

PROTON DECAY

Constraints on New Physics

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Kerkyra, 13th September 2014

IST-ID



TÉCNICO
LISBOA



1939: Baryon Number Conservation

*E.C.G. Stückelberg observes that **protons** and neutrons do not decay into any combination of electrons, neutrinos, muons, or their antiparticles. The **stability of the proton** cannot be explained in terms of energy or charge conservation.*

1956: Parity and Charge Conjugation Violation

1964: CP Violation

1976: B+L non-conservation

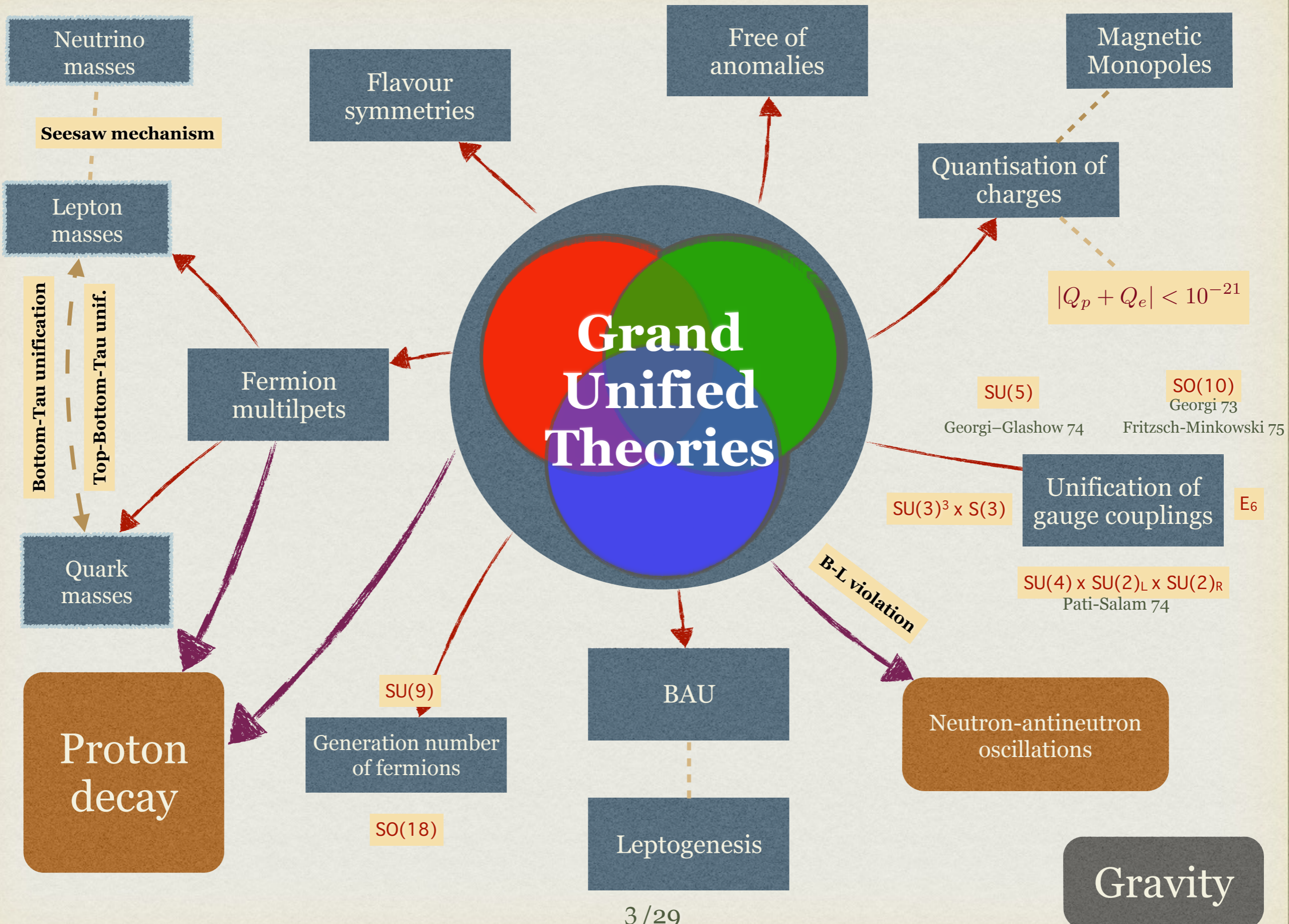
G. 't Hooft showed that in SM instantons induce B+L violation. B-L is still conserved.

1998: Lepton Family Number Violation

Neutrino oscillations are lepton family number violating.

Secular conservation laws: happen to be approx. true, but ultimately violated!

Grand Unified Theories



EXPERIMENTAL BOUNDS



Super-Kamiokande

22.5 kton fiducial volume

$$7.5 \times 10^{33} n + 6 \times 10^{33} p$$

SK-I: 1996 - 2001

11146 50-cm inner PMTs

40% coverage

1885 20-cm outer PMTs

SK-II: Jan 2003 - Oct 2005

Recovery from accident

5182 50-cm inner PMTs

Acrylic + FRP protective

Outer detector fully restored

SK-III: May 2006 - August 2008

Restored 40% coverage

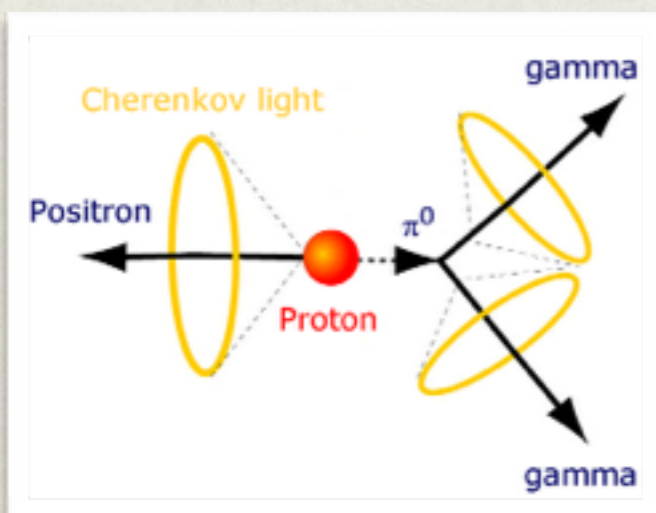
Outer detector segmented
(top | barrel | bottom)

SK-IV: September 2008 -

SK-IV Replace all electronics – 2008

T2K beam – late 2009

Add gadolinium



$$\tau(p \rightarrow e^+ \pi^0) > 1.01 \times 10^{34} \text{ yrs}$$

$$\tau(p \rightarrow K^+ \bar{\nu}) > 4 \times 10^{33} \text{ yrs}$$

- **Future prospects**

- Hyper-K (upgraded J-PARC): 20 times larger than Super-K
- LBNE (liquid Argon): the improvement in sensitivity compared to Super-K is not significant
- LENA (Liquid-scintillator detector): volume with for about **10** years it can reach $1.6 \times 10^{34} p$ years: $\tau_p \longrightarrow 4 \times 10^{34} \text{yrs}$

