

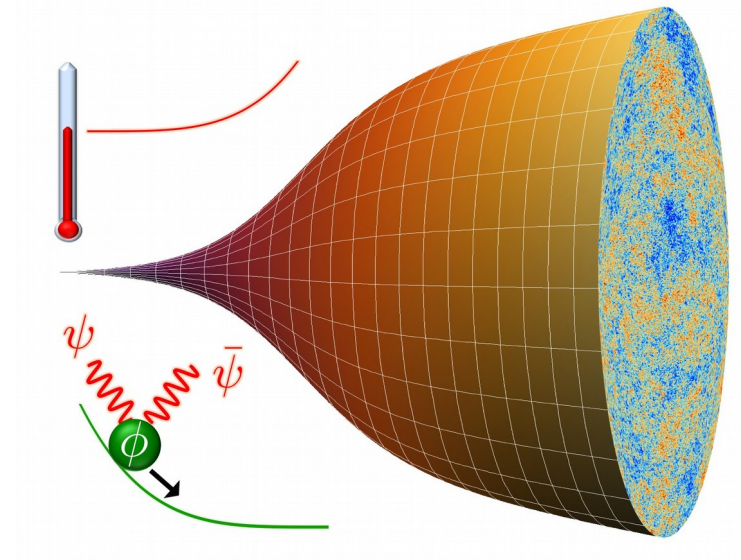
Little Warm Inflation

Cold inflation/Warm inflation

Dissipative coefficient:

High T regime: $Y(T) = C_T T$

Primordial spectrum: Chaotic models $\lambda \phi^4$



Mar Bastero Gil
University of Granada

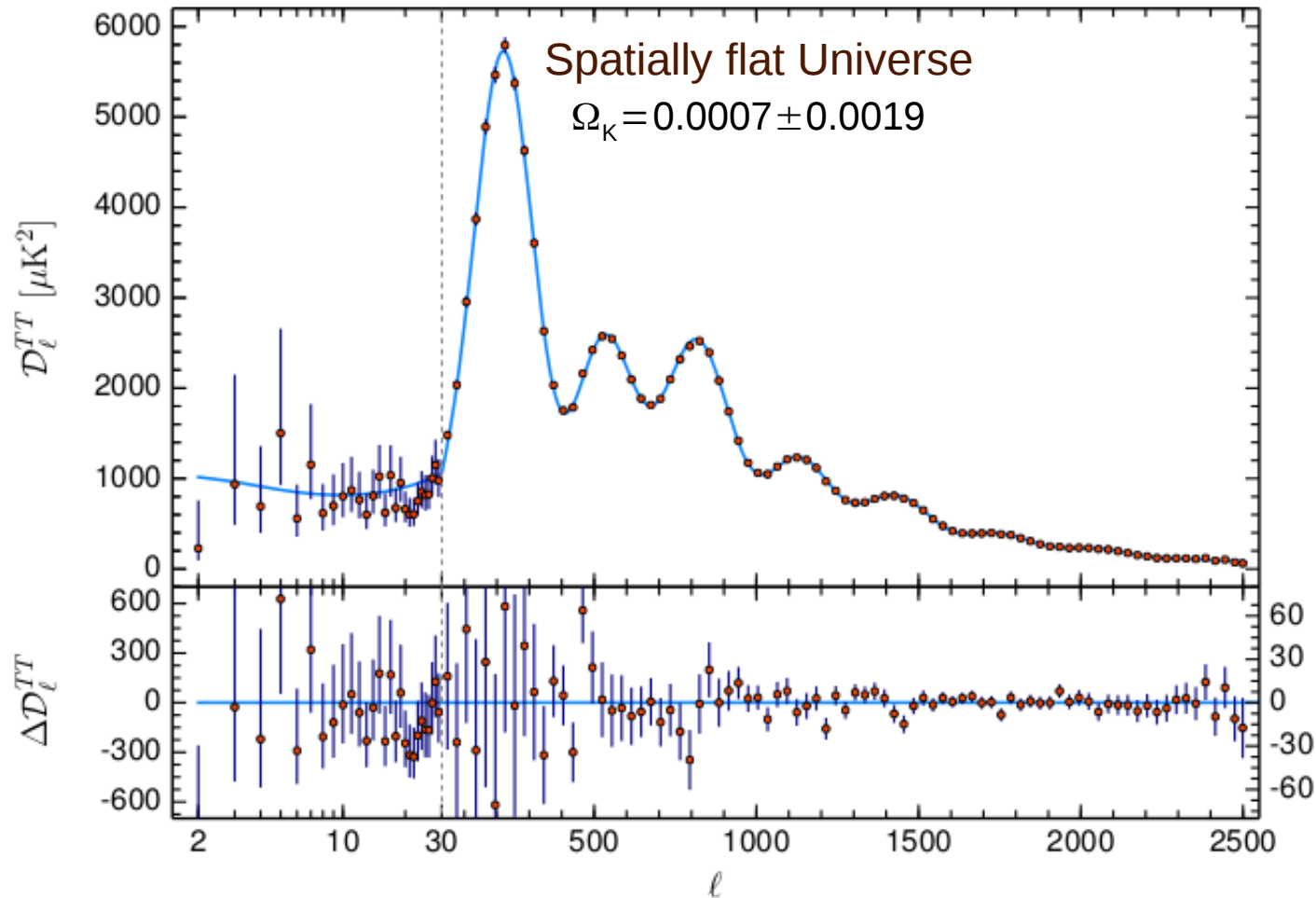
MBG, A. Berera, R. Ramos, J. Rosa PRL117 (2016) 151301

MBG S. Bhattacharya, K. Dutta, M. R. Gangopadhyay JCAP 1802 (2018)

MBG, A. Berera, R. Hernández-Jiménez, J. Rosa, arXiv: 1805.07186

Cosmic microwave background radiation (CMB)

Spectrum of T fluctuations



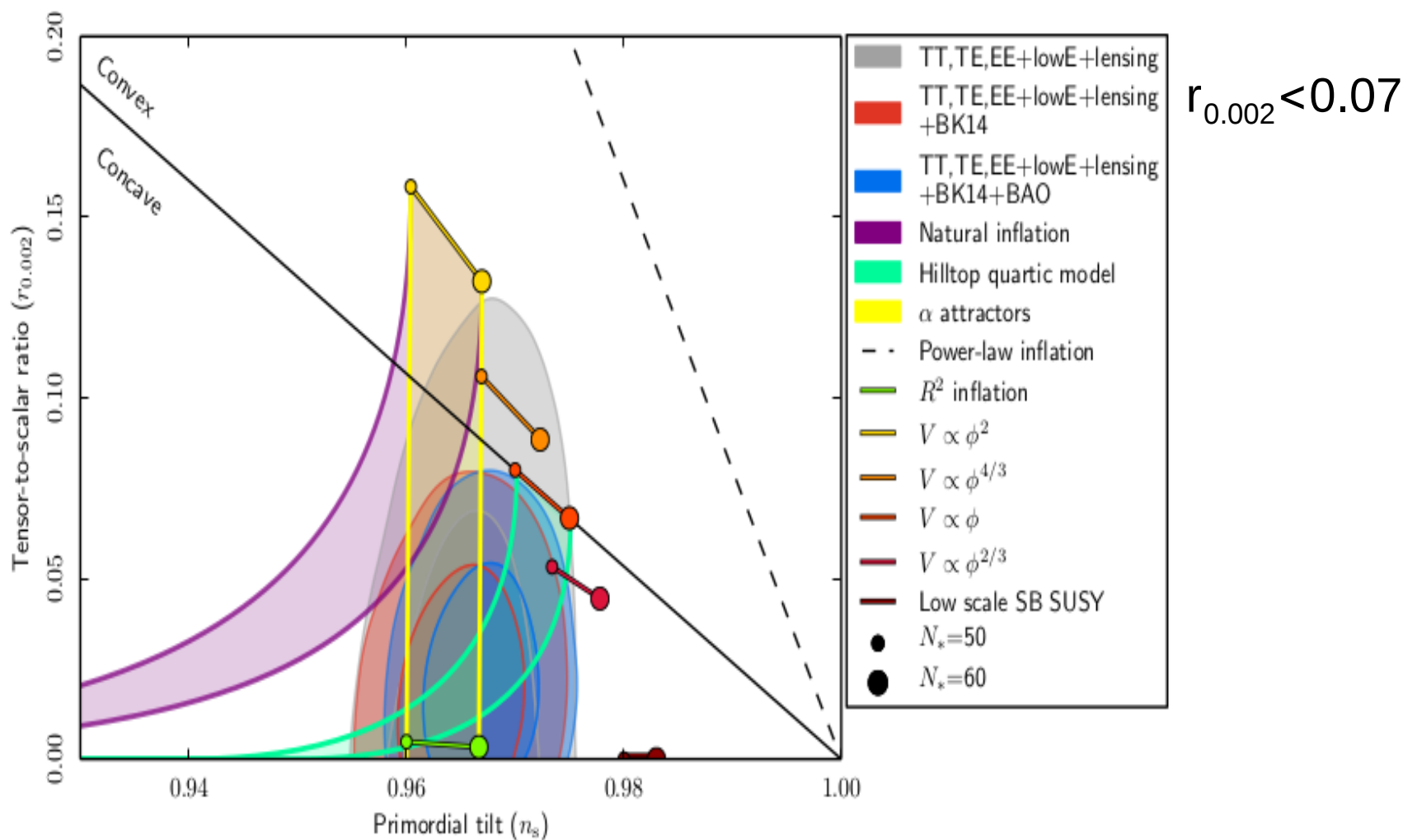
COBE (1992)
Boomerang
Maxima
DASI
CBI
VSA
.....
WMAP
SPT
BICEP/KEK
PLANCK
(14/05/09)

[Planck 2018: astro-ph/1807.06211]

Primordial spectrum: ~adiabatic, ~scale-invariant, gaussian?, tensors?

Primordial spectrum: $P_R = P_R(k_0)(k/k_0)^{n_s-1}$ $k_0 = 0.05 \text{ Mpc}^{-1}$

Tensor-to-scalar Ratio: $r = P_T/P_R$ $P_R = 2.2 \times 10^{-9}$



[Planck 2018.: 1807.06211]

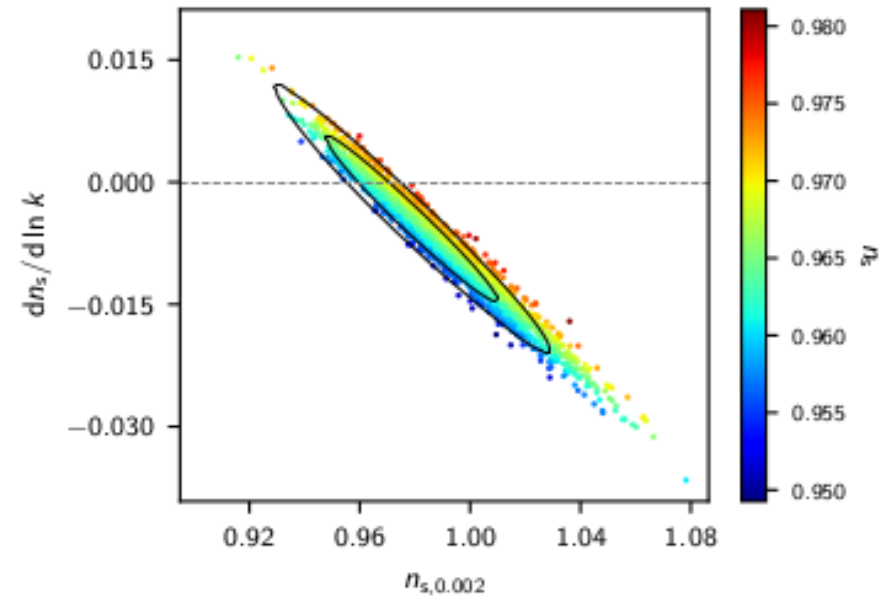
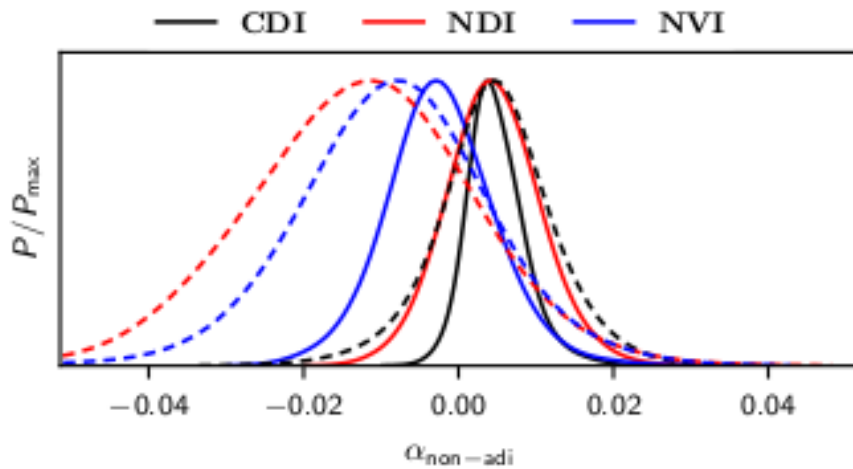
Primordial spectrum: $P_R = P_R(k_0) (k/k_0)^{n_s - 1 + \frac{1}{2} \alpha_s \ln k/k_0 + \dots}$ $k_0 = 0.05 \text{ Mpc}^{-1}$
adiabatic, gaussian, \sim scale-invariant spectrum

No evidence for:
isocurvature modes, non-gaussianity, or running of the spectral index

$$[f_{\text{NL}} = 2.5 \pm 5.7]$$

$$\alpha_s = -0.007 \pm 0.013, \quad r_{0.002} < 0.072$$

$$[n_t = -r/8 < 0]$$



[Planck 2018.: 1807.06211]

Expanding Universe

Flatness problem

$$\Omega_T = 1 \quad \longrightarrow \quad \Omega_T(t_{\text{nucl}}) - 1 \approx 10^{-16}$$

Horizon problem

The observable Universe was larger than the **particle horizon** at LSS

Inflation

Early period of accelerated expansion

$$\ddot{a} > 0: \quad P < -\rho/3$$

Superhorizon perturbations?

