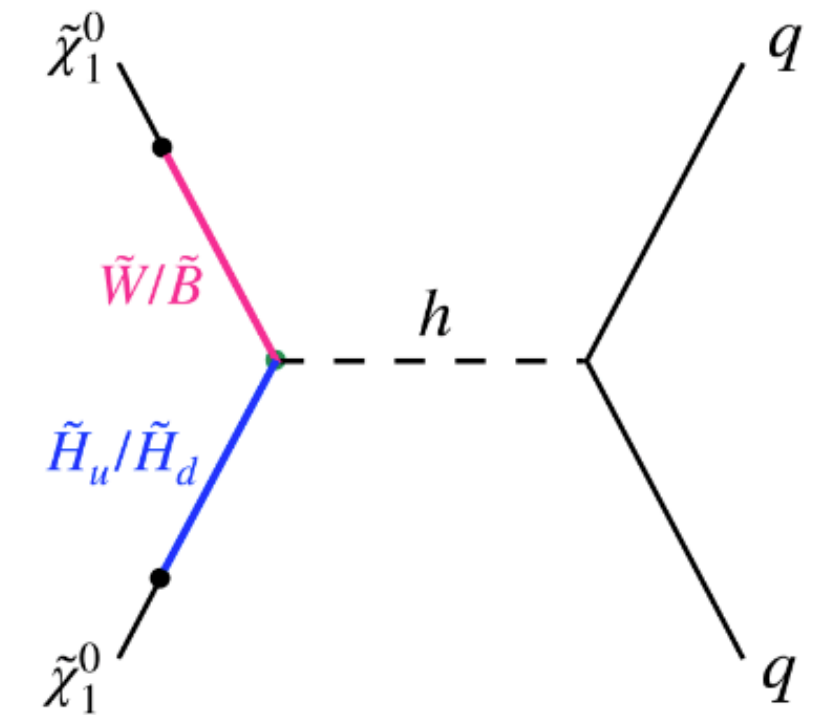
[2012.08600]

MSSM, WHL_μ

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \quad \tan\beta = 50, \quad A = 0, \quad \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$



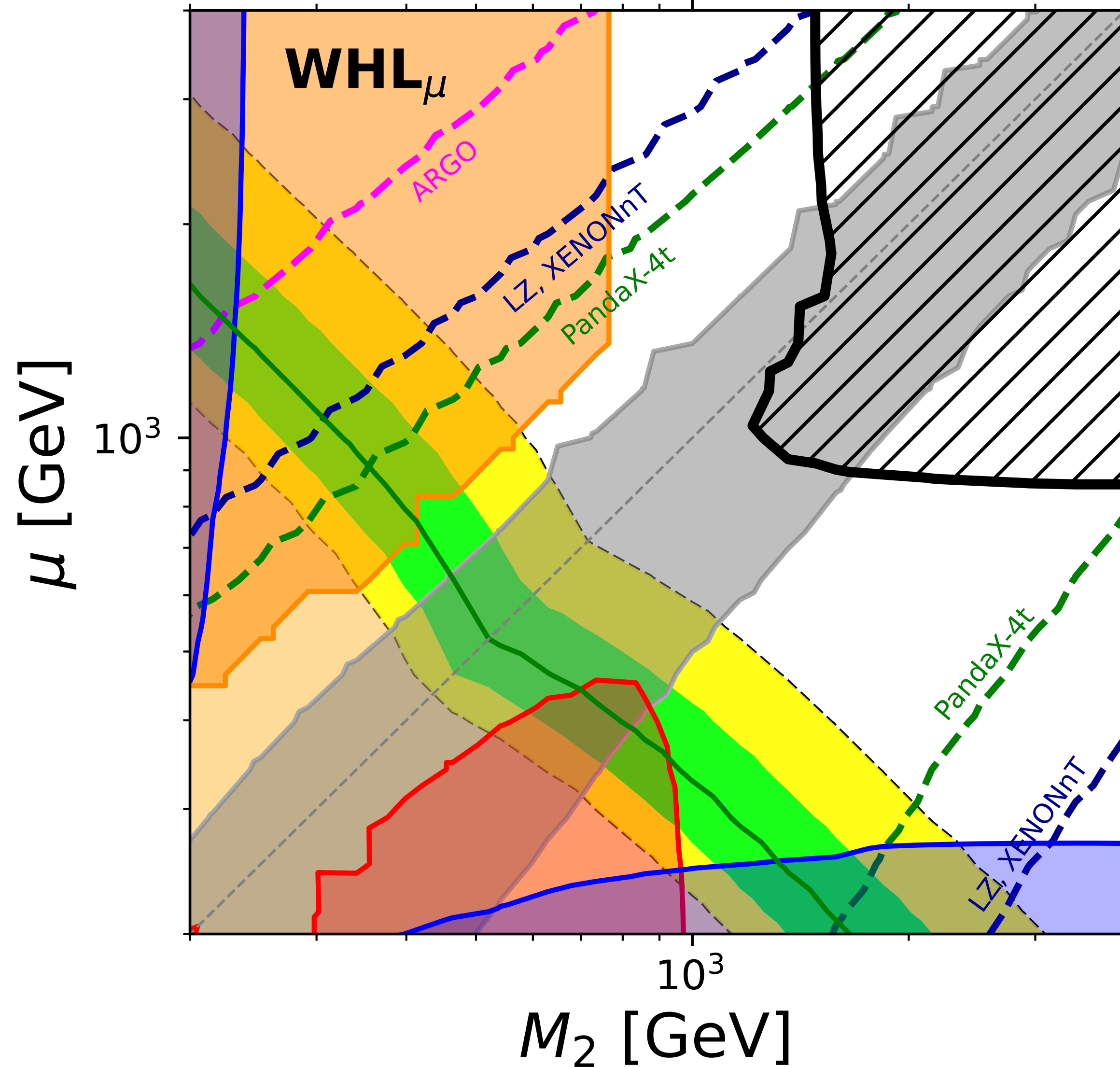
Large gaugino-Higgsino mixing leads to a **large cross-section for DM Direct Detection:**



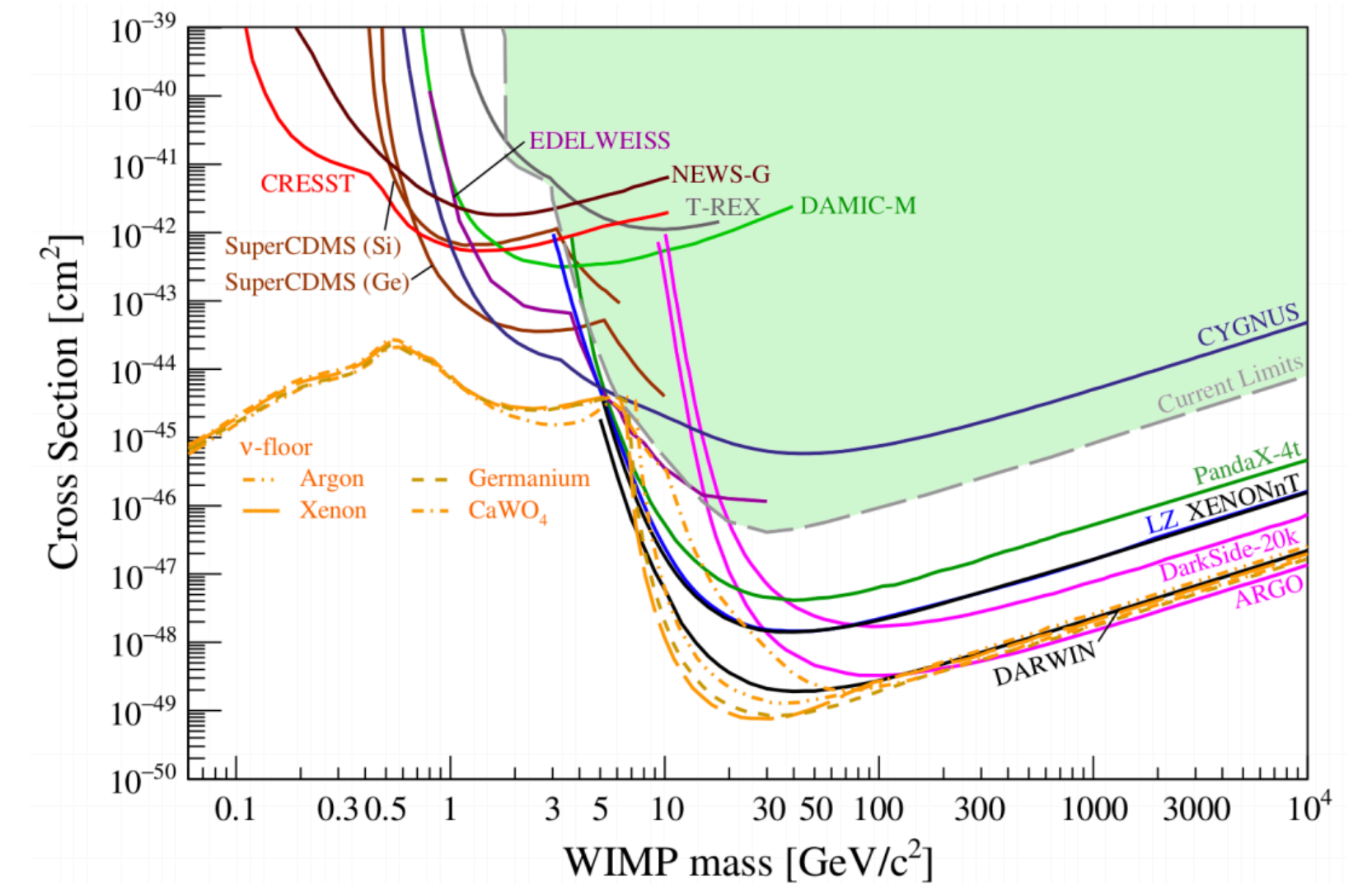
XENON1T
[1805.12562]

MSSM, WHL_μ

$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \quad \tan\beta = 50, \quad A = 0, \quad \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$



Whole $(g-2)_\mu$ relevant region will be probed in the near future!



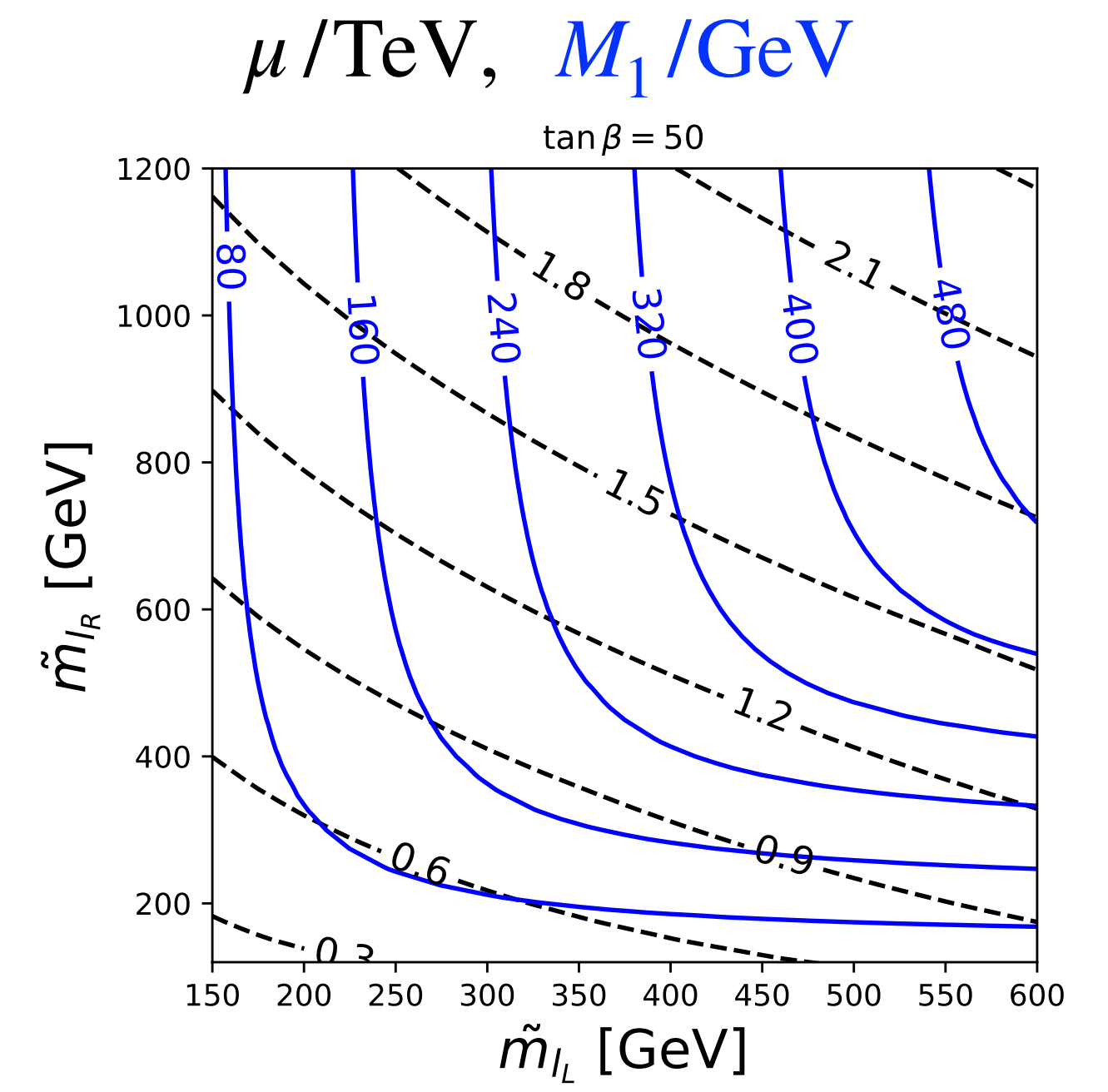
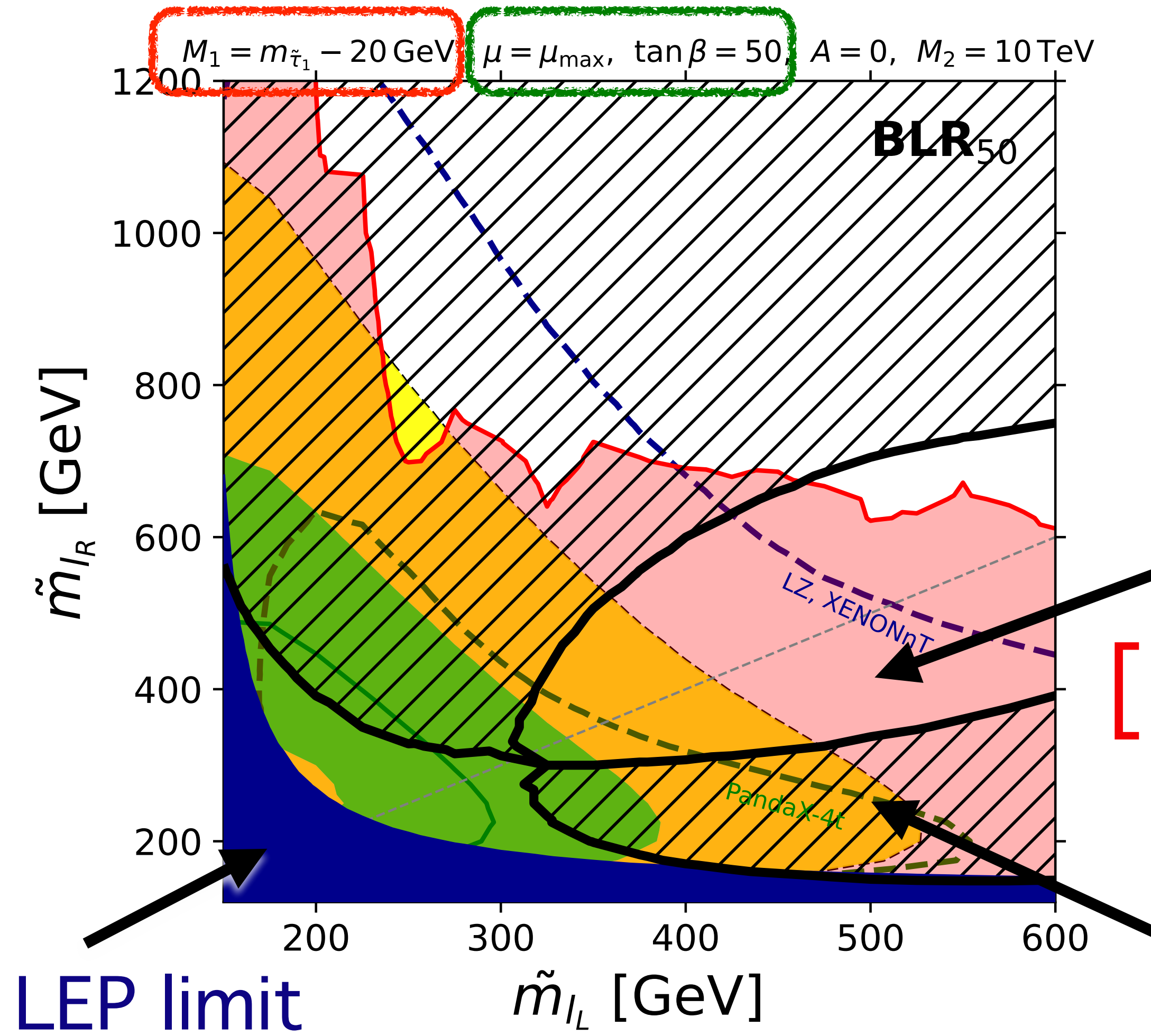
MSSM, BLR

compressed
mass spectrum
(stau coannihilation)

vacuum stability condition

$$|m_{\tilde{\ell}_{LR}}^2| \leq \left[1.01 \times 10^2 \text{ GeV} \sqrt{m_{\tilde{\ell}_L} m_{\tilde{\ell}_R}} + 1.01 \times 10^2 \text{ GeV} (m_{\tilde{\ell}_L} + 1.03 m_{\tilde{\ell}_R}) - 2.27 \times 10^4 \text{ GeV}^2 + \frac{2.97 \times 10^6 \text{ GeV}^3}{m_{\tilde{\ell}_L} + m_{\tilde{\ell}_R}} - 1.14 \times 10^8 \text{ GeV}^4 \left(\frac{1}{m_{\tilde{\ell}_L}^2} + \frac{0.983}{m_{\tilde{\ell}_R}^2} \right) \right]$$

[Kitahara, Yoshinaga 13]; [Endo, Hamaguchi, Kitahara, Yoshinaga 13]



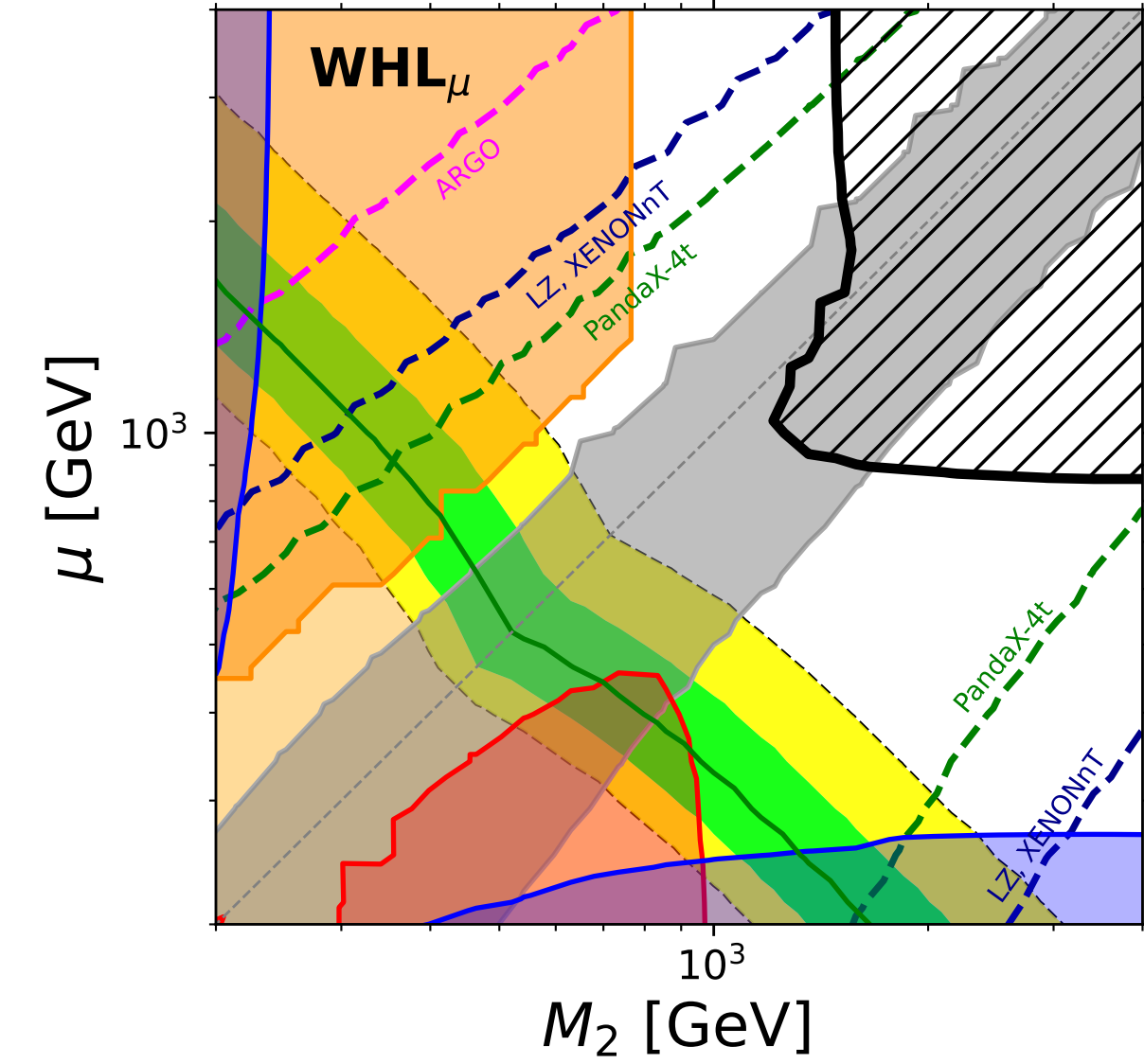
CMS I+I-
[2012.08600]

DM overproduction
due to Bino-like LSP
/09/05

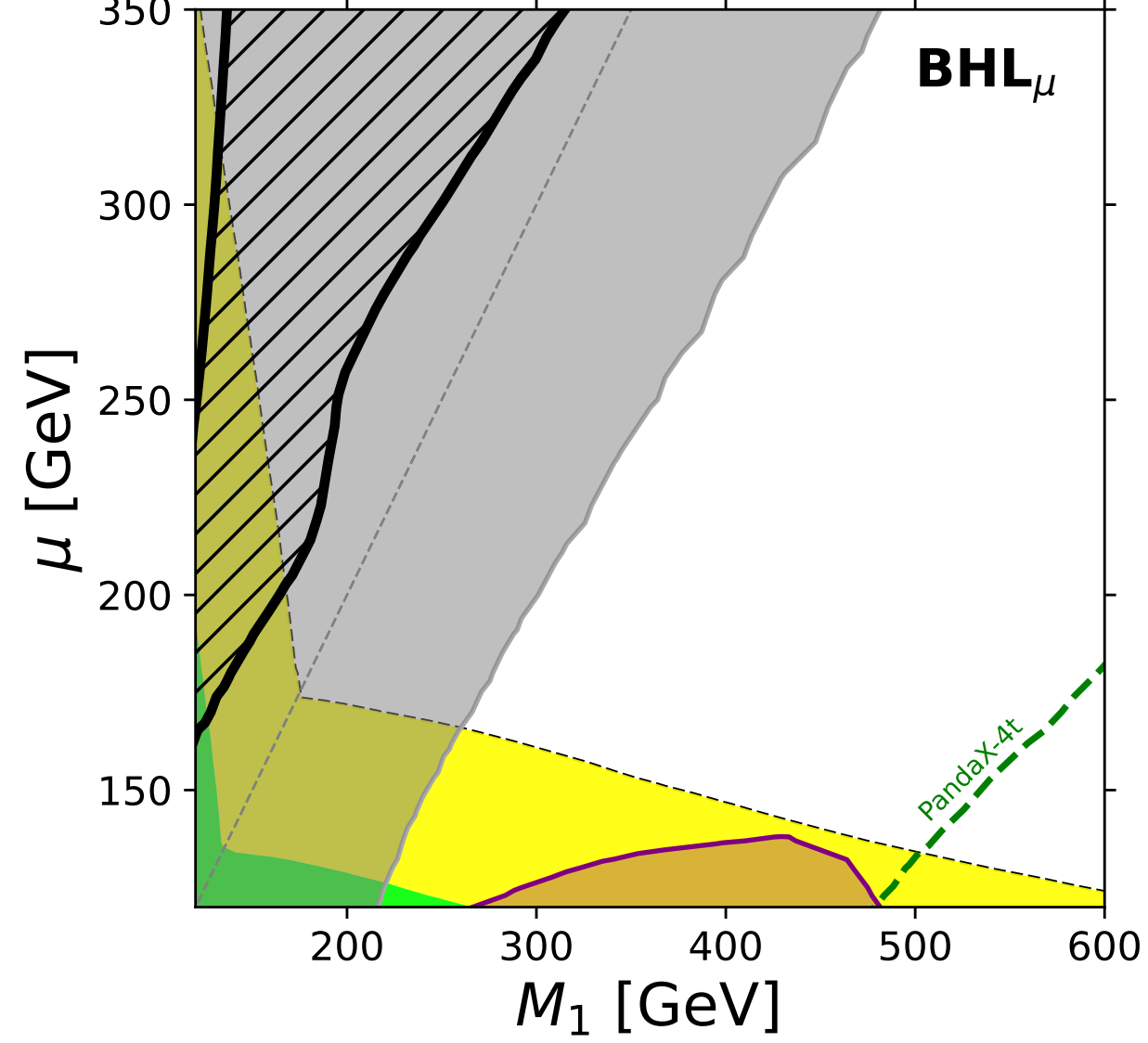


MSSM with stable neutralino

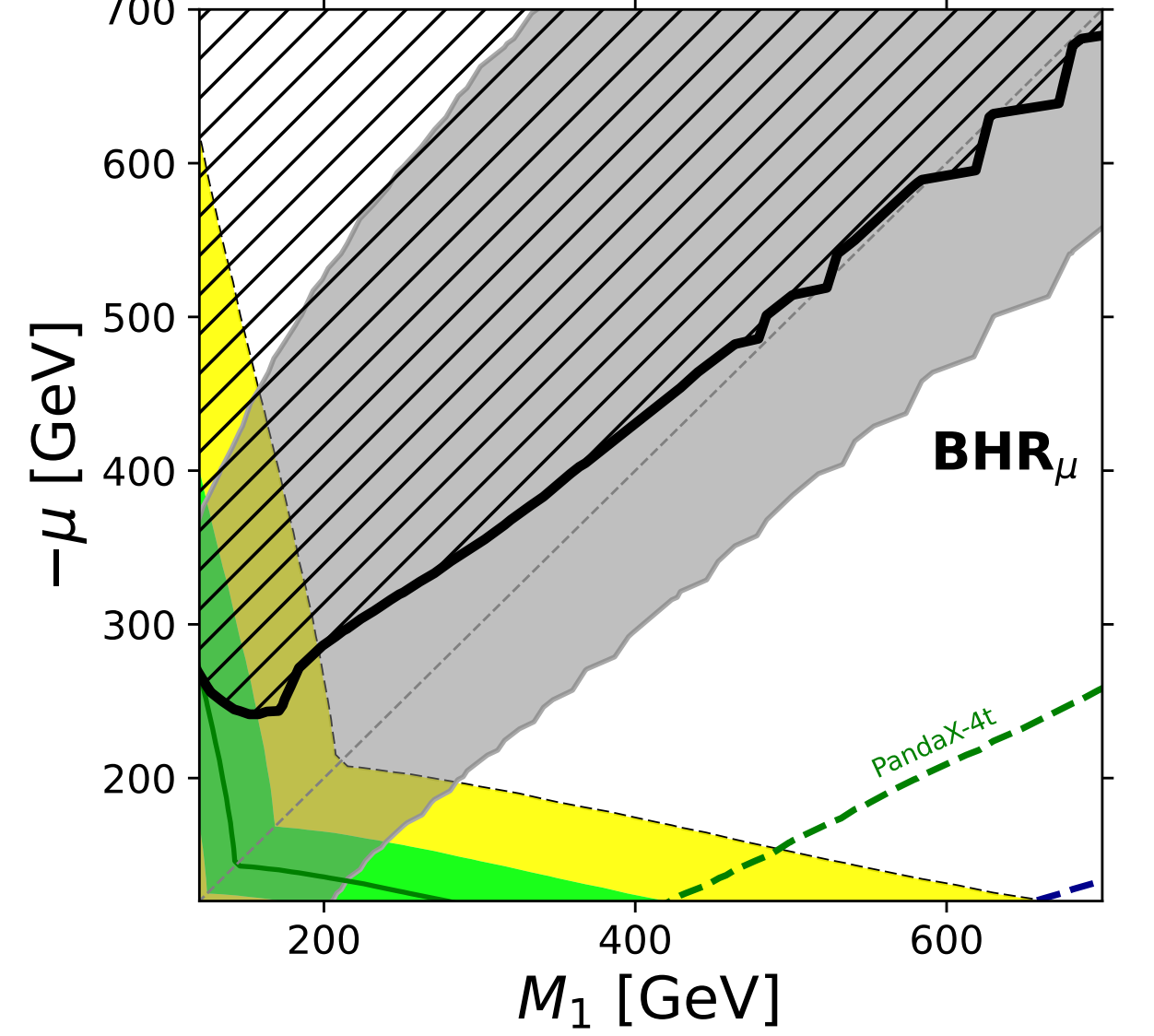
$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_R} = M_1 = 10\text{TeV}$