LAGUNA collaborative scientific project



STANDARD MODEL

- Gauge group (rank 4) :

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

$g_s \qquad g \qquad g'$

- Anomaly free theory with exact B-L symmetry
- 3 generations of fermions
- Right-handed neutrinos are absent
- Only one Higgs doublet needed

Quarks	$\begin{pmatrix} u \\ d \end{pmatrix}_L$	$\begin{pmatrix} u \\ d \end{pmatrix}_L$	$\begin{pmatrix} u \\ d \end{pmatrix}_L$	Leptons	$\begin{pmatrix} \nu \\ e^- \end{pmatrix}_L$
	u_R	u_R	u_R		
	d_R	d_R	d_R		e^-_R

STANDARD MODEL

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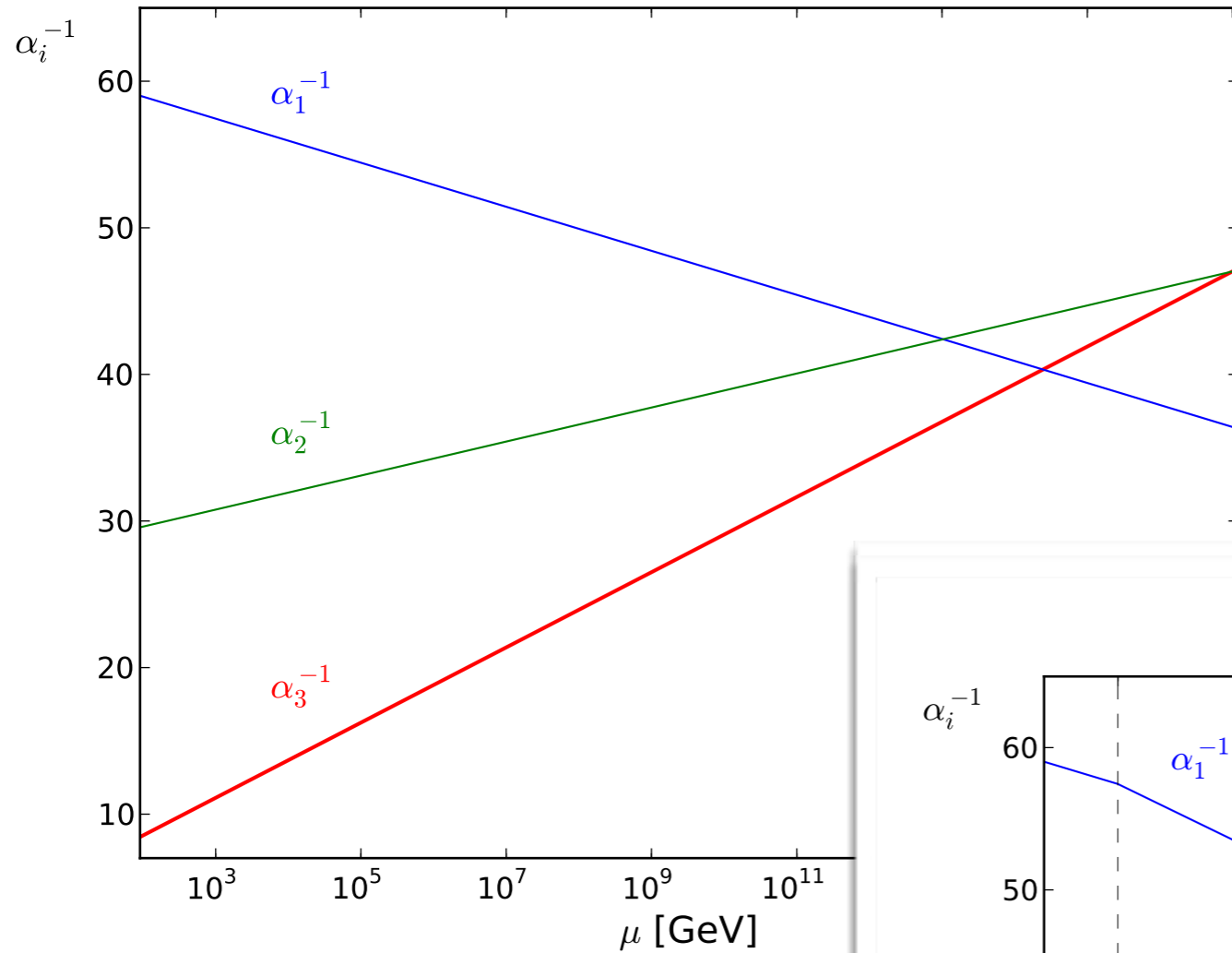
Quarks	$\begin{pmatrix} u \\ d \end{pmatrix}$	$\begin{pmatrix} u \\ d \end{pmatrix}$	$\begin{pmatrix} u \\ d \end{pmatrix}$	Leptons	$\begin{pmatrix} \nu \\ e^- \end{pmatrix}$
	u^c	u^c	u^c		e^+
	d^c	d^c	d^c		

SUPERSYMMETRY

- SUSY GUTs “natural extension of SM”
- Symmetry between fermions and bosons
- Stabilises the masses of the heavy scalar states ()
- Unification of gauge couplings
 - Needs threshold effects:
- Yukawa coupling unification $\Lambda \simeq 2 \times 10^{16} \text{GeV}, \alpha_5^{-1} \simeq 23$
- R-parity \longrightarrow LSP \longrightarrow dark matter candidate