Too small sub-horizon
(**causal**) perturbations

Unwanted relics...

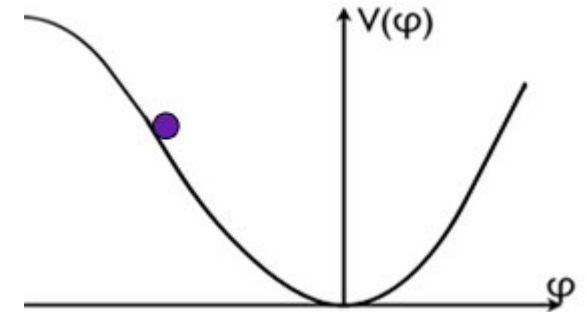
monopoles, moduli, gravitinos,...

Starobinsky '80; Guth '81; Albrecht, Steinhardt '82; Linde 1982

Slow Roll Inflation

Scalar field rolling down its (flat) potential

$$P = \dot{\varphi}^2/2 - V(\varphi) \approx -V(\varphi) \quad \text{negative pressure}$$



“Flat” potential

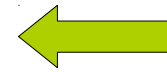
The curvature and the slope smaller than the (Hubble) expansion rate H

Kinetic energy \ll potential energy $H^2 \sim V/3m_p^2$ Hubble parameter ($H = \dot{a}/a$)
($a =$ scale factor)

Slow-roll parameters

$$|\eta_\varphi| = m_p^2 \left| \frac{V''}{V} \right| < 1$$

$$\epsilon_\varphi = \frac{m_p^2}{2} \left(\frac{V'}{V} \right)^2 < 1$$



curvature

slope

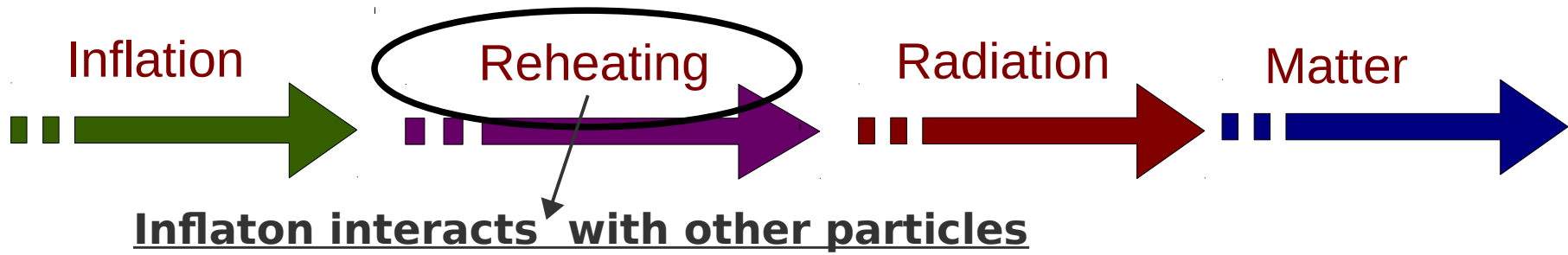
Slow-roll equation

$$\dot{\varphi} \simeq -V'/3H$$

Primordial spectrum

$$P_R \simeq \left(\frac{H}{\dot{\varphi}} \right)^2 \left(\frac{H}{2\pi} \right)^2 \quad n_s = 1 + 2\eta_\varphi - 6\epsilon_\varphi \quad r = 16\epsilon_\varphi$$

$$V^{1/4} \sim 10^{16} \left(\frac{r}{0.1} \right)^{1/4} \text{ GeV}$$

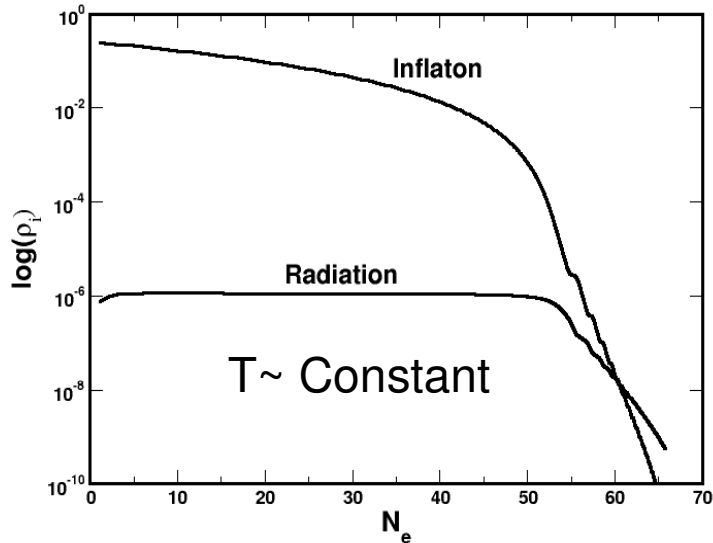


Interactions with the cosmic plasma induce **dissipation**

$$\ddot{\varphi} + (3H + Y)\dot{\varphi} + V_{\varphi} = 0$$

“Decay” into light dof = extra friction

“Warm” inflation:



A (small) fraction of the vacuum energy is converted into radiation during inflation

$$\dot{\rho}_R + 4H\rho_R = Y\dot{\varphi}^2 \quad \text{“Source term”}$$

$$\text{Slow-roll: } \begin{cases} (3H + Y)\dot{\varphi} \simeq -V_{\varphi} \\ 4H\rho_R \simeq Y\dot{\varphi}^2 \end{cases}$$

Extra friction term: $Q = Y/(3H)$ (Particle production versus Hubble friction)

- $Q \ll 1, T \ll H$ \longrightarrow Standard **Cold Inflation**
- $Q < 1, T > H$ \longrightarrow **Weak Dissipative Regime**

Standard slow-roll

- $Q > 1, T > H$ \longrightarrow **Strong Dissipative Regime**

Slow-roll : $3H(1+Q)\dot{\phi} \simeq -V_{\phi}(\phi, T), \quad \rho_r \simeq \frac{3}{4} Q \dot{\phi}^2$

$|n_{\phi}| < (1+Q), \quad \epsilon_{\phi} < (1+Q), \quad \beta_Y < (1+Q), \quad \delta_T < 1$

(Thermal corrections)

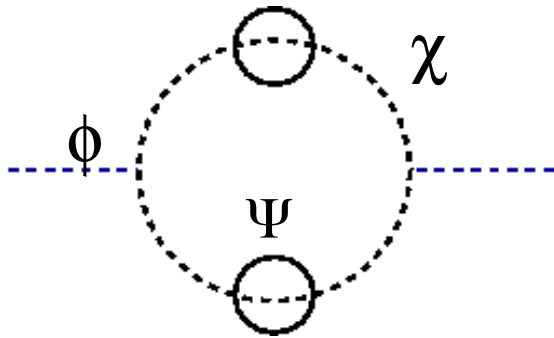
$\beta_Y = m_P^2 (Y_{\phi} V_{\phi}) / (Y V)$

$\delta_T = T V_{T\phi} / V_{\phi}$

- **Q varies during inflation**
- Extra friction prolongs inflation \longrightarrow Smaller ϕ values
- Dissipation induces thermal inflaton fluctuations

Interactions & Dissipative coefficient

Low T regime:



$$L = \dots - \frac{1}{2} m_\phi^2 \phi^2 - \frac{g^2}{2} \phi^2 \chi^2 + h \chi \psi \bar{\psi} + \dots$$

light fermions

heavy $m_\chi = g\phi > H, T$

BG, Berera, Ramos & Rosa 2012

$$Y \simeq \frac{32}{\sqrt{2\pi}} \frac{g^2 N_\chi}{h^2 N_Y} (m_\chi T)^{1/2} e^{-m_\chi/T} + 0.02 h^2 N_Y N_\chi \left(\frac{T^3}{\phi^2}\right) \simeq C_\phi \frac{T^3}{\phi^2}$$

Adiabatic approximation:



$$T > H$$

$$\dot{\phi}/\phi, \quad H < \Gamma_\chi \simeq h^2 m_\chi / (8\pi)$$

Macroscopic

Microscopic

- Easy to fulfill for not too small values of h

$$\frac{\Gamma_\chi}{\dot{\phi}/\phi} > \frac{\Gamma_\chi}{H} > \left(\frac{\Gamma_\chi}{m_\chi}\right) \left(\frac{m_\chi}{T}\right) \left(\frac{T}{H}\right) > 1$$

- Thermal corrections under control (inflaton coupled to heavy fields) + susy to control $T=0$ corrections

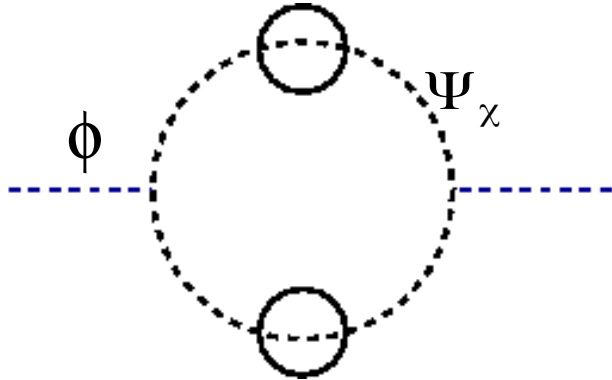
Getting 50-60 e-fold of inflation typically requires $C_\phi \sim 10^6$

Interactions & Dissipative coefficient

High T regime:

$$L = \dots - \frac{1}{2} m_\phi^2 \phi^2 - g \phi \bar{\psi}_\chi \psi_\chi - h \sigma \bar{\psi}_\chi \psi_\chi + \dots$$

light scalar



light $m_\psi = g\phi < H, T, \quad g \ll 1$

$$Y \simeq \frac{3}{1 - 0.34 \log h} \frac{g^2}{h^2} T$$

Linear T coefficient

Adiabatic approximation:



$T > H$

$$\dot{\phi}/\phi, \quad H < \Gamma_\chi \simeq \frac{\pi}{512} h^4 \left(\frac{T}{H} \right)$$

Macroscopic

Microscopic

- Small g coupling to keep fermions light

- Not too small h because of adiabatic condition

- How to avoid thermal corrections to inflaton potential due to light fields?

Thermal potential:

$$\Delta V_T = -\frac{\pi^2}{90} g_R T^4 + \frac{g^2 \phi^2}{12} T^2 + \dots$$

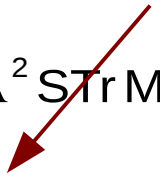
Little Higgs \longleftrightarrow Little inflaton

Naturalness problem in the SM (and inflation):

- Scalar field masses are not protected against quadratic radiative corrections by any sym. : **why $m_h = 125$ GeV ?** (why the inflaton is light $m_\phi < H$?)

(A) Susy : no. fermions = no. bosons

$$\Delta V_{T=0} \sim \Lambda^2 S \text{Tr} M^2 + \sum_{F,B} (-1)^{2s_i} (2s_i + 1) \frac{M^4}{64\pi^2} \ln \frac{M^2}{Q^2} + \dots$$



$$\xrightarrow{\text{green arrow}} \Delta V_T = -\frac{\pi^2}{90} g_R T^4 + \sum_{F,B} \frac{g_i^2 \phi^2}{12} T^2 + \dots \xrightarrow{\text{green arrow}} \text{Thermal Higgs mass}$$

(B) Little Higgs: Pseudo-Nambu Goldstone boson of a global symmetry
($m_h \sim$ soft breaking)

Cancellation of quadratic divergences occurs from particles of the same spin

$$\xrightarrow{\text{green arrow}} \Delta V_T = -\frac{\pi^2}{90} g_R T^4 + C T^2 + \dots \xrightarrow{\text{green arrow}} \text{No thermal Higgs mass (high T)}$$

Little warm inflation

- Consider a U(1) gauge theory spontaneously broken by two complex Higgs fields

$$\langle \varphi_1 \rangle = \langle \varphi_2 \rangle = M/\sqrt{2}$$

- One Nambu-Goldstone boson is “eaten” by the gauge field, and the other becomes the physical scalar inflaton field

$$\varphi_1 = \frac{M}{\sqrt{2}} e^{\varphi/M}, \quad \varphi_2 = \frac{M}{\sqrt{2}} e^{-\varphi/M}$$

- Couple the Higgses to charged and singlet Weyl fermions:

$$\begin{aligned} L &= \frac{g}{\sqrt{2}} (\varphi_1 + \varphi_2) \bar{\Psi}_{1L} \Psi_{1R} - i \frac{g}{\sqrt{2}} (\varphi_1 - \varphi_2) \bar{\Psi}_{2L} \Psi_{2R} + \text{hc} \\ &= gM \cos(\varphi/M) \bar{\psi}_1 \psi_1 - gM \sin(\varphi/M) \bar{\psi}_2 \psi_2 \end{aligned}$$

With interchange symmetry: $\varphi_1 \longleftrightarrow i\varphi_2$ $\Psi_{1L,R} \longleftrightarrow \Psi_{2L,R}$

Fermion masses are bounded!!