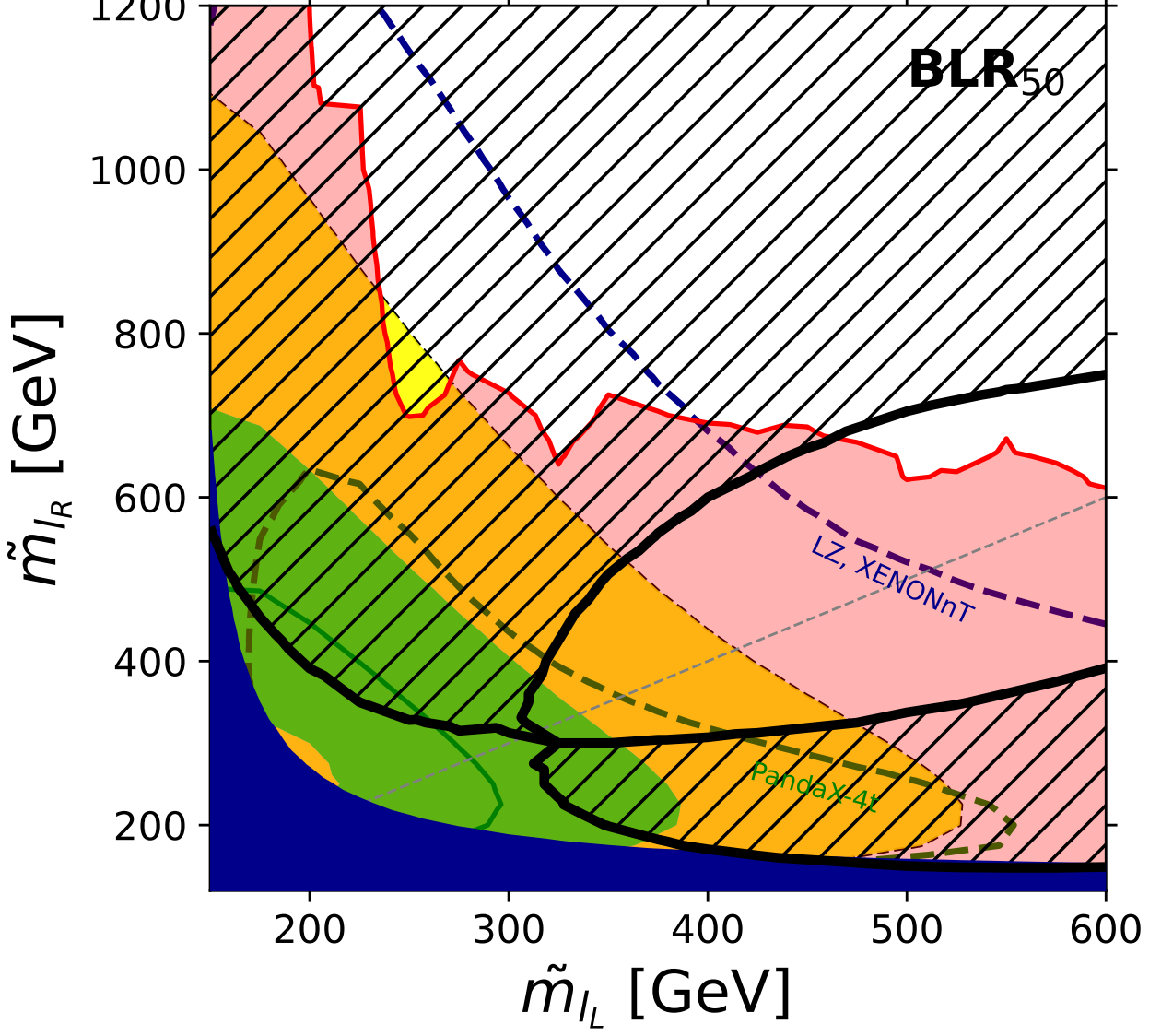
$\tilde{m}_{l_L} = \min(M_1, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_R} = M_2 = 10\text{TeV}$



$\tilde{m}_{l_R} = \min(M_1, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_L} = M_2 = 10\text{TeV}$

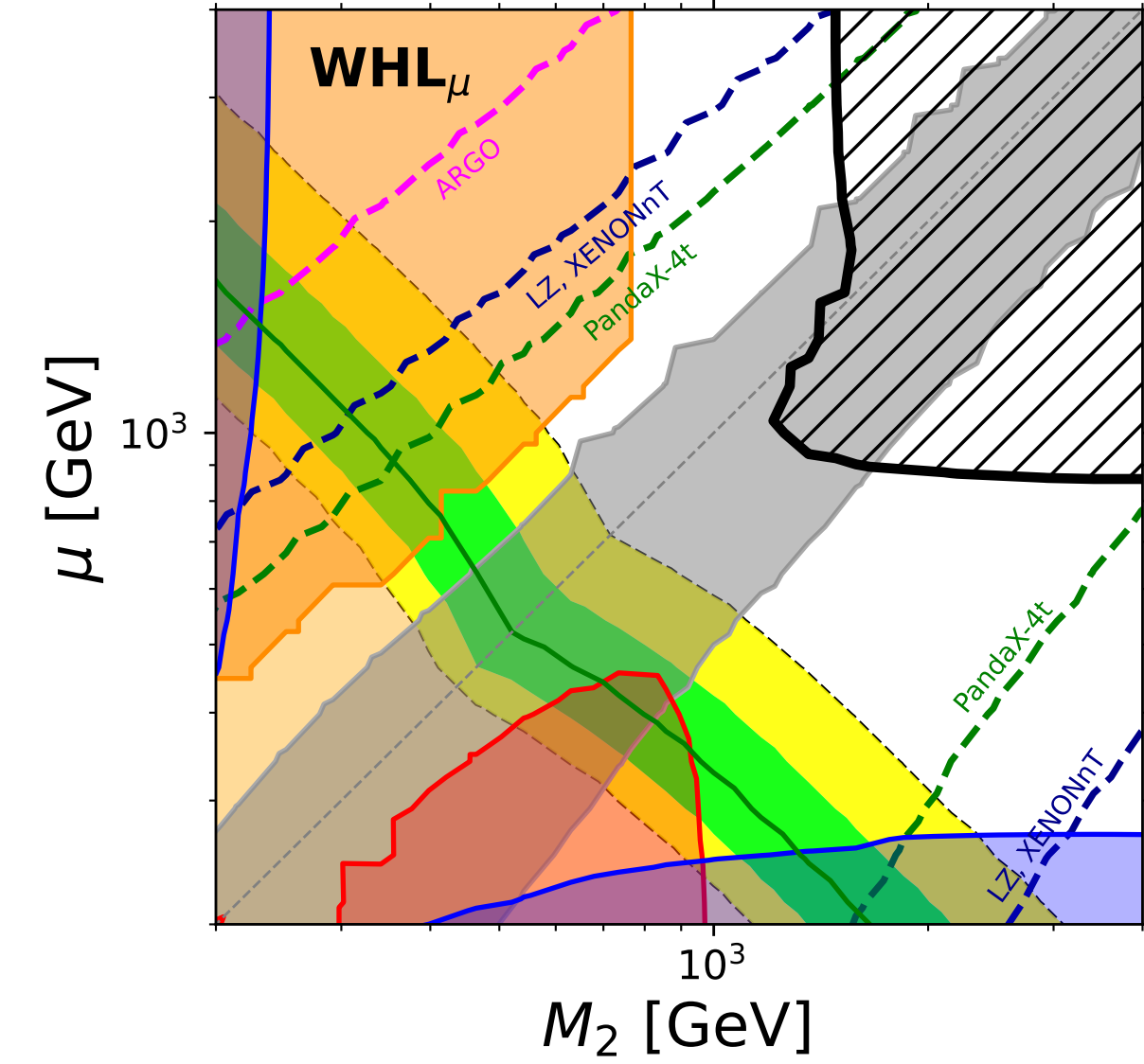


$M_1 = \tilde{m}_{\tilde{\tau}_1} - 20\text{GeV}$, $\mu = \mu_{\text{max}}$, $\tan\beta = 50$, $A = 0$, $M_2 = 10\text{TeV}$

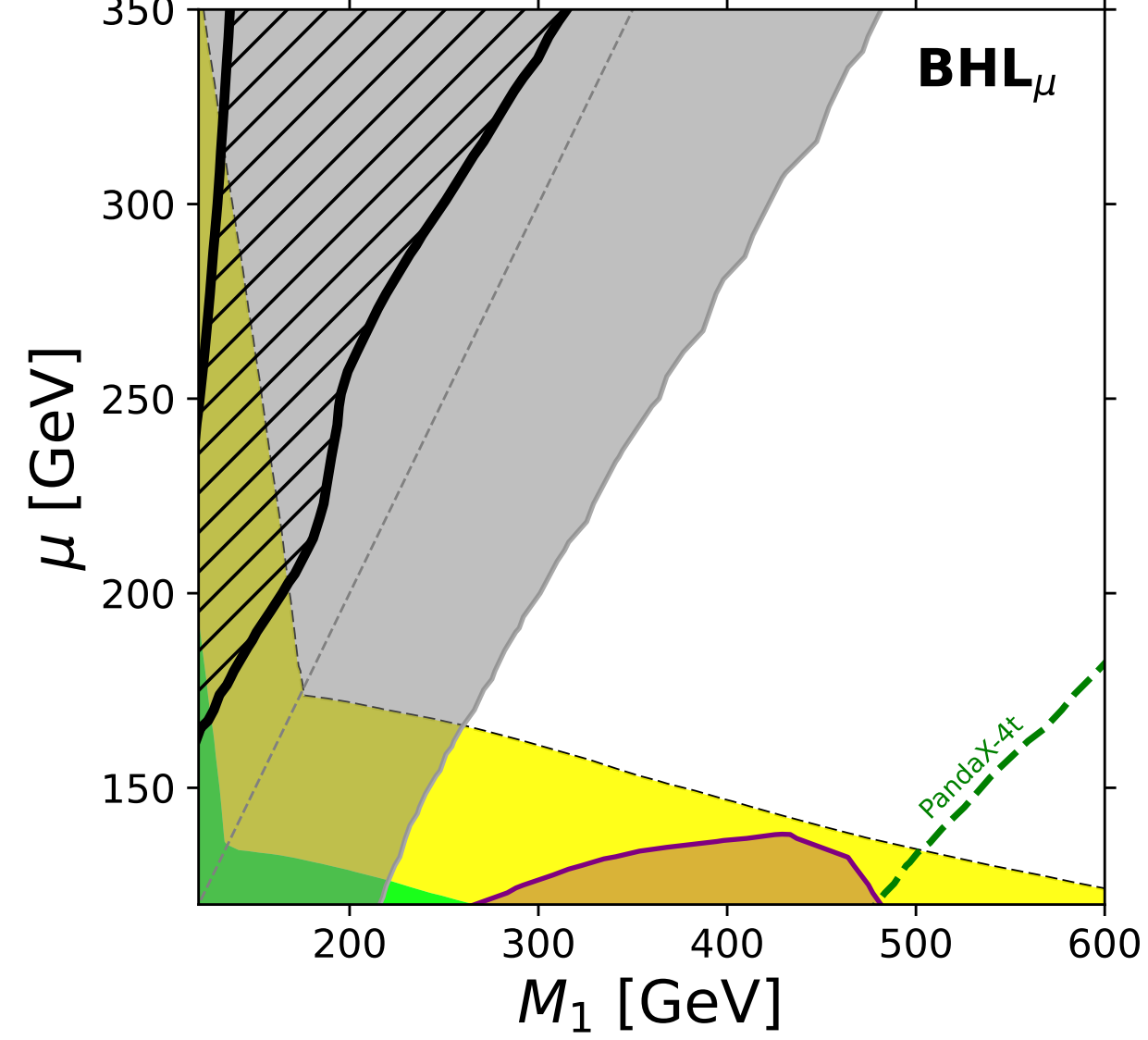


MSSM with stable neutralino

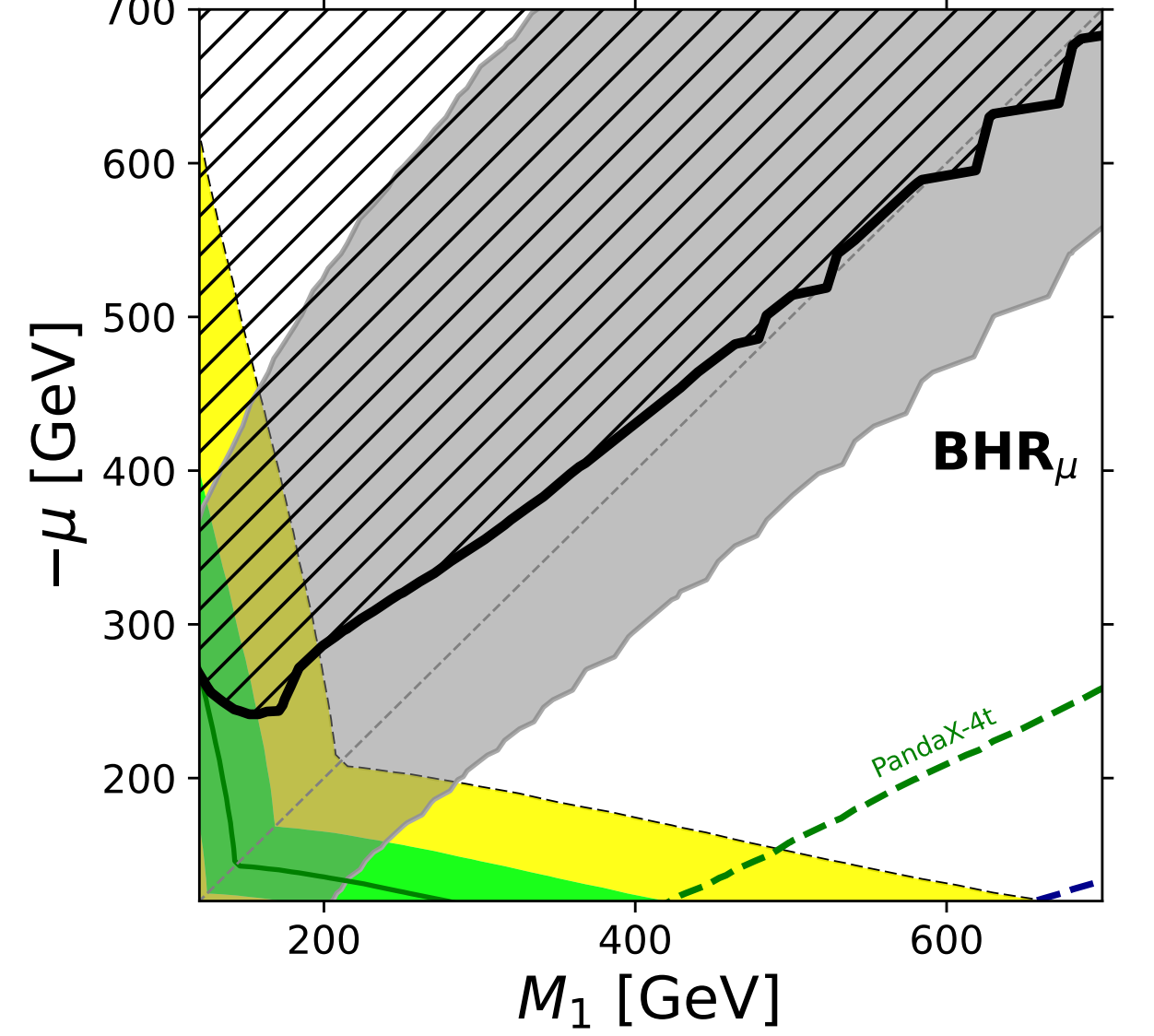
$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$



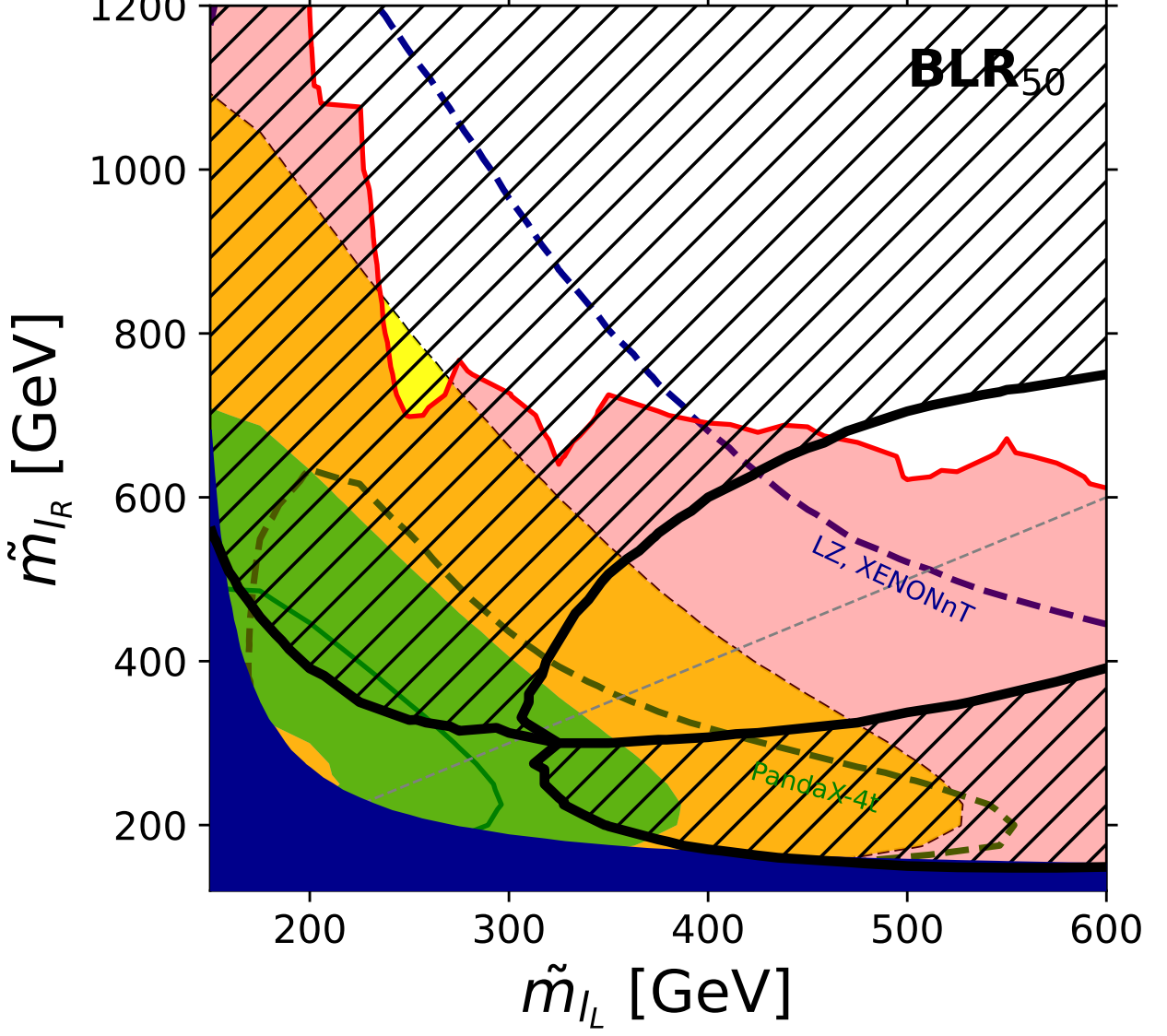
$$\tilde{m}_{l_L} = \min(M_1, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_R} = M_2 = 10\text{TeV}$$



$$\tilde{m}_{l_R} = \min(M_1, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_L} = M_2 = 10\text{TeV}$$

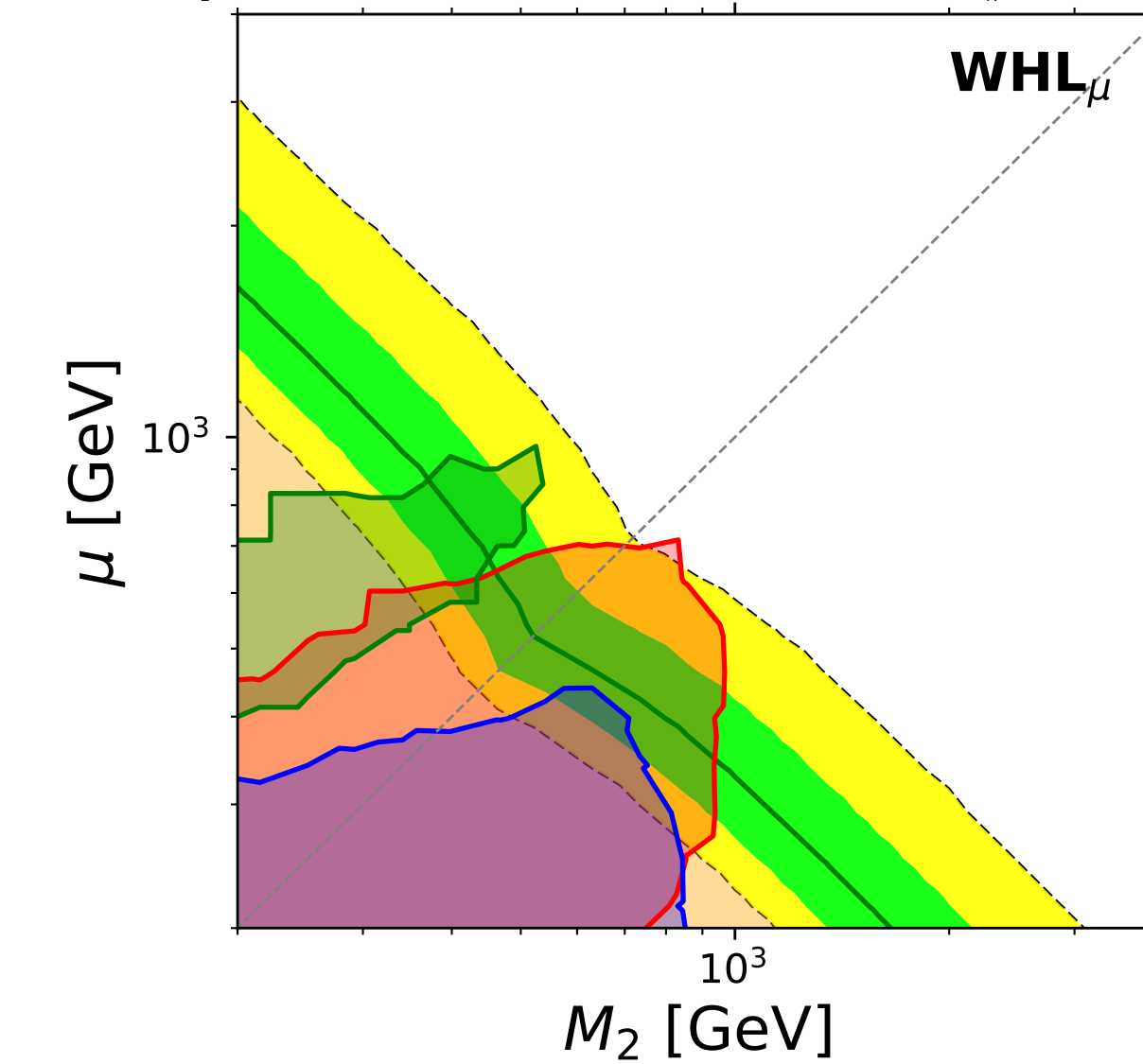


$$M_1 = m_{\tilde{\tau}_1} - 20\text{GeV}, \mu = \mu_{\max}, \tan\beta = 50, A = 0, M_2 = 10\text{TeV}$$

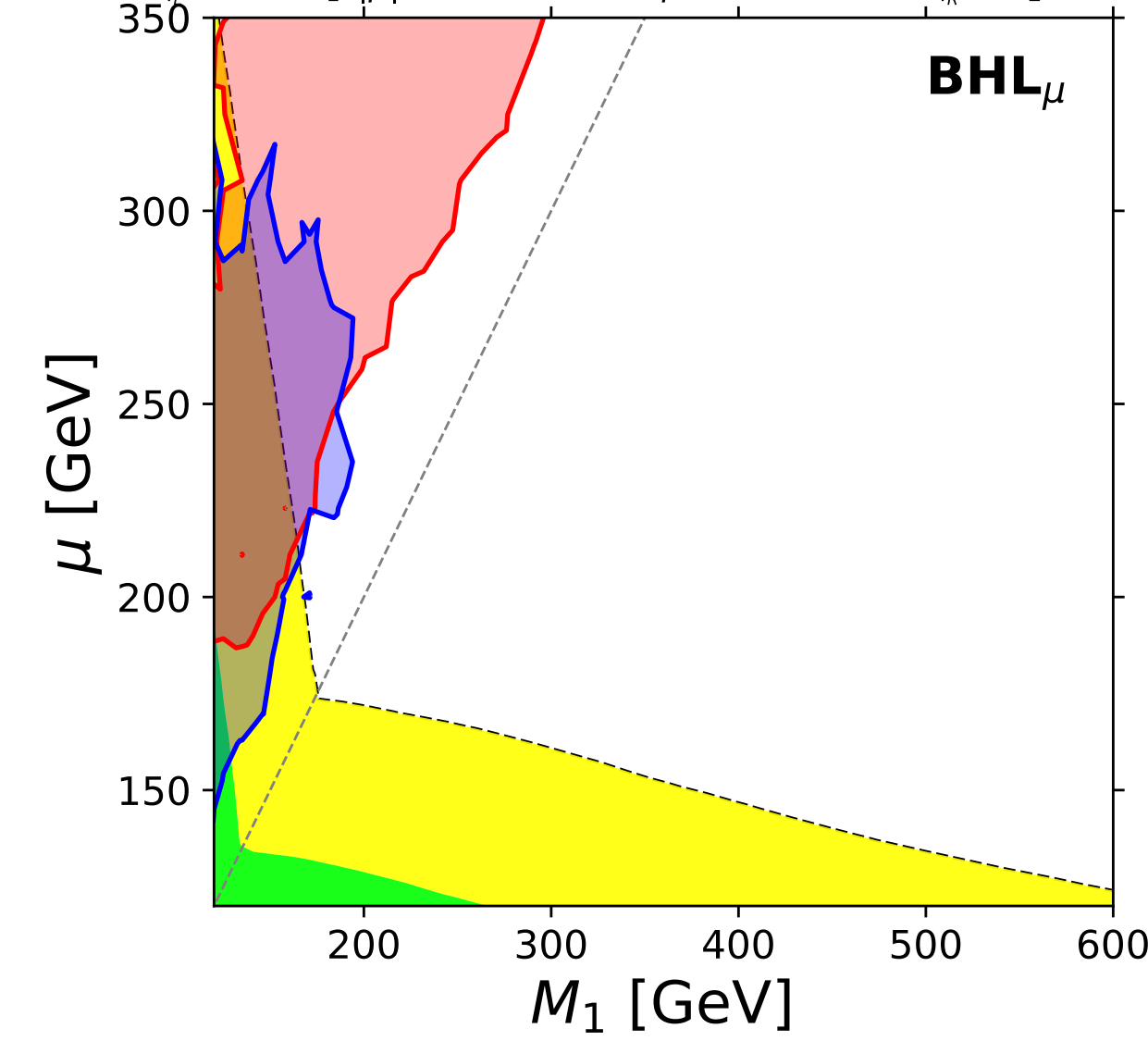


UDD RPV

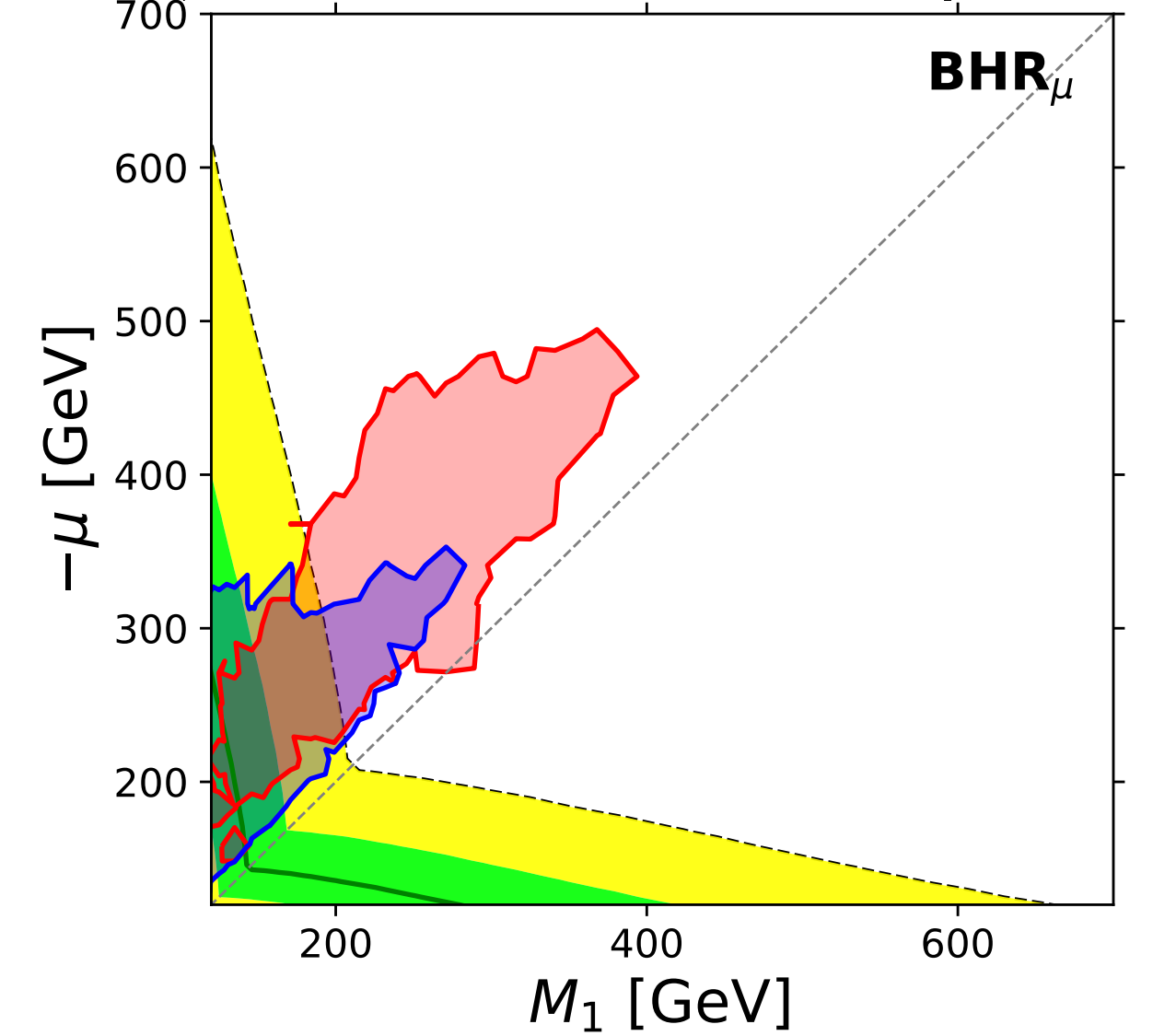
$$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_R} = M_1 = 10\text{TeV}$$