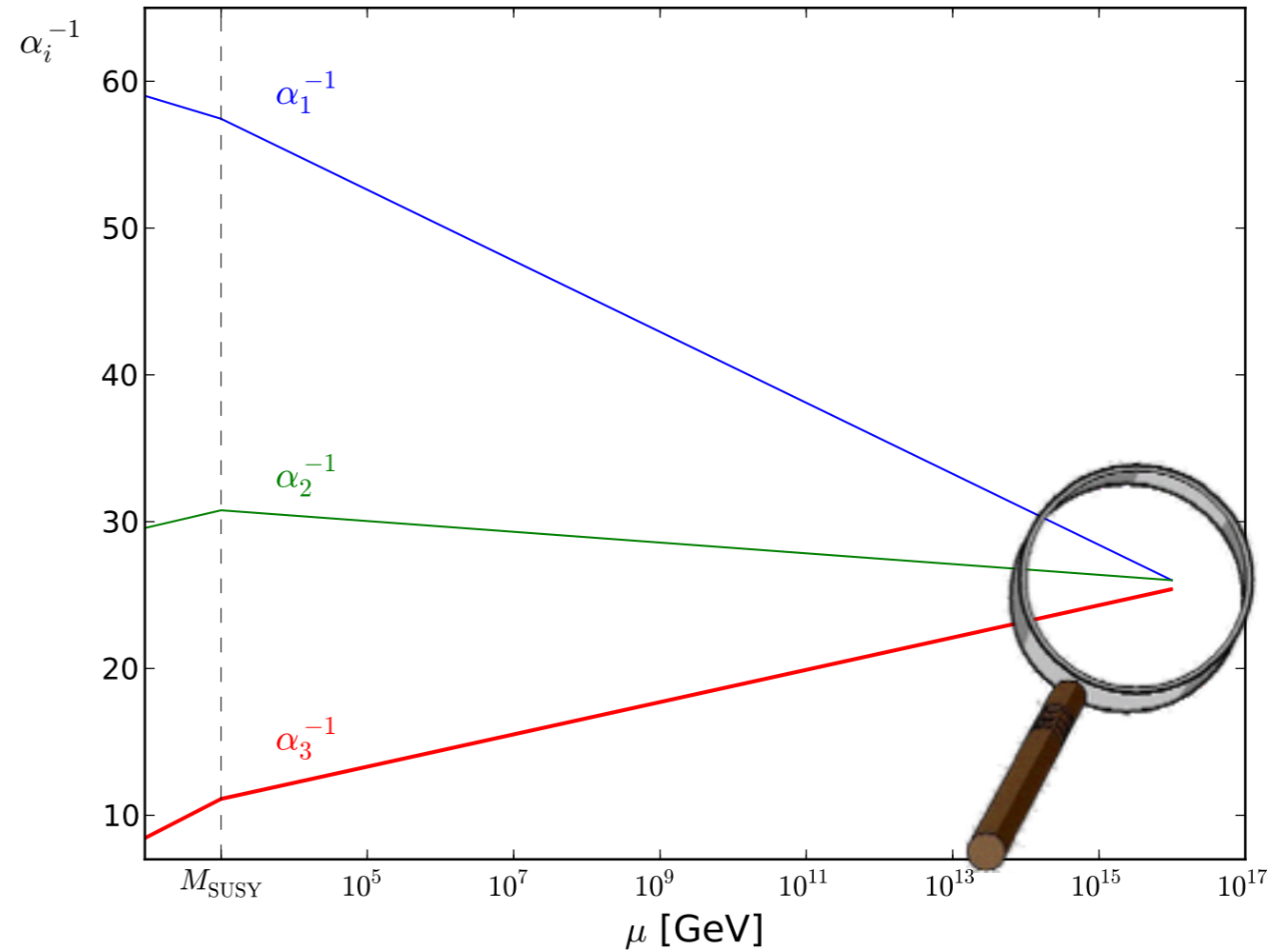
SM

$$\Lambda \simeq 10^{13-15} \text{ GeV}$$



MSSM

$$\Lambda \simeq 2 \times 10^{16} \text{ GeV}$$



MINIMAL (NON-)SUSY SU(5) GUT

[Georgi and Glashow]

- The simplest GUT group with rank 4
- Anomaly free and **B-L** conserving
- Contains the SM group $SU(3)_C \times SU(2)_L \times U(1)_Y$



$$5^* = \begin{pmatrix} d^c \\ d^c \\ d^c \\ e^- \\ -\nu \end{pmatrix} \quad 10 = \begin{pmatrix} 0 & u^c & -u^c & -u & -d \\ -u^c & 0 & u^c & -u & -d \\ u^c & -u^c & 0 & -u & -d \\ u & u & u & 0 & -e^+ \\ d & d & d & e^+ & 0 \end{pmatrix}$$

- Extra heavy gauge bosons X and Y that lead to **proton decay**

$$\alpha_3(\Lambda) = \alpha_2(\Lambda) = \frac{5}{3}\alpha_Y(\Lambda)$$

- **Breaking pattern (Higgs sector)**

$\Sigma(24)$ Breaks the GUT to the SM group

$H(5)$ Breaks the SM to QCD + QED

- **Higgs potential**

$$\frac{1}{2}m\text{Tr}\Sigma^2 + \frac{1}{3}a\text{Tr}\Sigma^3 + \frac{1}{4}\lambda_1\text{Tr}\Sigma^4 + \frac{1}{4}\lambda_2(\text{Tr}\Sigma^2)^2 + \overline{H}(\Sigma + 3\sigma)H$$

$$\langle \Sigma \rangle = \frac{\sigma}{\sqrt{60}} \text{diag}(2, 2, 2, -3, -3)$$

- **Doublet-triplet-splitting problem**

Fine-tuning

$$\mathcal{O}\left(\frac{v}{\sigma}\right) \sim 10^{-13}$$

- **Scalars after the spontaneous breaking**

$$H, H_c, \Sigma_3, \Sigma_8$$

- **Breaking pattern (Higgs sector)**

$\Sigma(24)$ Breaks the GUT to the SM group

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- **Higgs potential**

$$\frac{1}{2}m\text{Tr}\Sigma^2 + \frac{1}{3}a\text{Tr}\Sigma^3 + \frac{1}{4}\lambda_1\text{Tr}\Sigma^4 + \frac{1}{4}\lambda_2(\text{Tr}\Sigma^2)^2 + \overline{H}(\Sigma + 3\sigma)H$$

$$\langle \Sigma \rangle = \frac{\sigma}{\sqrt{60}} \text{diag}(2, 2, 2, -3, -3)$$

- **Doublet-triplet-splitting problem**

Missing Partner Mechanism

$$\mathcal{O}\left(\frac{v}{\sigma}\right) \sim 10^{-13}$$

- **Scalars after the spontaneous breaking**

$$H, H_c, \Sigma_3, \Sigma_8$$

- **Fermion masses**

$$\frac{1}{4} Y_1^{ij} 10_i 10_j H + \sqrt{2} Y_2^{ij} 10_i 5_j^* \bar{H}$$



Neutrinos are massless

$$Y_u^{ij} Q_i u_j^c H_f + Y_d^{ij} Q_i d_j^c \bar{H}_f + Y_e^{ij} e_i^c L_j \bar{H}_f$$

$$+ \frac{1}{2} Y_{qq}^{ij} Q_i Q_j H_c + Y_{ql}^{ij} Q_i L_j \bar{H}_c$$

$$+ Y_{ue}^{ij} u_i^c e_j^c H_c + Y_{ud}^{ij} u_i^c d_j^c \bar{H}_c$$

$$Y_u = Y_{qq} = Y_{ue} = Y_1 \quad Y_d = Y_e = Y_{ql} = Y_{ud} = Y_2$$

- **Predictions**

Incompatible

$M_e = M_d^T \quad M_u = M_u^T$
with observation extrapolated at GUT scale

$$m_b \approx m_\tau, \quad m_s \approx 3 m_\mu, \quad m_d \approx \frac{1}{3} m_e$$