- Light fermions: $gM < T < M$

Little warm inflation

High T regime:

Inflaton a PNCB of a broken U(1) symmetry + pair of fermions + exchange sym.

$$L = \dots - g M \cos(\varphi/M) \bar{\psi}_1 \psi_1 - g M \sin(\varphi/M) \bar{\psi}_2 \psi_2 - h \sigma \sum_{i=1,2} (\bar{\psi}_i \psi_\sigma + \bar{\psi}_\sigma \psi_i) + \dots$$

light Ψ : $gM < T < M, g < 1$

Thermal potential:

$$\Delta V_T = -\frac{\pi^2}{90} g_R T^4 + \underbrace{\frac{g^2 M^2}{12} T^2}_{\text{No thermal mass for the inflaton}} + \frac{g^4(\varphi) M^4}{16 \pi^2} (\log \frac{\mu^2}{T^2} - c_f)$$

Light dof \nearrow

Total energy density:

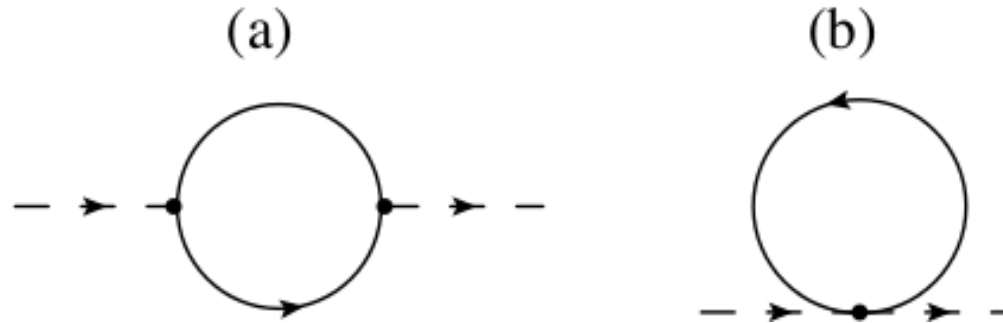
$$\rho_T = \frac{1}{2} \dot{\varphi}^2 + V(\varphi) + \rho_R \quad \left[\rho_R = \Delta V_T - T \frac{d\Delta V_T}{dT} = \frac{\pi^2}{30} g_R(\varphi, T) T^4 \right]$$

Effective no. of dof:

$$g_R(\varphi, T) \simeq g_R - \frac{5}{2\pi^2} \left(\frac{gM}{T}\right)^2 + \frac{15}{16\pi^4} \left(\frac{gM}{T}\right)^4 \left(3 + \cos\left(\frac{4\varphi}{M}\right)\right)$$

Inflaton self-energy

$$L = -\sum_i (m_i + g_i \delta\varphi + \frac{f_i}{2} \delta\varphi^2 + \dots) \bar{\Psi}_i \Psi_i$$



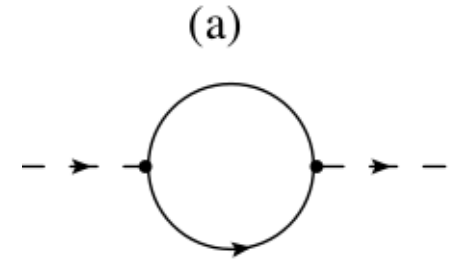
$$\Sigma_\varphi(0) = \sum_i (g_i^2 + m_i f_i) I_T(0) = g^2 \left(-\cos\left(2\frac{\varphi}{M}\right) + \cos\left(\frac{2\varphi}{M}\right) \right) I_T(0) = 0$$

$$I_T(0) = -\frac{\Lambda^2}{2\pi^2} + \frac{T^2}{6}$$

Cancellations of quadratic divergences and thermal masses!!

Dissipation

Dissipation comes from non-local terms (diagram (a))



No cancellation of dissipative terms:

$$Y = \frac{4}{T} \sum_i \int \frac{d^3 p}{(2\pi)^3} \frac{m_i^2}{\Gamma_i \omega_p^2} n_F(1+n_F) \simeq \frac{3}{1-0.34 \log h} \frac{g^2}{h^2} T$$

Linear T coefficient

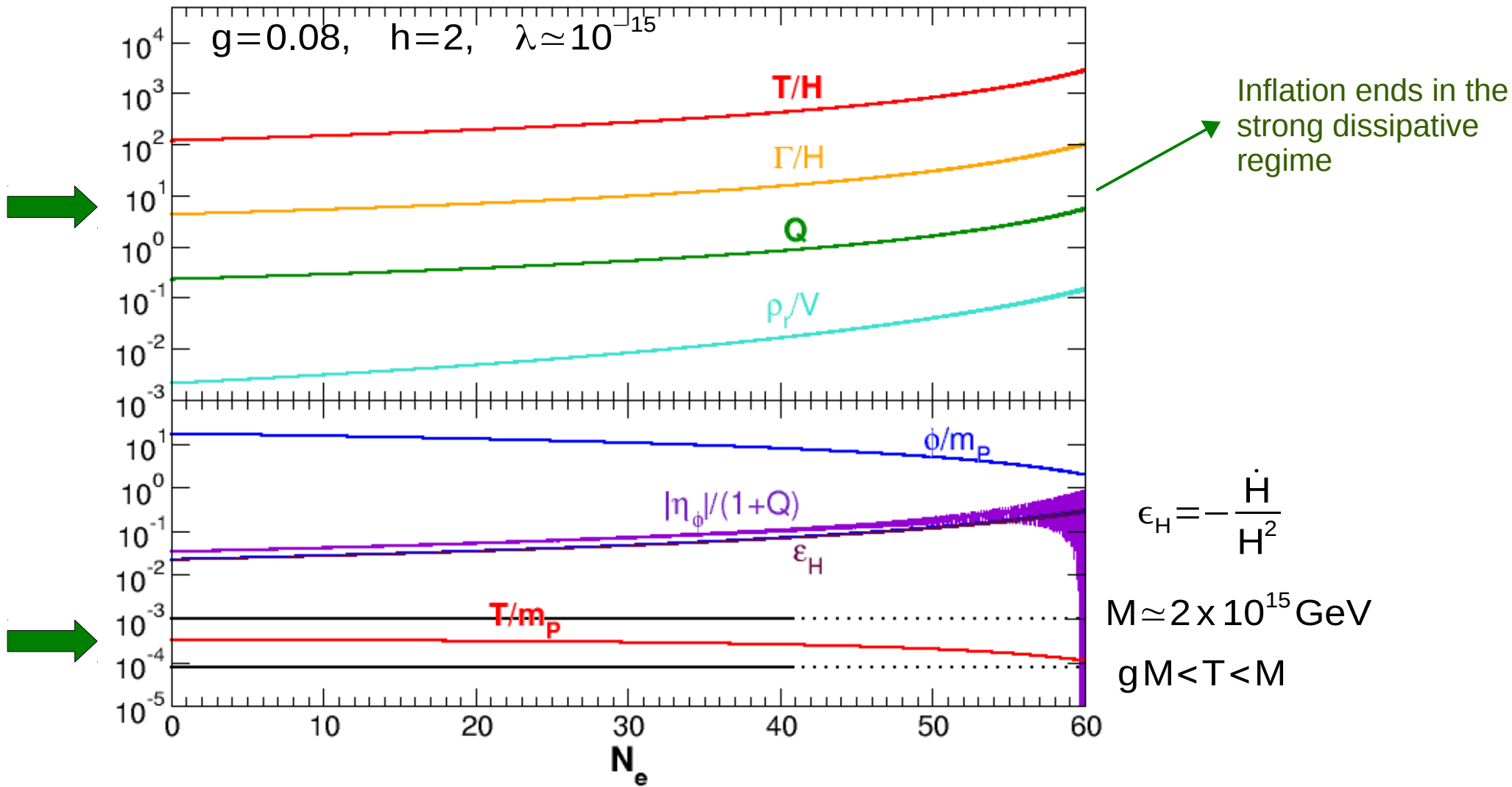
Decay rate $\Gamma_i = \frac{h^2}{16\pi} \frac{T^2 m_i^2}{\omega_p |\mathbf{p}|} F_T(\mathbf{p}/T, \omega_p/T)$ $[L = \dots - h\sigma \sum_i (\bar{\psi}_i \psi_\sigma + \bar{\psi}_\sigma \psi_i) + \dots]$