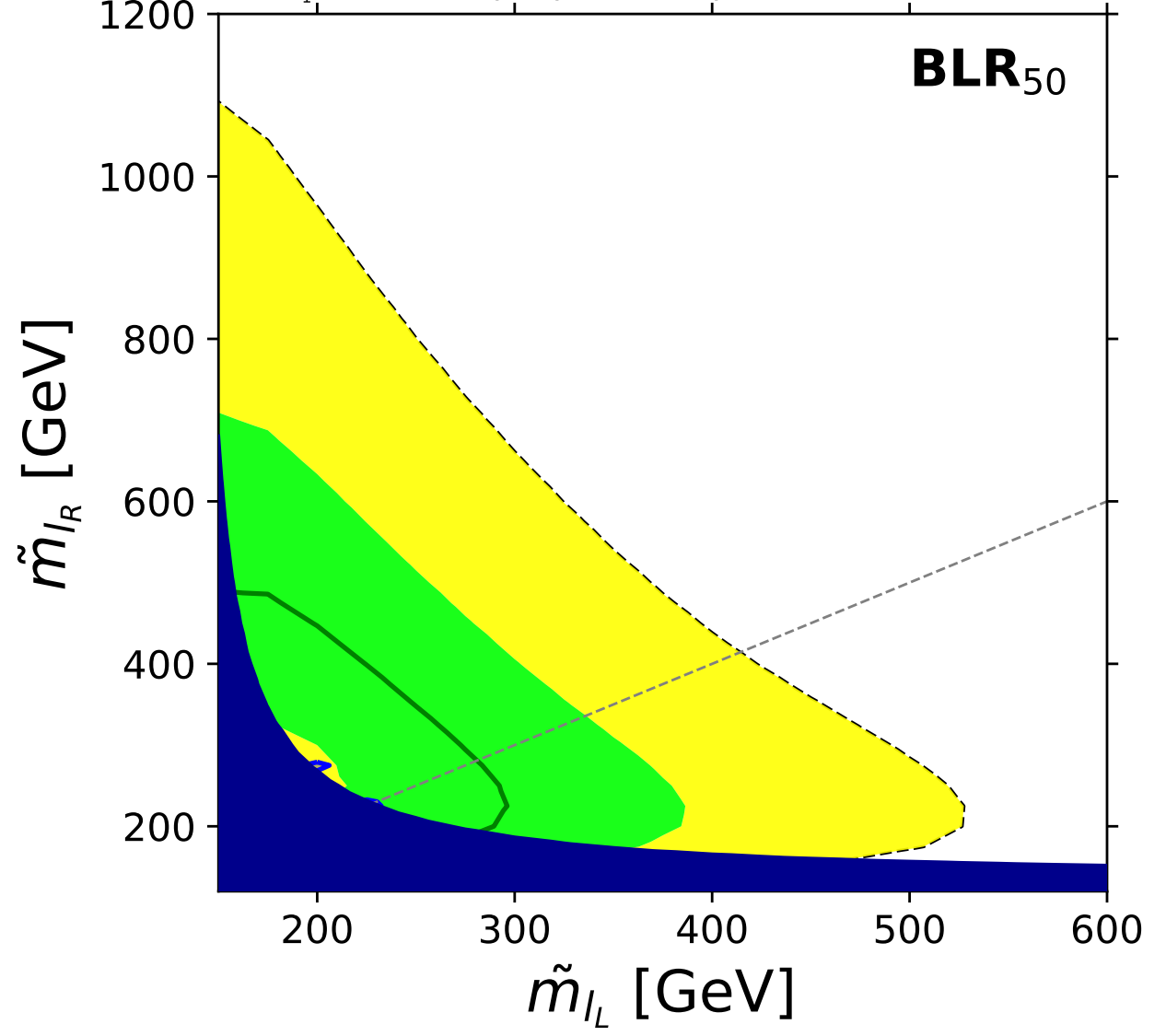
$$\tilde{m}_{l_L} = \min(M_1, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_R} = M_2 = 10\text{TeV}$$



$$\tilde{m}_{l_R} = \min(M_1, |\mu|) + 20\text{GeV}, \tan\beta = 50, A = 0, \tilde{m}_{l_L} = M_2 = 10\text{TeV}$$

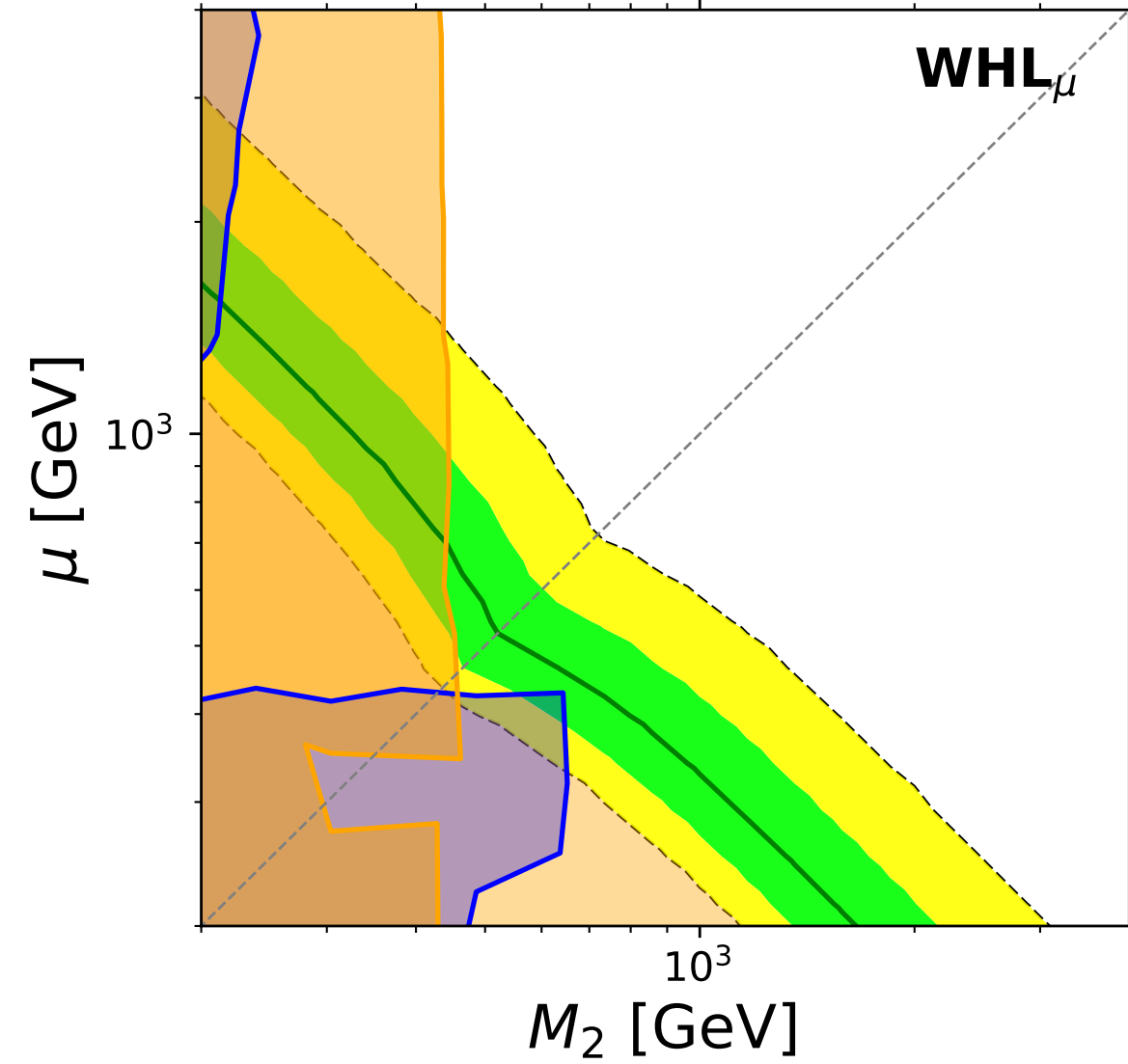


$$M_1 = m_{\tilde{\tau}_1} - 20\text{GeV}, \mu = \mu_{\max}, \tan\beta = 50, A = 0, M_2 = 10\text{TeV}$$

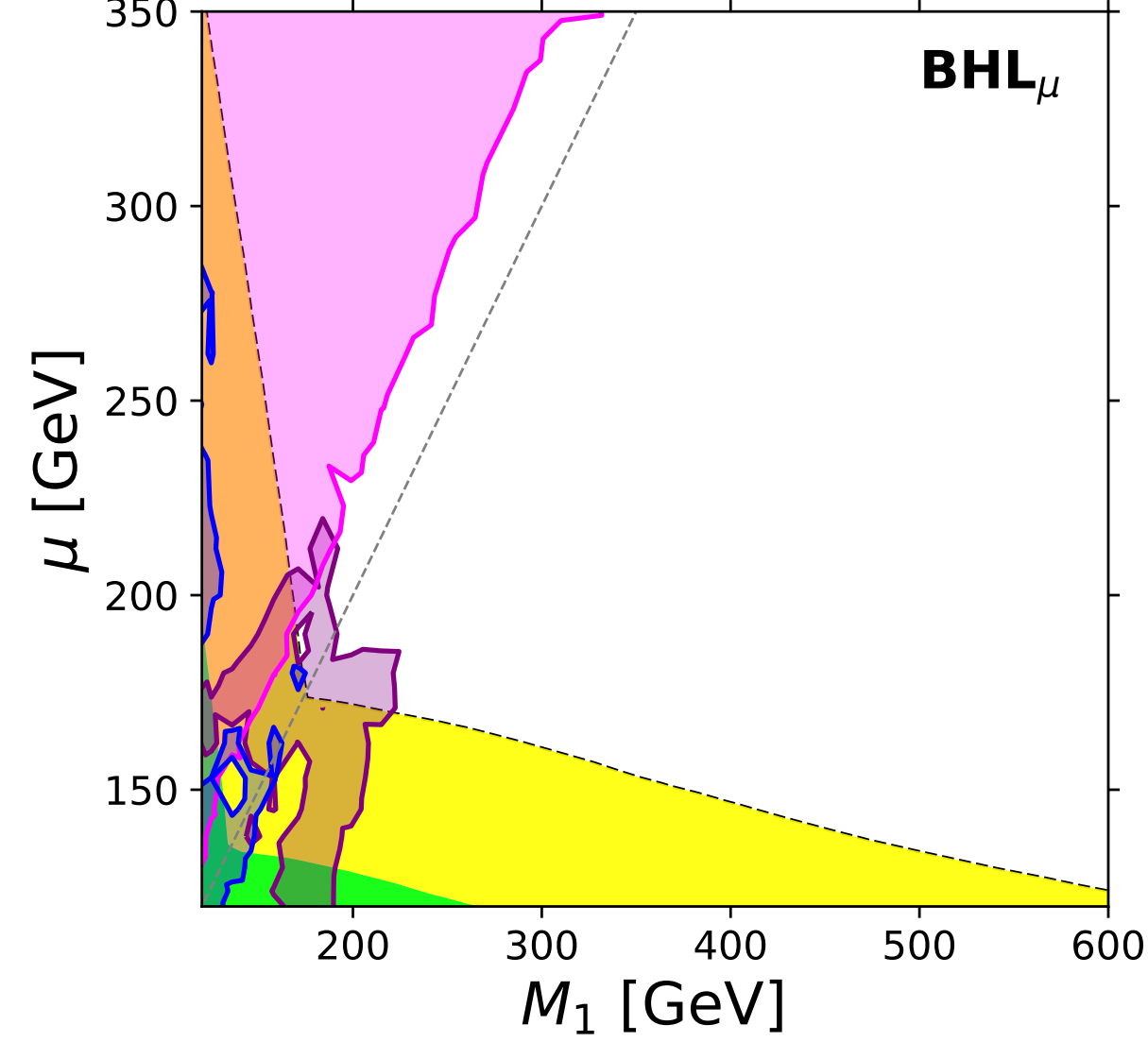


GMSB with slepton/sneutrino/stau NLPS

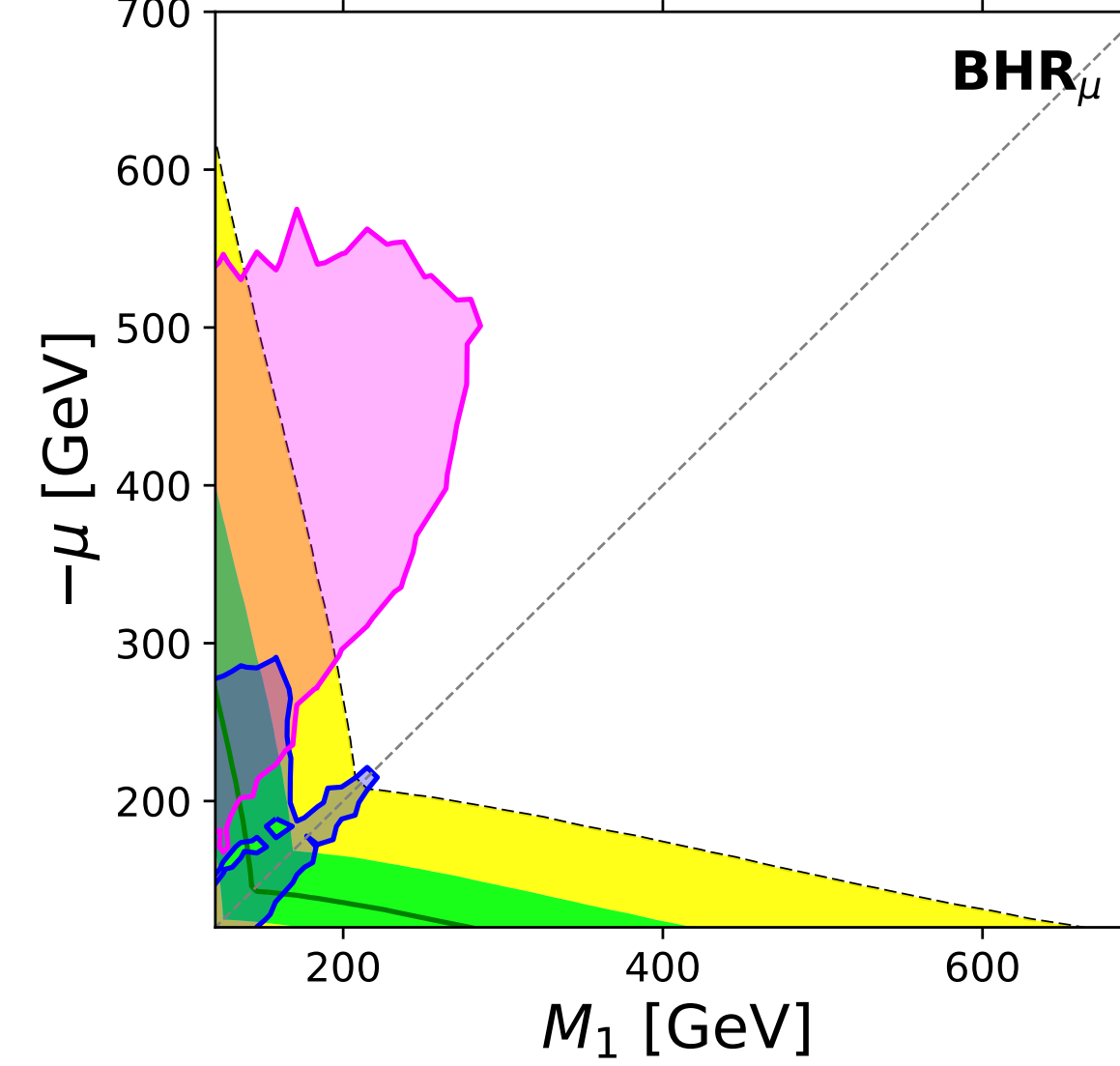
$\tilde{m}_{l_L} = \min(M_2, |\mu|) - 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_R} = M_1 = 10\text{TeV}$



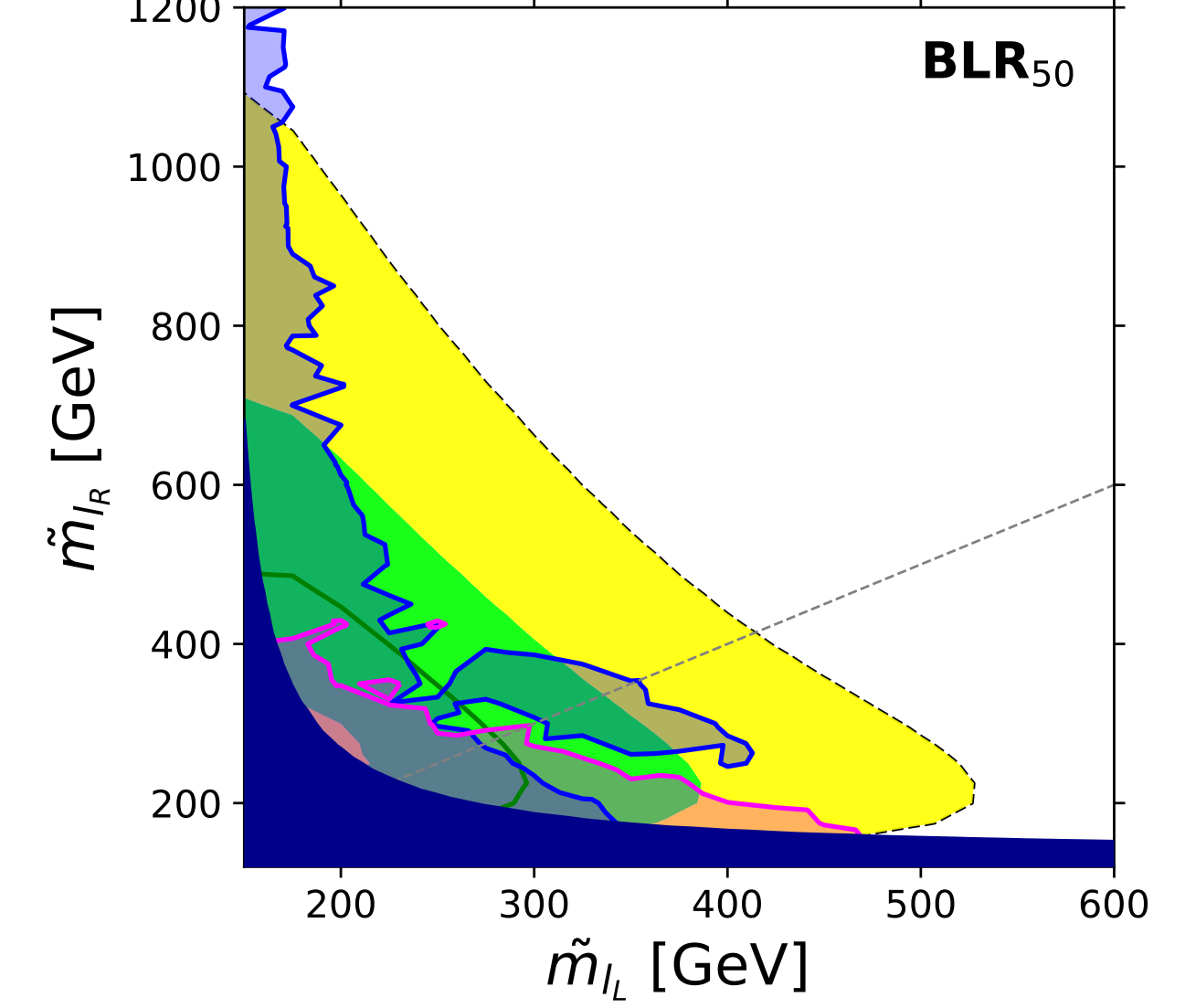
$\tilde{m}_{l_L} = \min(M_1, |\mu|) - 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_R} = M_2 = 10\text{TeV}$



$\tilde{m}_{l_R} = \min(M_1, |\mu|) - 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_L} = M_2 = 10\text{TeV}$

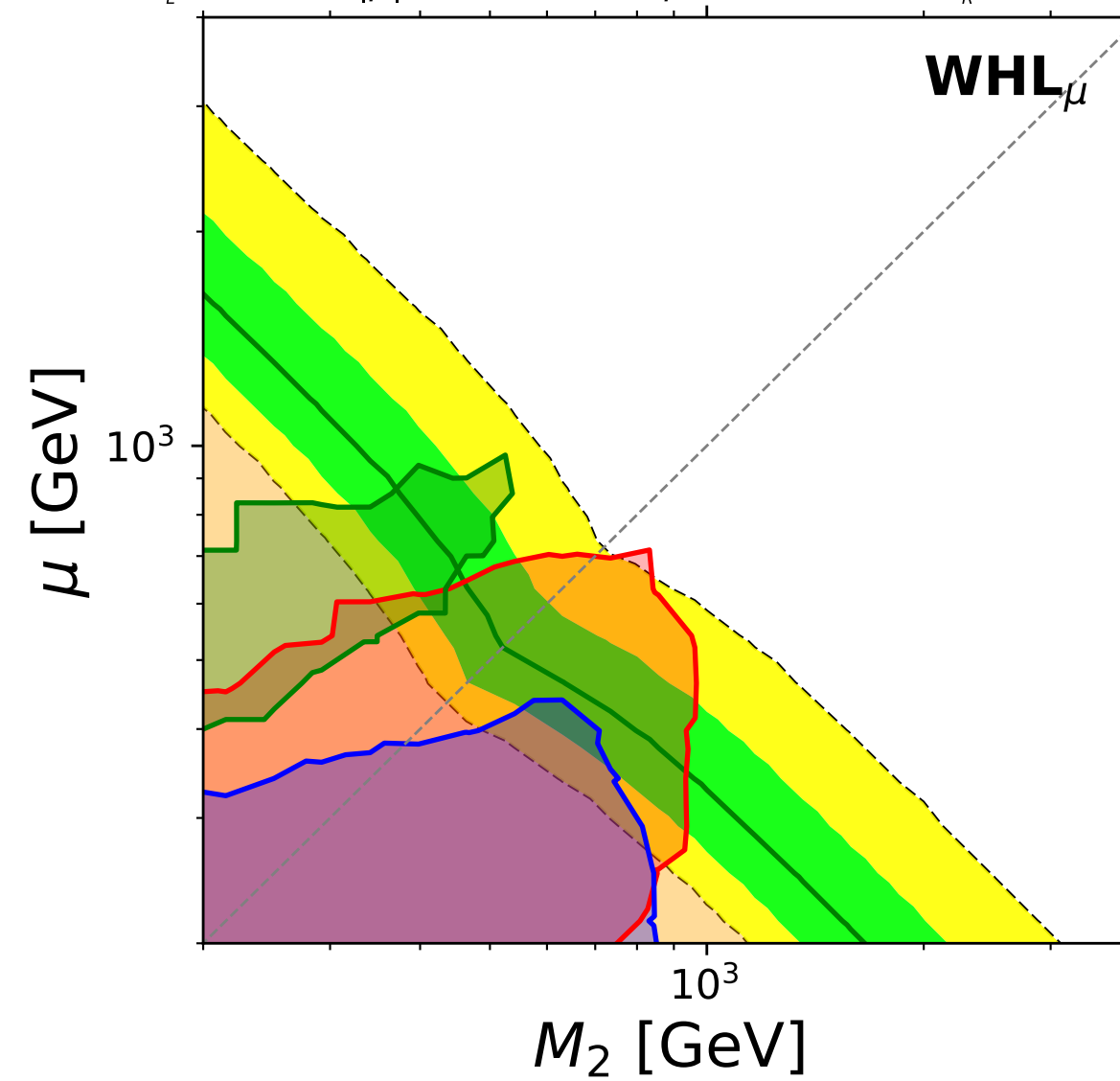


$M_1 = \tilde{m}_{\tilde{\tau}_1} - 20\text{GeV}$, $\mu = \mu_{\max}$, $\tan\beta = 50$, $A = 0$, $M_2 = 10\text{TeV}$

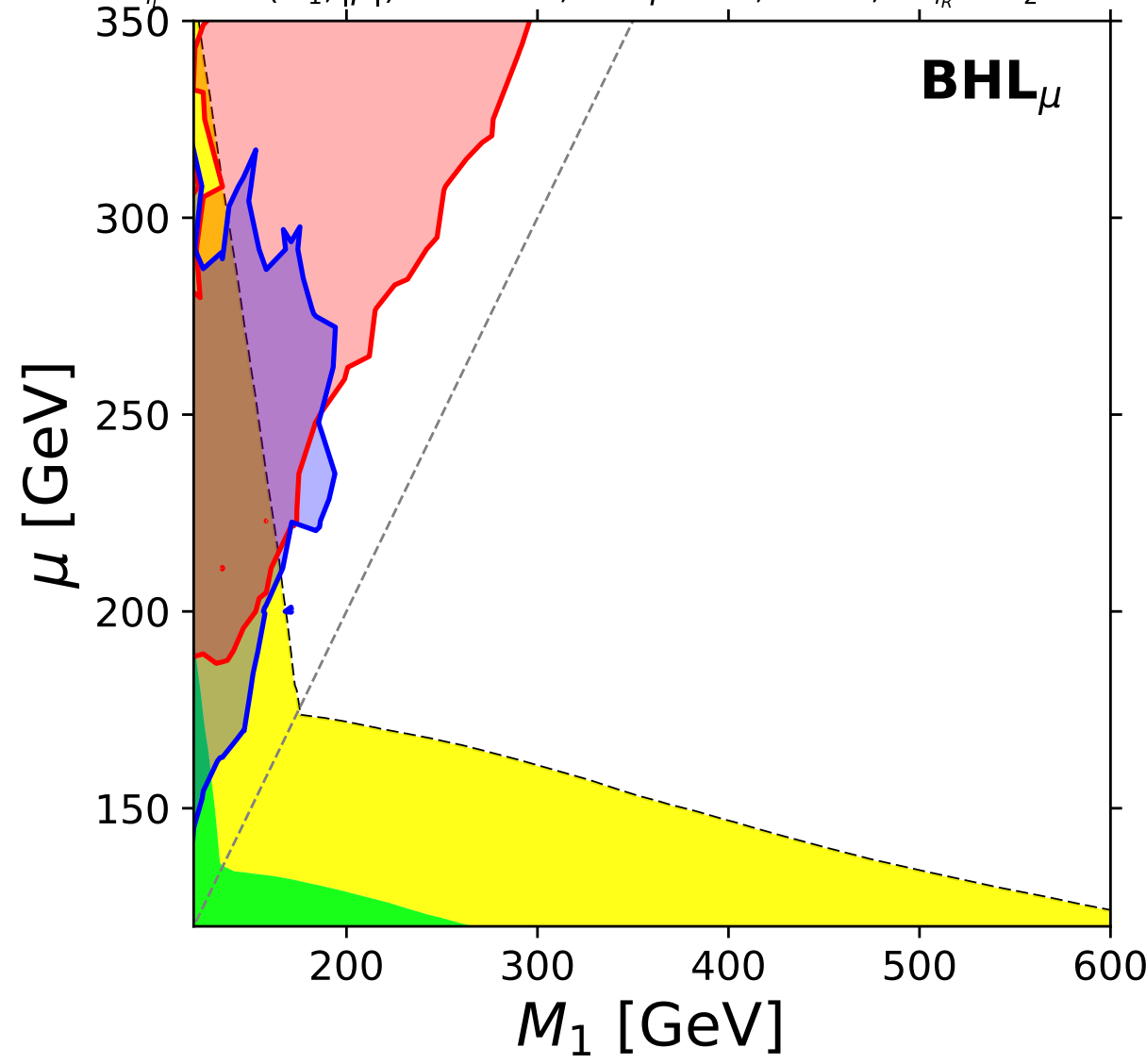


UDD RPV

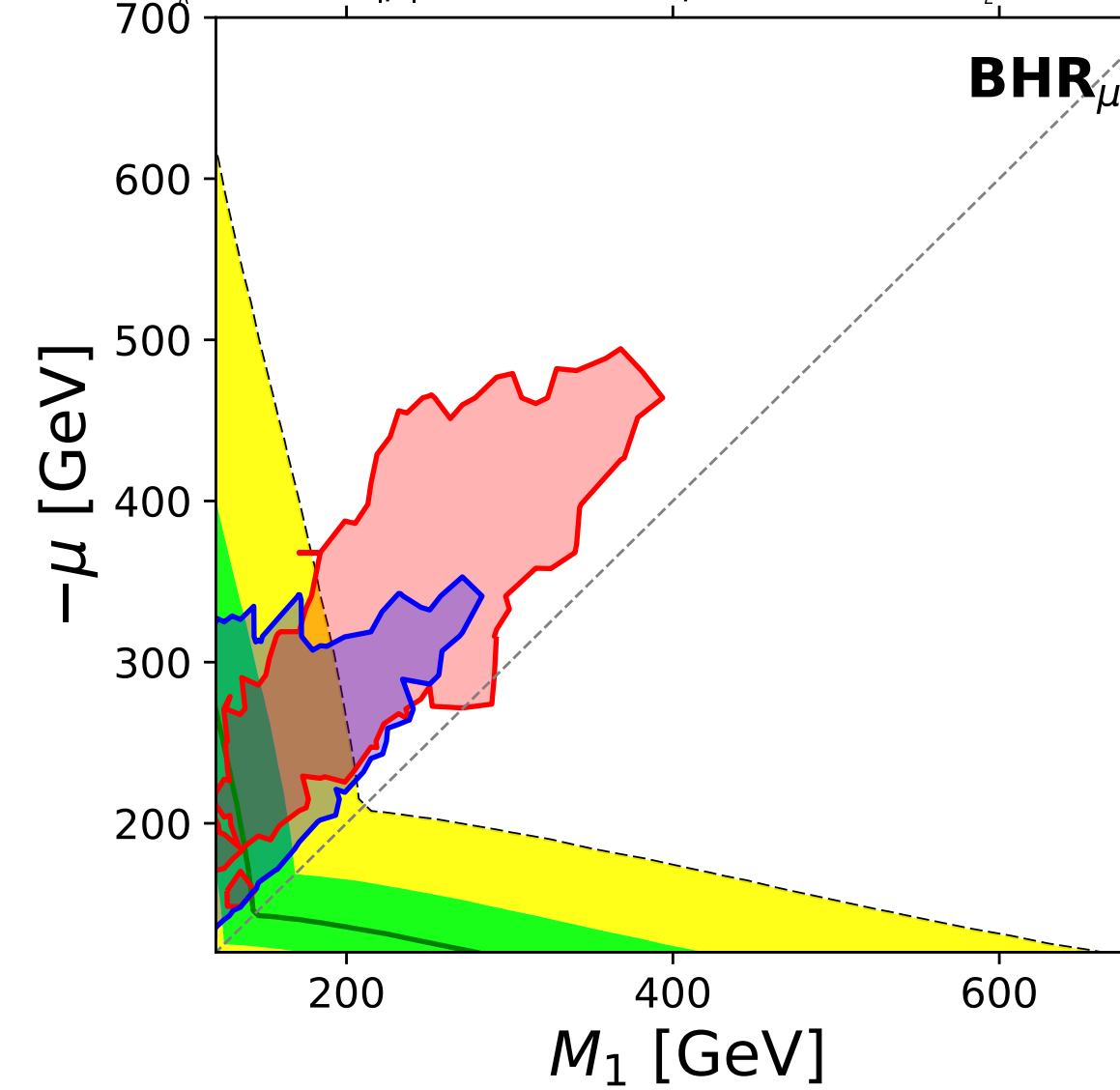
$\tilde{m}_{l_L} = \min(M_2, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_R} = M_1 = 10\text{TeV}$