- Fermion masses

$$\frac{1}{4} Y_1^{ij} 10_i 10_j H + \sqrt{2} Y_2^{ij} 10_i 5_j^* \bar{H}$$

SM

Neutrinos are massless

$$Y_u^{ij} Q_i u_j^c H_f + Y_d^{ij} Q_i d_j^c \bar{H}_f + Y_e^{ij} e_i^c L_j \bar{H}_f$$

$$+ \frac{1}{2} Y_{qq}^{ij} Q_i Q_j H_c + Y_{ql}^{ij} Q_i L_j \bar{H}_c$$

$$+ Y_{ue}^{ij} u_i^c e_j^c H_c + Y_{ud}^{ij} u_i^c d_j^c \bar{H}_c$$

$$Y_u = Y_{qq} = Y_{ue} = Y_1 \quad Y_d = Y_e = Y_{ql} = Y_{ud} = Y_2$$

- Predictions

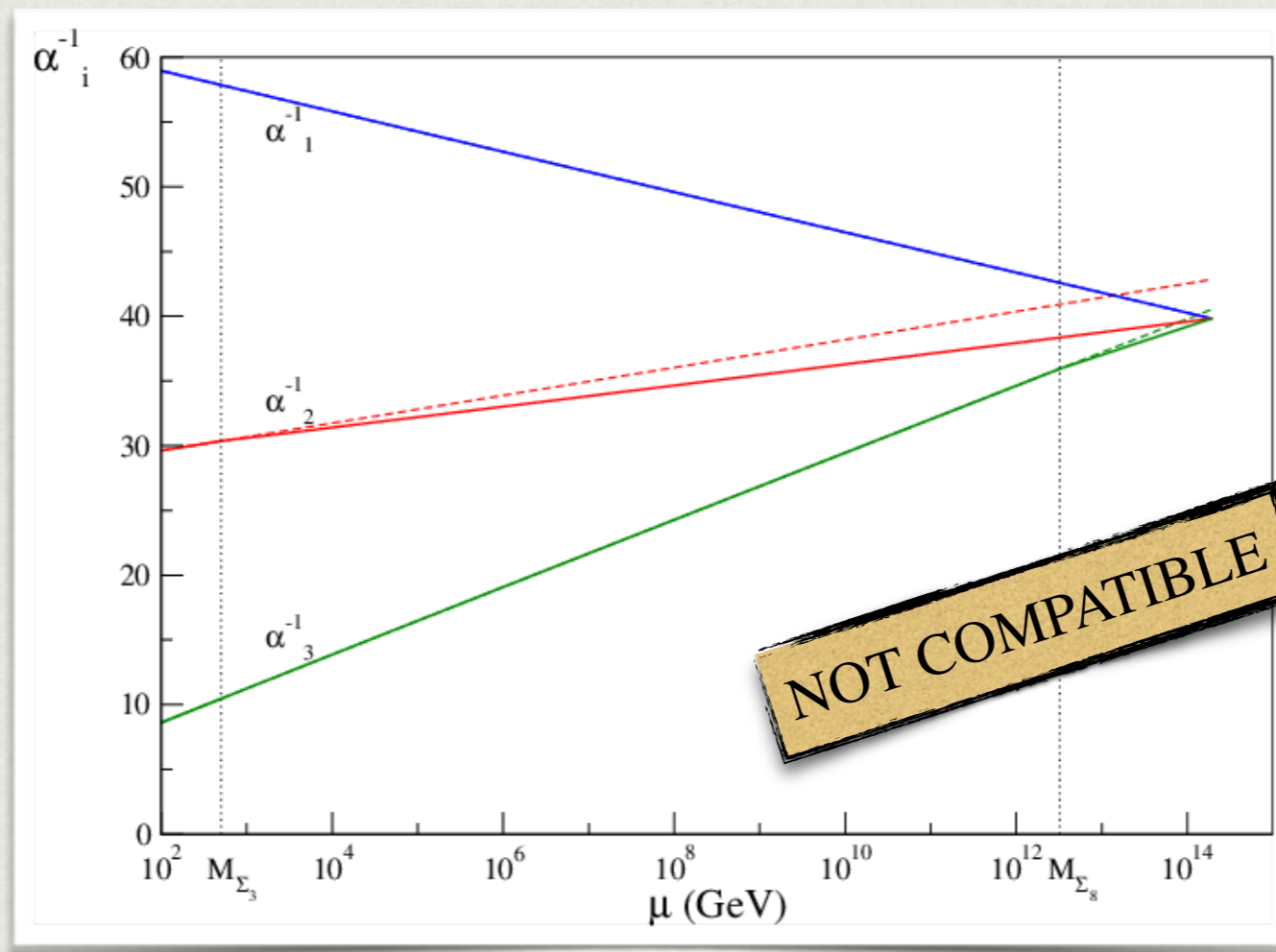
Incompatible

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with observation extrapolated at GUT scale

$$m_b \approx m_\tau, \quad m_s \approx 3 m_\mu, \quad m_d \approx \frac{1}{3} m_e$$

- Unification



$$1.3 \times 10^{14} \text{ GeV} \leq \Lambda \leq 2.4 \times 10^{14}$$

$$M_Z \leq M_{\Sigma_3} \leq 1.8 \times 10^4 \text{ GeV}$$

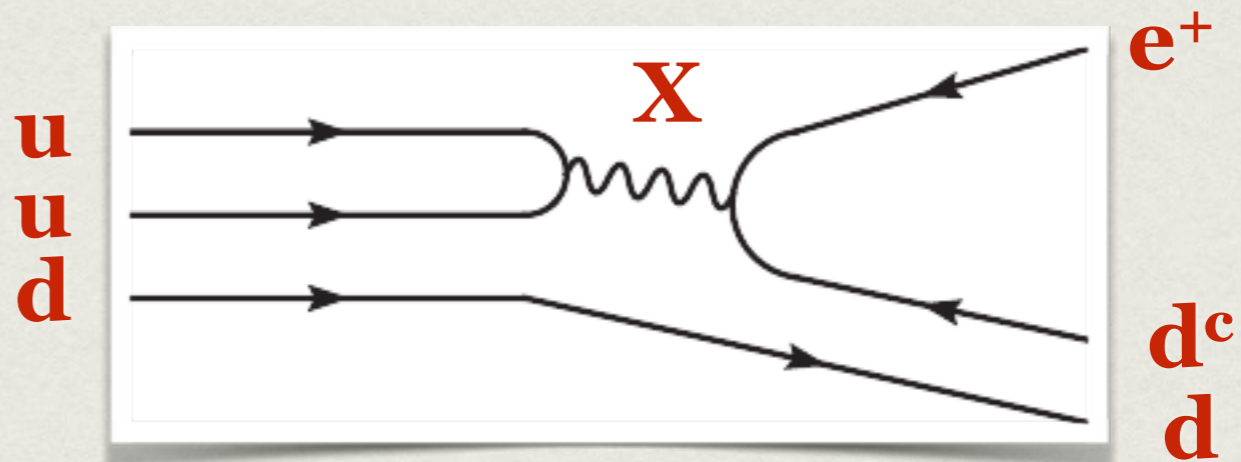
$$5.4 \times 10^{11} \text{ GeV} \leq M_{\Sigma_8} \leq 1.3 \times 10^{14} \text{ GeV}$$