Additional Yukawa interactions with a massless field

Masses $m_i^2 \simeq h^2 T^2/8$

Background dynamics

Quartic potential: $V(\varphi) = \frac{\lambda}{4} \varphi^4$

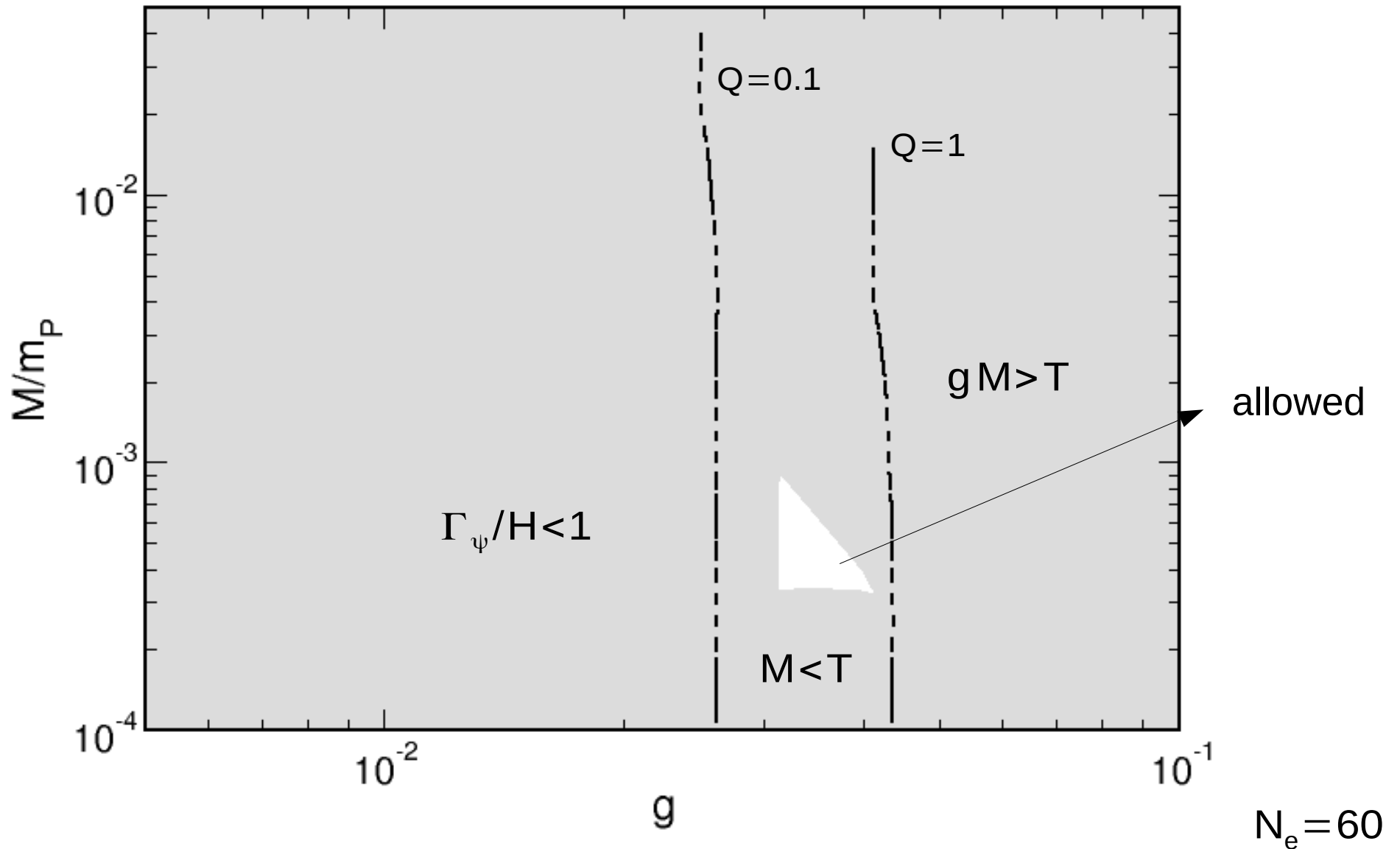


Parameter space: g, h, M

Decay rate: $\frac{\Gamma_\psi}{H} \simeq \frac{\pi}{514} h^4 \frac{T}{H} > 1$

$h=1$

Light fermions: $gM < T < M$

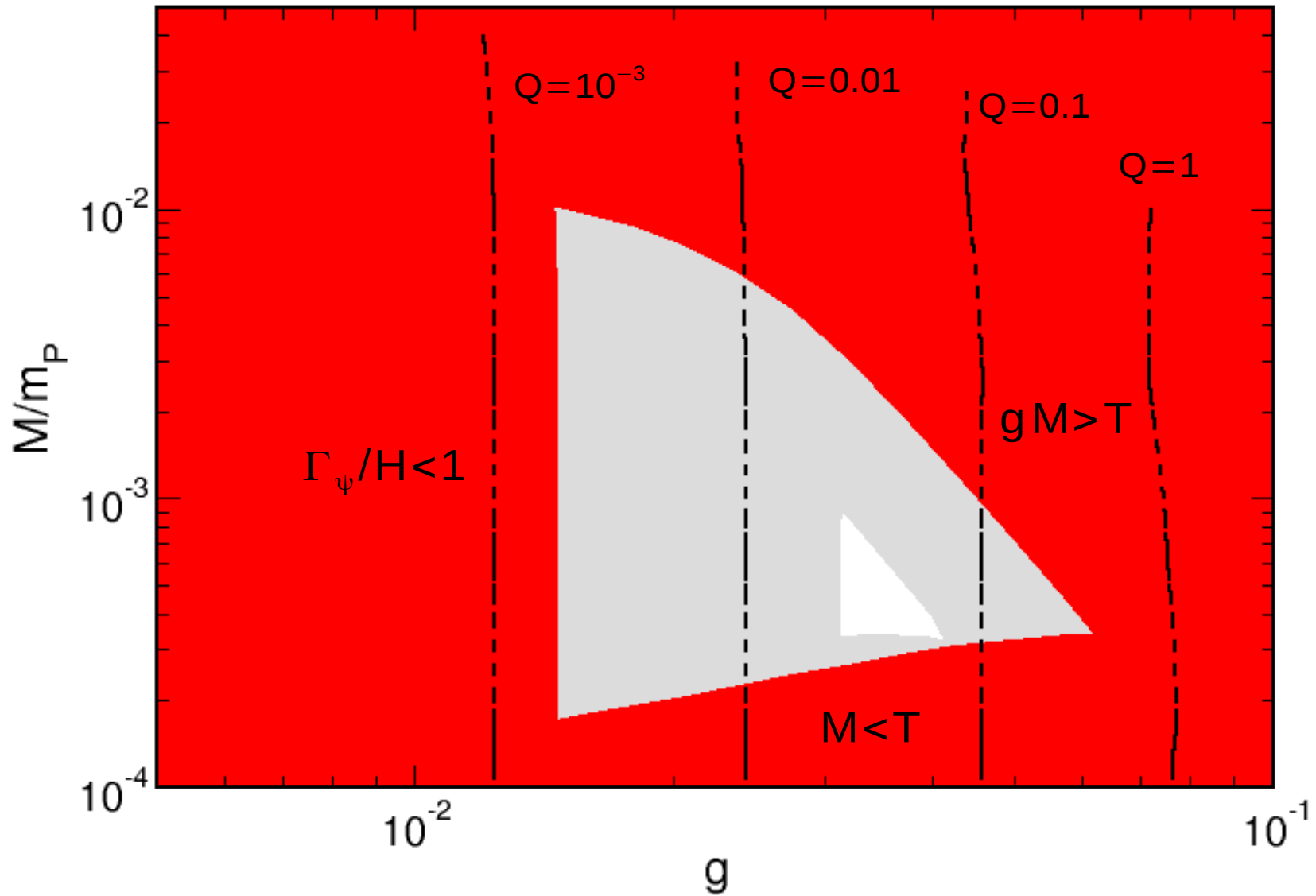


Parameter space: g, h, M

Decay rate: $\frac{\Gamma_\psi}{H} \simeq \frac{\pi}{514} h^4 \frac{T}{H} > 1$

$h=2$

Light fermions: $gM < T < M$



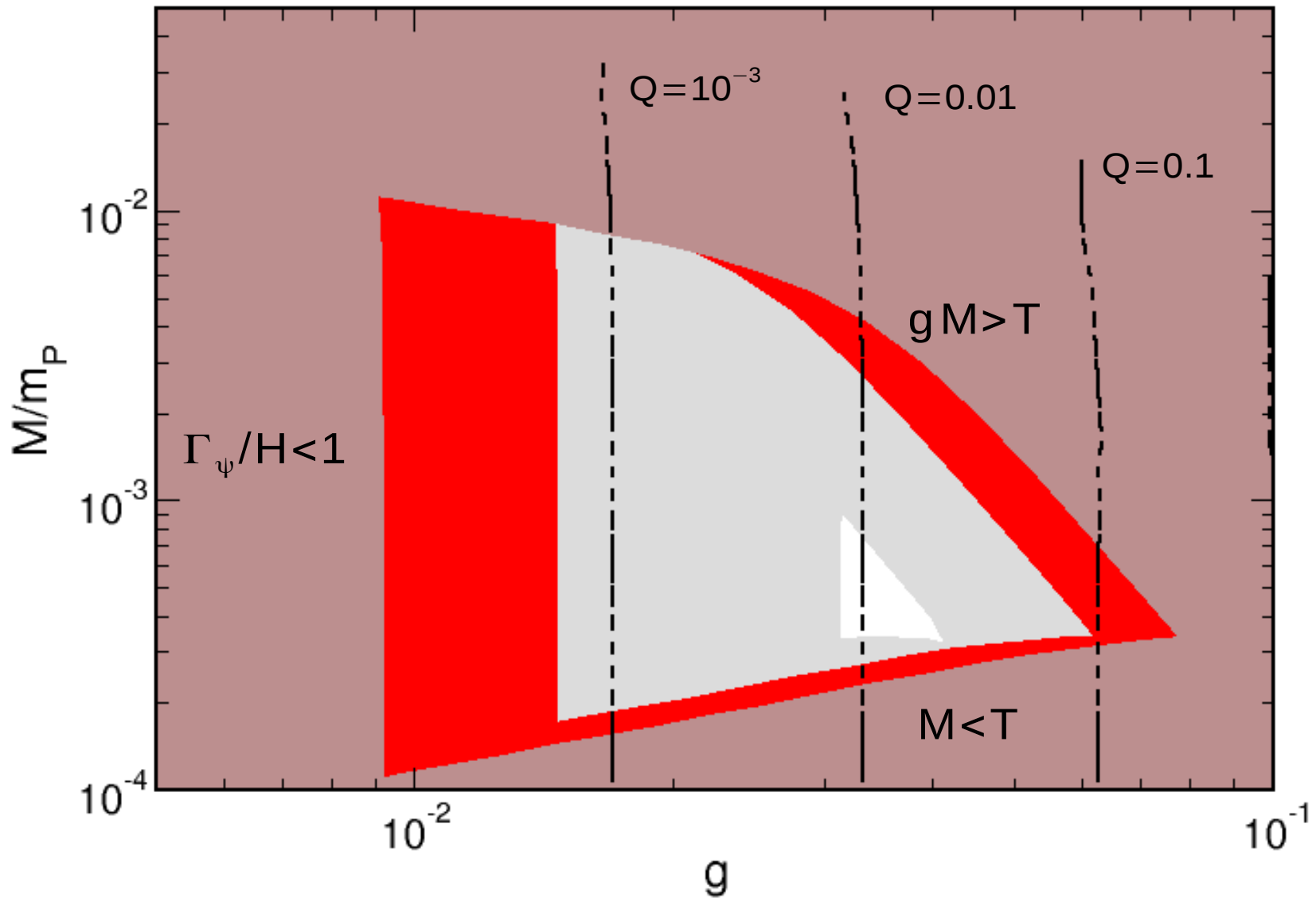
$N_e = 60$

Parameter space: g, h, M

Decay rate: $\frac{\Gamma_\psi}{H} \simeq \frac{\pi}{514} h^4 \frac{T}{H} > 1$

$h=3$

Light fermions: $gM < T < M$

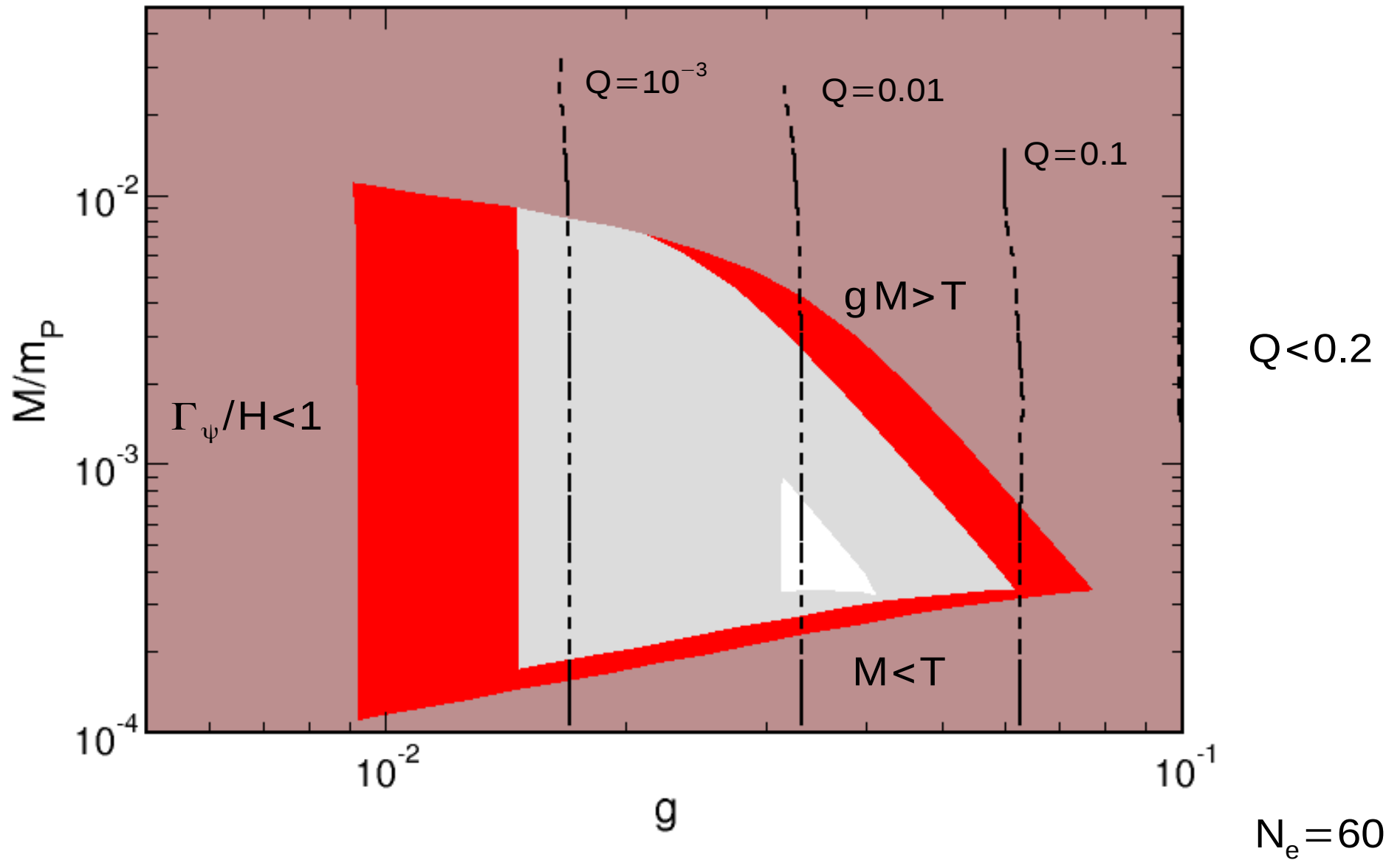


$N_e = 60$

Parameter space: g, h, M

$$10^{14} \text{ GeV} < M < 10^{16} \text{ GeV}$$

$h=3$



Fluctuations & primordial spectrum: coupled system

Field EOM:

$$\delta \ddot{\varphi}_k^{\text{GI}} + (3H + Y) \delta \dot{\varphi}_k^{\text{GI}} + \dot{\varphi} \delta Y^{\text{GI}} + \left(\frac{k^2}{a^2} + V_{\varphi\varphi} \right) \delta \varphi_k^{\text{GI}} \simeq (2Y\mathcal{T})^{1/2} \hat{\xi}_k$$

\rightarrow

$$\frac{\delta Y^{\text{GI}}}{Y} = \frac{1}{4} \frac{\delta \rho_r^{\text{GI}}}{\rho_r} \simeq \frac{\delta \mathcal{T}}{\mathcal{T}}$$
 \rightarrow
Coupled system
inflaton-radiation

Radiation (fluid stress energy-tensor): $T_{\text{rad}}^{\mu\nu} = (\rho_r + p_r) u^\mu u^\nu + p_r g^{\mu\nu}$

$$\delta \dot{\rho}_r^{\text{GI}} + 4H \delta \rho_r^{\text{GI}} \simeq \frac{k^2}{a^2} \Psi_r^{\text{GI}} + \dot{\varphi}^2 \delta Y^{\text{GI}} + 2\dot{\varphi} Y \delta \dot{\varphi}^{\text{GI}}$$

$$\dot{\Psi}_r^{\text{GI}} + 3H \Psi_r^{\text{GI}} \simeq -\delta \rho_r^{\text{GI}} / 3 - \dot{\varphi} Y \delta \varphi^{\text{GI}} \quad \text{Momentum density}$$

(Gauge invariant perturbations: $\delta \varphi_k^{\text{GI}} = \delta \varphi - \frac{H}{\dot{\varphi}} \phi$, ϕ :metric perturbation)