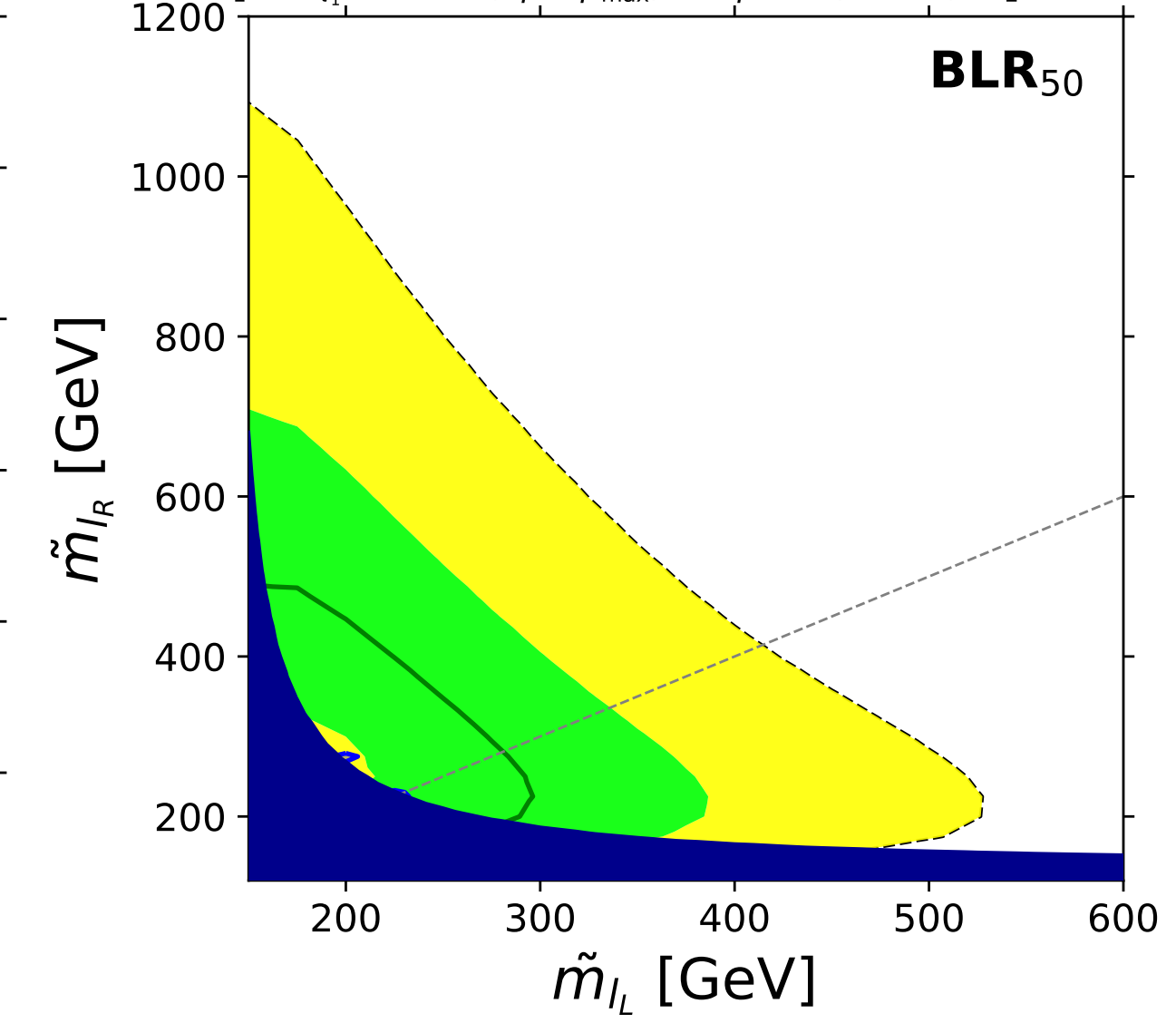
$\tilde{m}_{l_L} = \min(M_1, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_R} = M_2 = 10\text{TeV}$



$\tilde{m}_{l_R} = \min(M_1, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_{l_L} = M_2 = 10\text{TeV}$



$M_1 = \tilde{m}_{\tilde{\tau}_1} - 20\text{GeV}$, $\mu = \mu_{\max}$, $\tan\beta = 50$, $A = 0$, $M_2 = 10\text{TeV}$



Summary

⊗ There is a 4.2σ discrepancy for $(g-2)_\mu$ between experiment and SM prediction

⊗ SUSY can explain $(g-2)_\mu$, but:

⊗ $\tilde{\chi}_1^0$ is LSP and stable \implies constraint from large E_T^{miss}

⊗ $|\mu| \approx M_1 (M_2) \implies$ constraint from DM-DD experiments

⊗ slepton and Bino are light \implies DM overproduction

⊗ If $\tilde{\chi}_1^0$ is not stable LSP, DM constraints go away, and LHC signature changes:

⊗ RPV with UDD \implies LHC constraints from multijet + lepton

⊗ Gravitino LSP with $\tilde{\chi}_1^0$ NLSP \implies $(g-2)_\mu$ region excluded by $\gamma + E_T^{\text{miss}}$ channel

⊗ Gravitino LSP with $\tilde{l}/\tilde{\nu}/\tilde{\tau}$ NLSP \implies LHC constraints from soft lepton/tau



Thank you for attention!

r.maselek@uw.edu.pl

Dolina Chochołowska, Poland
photo by Piotr Kałuża

Backup slides

Tension between experiment and white paper SM calculations

$$a_{\mu}^{exp} - a_{\mu}^{SM} = (25 \pm 6) \times 10^{-10} \sim \mathcal{O} \left(\Delta a_{\mu}^{SM,EW} \right)$$

We need **very light BSM particles** OR **enhancement from coupling**

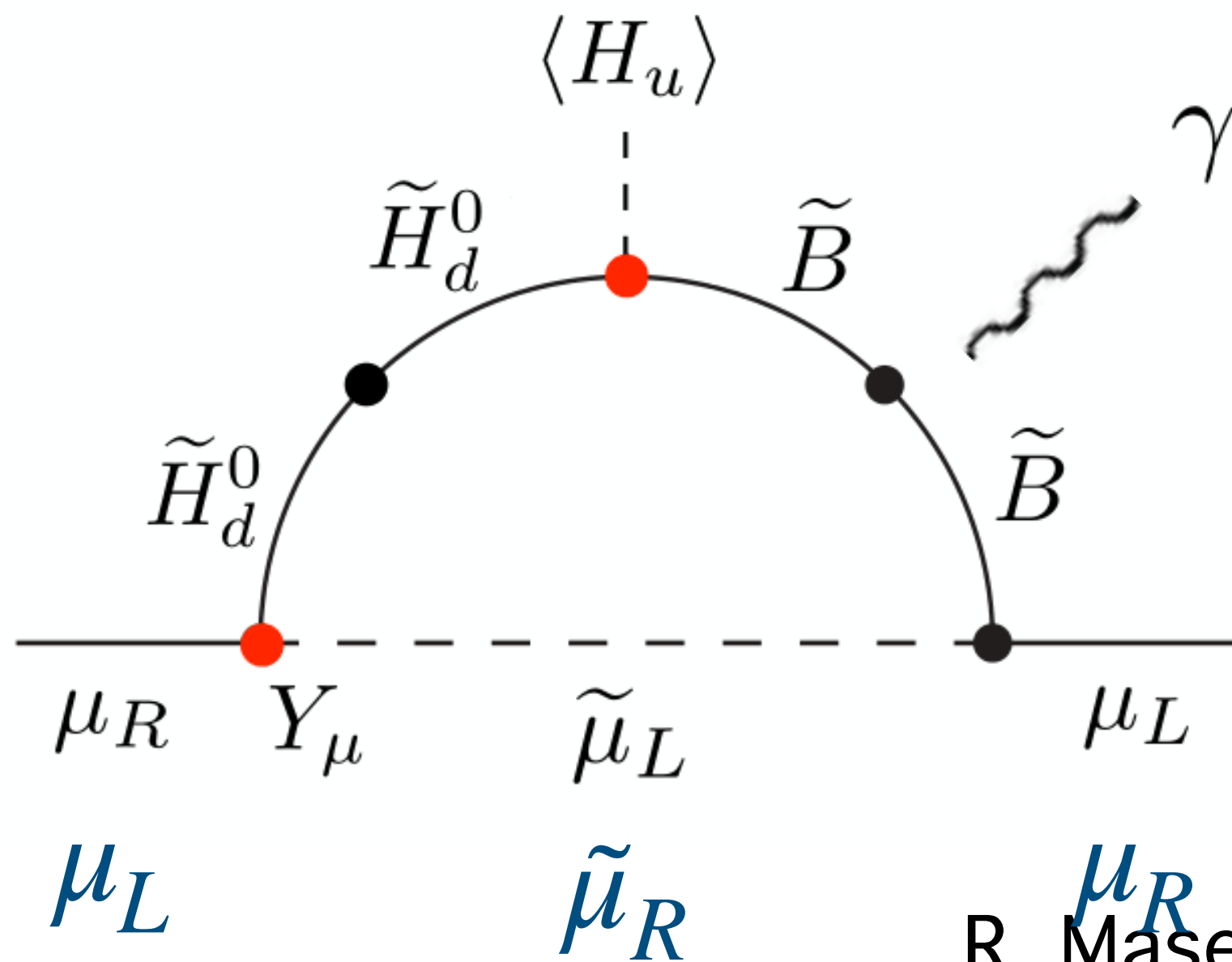
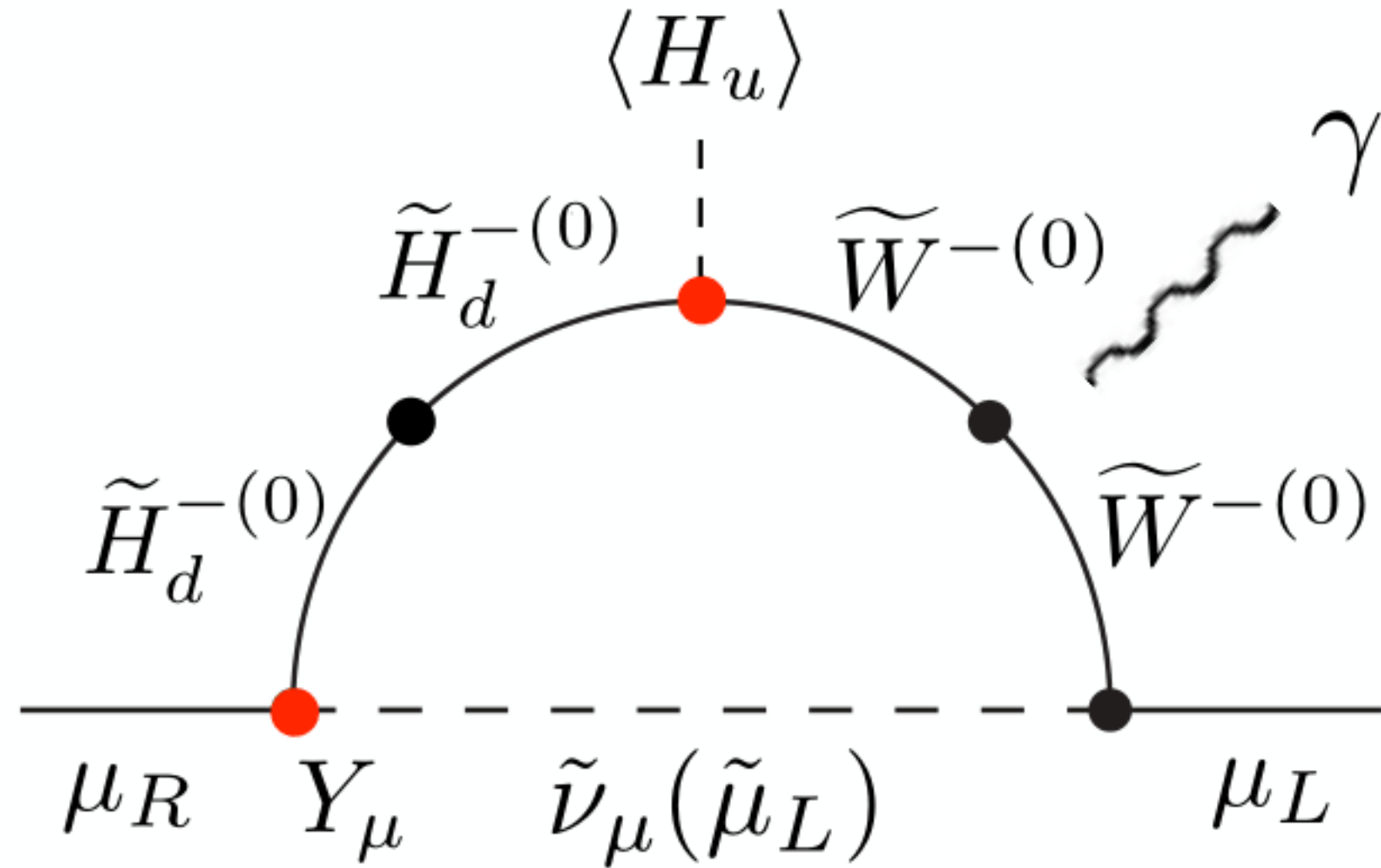
$$\Delta a_{\mu}^{BSM} \sim \Delta a_{\mu}^{SM,EW} \cdot \left(\frac{m_W^2}{m_{BSM}^2} \right) \cdot \text{coupling}$$

$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$

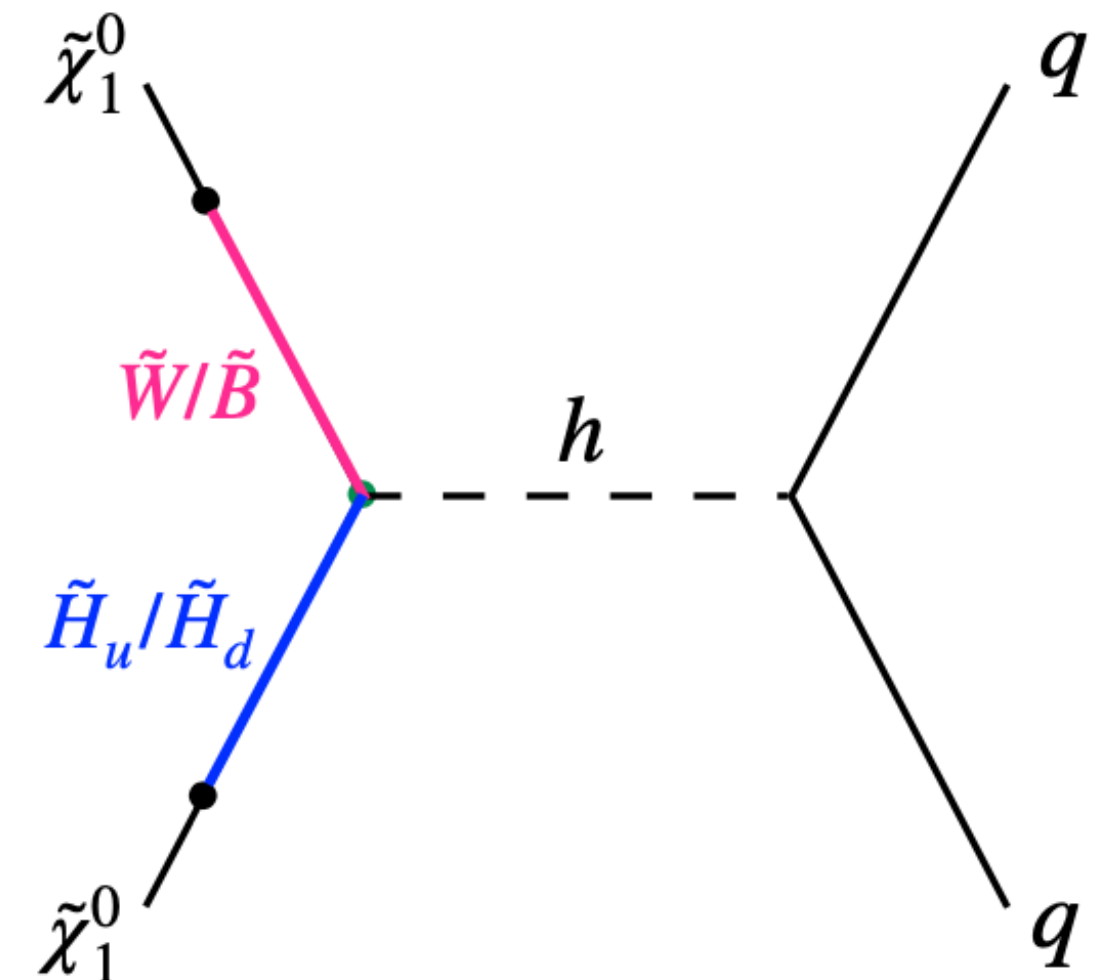
$$\Delta a_\mu^{\text{WHL}}(M_2, \mu, m_{\tilde{l}_L}) = + \frac{\alpha_W}{8\pi} \frac{m_\mu^2}{\mu M_2} \tan \beta \cdot f_{\text{WHL}}(\mathbf{m})$$

$$\Delta a_\mu^{\text{BHL}}(M_1, \mu, m_{\tilde{l}_L}) = + \frac{\alpha_Y}{8\pi} \frac{m_\mu^2}{\mu M_1} \tan \beta \cdot f_{\text{BHL}}(\mathbf{m})$$

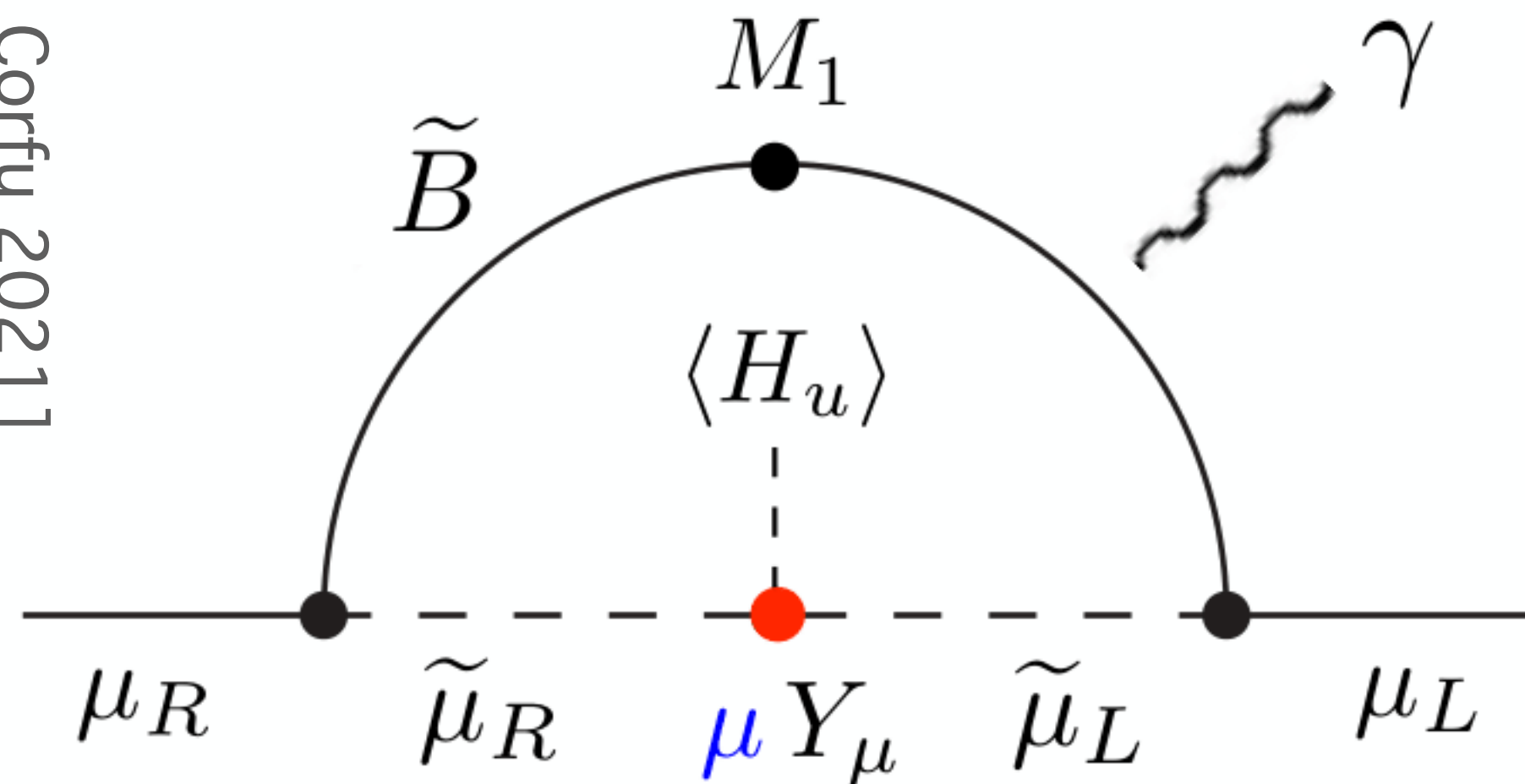
$$\Delta a_\mu^{\text{BHR}}(M_1, \mu, m_{\tilde{l}_R}) = - \frac{\alpha_Y}{8\pi} \frac{m_\mu^2}{\mu M_1} \tan \beta \cdot f_{\text{BHR}}(\mathbf{m})$$



Large gaugino-Higgsino mixing leads to a large cross-section for DM Direct detection



$$\Delta a_\mu^{\text{SUSY}} = \Delta a_\mu^{\text{WHL}} + \Delta a_\mu^{\text{BHL}} + \Delta a_\mu^{\text{BHR}} + \Delta a_\mu^{\text{BLR}}$$



$$\Delta a_\mu^{\text{BLR}}(M_1, m_{\tilde{l}_L}, m_{\tilde{l}_R}; \mu) = + \frac{\alpha_Y}{4\pi} m_\mu^2 \frac{\mu M_1}{m_{\tilde{\mu}_L}^2 m_{\tilde{\mu}_R}^2} \tan \beta \cdot f_{\text{BLR}}(\mathbf{m})$$

large μ needed

Stau mass squared becomes too small or even negative!

$$M_{\tilde{\tau}}^2 \sim \begin{pmatrix} m_{\tilde{\tau}_R}^2 & Y_\tau \mu \langle H_u \rangle \\ Y_\tau \mu \langle H_u \rangle & m_{\tilde{\tau}_L}^2 \end{pmatrix}$$

Constraints on staus:

⊗ charge breaking vacuum: $m_{\tilde{\tau}_1}^2 > 0$

⊗ LEP bound: $m_{\tilde{\tau}_1} > 81.9 \text{ GeV}$

⊗ stau LSP: $m_{\tilde{\tau}_1} > m_{\tilde{\chi}_1^0}$

⊗ vacuum (meta-)stability

Parameter planes definition

name	axes	range [TeV]	other parameters	$\tan \beta$
WHL _{μ}	(M_2, μ)	$([0.2, 4], [0.2, 4])$	$\tilde{m}_{l_L} = \min(M_2, \mu) + 20 \text{ GeV}, M_1 = \tilde{m}_{l_R} = 10 \text{ TeV}$	50
WHL _L	(M_2, \tilde{m}_{l_L})	$([0.2, 4], [0.2, 2])$	$\mu = \min(M_2, \tilde{m}_{l_L}) - 20 \text{ GeV}, M_1 = \tilde{m}_{l_R} = 10 \text{ TeV}$	50
BHL _{μ}	(M_1, μ)	$([0.12, 0.6], [0.12, 0.35])$	$\tilde{m}_{l_L} = \min(M_1, \mu) + 20 \text{ GeV}, M_2 = \tilde{m}_{l_R} = 10 \text{ TeV}$	50
BHL _L	(M_1, \tilde{m}_{l_L})	$([0.12, 0.8], [0.14, 0.22])$	$\mu = \min(M_1, \tilde{m}_{l_L}) - 20 \text{ GeV}, M_2 = \tilde{m}_{l_R} = 10 \text{ TeV}$	50
BHR _{μ}	(M_1, μ)	$([0.12, 0.7], [0.12, 0.7])$	$\tilde{m}_{l_R} = \min(M_1, \mu) + 20 \text{ GeV}, M_2 = \tilde{m}_{l_L} = 10 \text{ TeV}$	50
BHR _L	(M_1, \tilde{m}_{l_R})	$([0.12, 0.8], [0.14, 0.25])$	$-\mu = \min(M_1, \tilde{m}_{l_R}) - 20 \text{ GeV}, M_2 = \tilde{m}_{l_L} = 10 \text{ TeV}$	50
BLR ₅₀	$(\tilde{m}_{l_L}, \tilde{m}_{l_R})$	$([0.15, 0.6], [0.12, 1.2])$	$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}, \mu = \mu_{\text{max}}, M_2 = 10 \text{ TeV}$	50
BLR ₁₀	$(\tilde{m}_{l_L}, \tilde{m}_{l_R})$	$([0.15, 0.6], [0.12, 1.2])$	$M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV}, \mu = \mu_{\text{max}}, M_2 = 10 \text{ TeV}$	10

Table 1: The parameter planes and choices of the other parameters. μ_{max} is defined as the maximum value allowed by the vacuum stability constraint.

For GMSB we modify the planes to ensure that slepton/stau/sneutrino is the NLSP.

ATLAS DT [2201.02472]

ATLAS soft- l [1911.12606]

CMS $l+l-$ [2004.05153]

XENON1T [1805.12562]

ATLAS jets + E_T^{miss}

[ATLAS-CONF-2019-040]

CMS multilepton [1709.05406]

ATLAS multijet+ l [2106.09609]

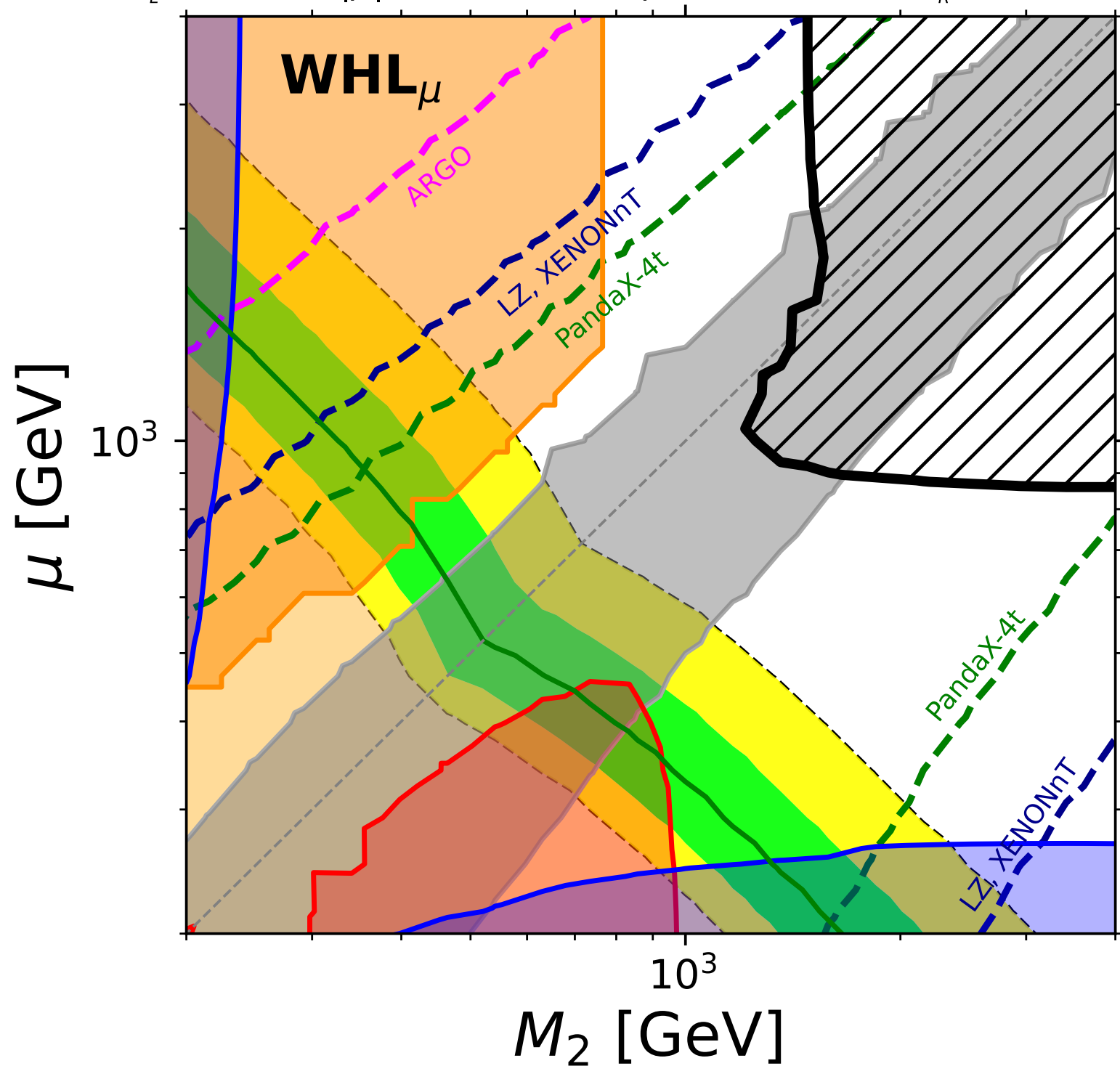
CMS soft $l+l-$

[1801.01846]