- **Heavy gauge bosons X and Y**

$$M_V = \frac{25}{8} g_U^2 \sigma^2$$

- **Dominant contribution**

$$\Gamma \approx \alpha_U^2 \frac{m_p^5}{M_V^4}$$



$$\tau(p \rightarrow \pi^0 e^+) > 1.4 \times 10^{34} \text{ y} \implies M_V > (4.9 - 5.1) \times 10^{15} \text{ GeV}$$

- **Yukawa coupling contribution is suppressed**

$$\frac{(\Gamma_u)_{ij} (\Gamma_d)_{kl}}{M_{H_c}^2} \left[\frac{1}{2} (Q_i Q_j)(Q_k L_l) + (u_i^c e_j^c)(u_k^c d_l^c) \right]$$

CONSISTENT SU(5) MODEL

[Felevez-Pérez, Senjanovic, Bajc, Dorsner; E.-C., Wiesenfeldt]

- Non-renormalisable
- Fifth dimensional operators to account for the mismatch
- One expects new interactions above GUT scale (e.g. M_{Pl})
- Neutrinos are introduced as singlet fermionic fields
- Splitting between Σ_3, Σ_8 is more natural
- Unification issue can only be solved in SUSY

$$\sum_{n=1,2} \frac{\sqrt{2}}{\Lambda'} (\Delta_n)_{ij} H_{n a}^* 10_i^{ab} \Sigma_b^c 5_{jc}^*$$

$$M_d - M_e^\top = 5 \frac{\sigma}{\Lambda'} (v_1^* \Delta_1 + v_2^* \Delta_2)$$

two Higgs doublet needed

ADJOINT SU(5) MODEL

[Georgi, Jarlskog; Felevez-Pérez; Senjanovic et al.]

- Renormalisable

$$45_H = S_{(8,2)_{\frac{3}{10}}} \oplus S_{(6^*,1)_{-\frac{1}{5}}} \oplus S_{(3^*,2)_{-\frac{7}{10}}} \oplus S_{(3^*,1)_{\frac{4}{5}}} \oplus \Delta \oplus T_2 \oplus H_2$$

$$\langle 45_H^{\alpha 5}_{\beta} \rangle = v_{45} \left(\delta_{\alpha}^{\beta} - 4 \delta_4^{\alpha} \delta_{\beta}^4 \right), \alpha, \beta = 1, \dots, 4$$

- Neutrinos masses are via a fermionic $\rho(24)$
- Unification is successful
- Solves the mass mismatch

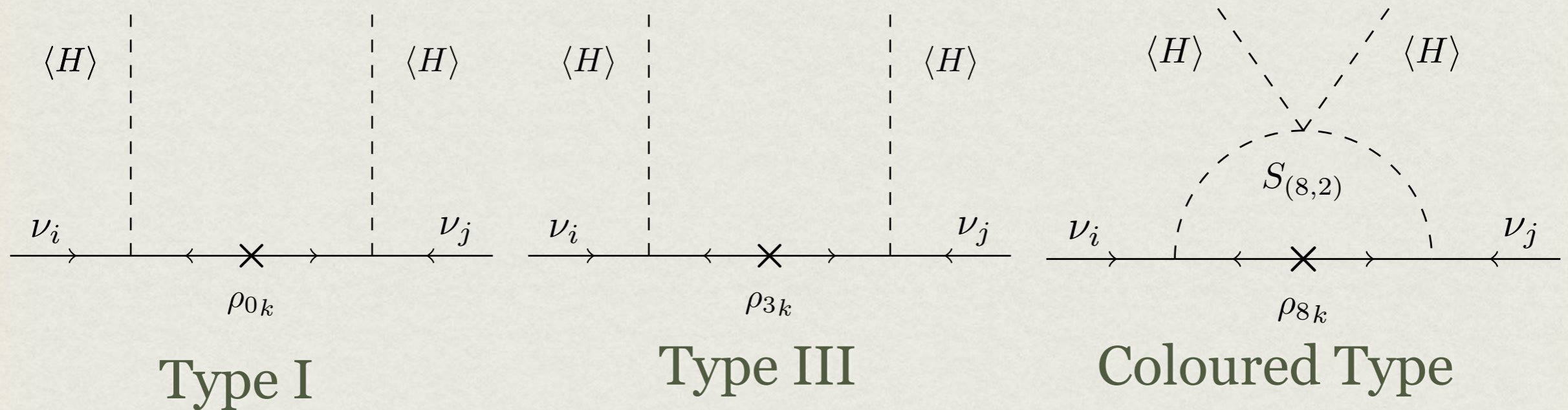
$$M_u = v_5 \Gamma_u^1 + 2 v_{45} \Gamma_u^2$$

$$M_d = v_5^* \Gamma_d^1 + 2 v_{45}^* \Gamma_d^2$$

$$M_e^T = v_5^* \Gamma_d^1 - 6 v_{45}^* \Gamma_d^2$$

$$M_d - M_e^T = 8 v_{45}^* \Gamma_d^2$$

- Neutrino masses (three seesaw mechanisms)



- Proton decay channels

$$\frac{(\Gamma_u^1)_{ij} (\Gamma_d^1)_{kl}}{M_{T_1}^2} \left[\frac{1}{2} (Q_i Q_j)(Q_k L_l) + (u_i^c e_j^c)(u_k^c d_l^c) \right]$$