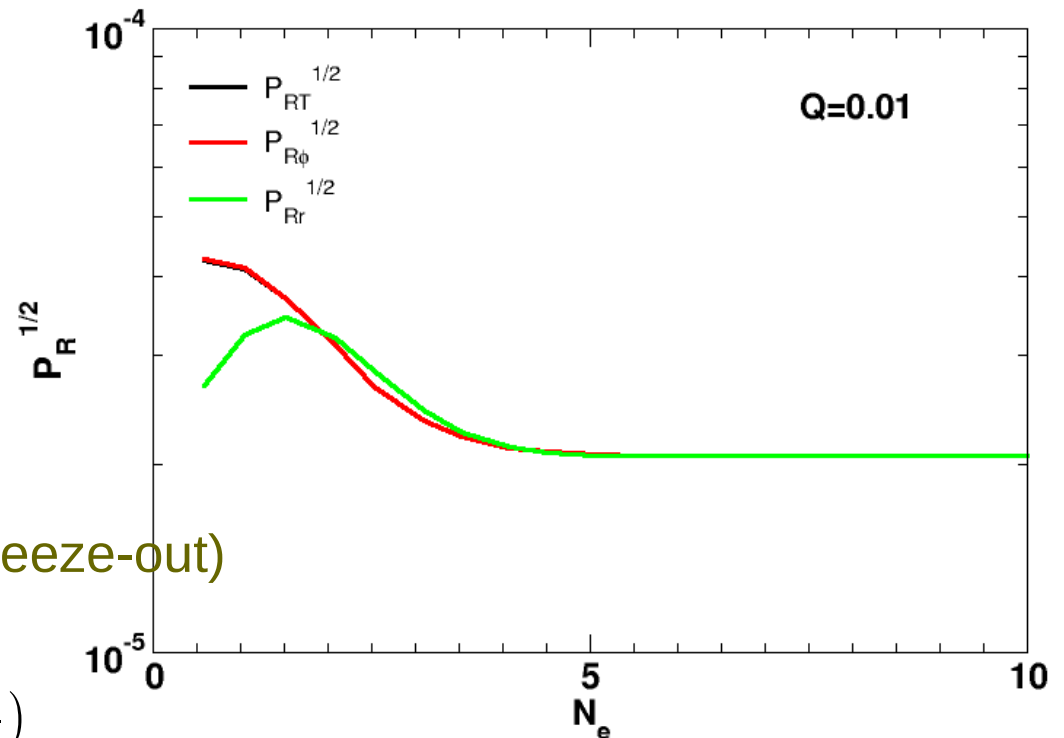
Fluctuations & primordial spectrum: coupled system

Weak dissipative regime ($Q=Y/H \ll 1$) : field decoupled from radiation

$$\delta \ddot{\varphi}_k^{GI} + (3H + Y) \delta \dot{\varphi}_k^{GI} + \left(\frac{k^2}{a^2} + V_{\varphi\varphi} \right) \delta \varphi_k^{GI} \simeq (2YT)^{1/2} \hat{\xi}_k$$

$$P_{\delta\varphi} \simeq \frac{HT}{2\pi} \frac{Q}{\sqrt{1+4\pi Q/3}}$$

Primordial spectrum: $P_R \simeq \left(\frac{H}{\dot{\varphi}} \right)^2 P_{\delta\varphi}$



R is constant after horizon crossing (freeze-out)

$$P_R \simeq (P_R)_{Q=0} \left(1 + 2N + \frac{T}{H} \frac{4\pi Q}{\sqrt{1+4\pi Q/3}} \right)$$

Dissipative processes may maintain a non-trivial distribution of inflaton particles:

$$N \simeq n_{BE} = (e^{k/aT} - 1)^{-1}$$

Fluctuations & primordial spectrum: coupled system

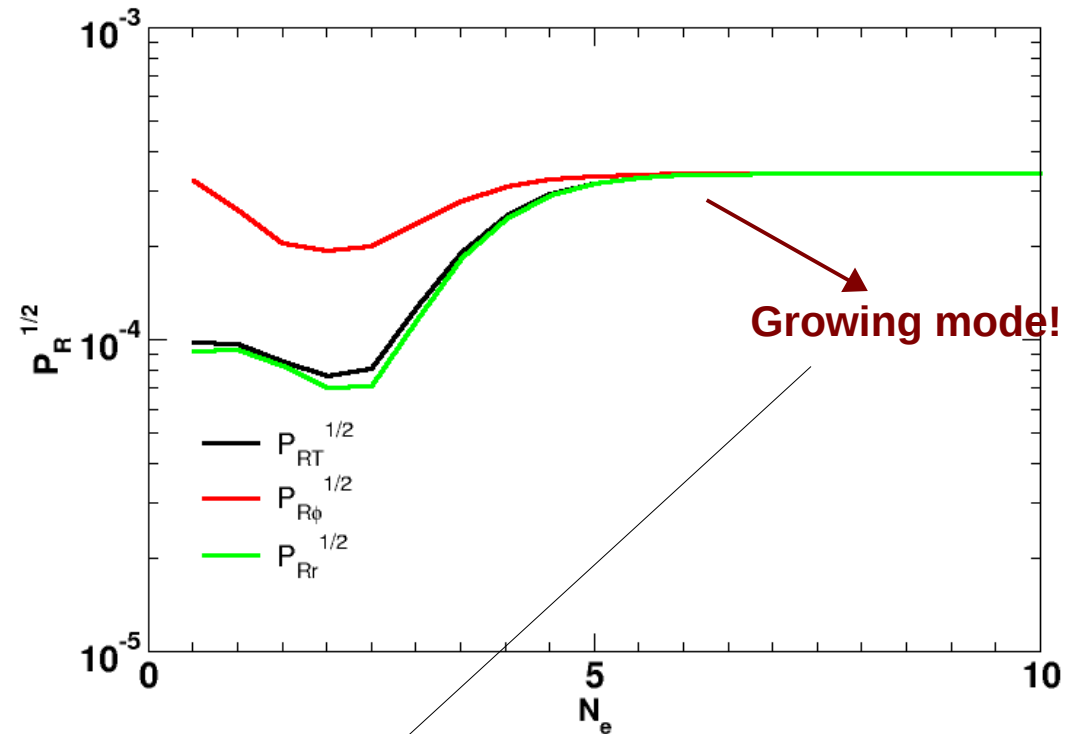
Strong dissipative regime ($Q=Y/H>1$) : coupled system

$$\delta \ddot{\varphi}_k^{GI} + (3H + Y) \delta \dot{\varphi}_k^{GI} + \dot{\varphi} \delta Y^{GI} + \left(\frac{k^2}{a^2} + V_{\varphi\varphi} \right) \delta \varphi_k^{GI} \simeq (2YT)^{1/2} \hat{\xi}_k$$

$Q=10$

Primordial spectrum:

$$P_R = \frac{h_\varphi}{h_T} P_{R_\varphi} + \frac{h_r}{h_T} P_{R_r} \simeq P_{R_r} \simeq P_{R_\varphi}, \quad (h_i = \rho_i + p_i)$$

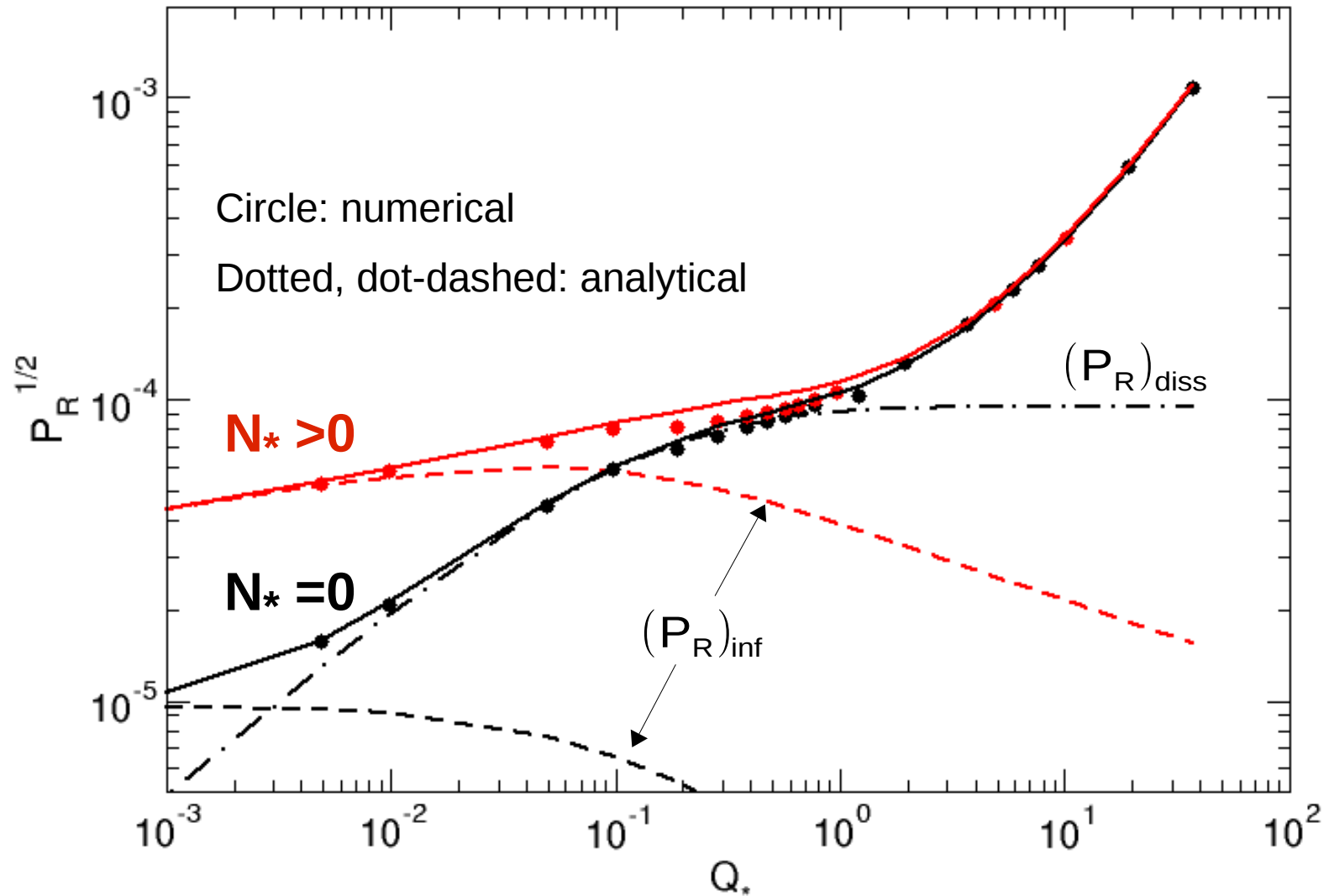


R is constant after horizon crossing

$$P_R \simeq \left(\frac{H}{\dot{\varphi}} \right)^2 \left(\frac{H}{2\pi} \right)^2 \left(1 + 2N + \frac{T}{H} \frac{4\pi Q}{\sqrt{1 + 4\pi Q/3}} \right) \times G[Q], \quad Q = Y/(3H)$$

Primordial spectrum

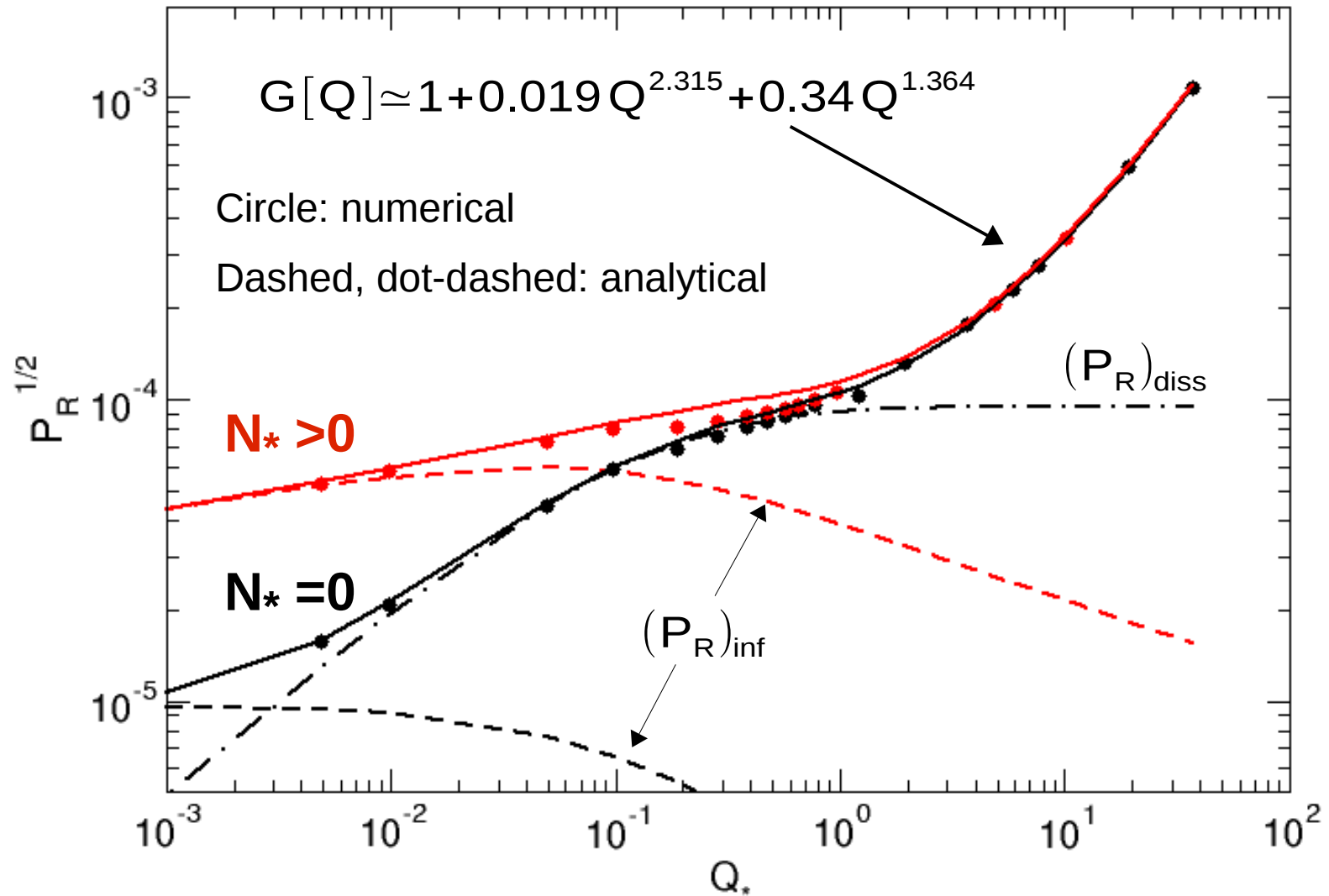
$$P_R \simeq ((P_R)_{\text{vac}} + (P_R)_{\text{diss}}) G[Q]$$