CMS multilepton

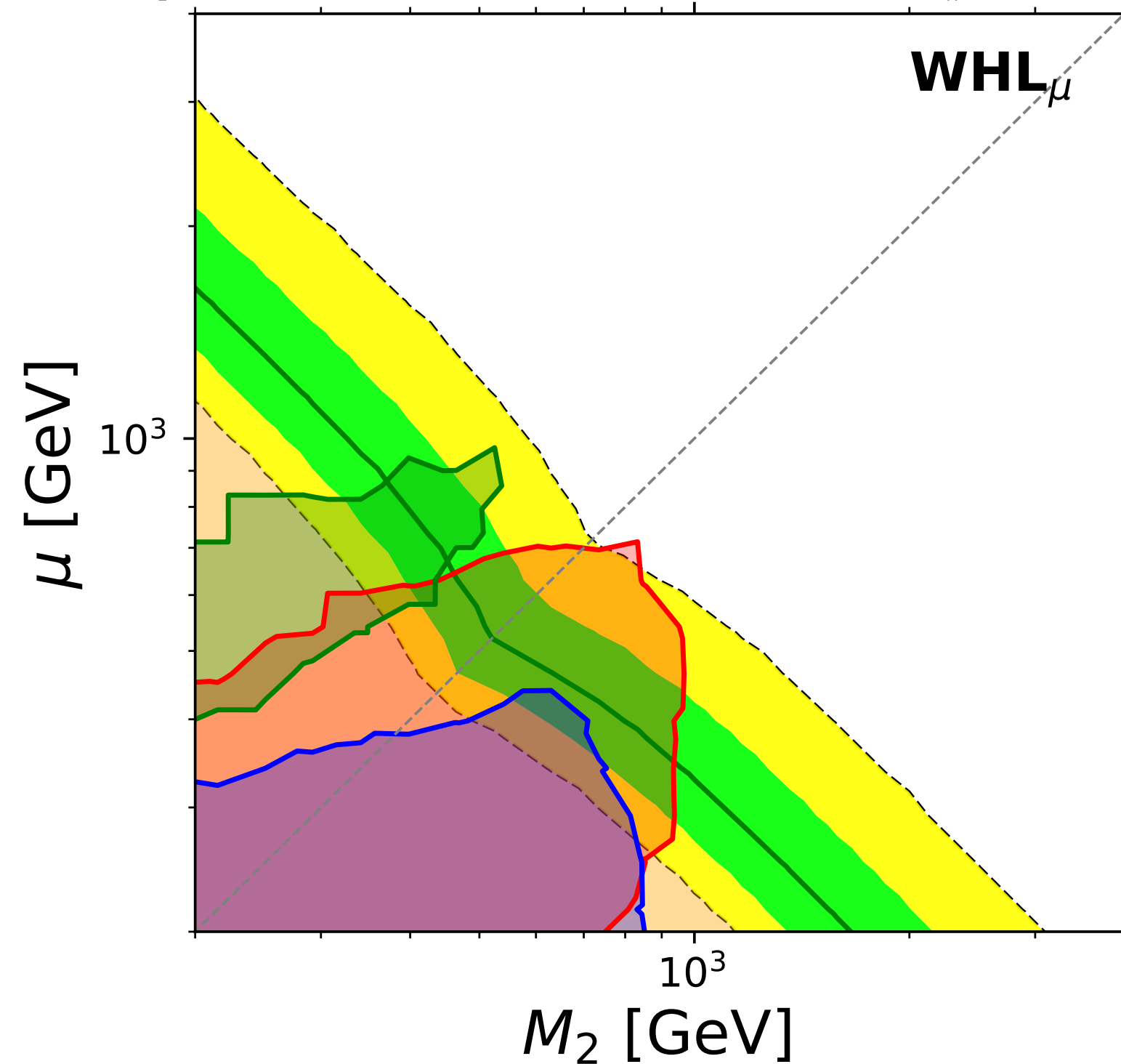
[1709.05406]

$\tilde{m}_L = \min(M_2, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_R = M_1 = 10\text{TeV}$



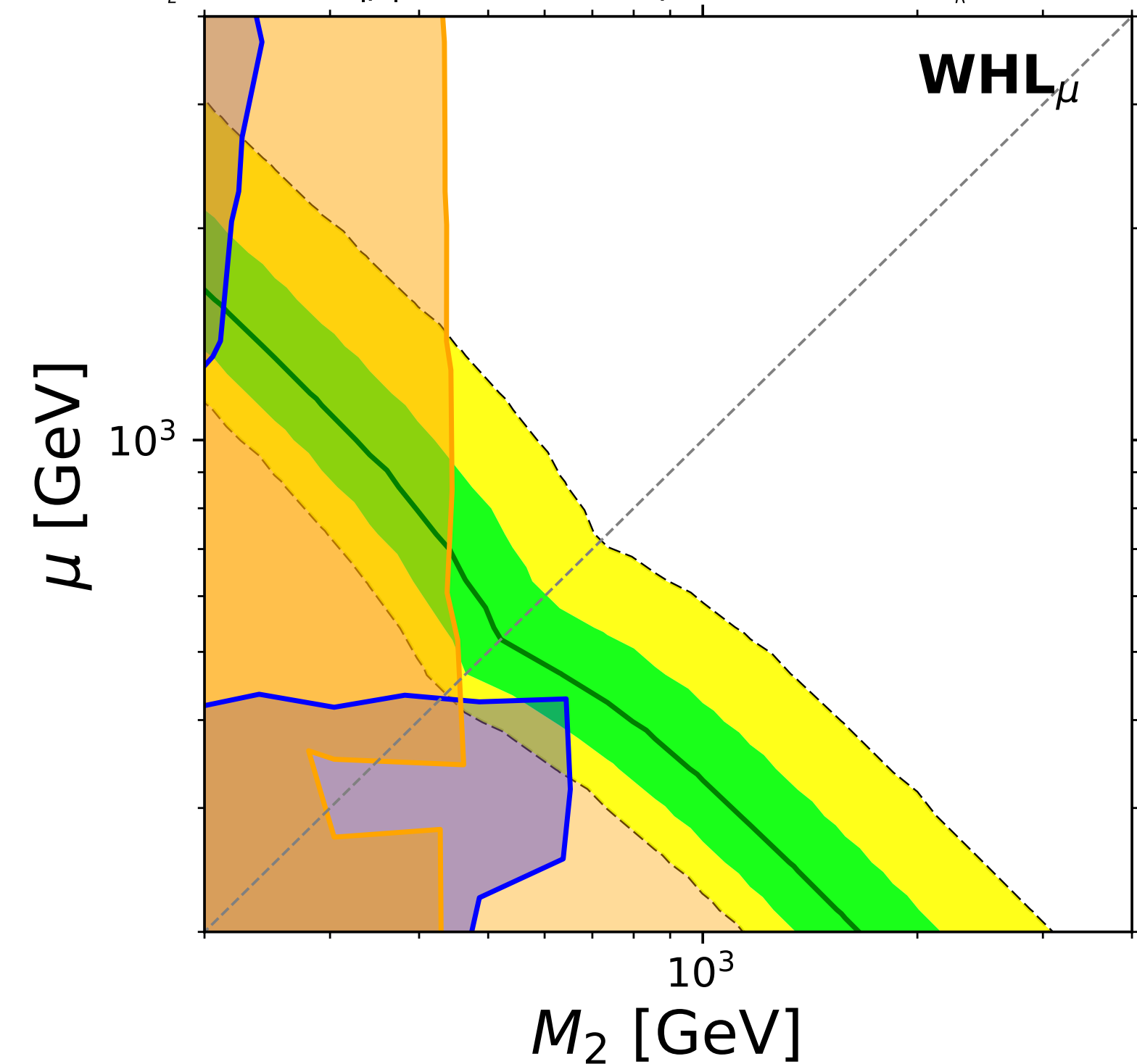
MSSM

$\tilde{m}_L = \min(M_2, |\mu|) + 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_R = M_1 = 10\text{TeV}$



RPV

$\tilde{m}_L = \min(M_2, |\mu|) - 20\text{GeV}$, $\tan\beta = 50$, $A = 0$, $\tilde{m}_R = M_1 = 10\text{TeV}$



GMSB

WHL $_{\mu}$

ATLAS soft-I [1911.12606]

CMS I+I- [2004.05153]

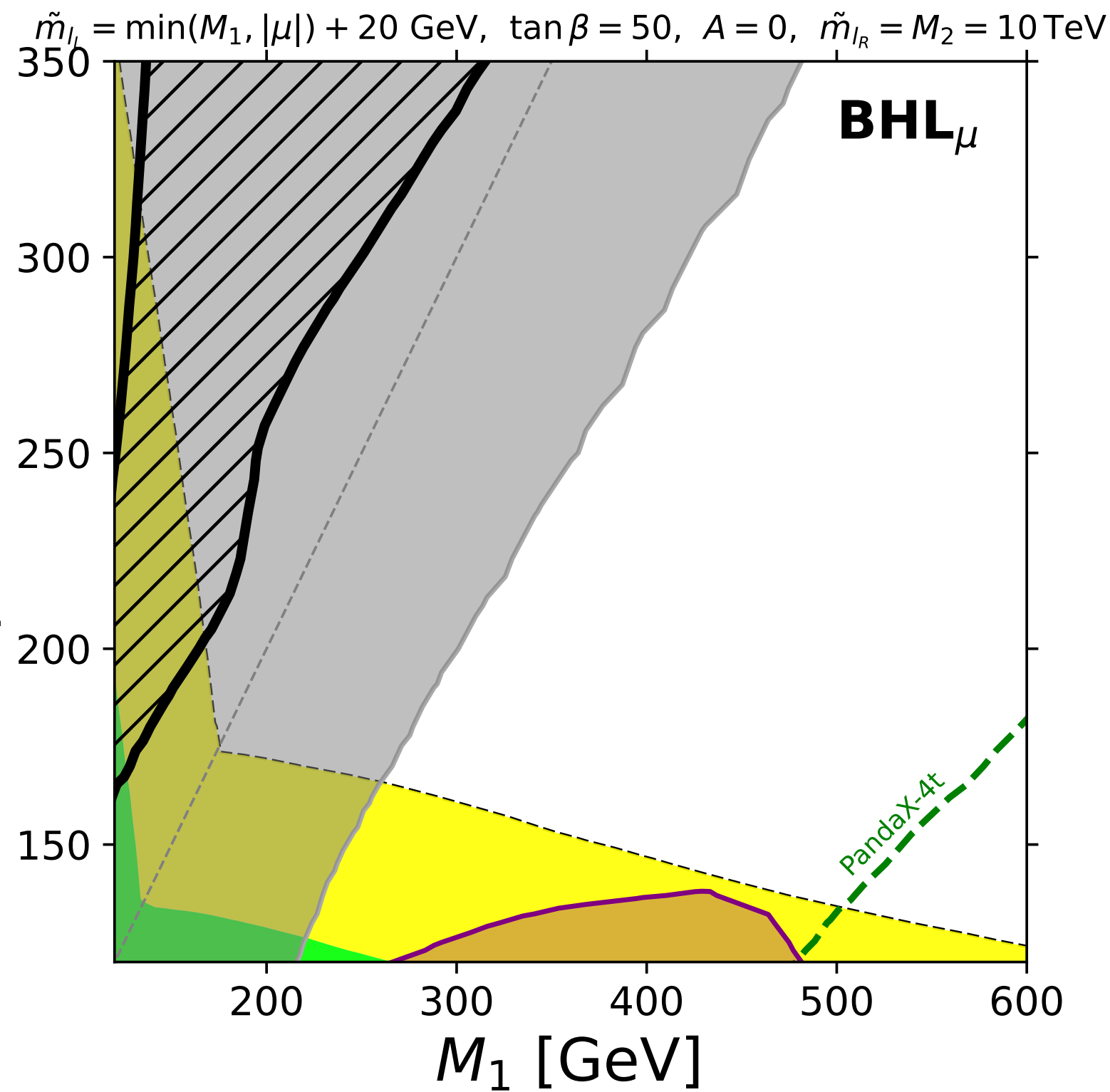
XENON1T [1805.12562]

CMS multilepton [1709.05406]

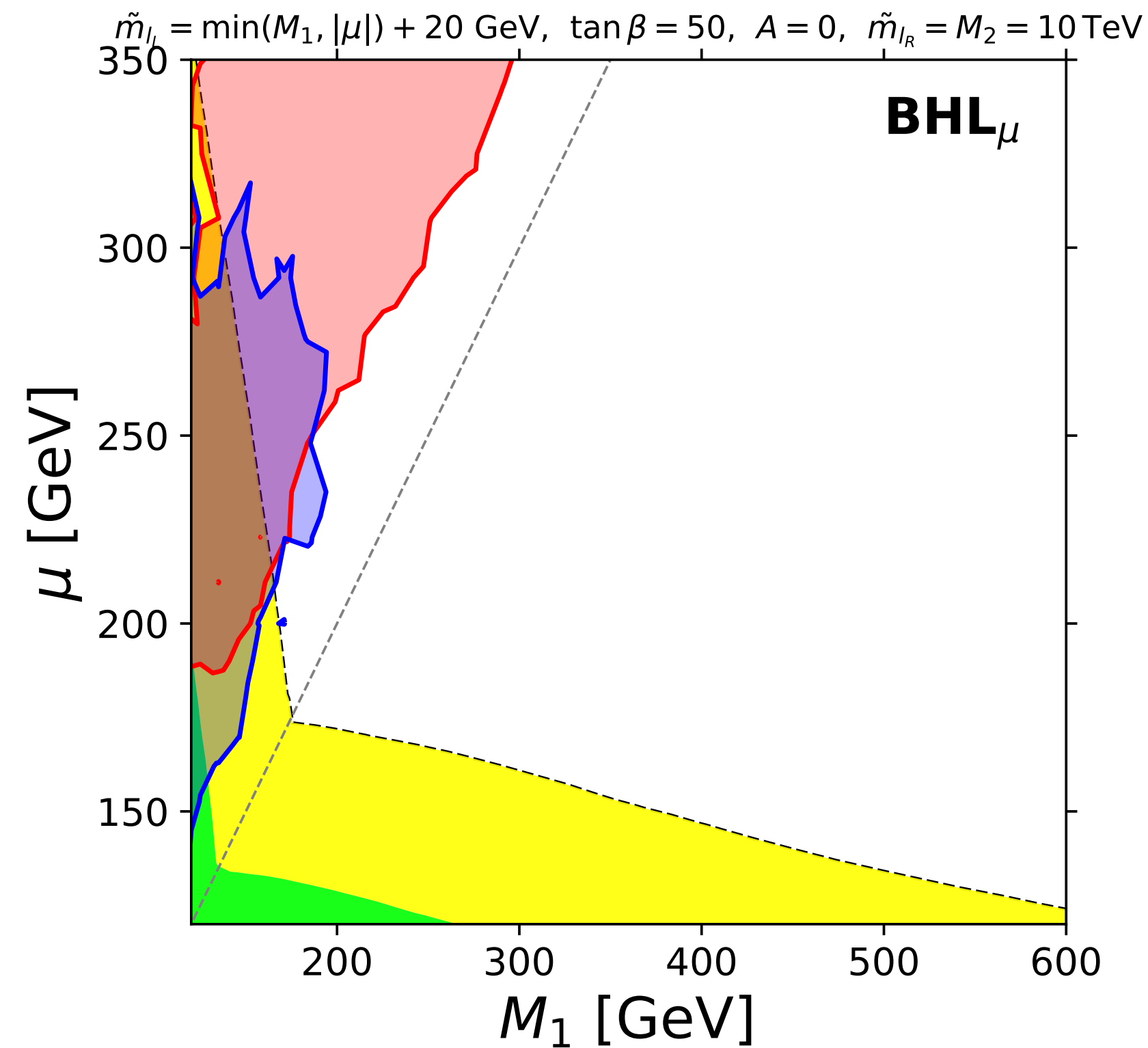
ATLAS multijet+I [2106.09609]

ATLAS soft-I [1712.08119]

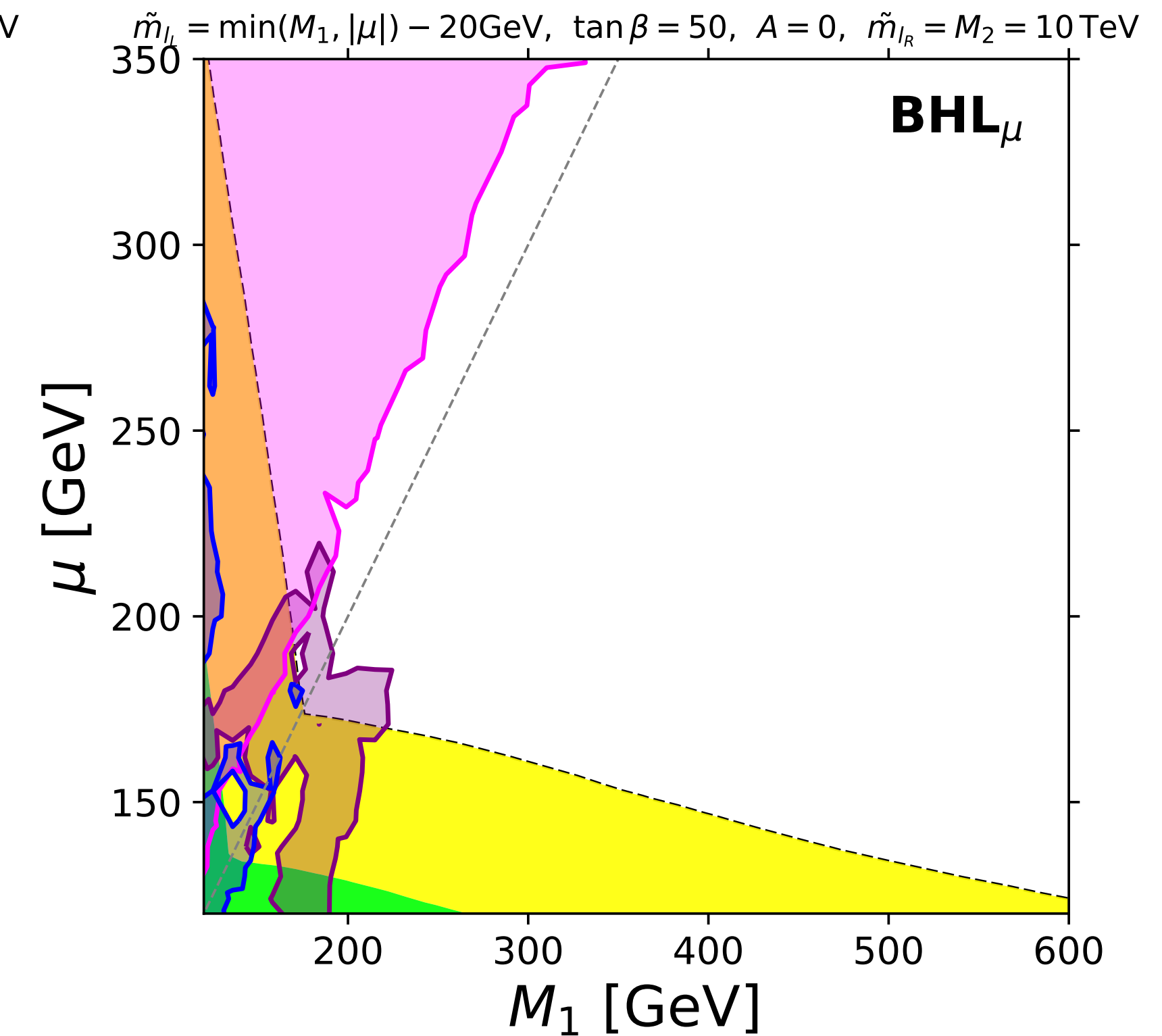
ATLAS $\tau^+\tau^-$
[1911.06660]



MSSM



RPV



GMSB

BHL $_{\mu}$

CMS multilepton

[1709.05406]

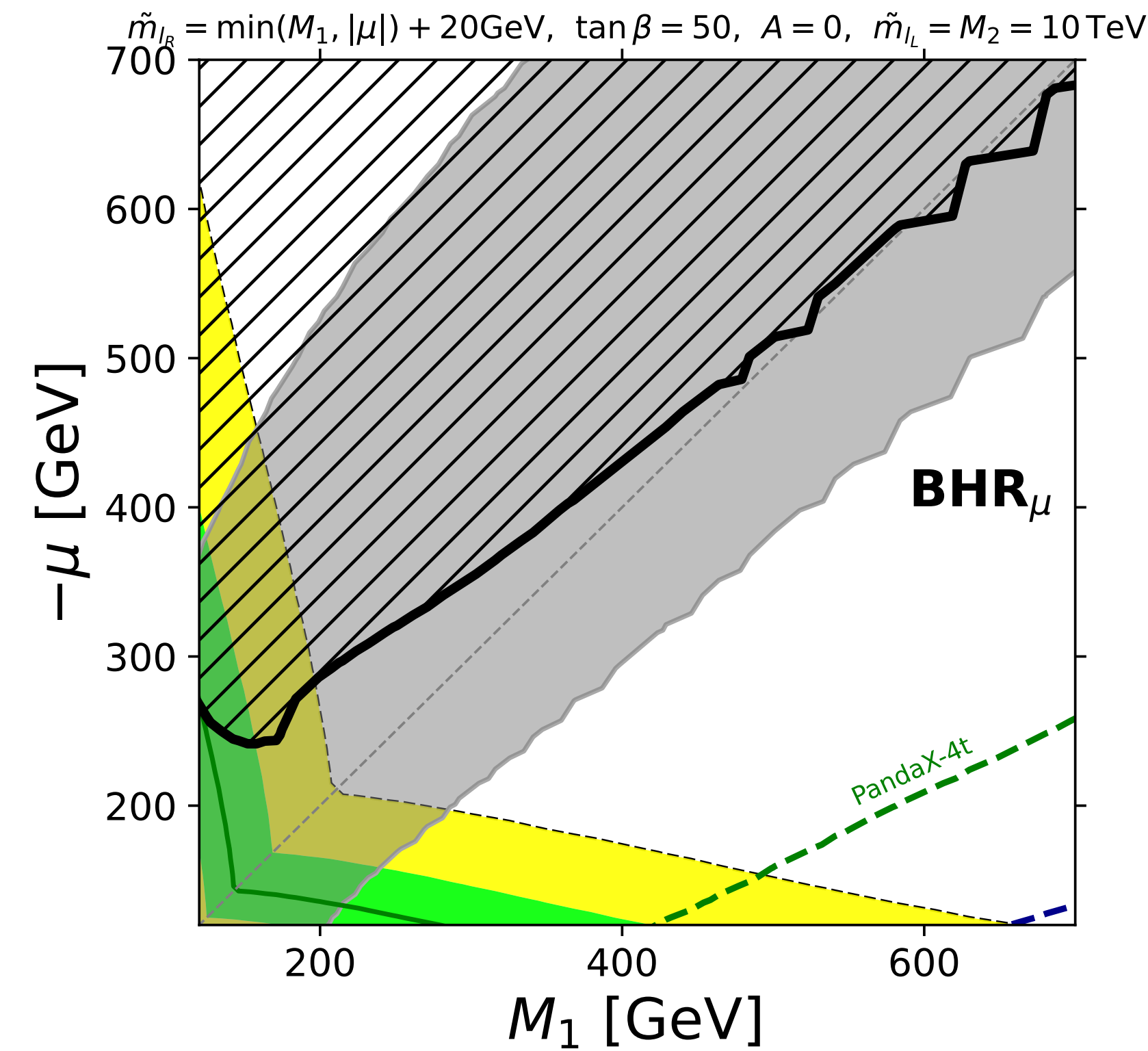
ATLAS $\tau^+\tau^-$

[1911.06660]

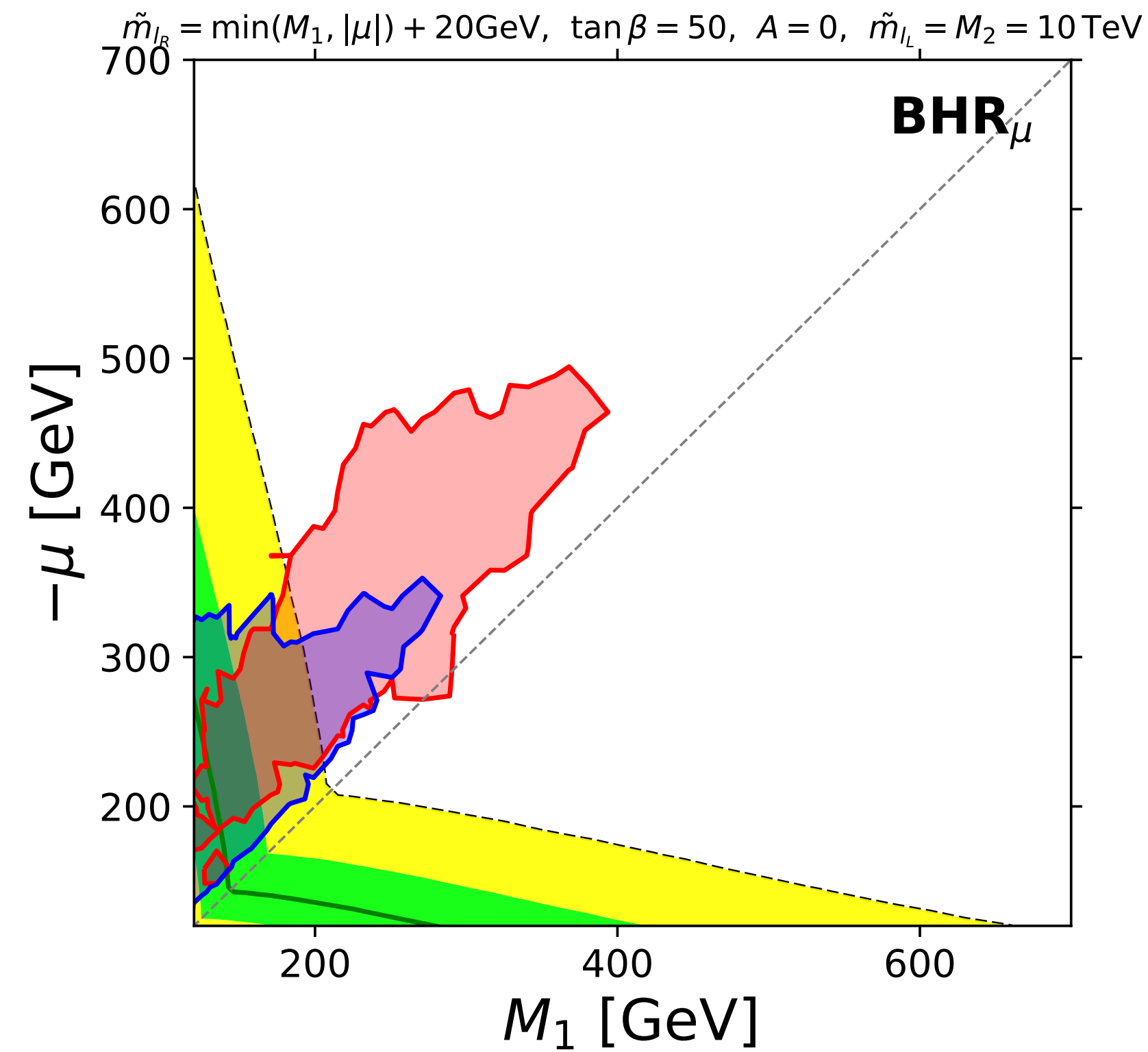
CMS multilepton [1709.05406]

ATLAS multijet+l [2106.09609]

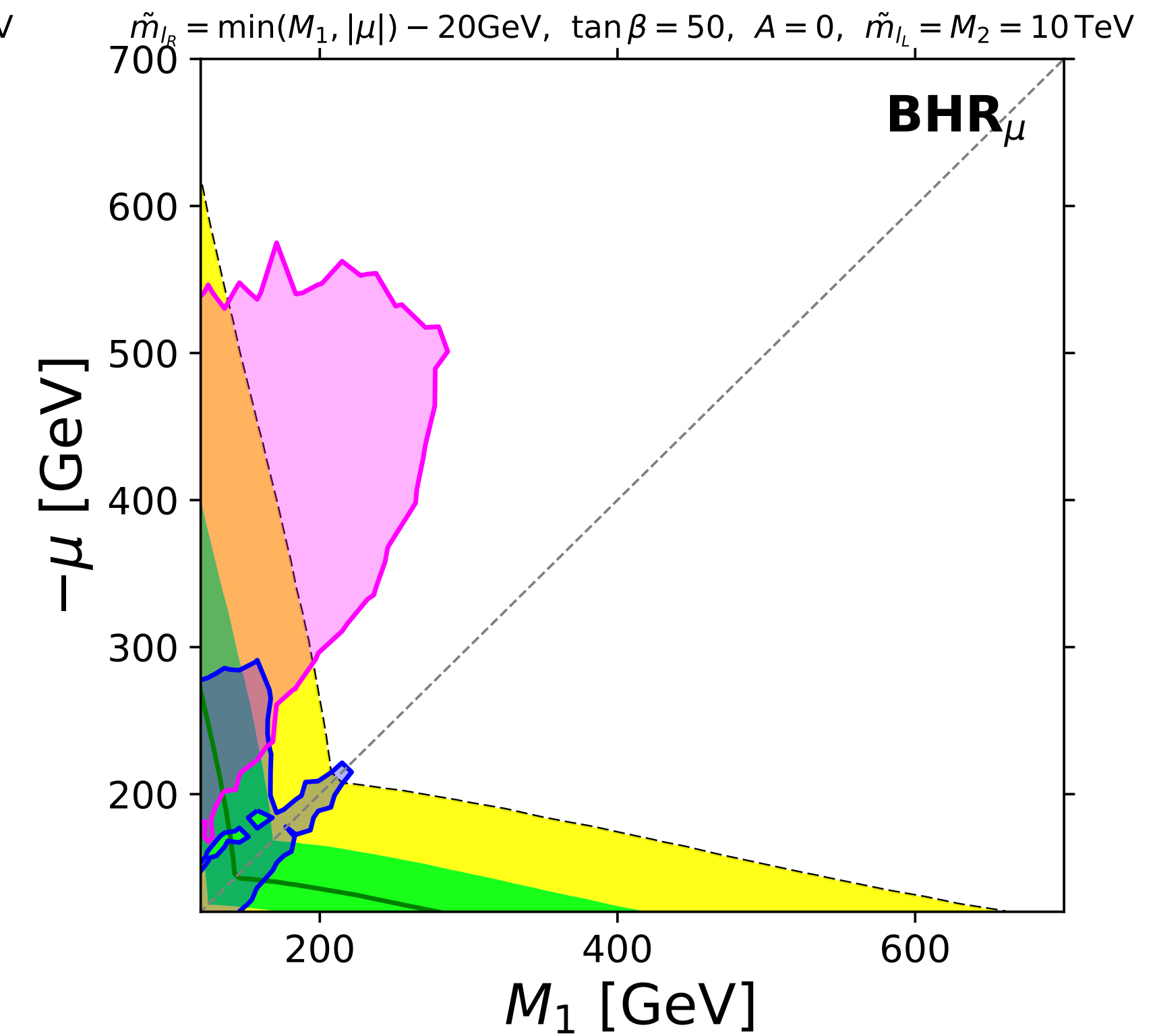
XENON1T [1805.12562]