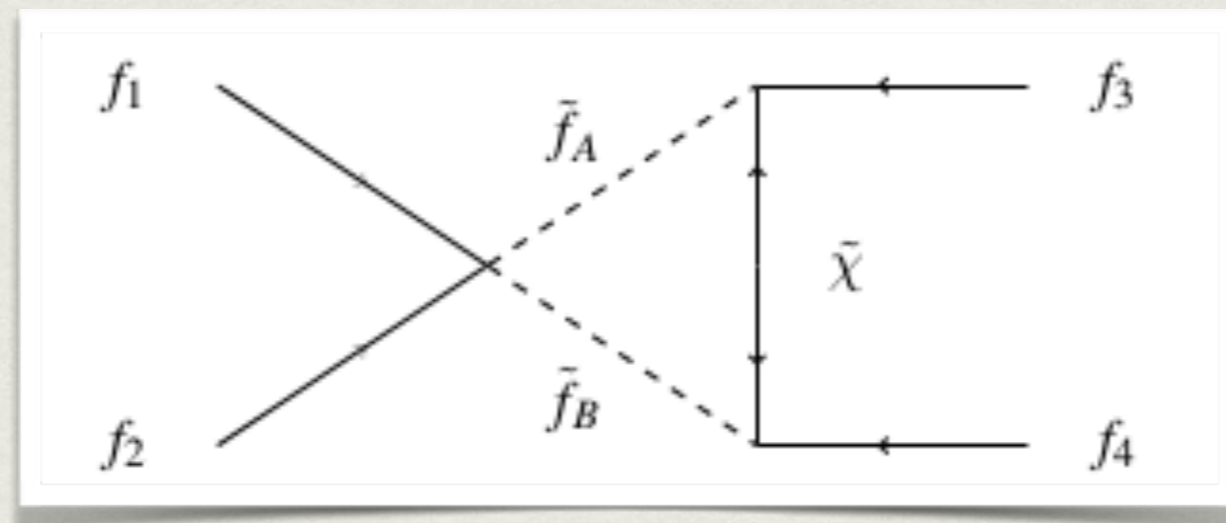
$$\frac{4 (\Gamma_u^2)_{ij} (\Gamma_d^2)_{kl}}{M_{T_2}^2} (u_i^c e_j^c)(u_k^c d_l^c)$$

$$\frac{(\Gamma_u^2)_{ij} (\Gamma_d^2)_{kl}}{2} \left\{ \frac{1}{M_{\Delta^{-1/3}}^2} \left[(u_i d_j)(u_k e_l) + (u_i d_j)(d_k \nu_l) \right] - \frac{1}{M_{\Delta^{2/3}}^2} (d_i d_j)(u_k \nu_l) \right\}$$

SUSY SU(5) MODEL

[Dimopoulos, Georgi; Sakai;
Hisano, Murayama, Yanagida;
Goto, Nihei;
D.E.C., Wiesenfeldt]

- Higgs triplet exchange is now dominant



$$\mathcal{M} \sim \frac{1}{M_{HC}} \tilde{C}_5 g^2 V_{CKM} V_{CKM} |X^{\tilde{f}_A}|^2 |X^{\tilde{f}_B}|^2 V^* U^* f(M_{\tilde{\chi}}, m_A, m_B)$$

Wilson Coefficient

- **Dimension 5 operators**

$$W_{D=5} = -\frac{1}{M_{H_c}} \left[C_{5L}^{ijkl} Q_i Q_j Q_k L_l + C_{5R}^{ijkl} U_i^c E_j^c U_k^c D_l^c \right]$$

- **SU(5) minimal content**

$$C_{5L}^{ijkl} = \frac{1}{2} \left(\tilde{U}_{uL} D_u P \tilde{U}_{uL}^\top \right)^{ij} \left(\tilde{U}_{dL} D_d \tilde{U}_{eL}^\dagger \right)^{kl}$$

$$C_{5R}^{ijkl} = \left(\tilde{U}_{uR}^* D_u V_{CKM}^* \tilde{U}_{eR}^\top \right)^{ij} \left(\tilde{U}_{uR}^* P^* V_{CKM} D_d \tilde{U}_{dR}^\dagger \right)^{kl}$$

- **Proton decay in SU(5) depends on the choice:**

$$Y_e = Y_d^{\top \text{exp.}} \quad \text{or} \quad Y_d = Y_e^{\top \text{exp.}}$$

- **Dimension 5 operators**

$$W_{D=5} = -\frac{1}{M_{H_c}} \left[C_{5L}^{ijkl} Q_i Q_j Q_k L_l + C_{5R}^{ijkl} U_i^c E_j^c U_k^c D_l^c \right]$$

- **SU(5) minimal content**

$$C_{5L}^u = \frac{1}{2} (D_u P) (V_{CKM} D_d) \quad C_{5L}^d = \frac{1}{2} (V_{CKM}^\dagger D_u P V_{CKM}^*) (D_d)$$

$$C_{5R}^{u,d} = (D_u V_{CKM}^*) (P^* V_{CKM} D_d)$$

- **Proton decay in SU(5) depends on the choice:**

$$Y_e = Y_d^{\text{exp.}} \quad \text{or} \quad Y_d = Y_e^{\text{exp.}}$$

- **Renormalisation group Factors**

- From GUT to SUSY scale the *Wilson coefficients* are fully evolved with RGE (including all *Yukawas*) and A_L factors

$$A_L = \left(\frac{\alpha_3(\mu_{had})}{\alpha_3(m_c)} \right)^{4/9} \left(\frac{\alpha_3(m_c)}{\alpha_3(m_b)} \right)^{12/25} \left(\frac{\alpha_3(m_b)}{\alpha_3(m_Z)} \right)^{12/23}$$

- **Chiral perturbation theory**

$$\begin{aligned} A(K^+ \bar{\nu}) = A_l \left\{ \right. & [\beta \mathcal{M}_{LL}^{usd\nu} + \alpha \mathcal{M}_{RL}^{usd\nu}] \frac{2m_p}{3m_B} D \\ & + [\beta \mathcal{M}_{LL}^{uds\nu} + \alpha \mathcal{M}_{RL}^{uds\nu}] \left(1 + \frac{m_p}{3m_B} (3F + D) \right) \\ & \left. + [\beta \mathcal{M}_{LL}^{dsu\nu} + \alpha \mathcal{M}_{RL}^{dsu\nu}] \left(1 - \frac{m_p}{3m_B} (3F - D) \right) \right\} \end{aligned}$$

- **Dependence on $\tan \beta$**

LLLL contribution $1 / \sin^2 \beta$

RRRR contribution $(\tan \beta + \frac{1}{\tan \beta})^2$

- **Decay width**

$$\Gamma(p \rightarrow K^+ \bar{\nu}) = \frac{(m_p^2 - m_K^2)^2}{32\pi m_p^3 f_\pi^2} \sum_{i=e,\mu,\tau} |\mathcal{A}(K^+ \bar{\nu}_i)|^2$$