Chaotic model: $V(\varphi) = \lambda \varphi^4 / 4$, $\lambda = 10^{-14}$, $N_e = 50$

Primordial spectrum

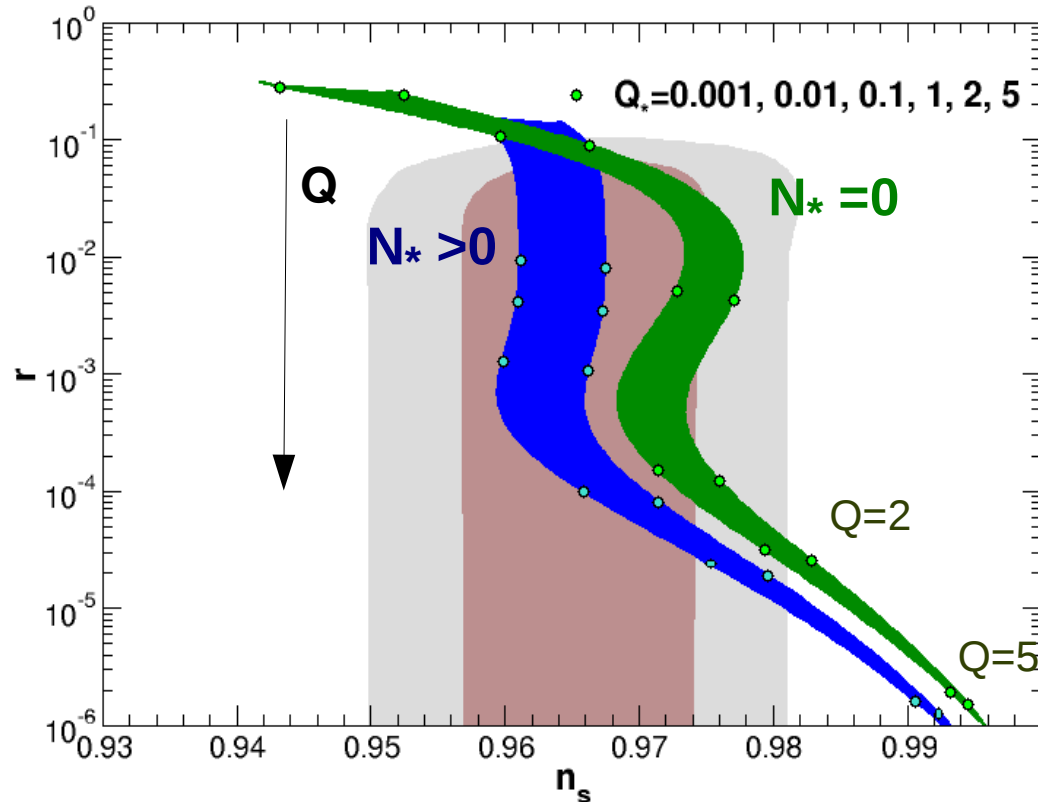
$$P_R \simeq ((P_R)_{\text{vac}} + (P_R)_{\text{diss}}) G[Q]$$



Chaotic model: $V(\varphi) = \lambda \varphi^4 / 4$, $\lambda = 10^{-14}$, $N_e = 50$

Primordial spectrum: quartic chaotic model

$$V(\varphi) = \frac{\lambda}{4} \varphi^4, \quad N_e = 50 - 60$$



$$n_s - 1 = \frac{d \ln P_R}{d N_e} = (n_s - 1)_N + (n_s - 1)_{\text{diss}} + (n_s - 1)_G, \quad (n_s - 1)_G > 0$$

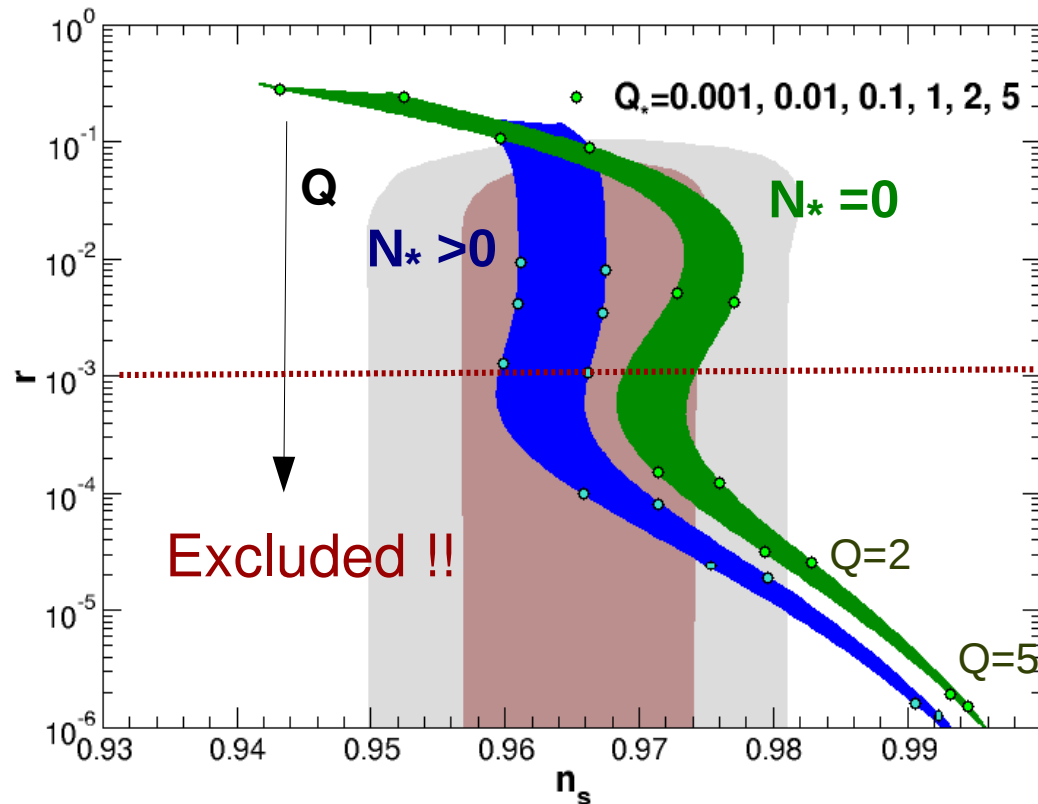
$$r \simeq \frac{16 \epsilon_\phi}{(1 + 2N + \Delta_Q) G[Q]} \leq 16 \epsilon_\phi$$

Quartic:

$$N \neq 0, Q < 1 : n_s \simeq 1 - 2/N_e, \quad r \simeq 16 \epsilon_\phi \left(\frac{H}{T} \right) \ll 0.1$$

Primordial spectrum: quartic chaotic model

$$V(\varphi) = \frac{\lambda}{4} \varphi^4, \quad N_e = 50 - 60$$



$Q > 0.1, \quad r > 0.001$

$$n_s - 1 = \frac{d \ln P_R}{dN_e} = (n_s - 1)_N + (n_s - 1)_{\text{diss}} + (n_s - 1)_G, \quad (n_s - 1)_G > 0$$

$$r \simeq \frac{16 \epsilon_\phi}{(1 + 2N + \Delta_Q) G[Q]} \leq 16 \epsilon_\phi$$

Quartic:

$$N \neq 0, \quad Q < 1 : \quad n_s \simeq 1 - 2/N_e, \quad r \simeq 16 \epsilon_\phi \left(\frac{H}{T} \right) \ll 0.1$$

Little warm inflation & CMB data

$$V(\varphi) = \lambda \varphi^4, \quad Q = C_T (T/3H), \quad \rho_R = \pi^2 g_r / 30 T^4 = C_r T^4$$

- **CosmoMC:** Λ CDM: $\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, \ln(A_s \times 10^{10}), n_s, r,$
6 parameters fit
- **WLI:** $\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, \lambda, C_T, g_r$

- **Input:** $P_R[N_e] \simeq \left(\frac{H}{\dot{\varphi}}\right)^2 \left(\frac{H}{2\pi}\right)^2 \left(1 + 2N + \frac{T}{H} \frac{4\pi Q}{\sqrt{1 + 4\pi Q/3}}\right) \times G[Q] \rightarrow P_R[k]$

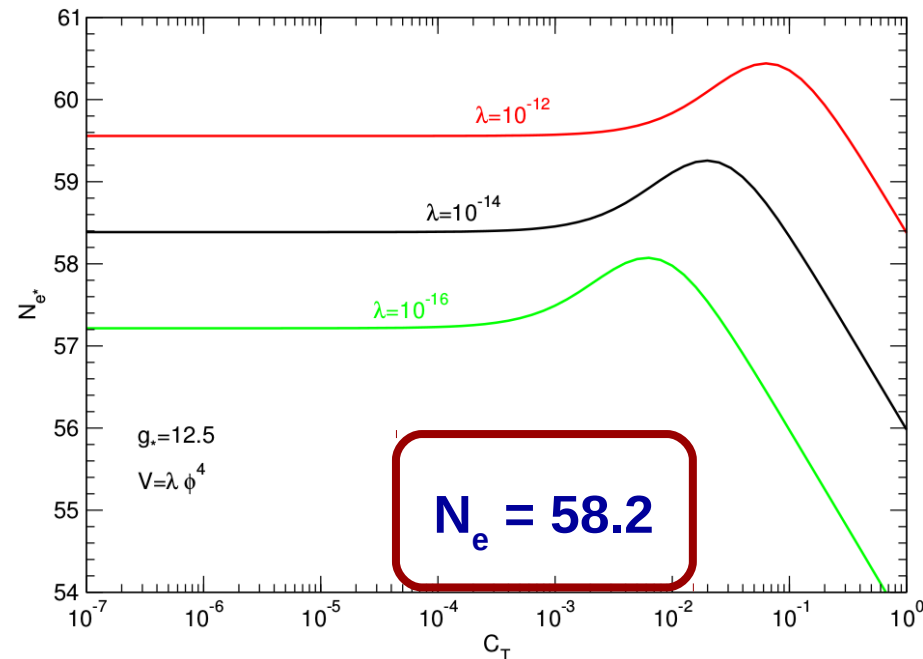
- $N_e = 56.12 - \ln \frac{k}{k_0} + \frac{1}{3(1+\tilde{w})} \ln \frac{2}{3} + \ln \frac{V_k^{1/4}}{V_{end}^{1/4}} + \frac{(1-3\tilde{w})}{3(1+\tilde{w})} \ln \frac{\rho_{RH}^{1/2}}{V_{end}^{1/4}} + \ln \frac{V_k^{1/4}}{10^{16} \text{ GeV}}$

\tilde{w} : Effective equation of state during reheating

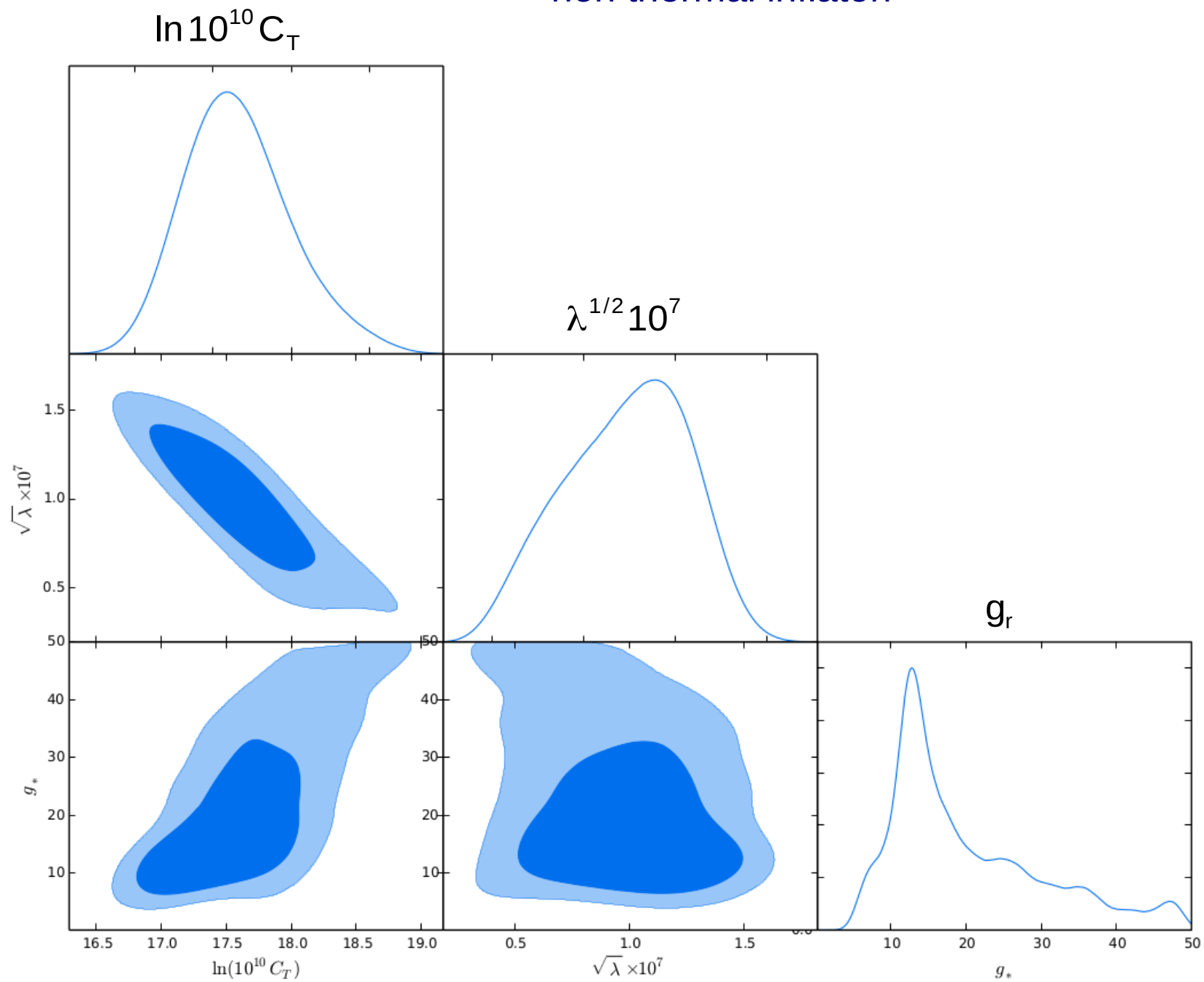
➔ $\tilde{w} = 1/3$ for a quartic chaotic model