MSSM



RPV



GMSB

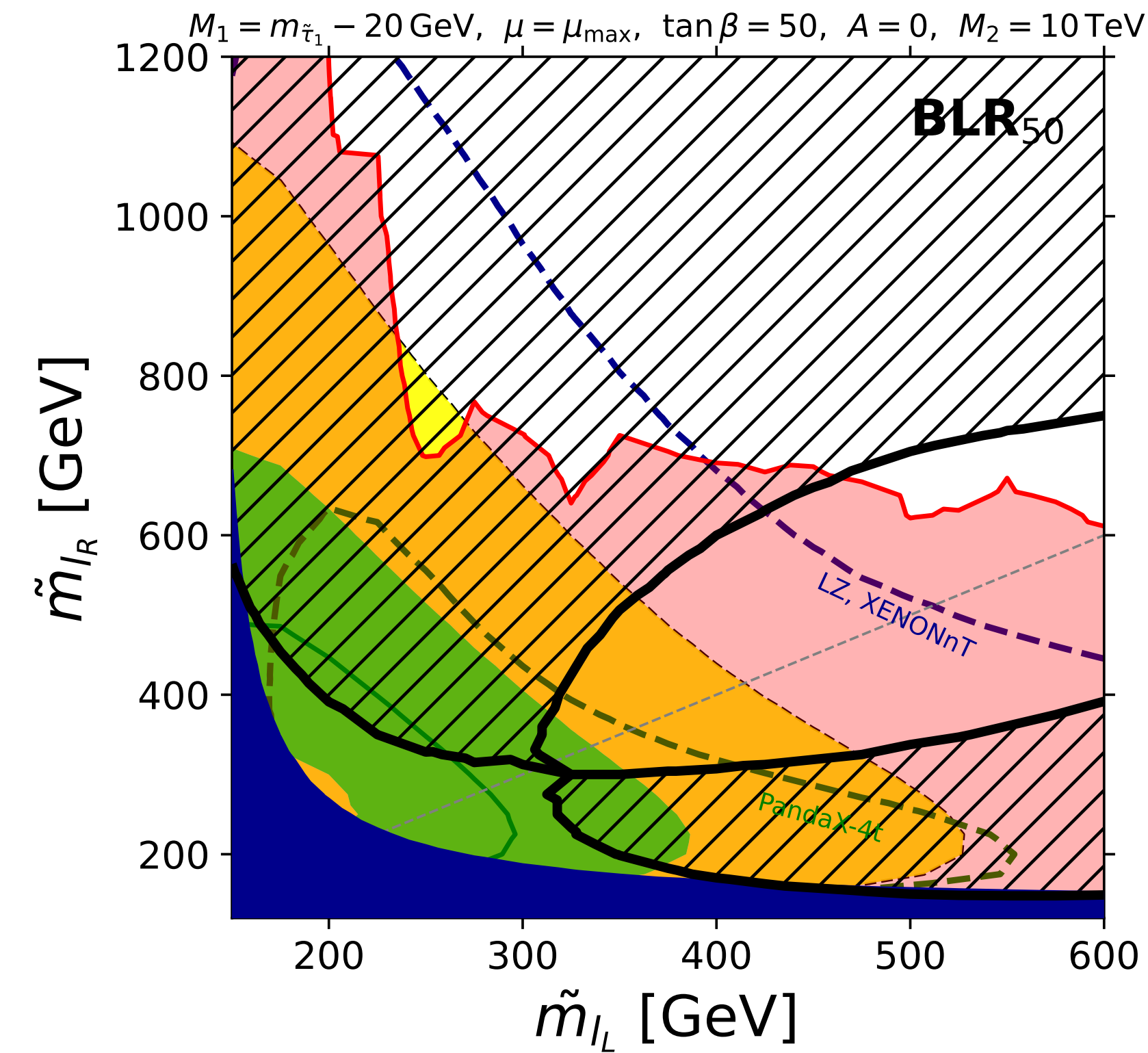
BHR $_{\mu}$

LEP stau mass bound

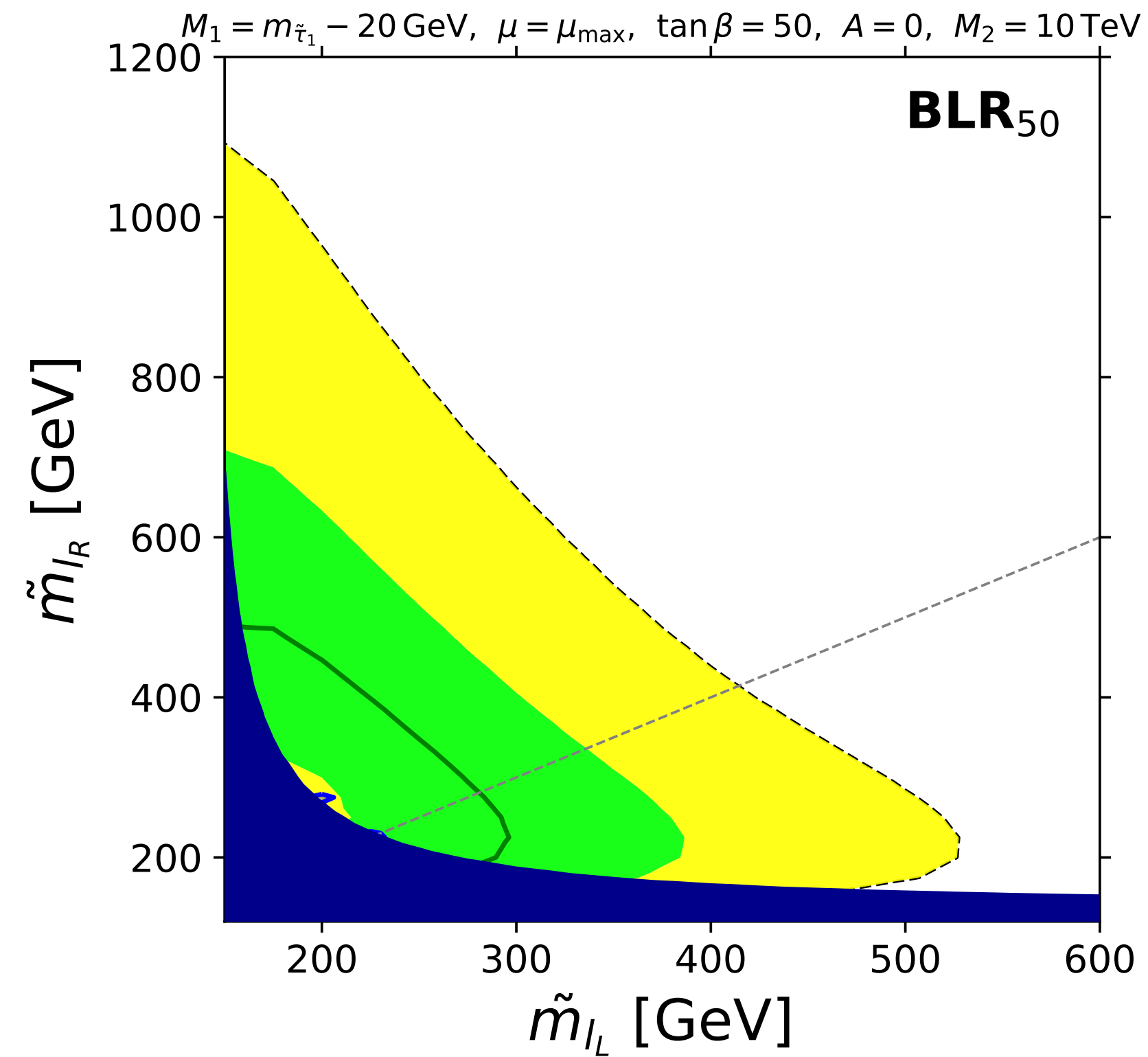
CMS $|\tau\tau|$ [2004.05153]

XENON1T [1805.12562]

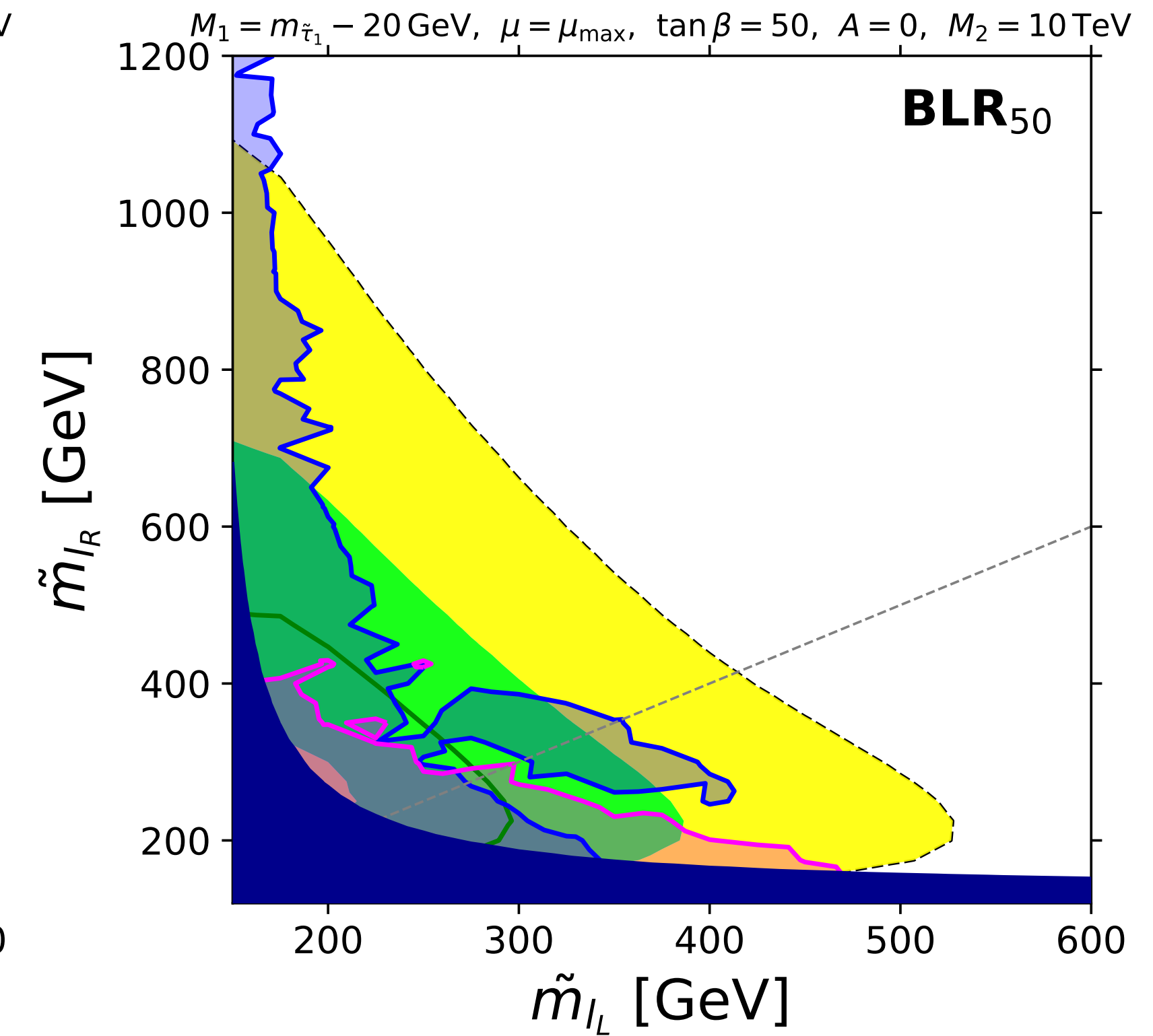
CMS multilepton
[1709.05406]



MSSM



RPV



GMSB

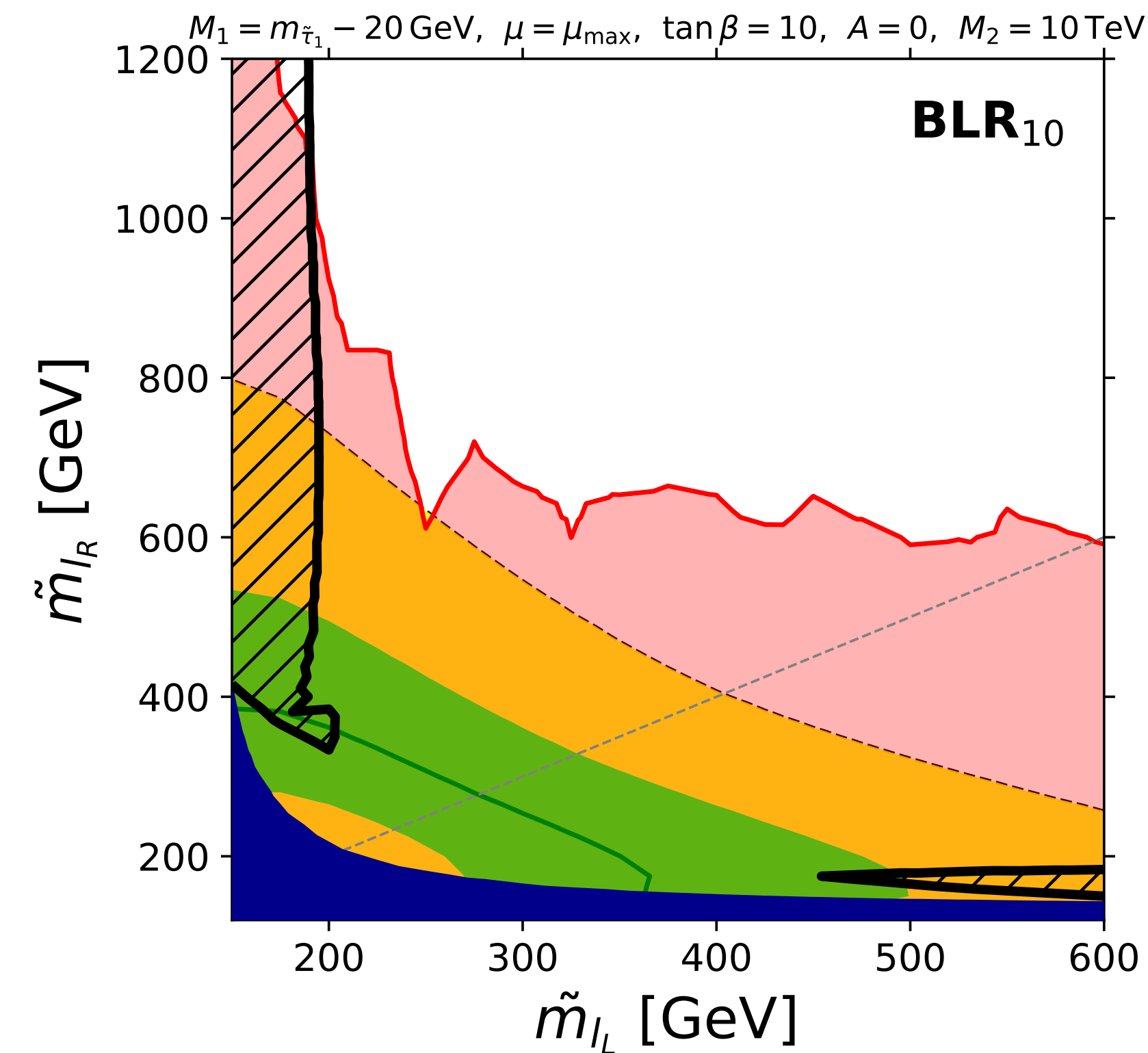
BLR₅₀

LEP stau mass bound

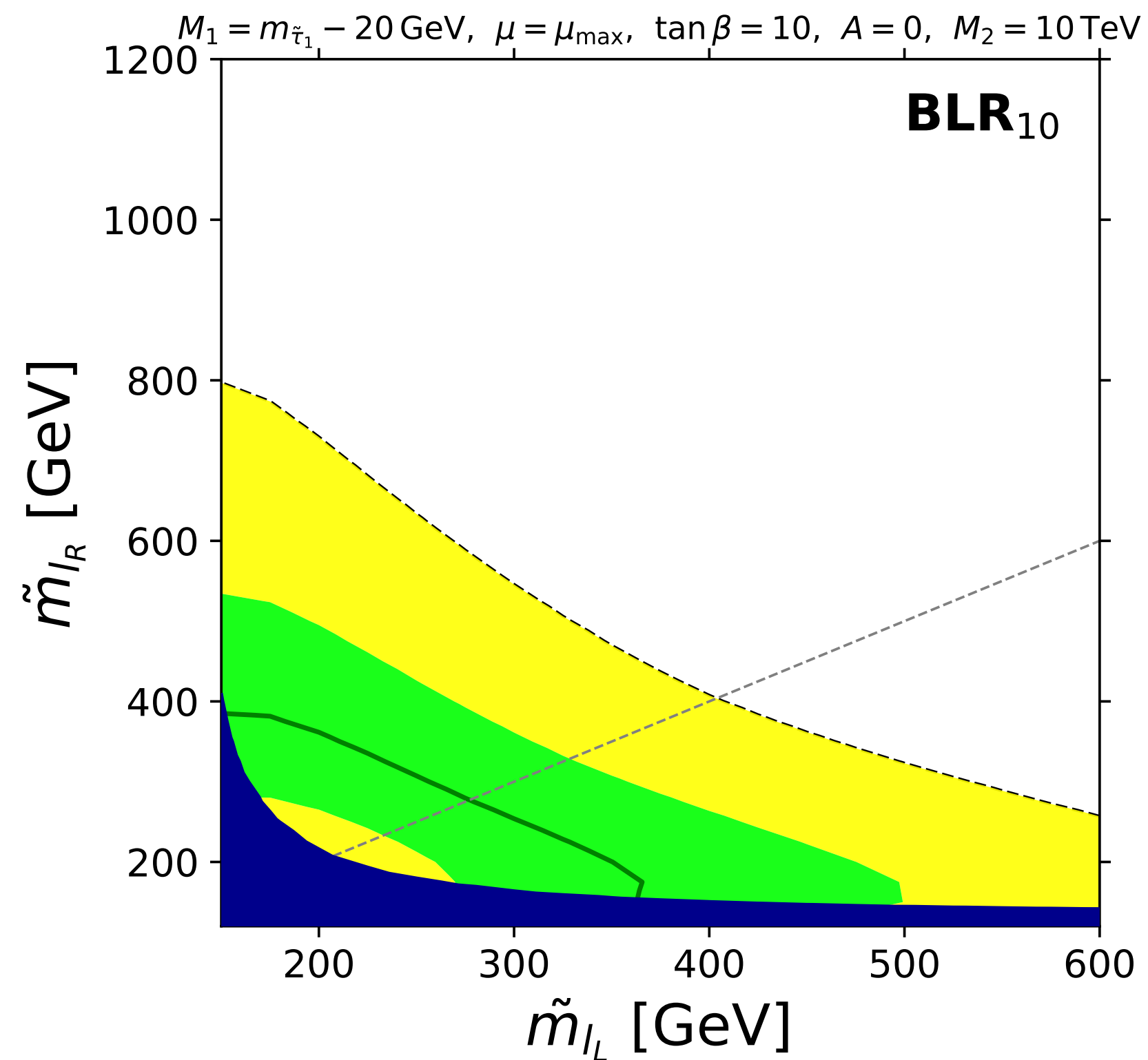
CMS $|\tau|\tau$ [2004.05153]

XENON1T [1805.12562]

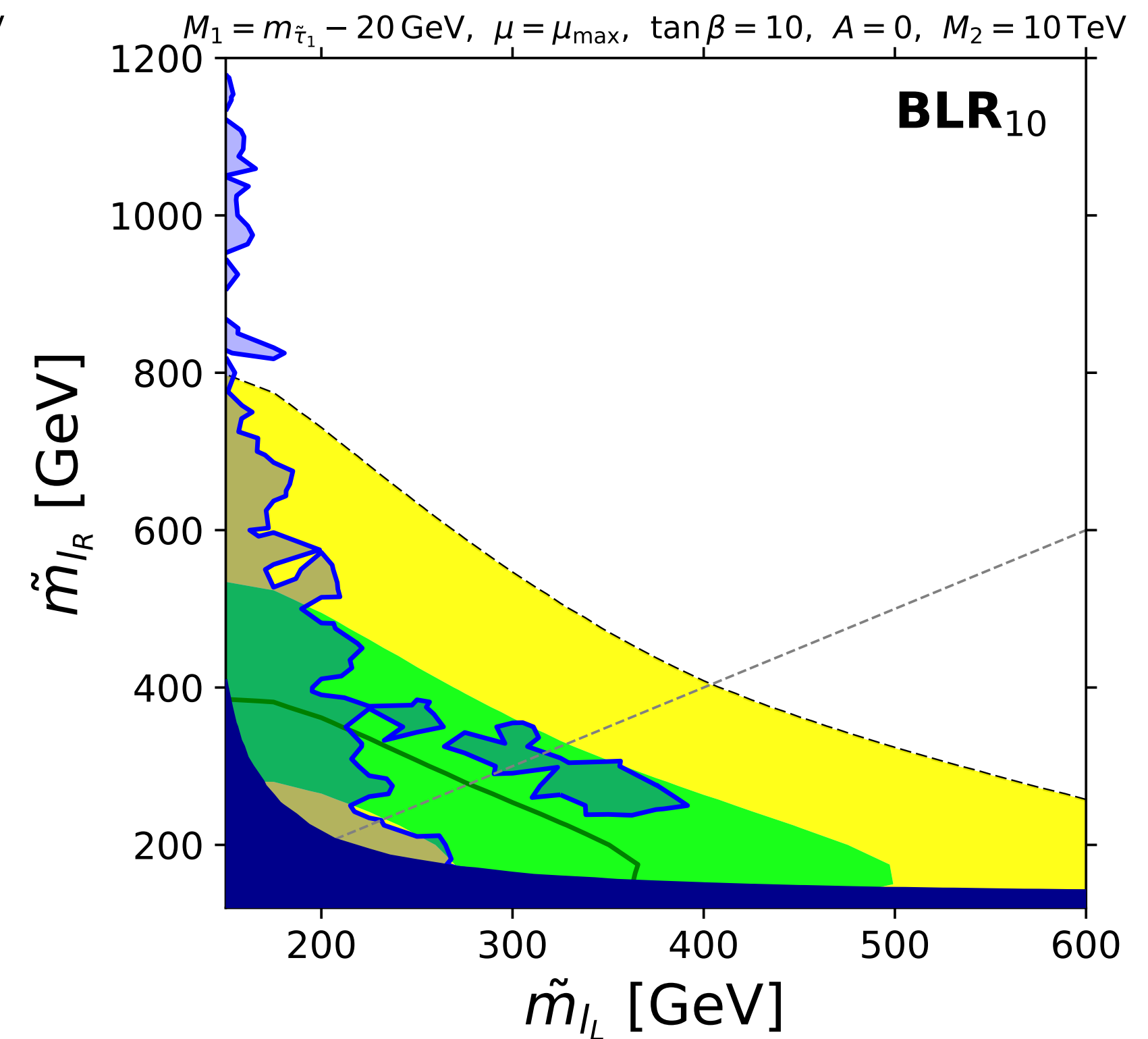
CMS multilepton
[1709.05406]



MSSM



RPV



GMSB

BLR₁₀

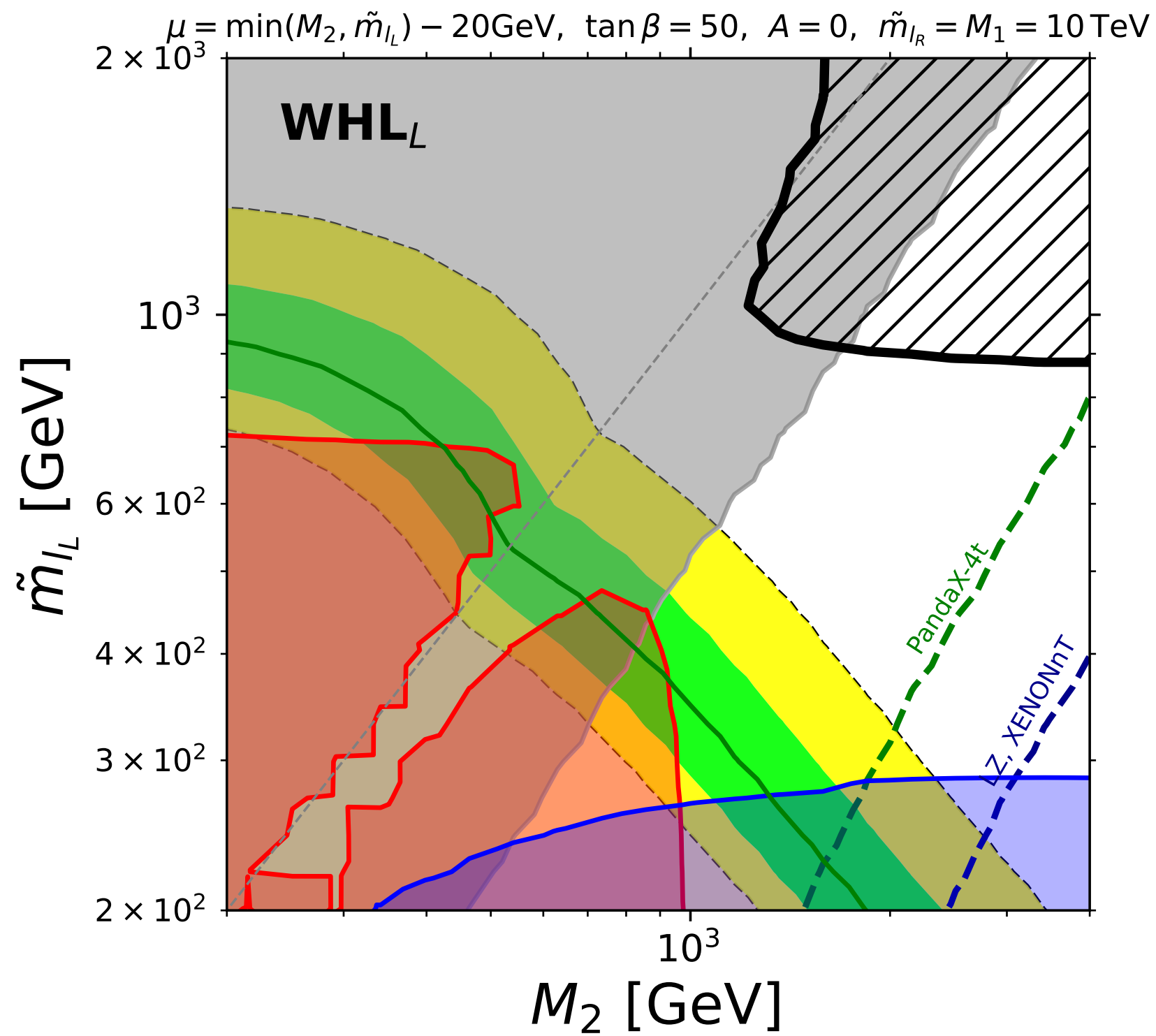
ATLAS soft-| [1911.12606]

CMS |+|- [2004.05153]

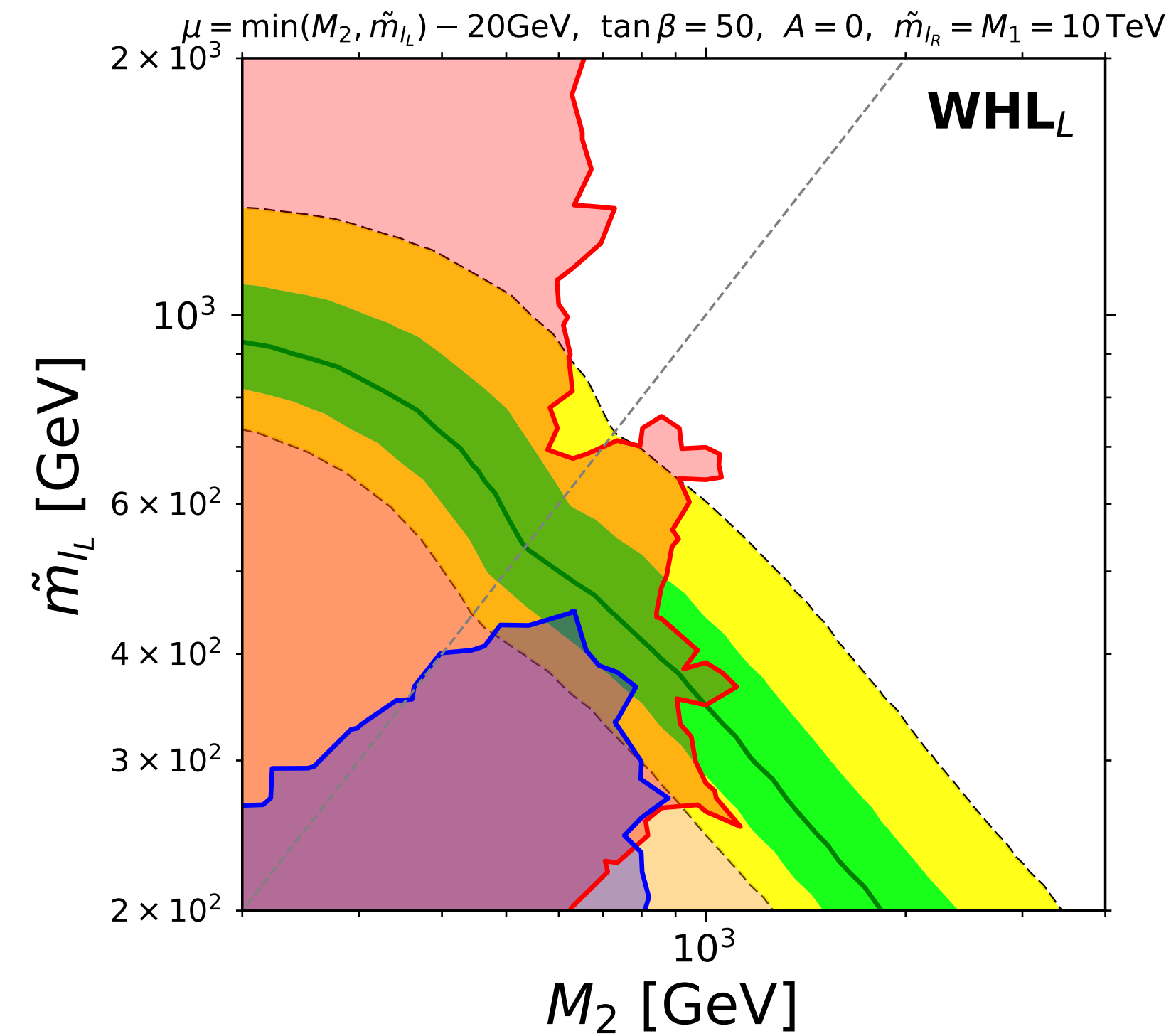
XENON1T [1805.12562]