- **All the numerics were made in mSUGRA**

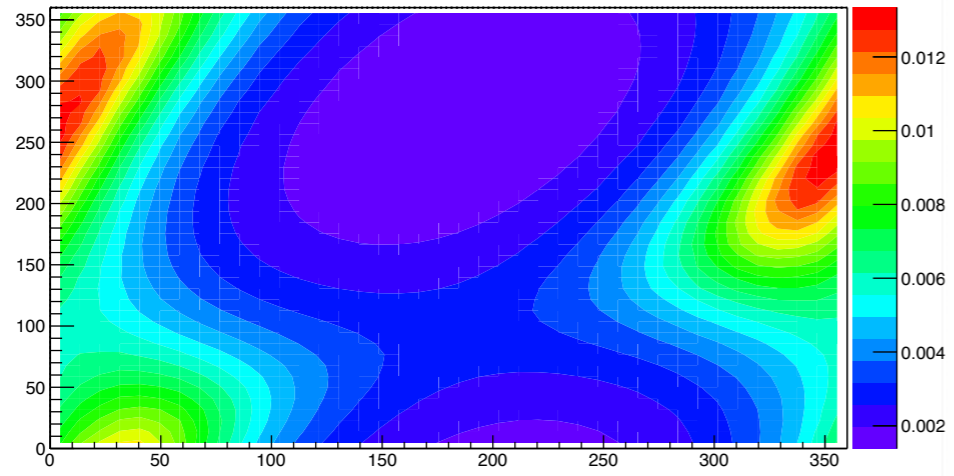
Point	m_0	$m_{1/2}$	A_0	$\tan \beta$	$m_{\tilde{t}}$	$m_{\tilde{\chi}^0}$	$m_{\tilde{\chi}^\pm}$	m_h
1	1000	125	0	2.5	526	47.6	92.2	92.7
2	1472	711	-3157	34.1	920	307	589	124.1
3	7126	595	5968	29.8	4164	244	318	124.7
4	22000	4207	20823	7.3	14176	1949	2744	126.8
5	25000	1200	-20823	7.3	14548	567	1100	127.9
6	20000	115	-19500	7.3	11568	63	131	126.6

- **Coloured Higgs triplet mass**

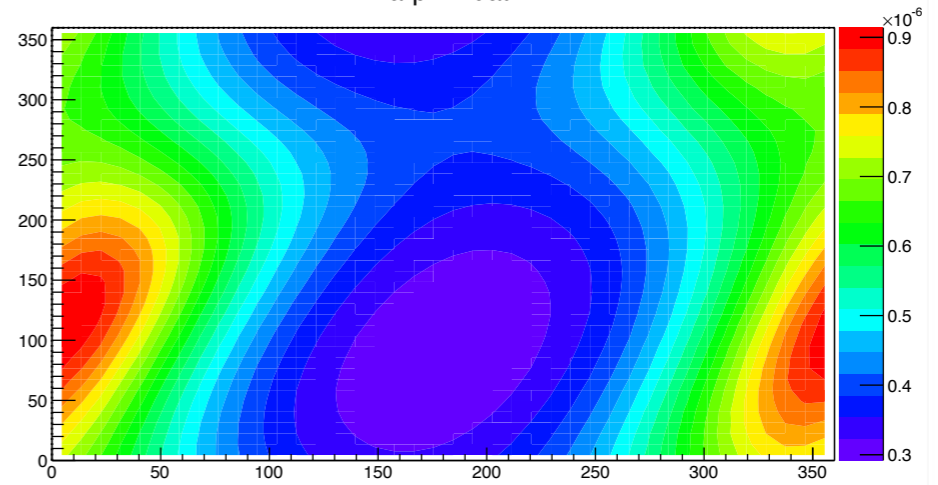
$$3.5 \times 10^{14} \text{ GeV} \leq M_{HC} \leq 3.6 \times 10^{15} \text{ GeV}$$