➔ $N_e[k]$ Independent of T_{RH}

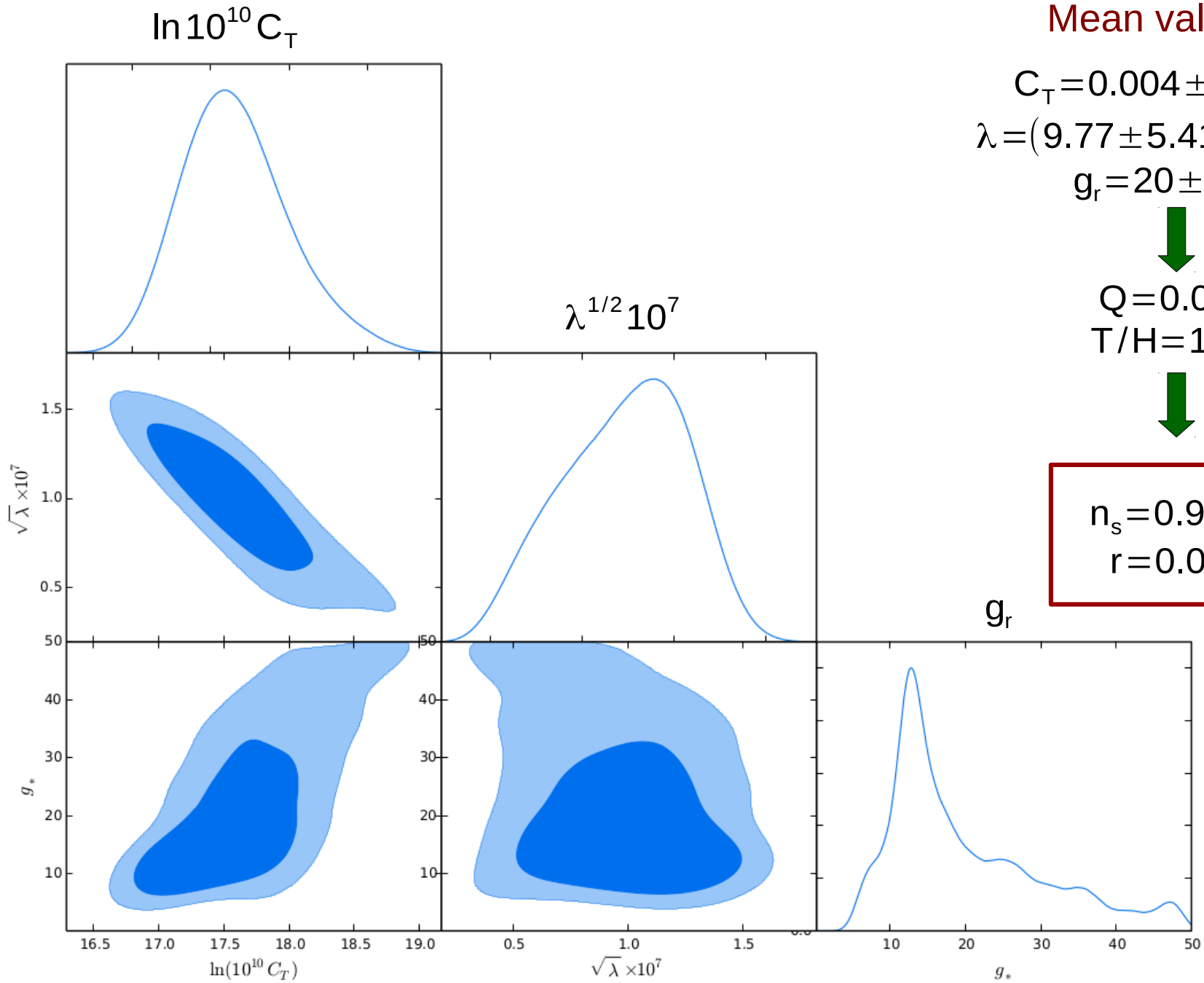
See also:
M. Benetti, R. Ramos, PRD95 (2017)
R. Ayra et al, JCAP02(2018)



Little warm inflation & CMB data: non thermal inflaton



Little warm inflation & CMB data: non thermal inflaton



Mean values

$$C_T = 0.004 \pm 0.002$$

$$\lambda = (9.77 \pm 5.41) \times 10^{-15}$$

$$g_r = 20 \pm 10$$



$$Q = 0.019$$

$$T/H = 19.3$$



$$n_s = 0.974$$

$$r = 0.06$$

Little warm inflation & CMB data: thermal inflaton

$\ln 10^{10} C_T$

Mean values

$$C_T = 0.010 \pm 0.008$$

$$\lambda = (9.74 \pm 6.78) \times 10^{-16}$$

$$g_r = 140 \pm 488$$

$$Q = 0.14$$

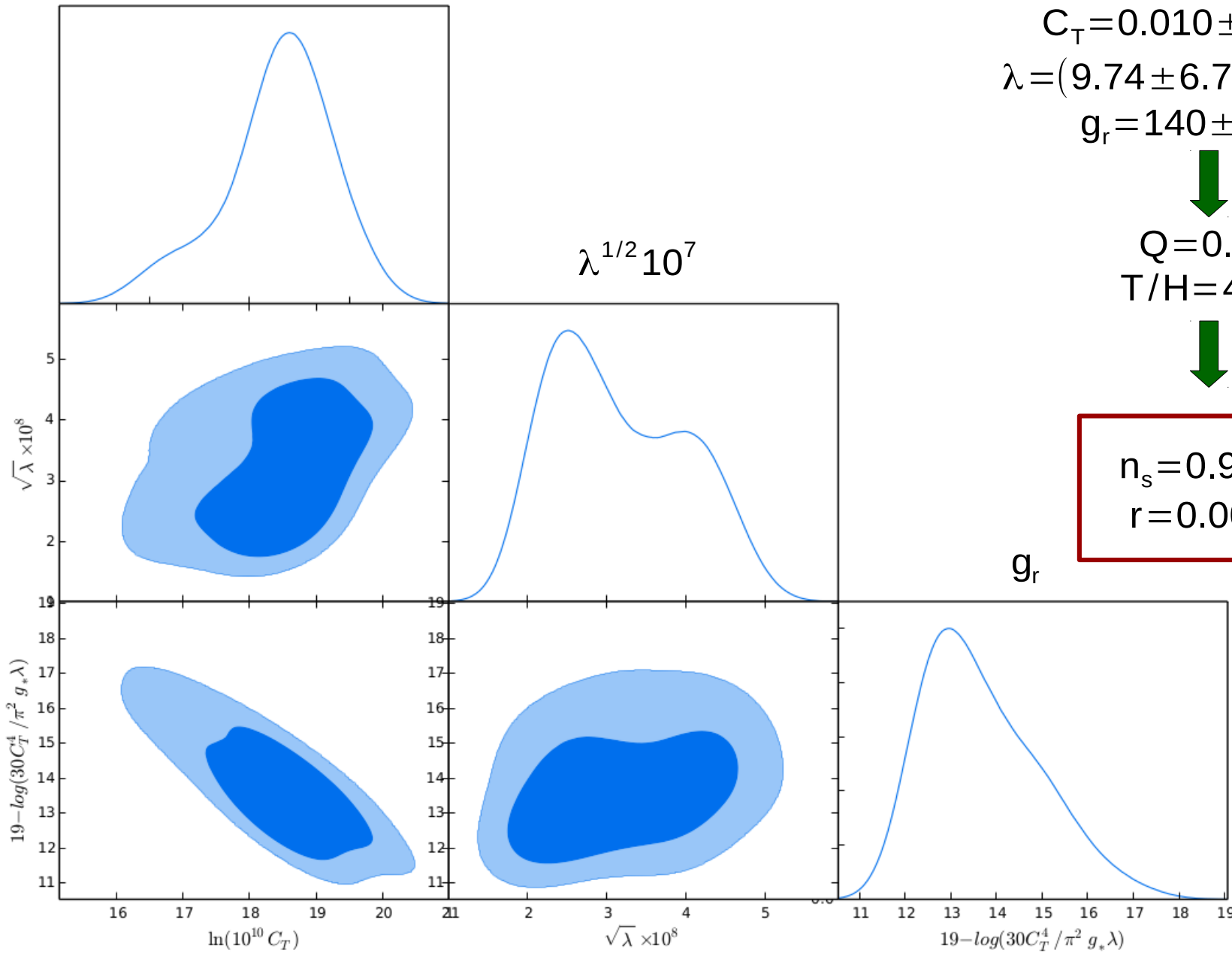
$$T/H = 40.7$$

$$n_s = 0.965$$

$$r = 0.006$$

$\lambda^{1/2} 10^7$

g_r



Summary

- Dissipative effects due to decaying fields can be relevant during inflation, and modify the inflationary predictions

- “Low T” regime for dissipation (massive scalar χ decaying into light dof): thermal corrections under control, but required large number of fields $N_\chi \sim 10^6$

- “High T” regime for dissipation (light fermion ψ decaying into light dof): $Y = C_T T$

Inflaton a PNCB of a broken U(1) symmetry + pair of fermions + exchange sym.

Light fermions: $gM < T$ + thermal corrections under control + minimal matter content

$\lambda\phi^4$ compatible with data, $Q^* \sim 0.01-0.1$, $r \sim 0.1-10^{-3}$

- For a T dependent dissipative coefficient, the field and radiation perturbation EOM form a coupled system: Field fluctuations are amplified before freeze-out ($Q < 1$)

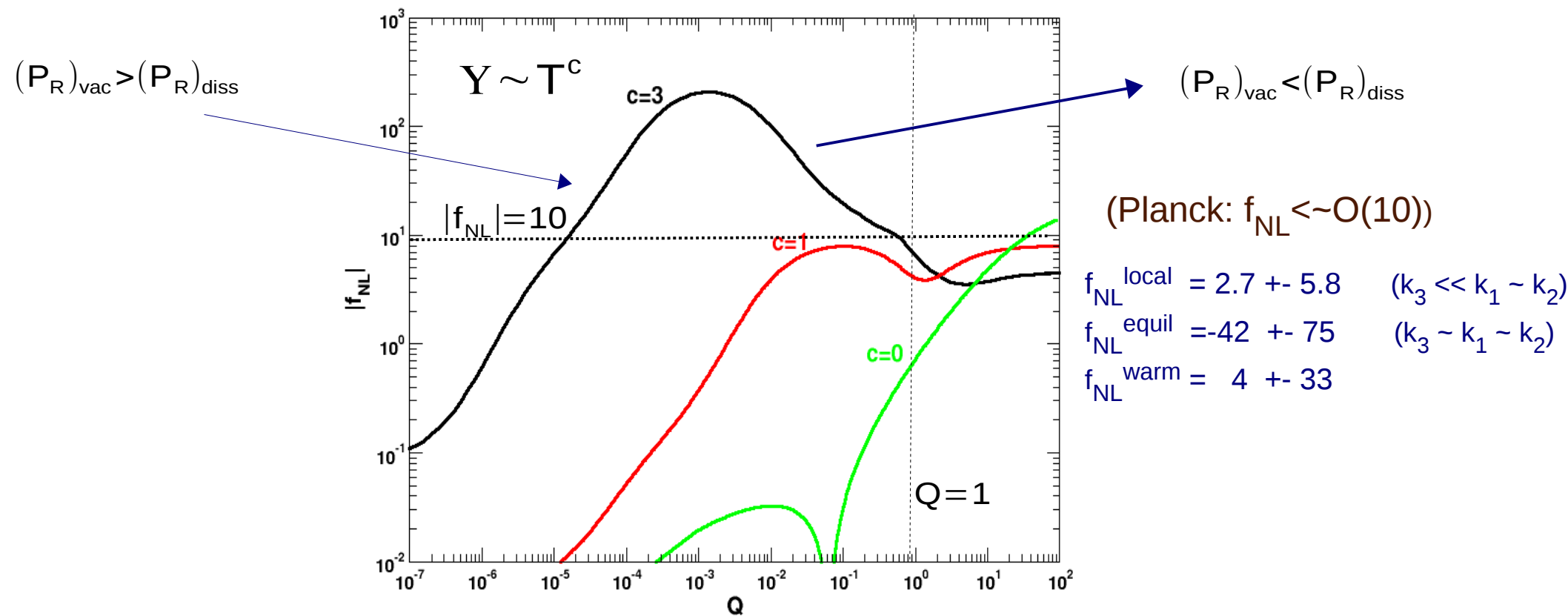
Blue-tilted spectrum for $Q \gg 1$

- Non-gaussianity compatible with observations for both weak and strong dissipative regime, with a characteristic shape