CMS multilepton [1709.05406]

ATLAS multijet+| [2106.09609]



MSSM



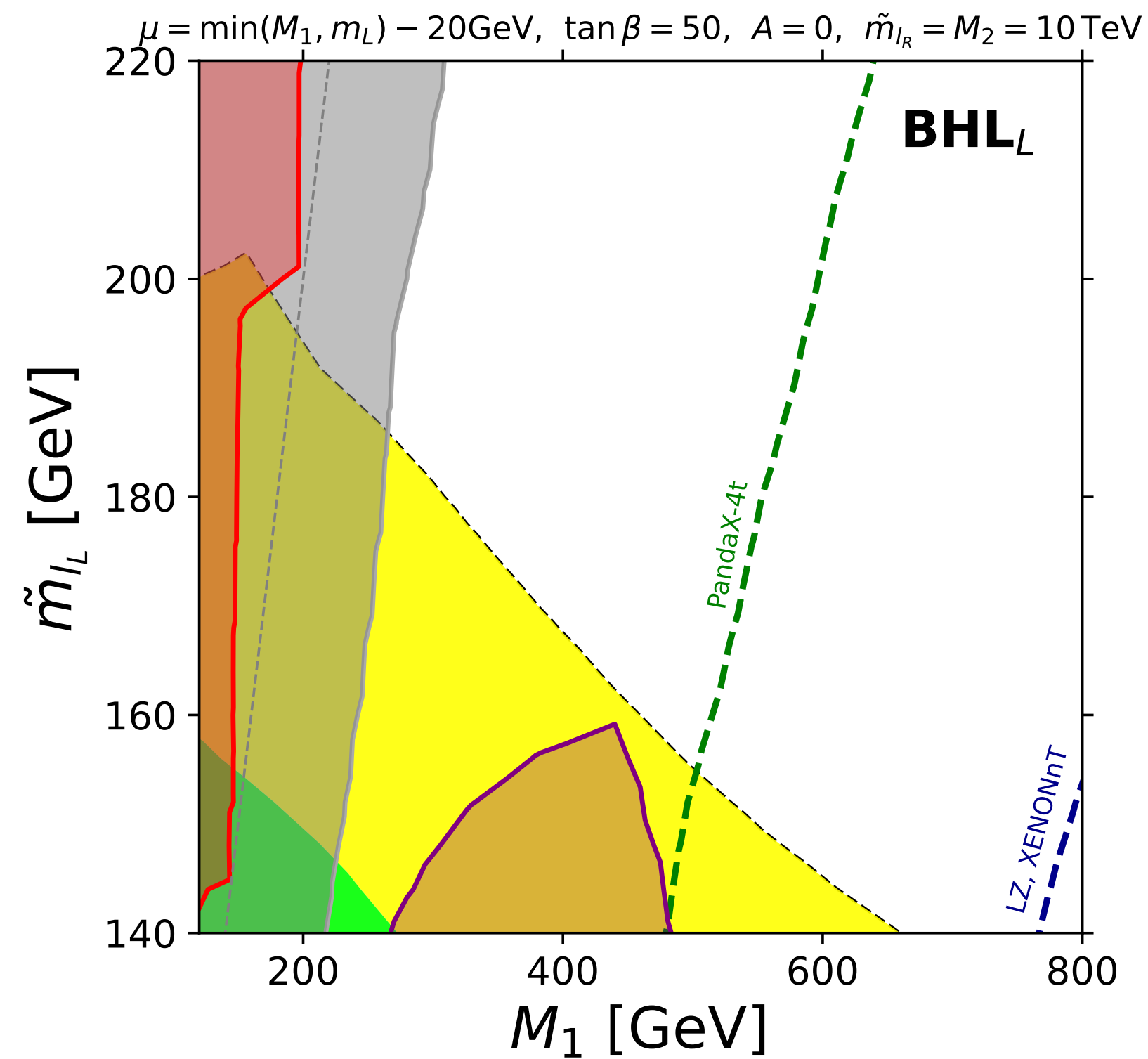
RPV

WHL_L

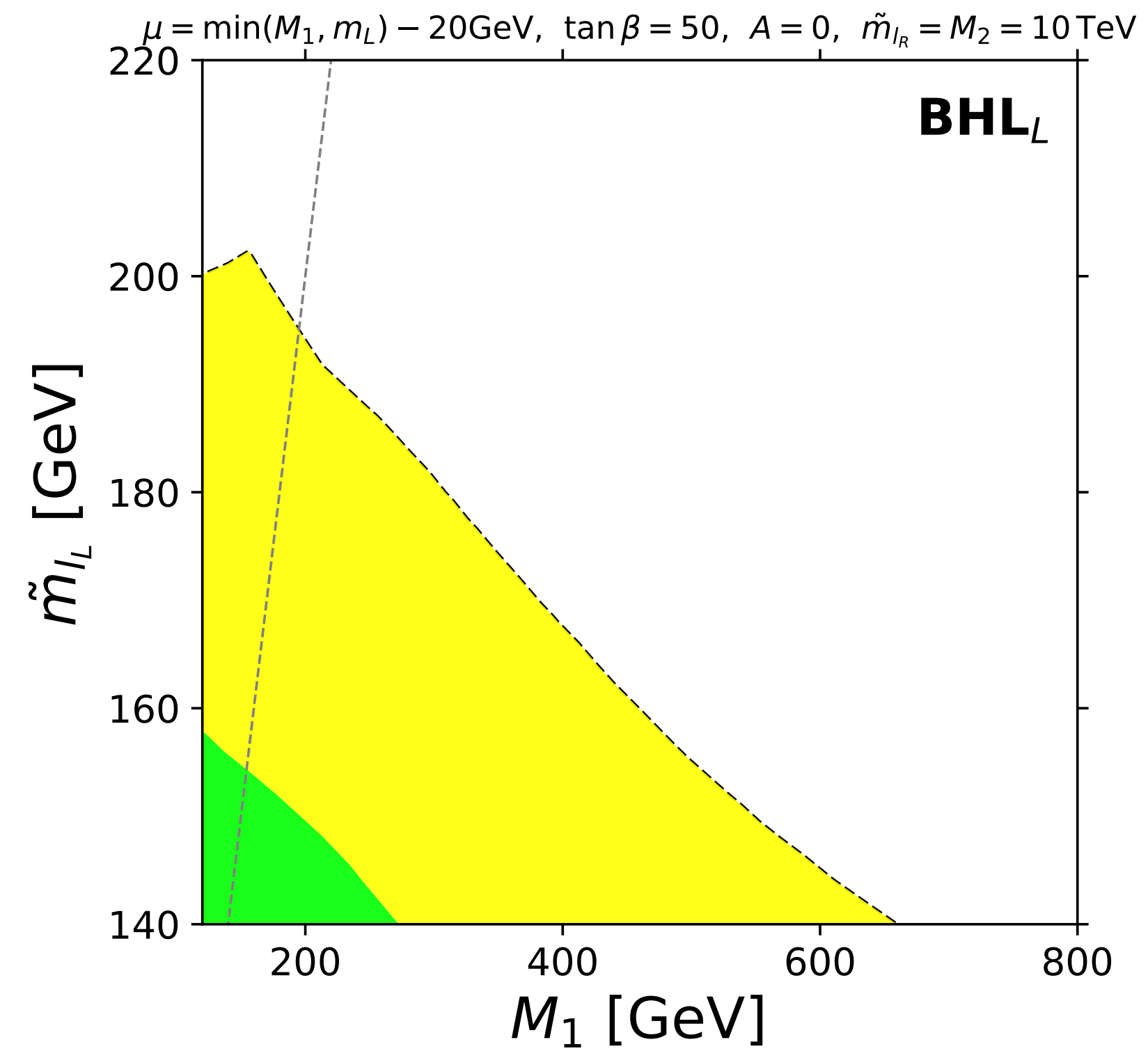
ATLAS soft-| [1911.12606]

CMS |+|- [2004.05153]

XENON1T [1805.12562]



MSSM



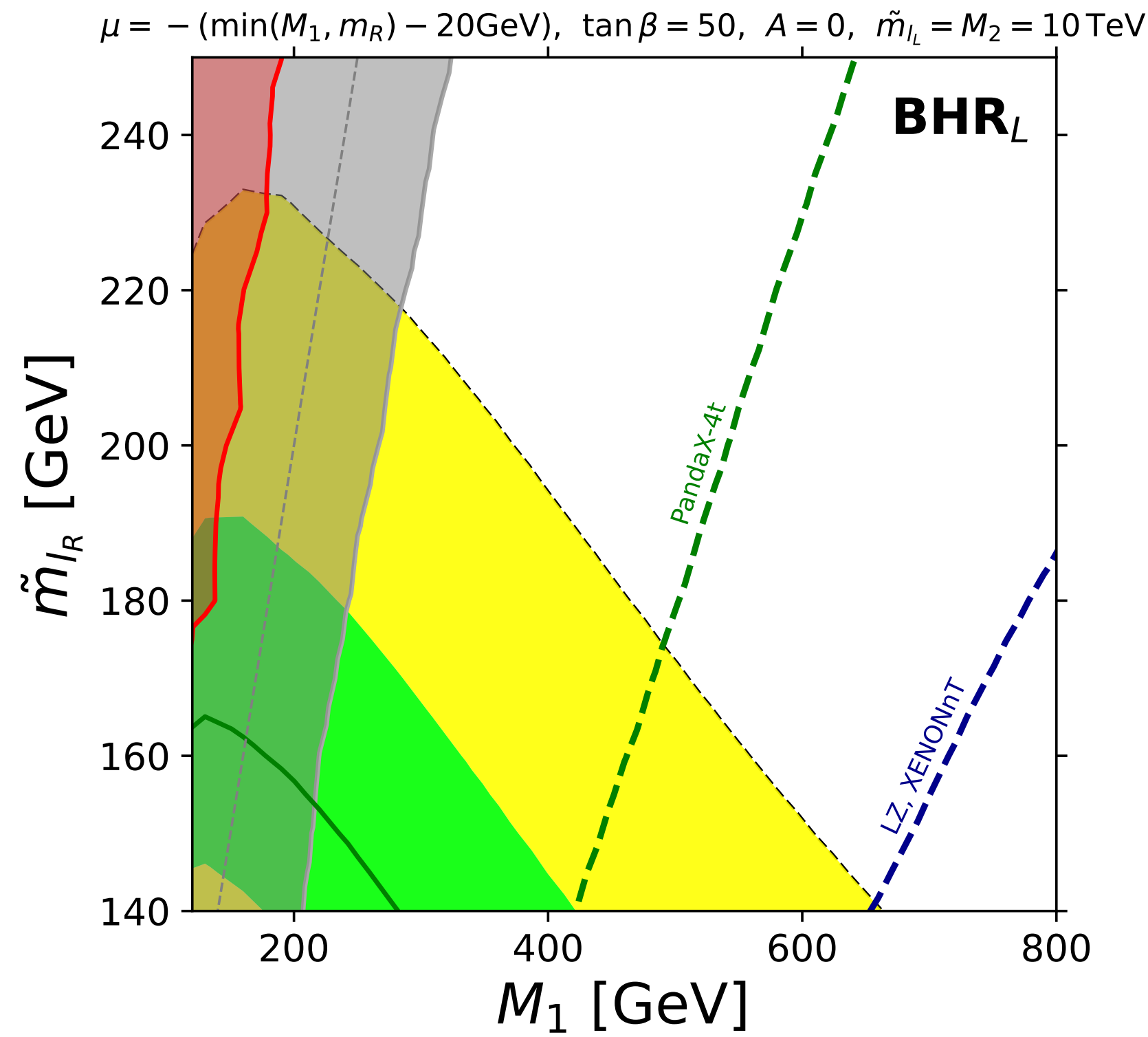
RPV

BHL_L

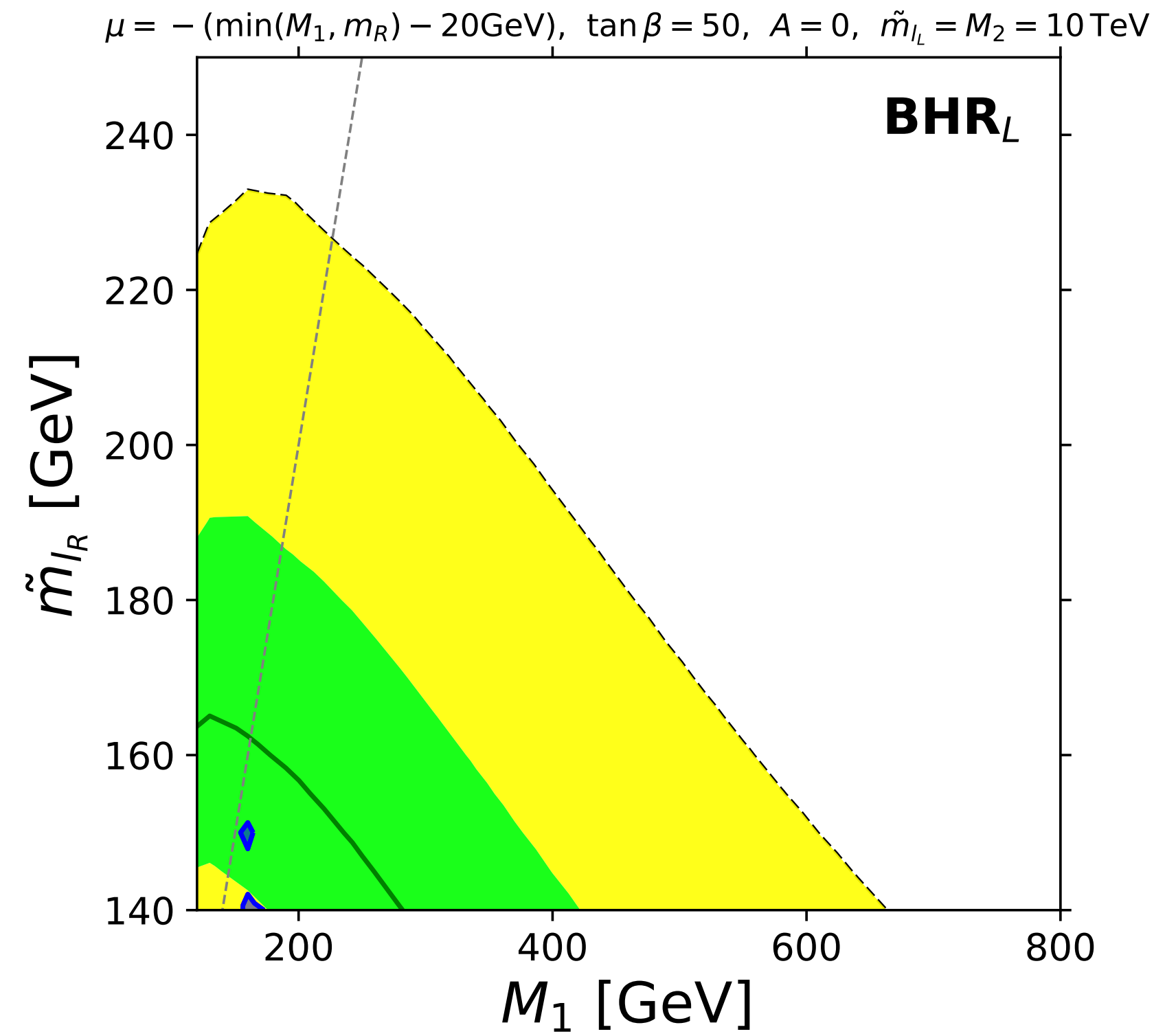
CMS $|+|-$ [2004.05153]

XENON1T [1805.12562]

CMS multilepton [1709.05406]

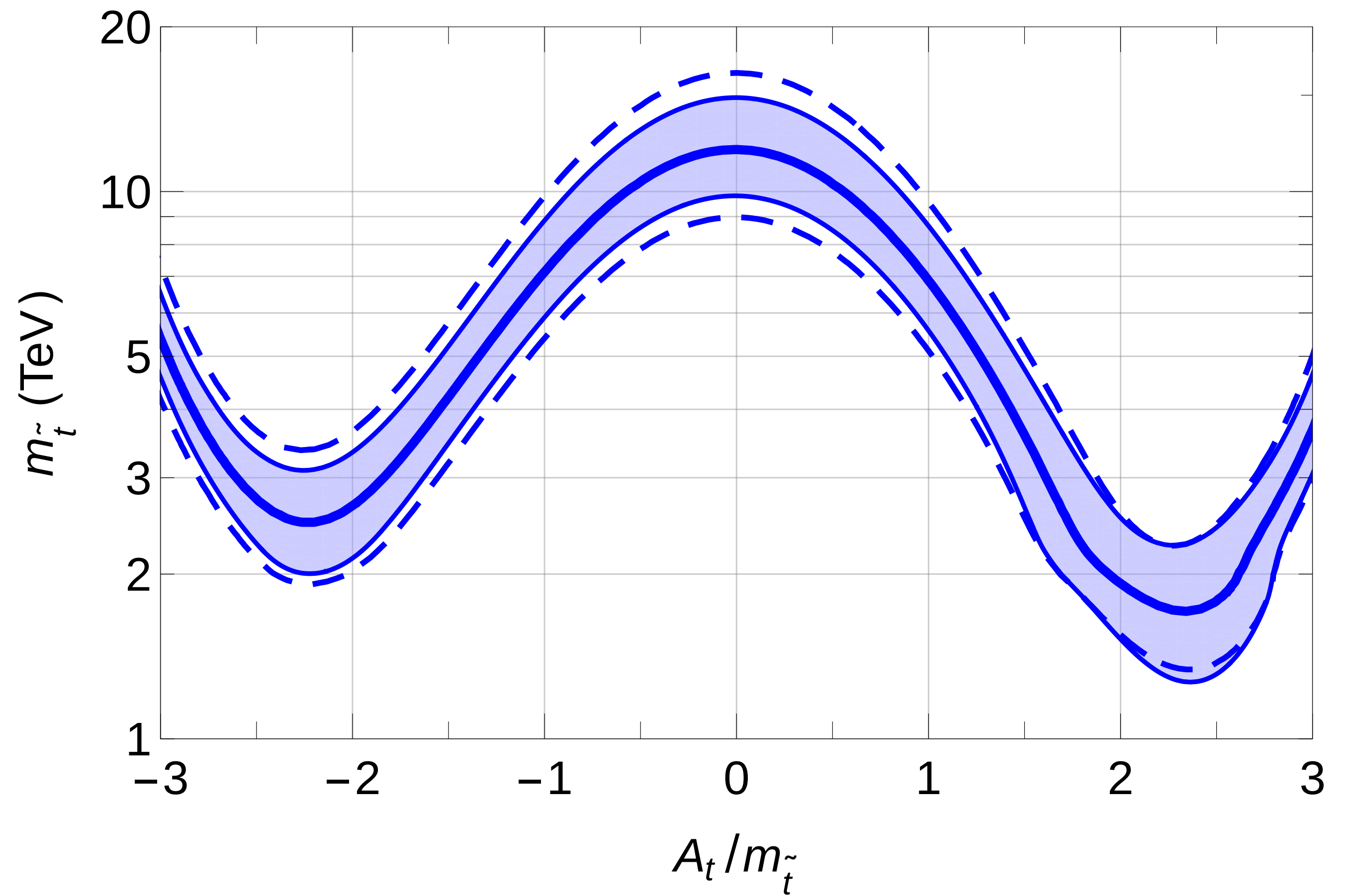


MSSM



RPV

BHR_L



$$m_{\tilde{G}} = \frac{F_X}{\sqrt{3}M_{\text{Pl}}}, \quad M_3 = \frac{\alpha_3}{4\pi} \frac{F_X}{M_{\text{mess}}}$$

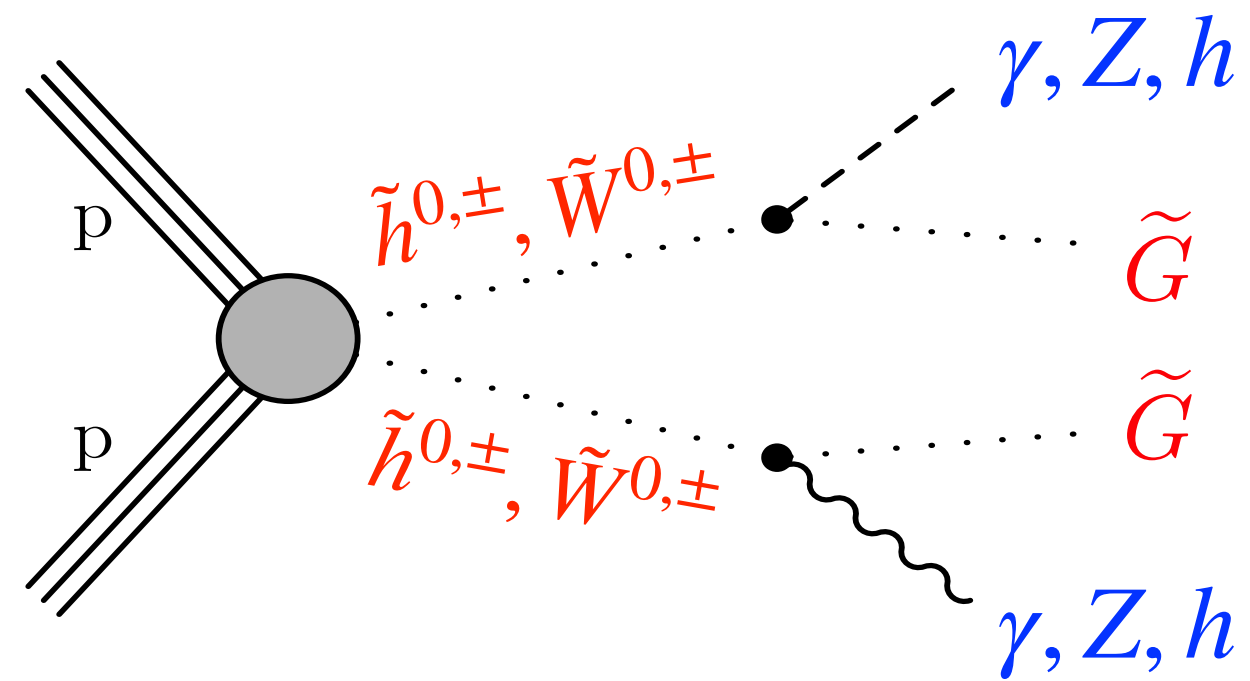
$$m_{\tilde{G}} = \sim 10 \text{ eV} \cdot \left(\frac{m_{\tilde{t}}}{10\text{TeV}} \right) \left(\frac{M_{\text{mess}}}{10\text{TeV}} \right)$$

[1504.05200]

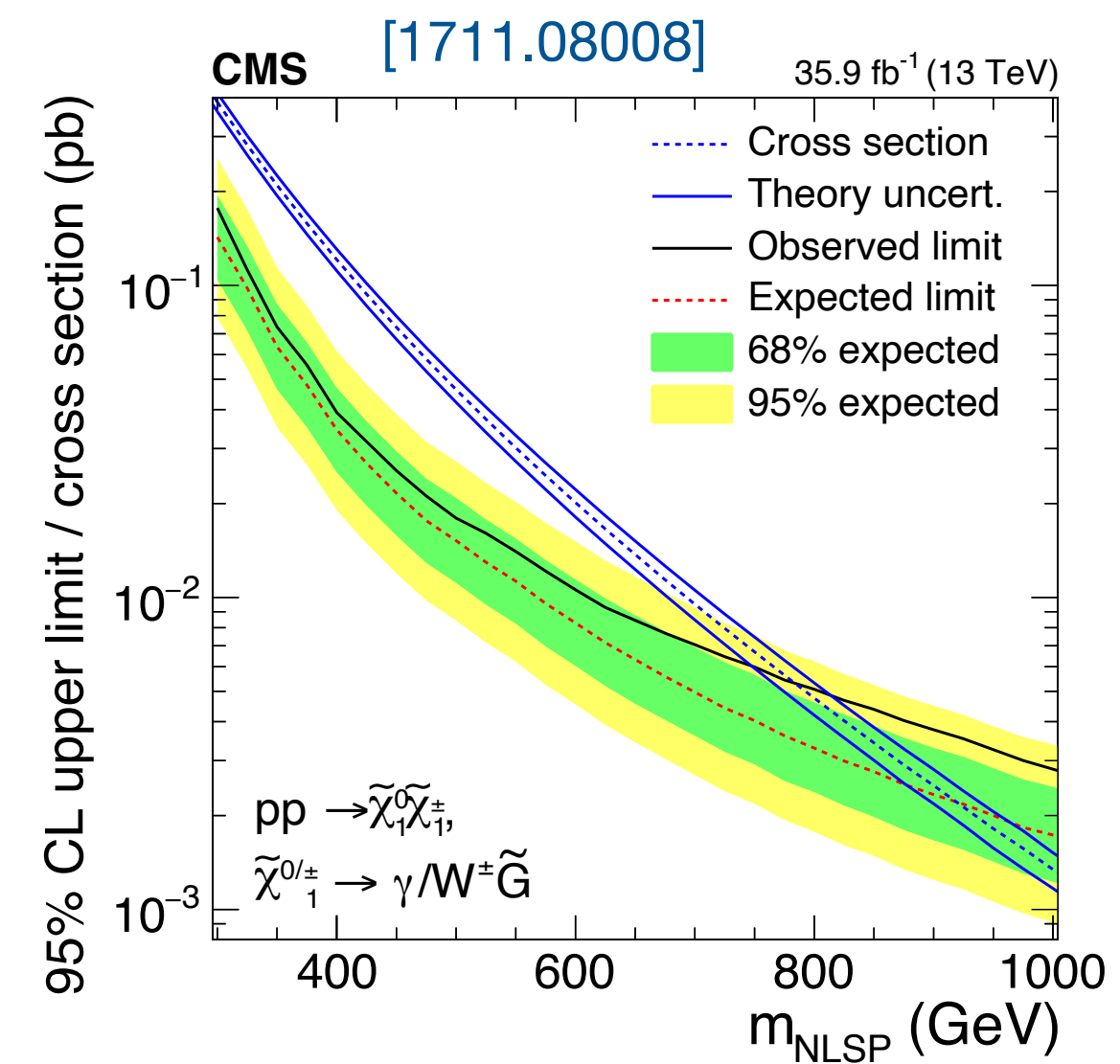
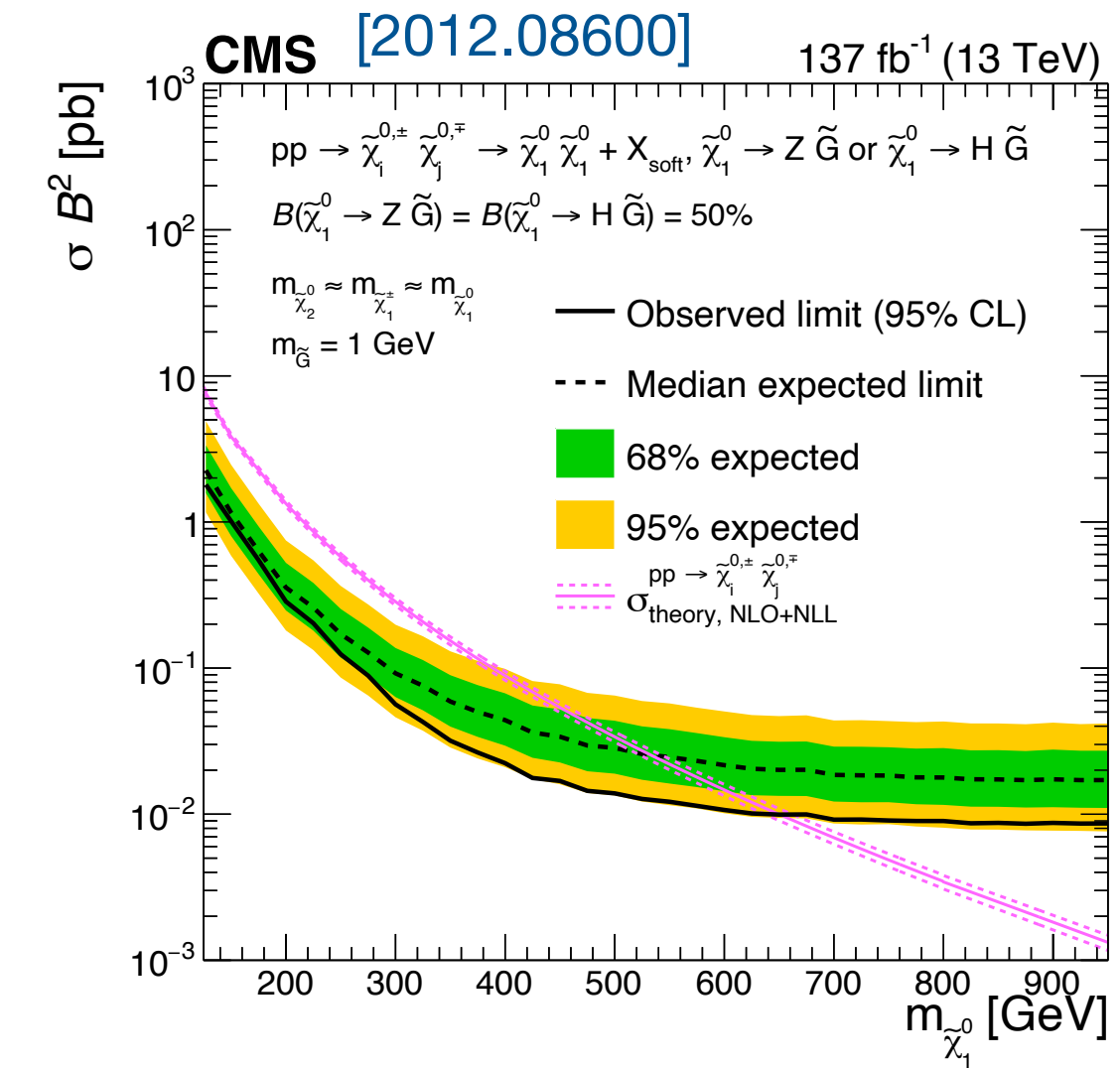
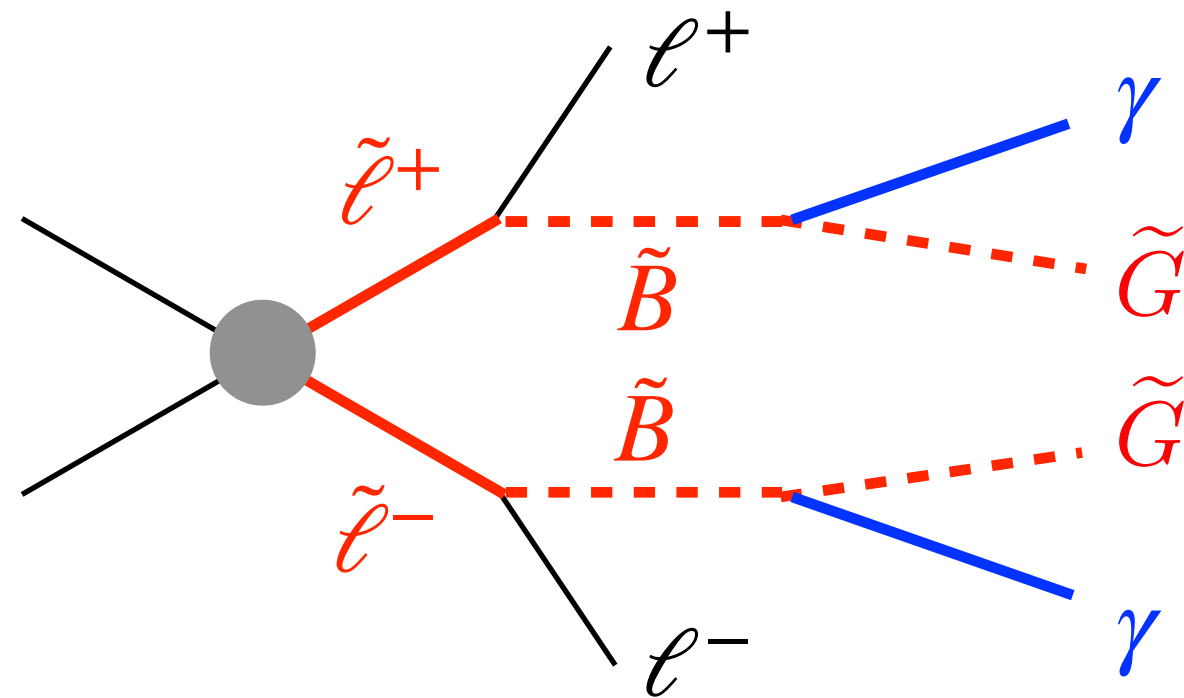
Gravitino LSP

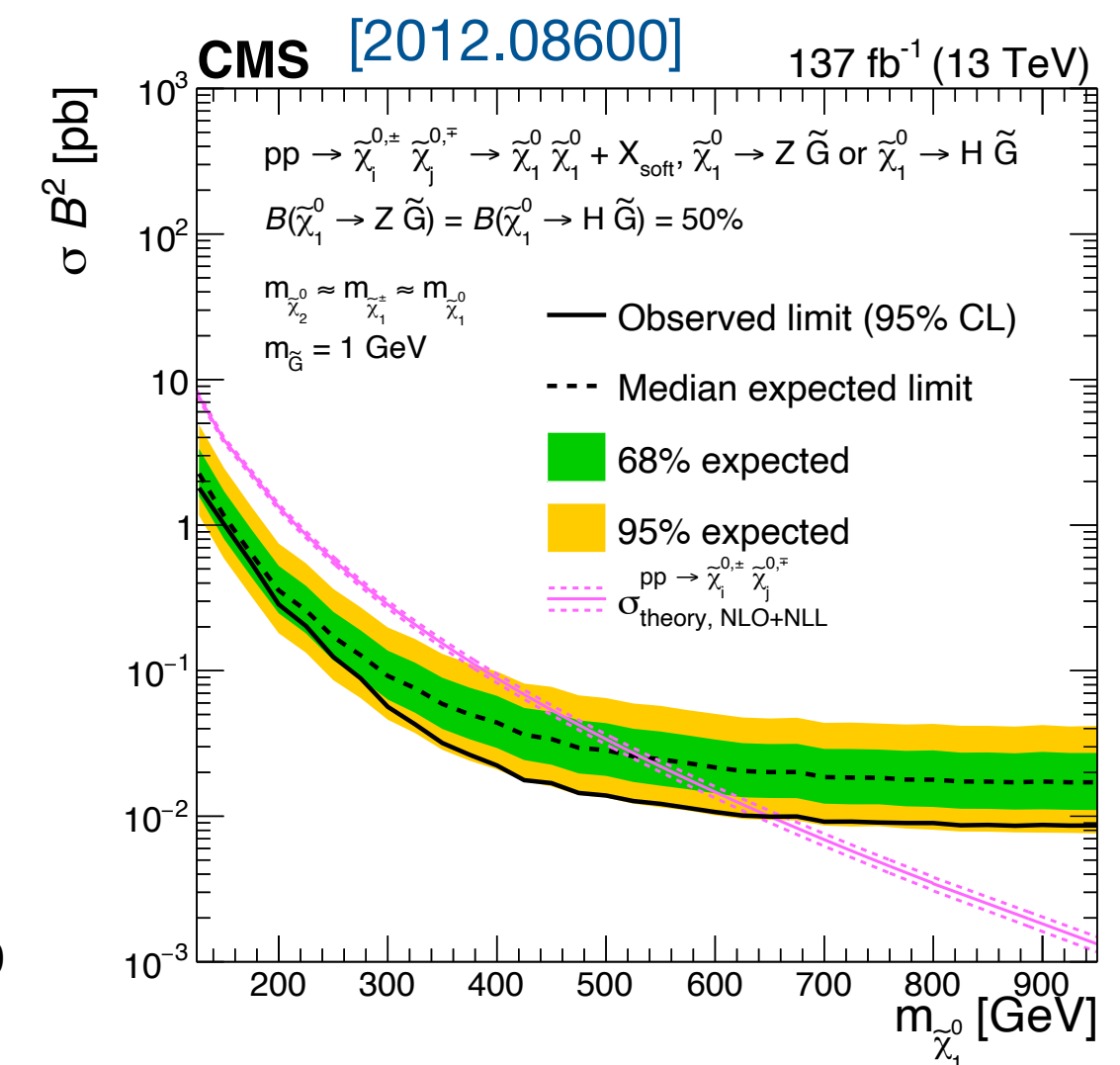
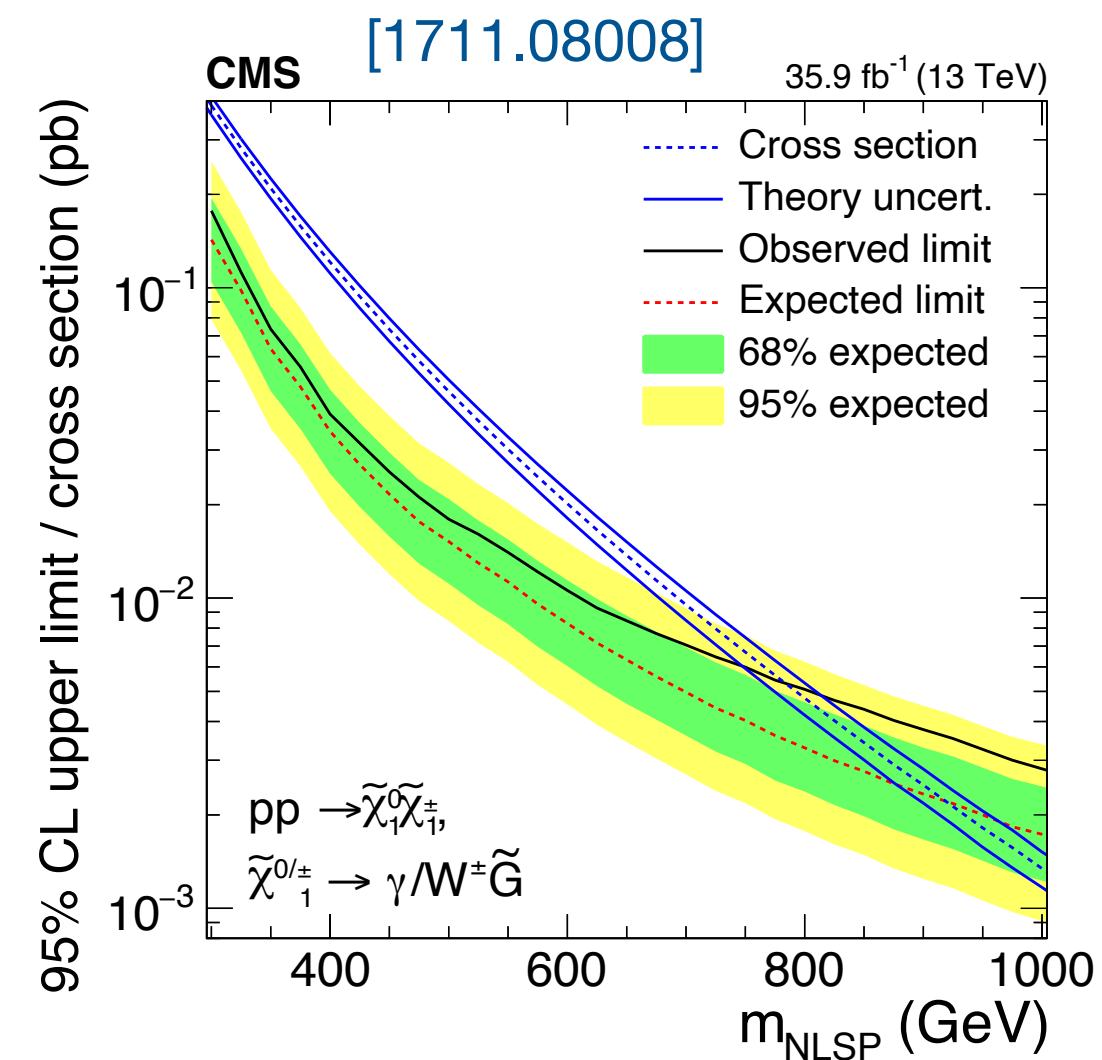
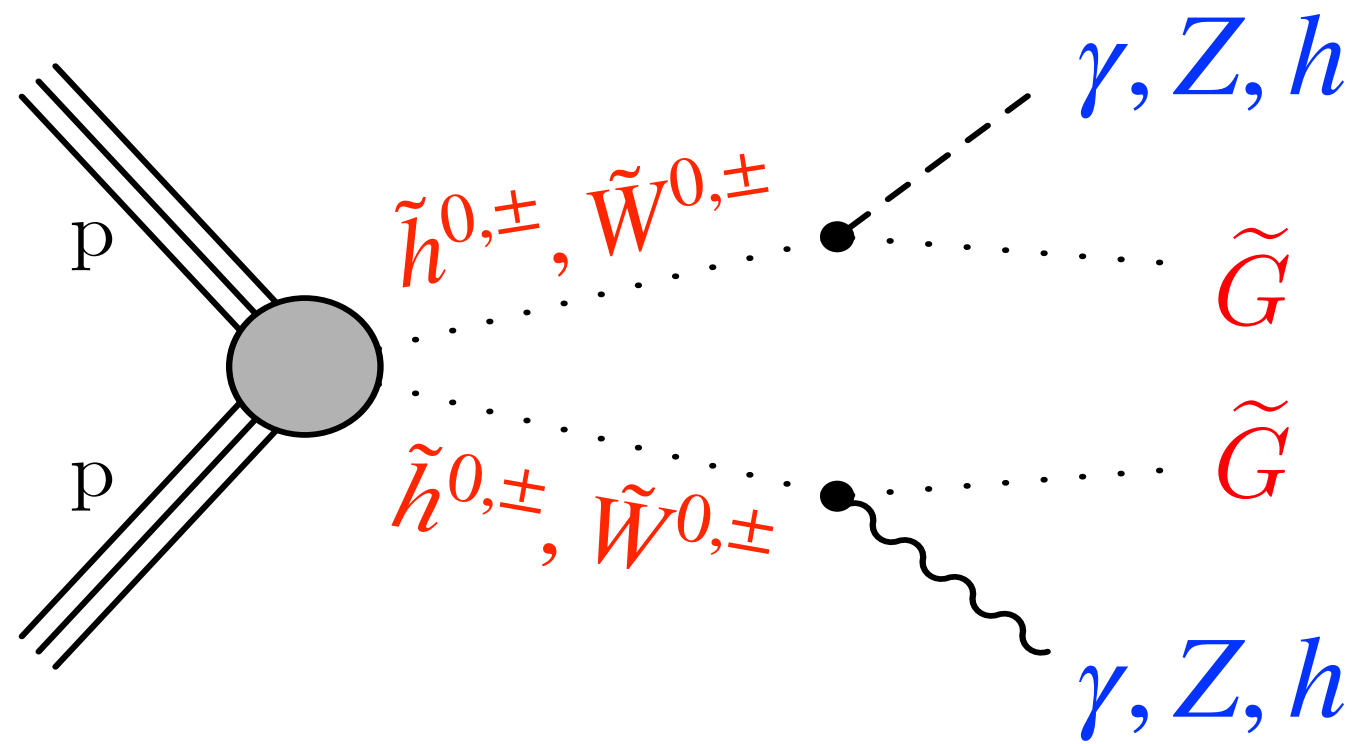
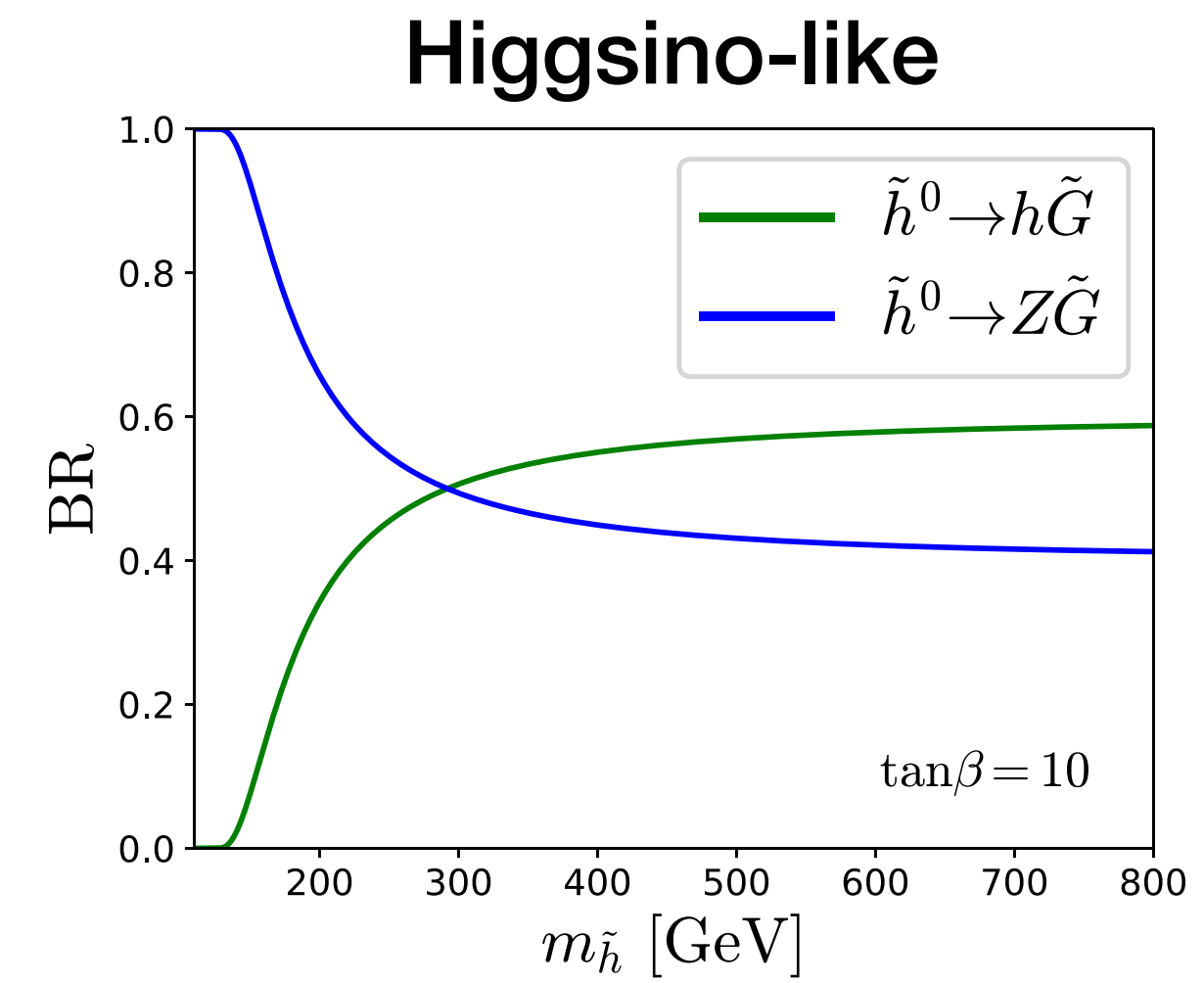
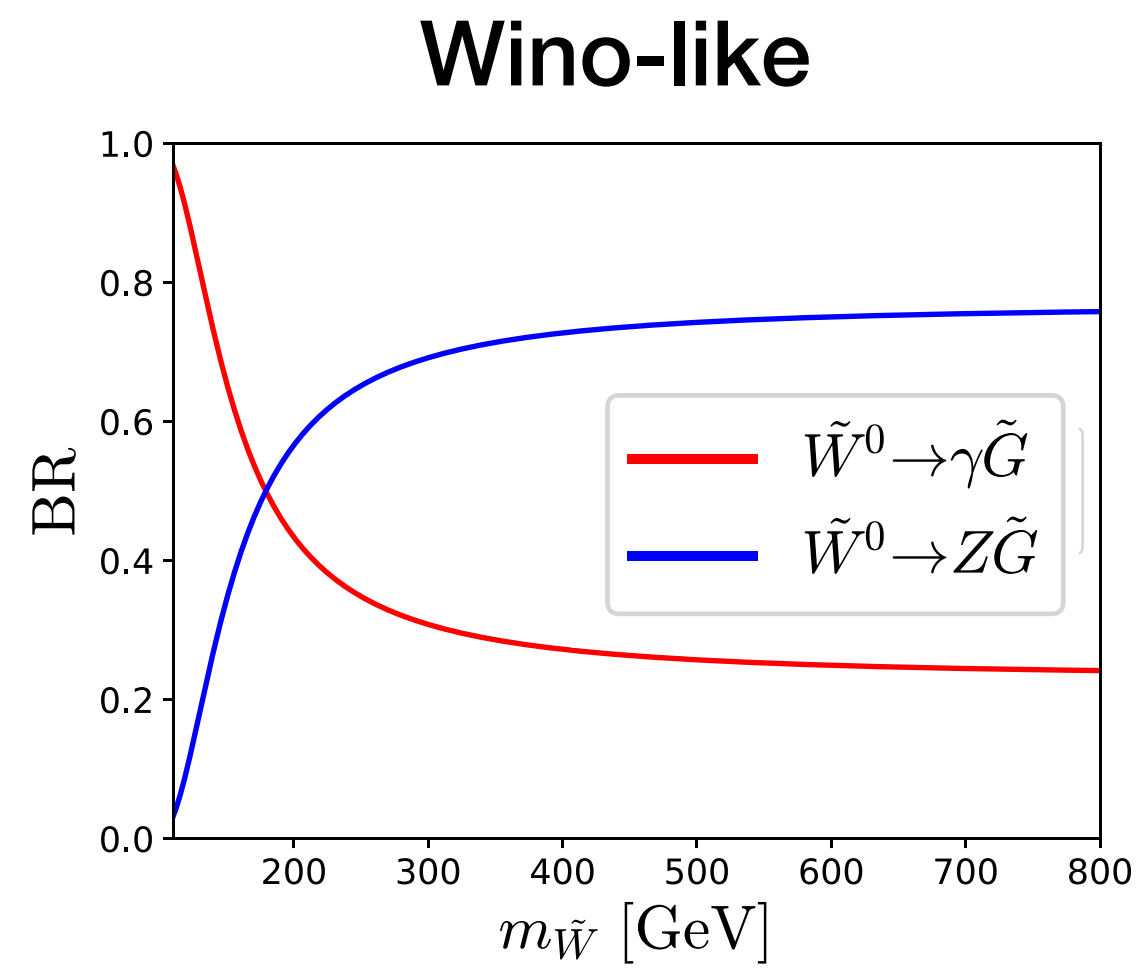
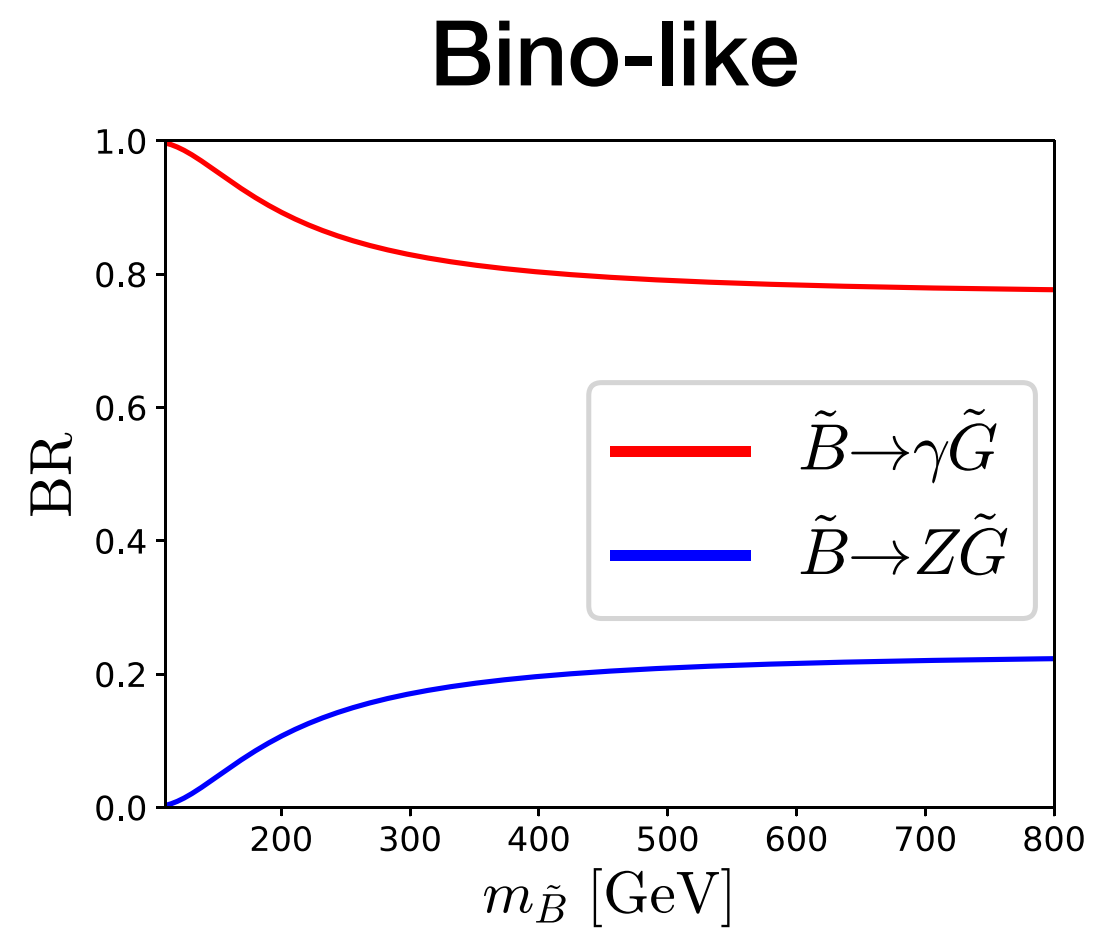
We assume a **massless** gravitino ($m < 1\text{ GeV}$) and **prompt** neutralino decay.

Wino, Higgsino NLSP



Bino NLSP

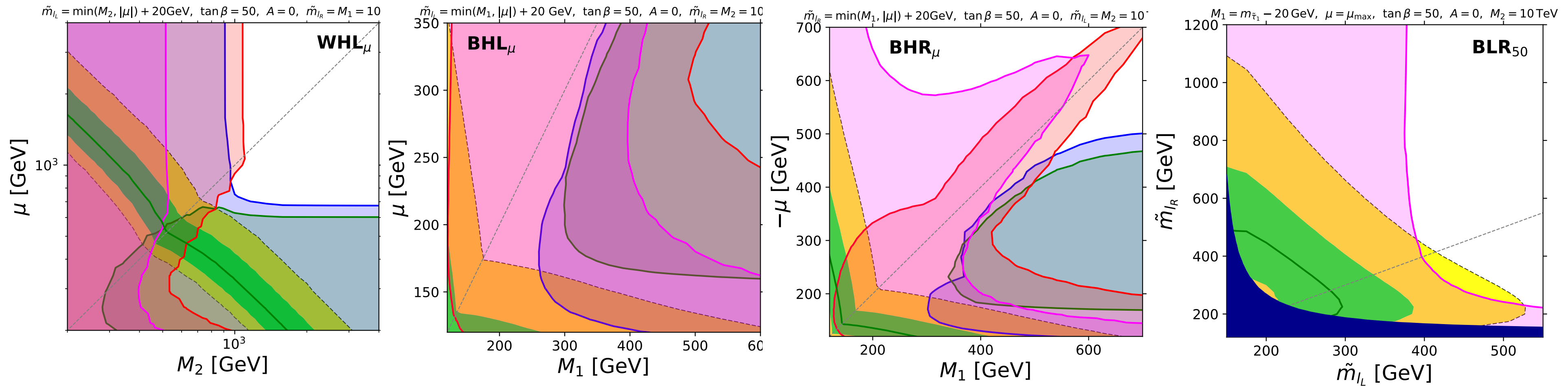




- Higgsino, Wino direct production excluded up to $\sim 700\text{GeV}$
- SUSY g-2 requires Higgsino or Wino with $m < 600 \text{ GeV}$

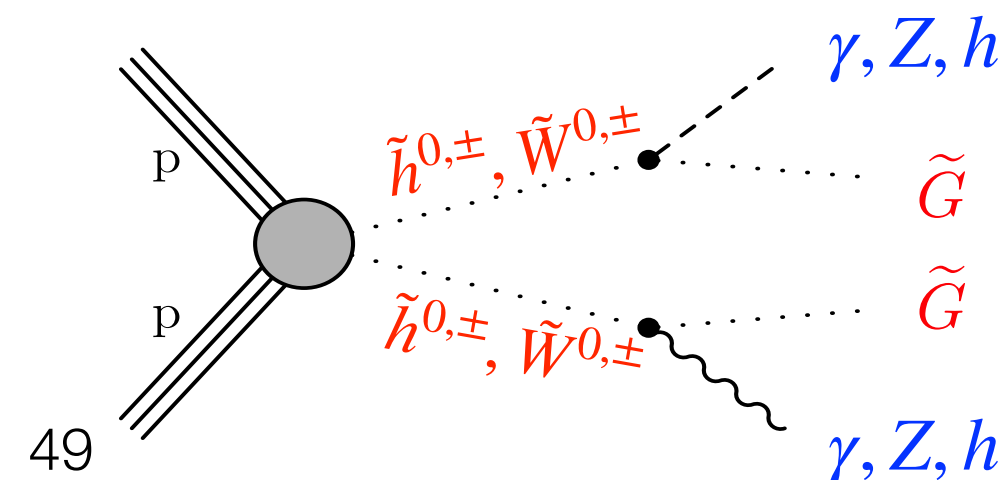
**SUSY (g-2)_μ
incompatible
with LHC**

Gravitino LSP

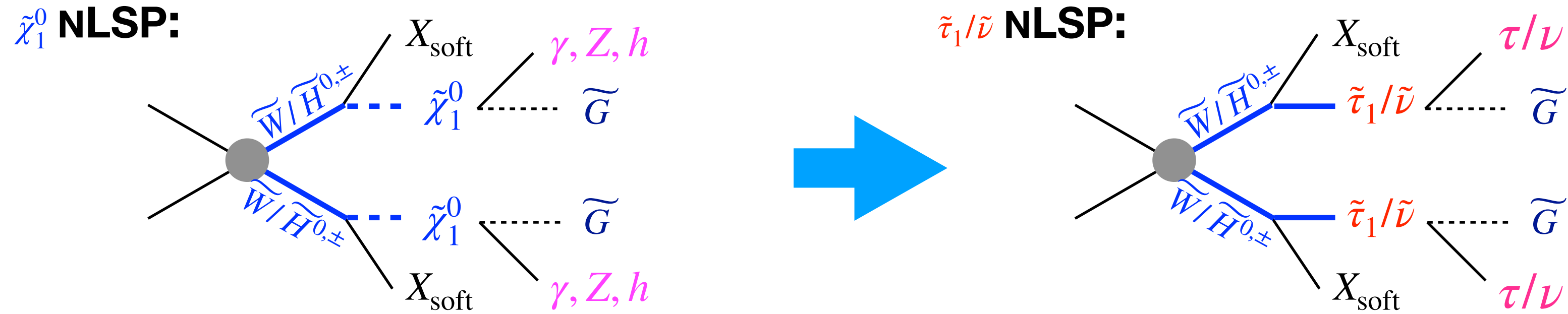


[(massless) gravitino LSP + neutralino NLSP] cannot explain muon g-2

Unlike MSSM, in gravitino LSP, one cannot hide high pT decay products and E_T^{miss} by making mass spectrum compressed.



Gravitino LSP with slepton NLSP



WHL plane:

$$(M_2 \text{ vs } \mu) \text{ with } \tilde{m}_{l_L} = \min(M_2, \mu) + 20 \text{ GeV} \implies m_{l_L} = \min(M_2, \mu) - 20 \text{ GeV} \left. \vphantom{\begin{matrix} (M_2 \text{ vs } \mu) \\ (M_1 \text{ vs } \mu) \end{matrix}} \right\} \tilde{\nu}_L \text{ NLSP}$$

BHL plane:

$$(M_1 \text{ vs } \mu) \text{ with } \tilde{m}_{l_L} = \min(M_1, \mu) + 20 \text{ GeV} \implies m_{l_L} = \min(M_2, \mu) - 20 \text{ GeV}$$

BHR plane:

$$(M_1 \text{ vs } \mu) \text{ with } \tilde{m}_{l_R} = \min(M_1, |\mu|) + 20 \text{ GeV} \implies m_{l_R} = \min(M_1, \mu) - 20 \text{ GeV} \left. \vphantom{\begin{matrix} (M_1 \text{ vs } \mu) \\ (M_1 \text{ vs } \mu) \end{matrix}} \right\} \tilde{e}_R, \tilde{\mu}_R, \tilde{\tau}_R \text{ NLSP}$$

BLR plane:

$$(\tilde{m}_{l_L} \text{ vs } \tilde{m}_{l_R}) \text{ with } M_1 = m_{\tilde{\tau}_1} - 20 \text{ GeV} \implies M_1 = m_{\tilde{\tau}_1} + 20 \text{ GeV} \left. \vphantom{(\tilde{m}_{l_L} \text{ vs } \tilde{m}_{l_R})} \right\} \tilde{\tau}_1 \text{ NLSP}$$