Warm inflation & Non-gaussianity : T dependent diss. coefficient

- Bispectrum:** $B_R(k_1, k_2, k_3) = \sum_{\text{cyc}} \langle R_1(k_1) R_1(k_2) R_2(k_3) \rangle = A_B(k) \bar{B}(k_1, k_2, k_3)$
- ↘ **shape**
- $$f_{\text{NL}} = \frac{18}{5} \frac{A_B(k)}{P_R(k)^2} \quad \text{Non-linear parameter}$$

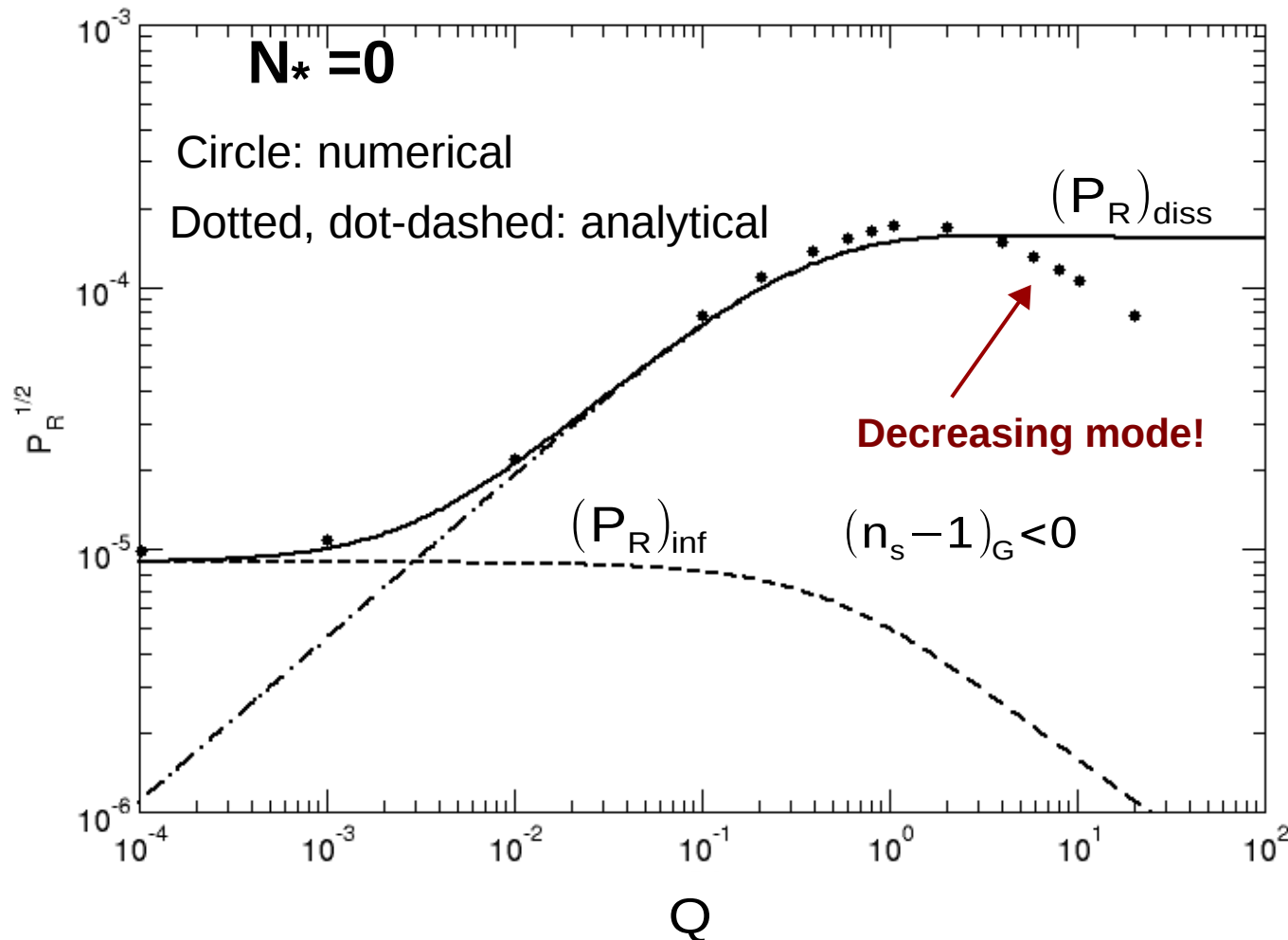
$$P_R \simeq ((P_R)_{\text{vac}} + (P_R)_{\text{diss}}) F[Q]$$



Primordial spectrum: $Y = C/T$

Light bosons decaying into light dof

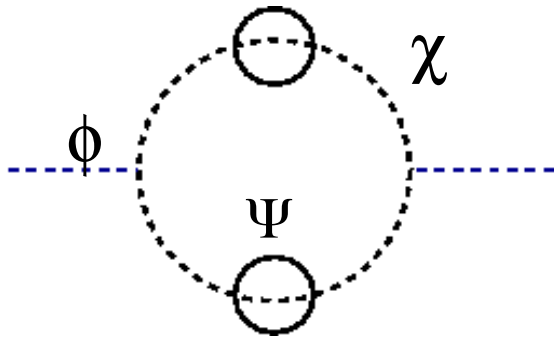
$$P_R \simeq ((P_R)_{\text{vac}} + (P_R)_{\text{diss}}) G[Q]$$



Chaotic model: $V(\varphi) = \lambda \varphi^4 / 4$, $\lambda = 10^{-14}$, $N_e = 50$

Interactions & Dissipative coefficient

Low T regime: (no thermal corrections)



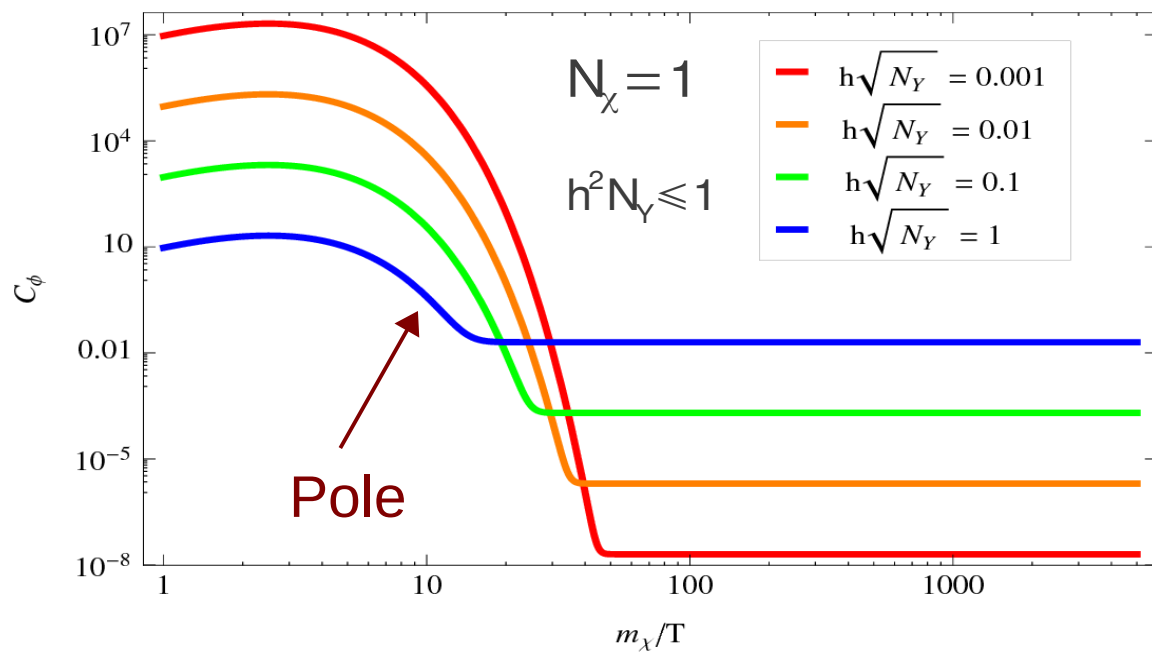
$$L = \dots - \frac{1}{2} m_\phi^2 \phi^2 - \frac{g^2}{2} \phi^2 \chi^2 + h \chi \psi \bar{\psi} + \dots$$

light fermions

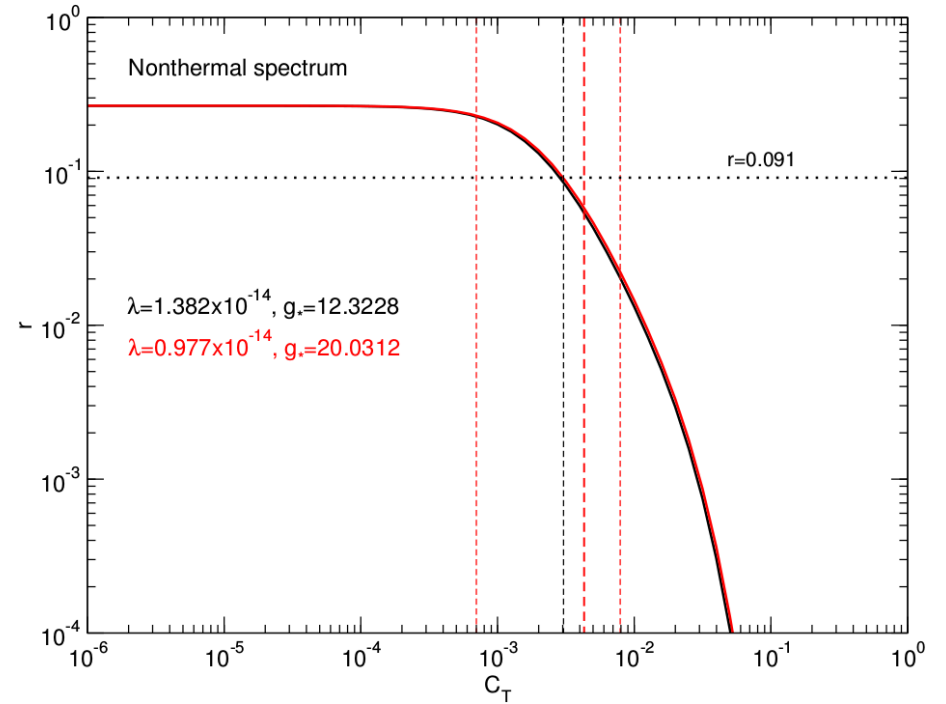
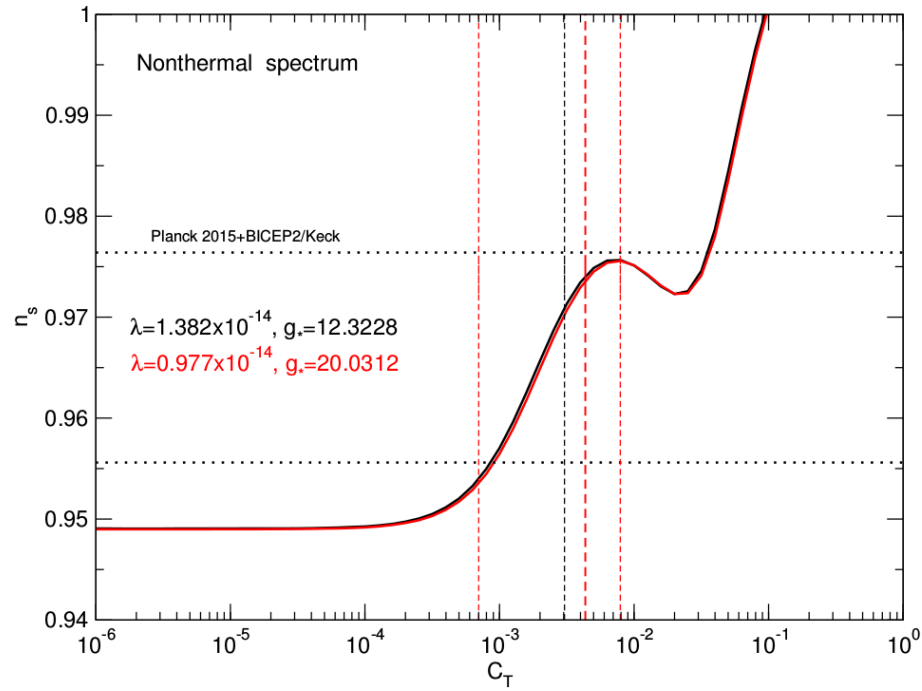
heavy $m_\chi = g\phi > H, T$

BG, Berera, Ramos & Rosa 2012

$$Y \simeq \frac{32}{\sqrt{2\pi}} \frac{g^2 N_\chi}{h^2 N_Y} (m_\chi T)^{1/2} e^{-m_\chi/T} + 0.02 h^2 N_Y N_\chi \left(\frac{T^3}{\phi^2}\right) \simeq C_\phi \frac{T^3}{\phi^2}$$



Little warm inflation & CMB data: non thermal inflaton



Little warm inflation & CMB data: thermal inflaton