NUMERICS

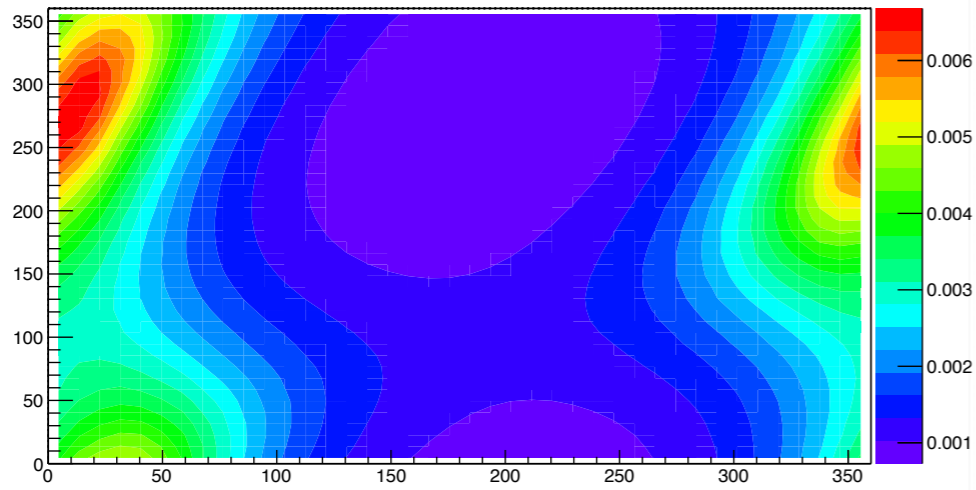
varphiK.dat



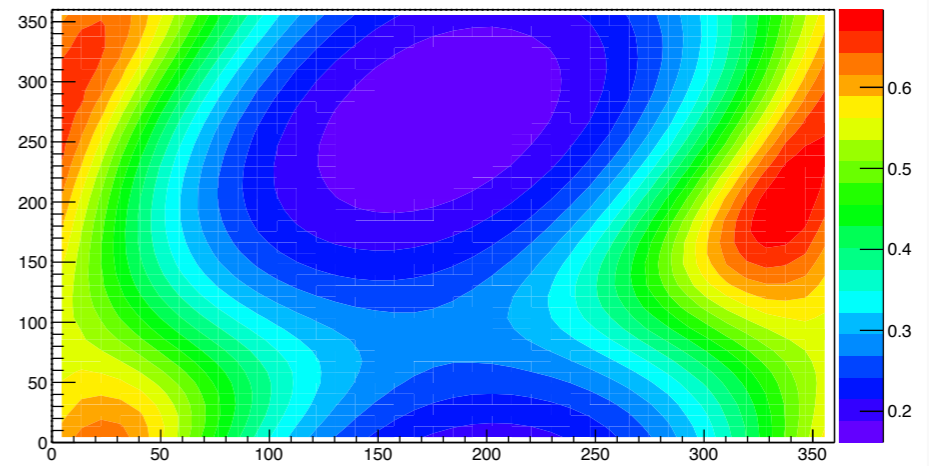
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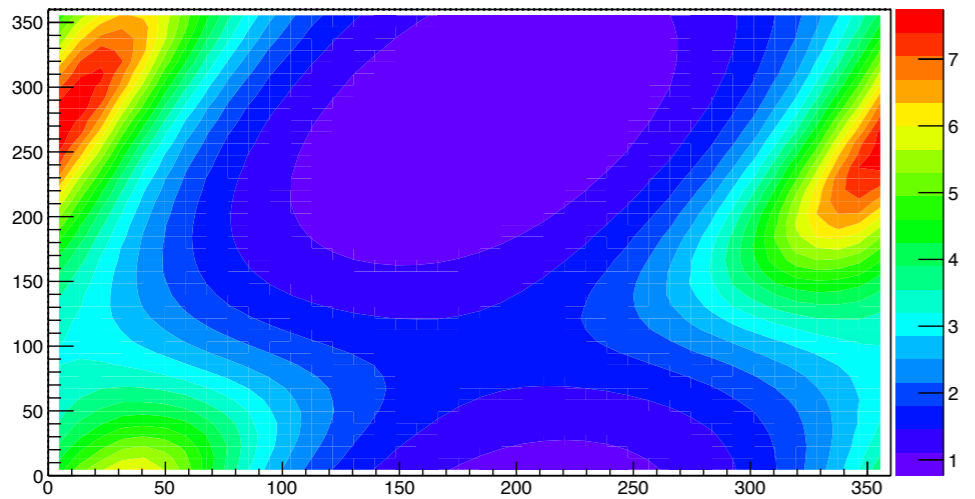
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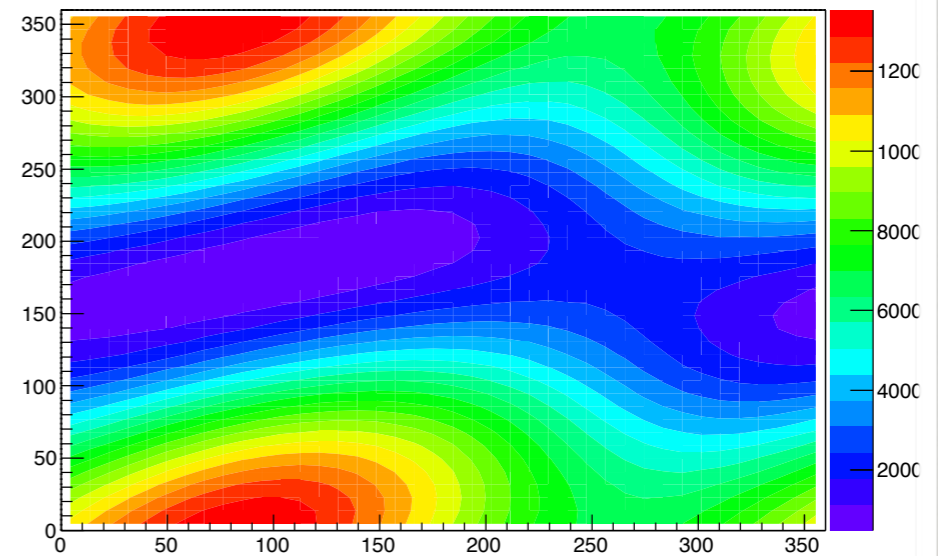
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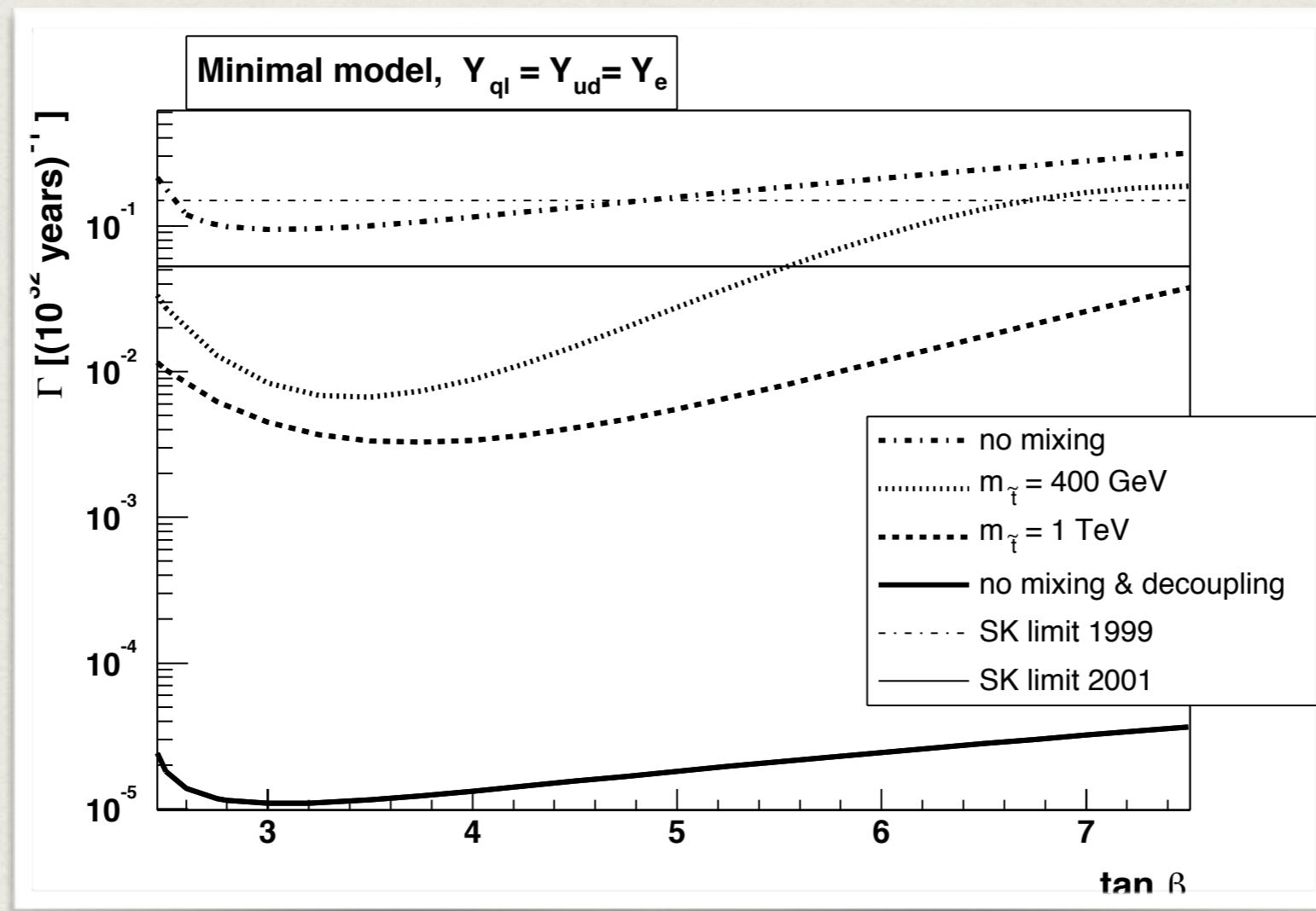


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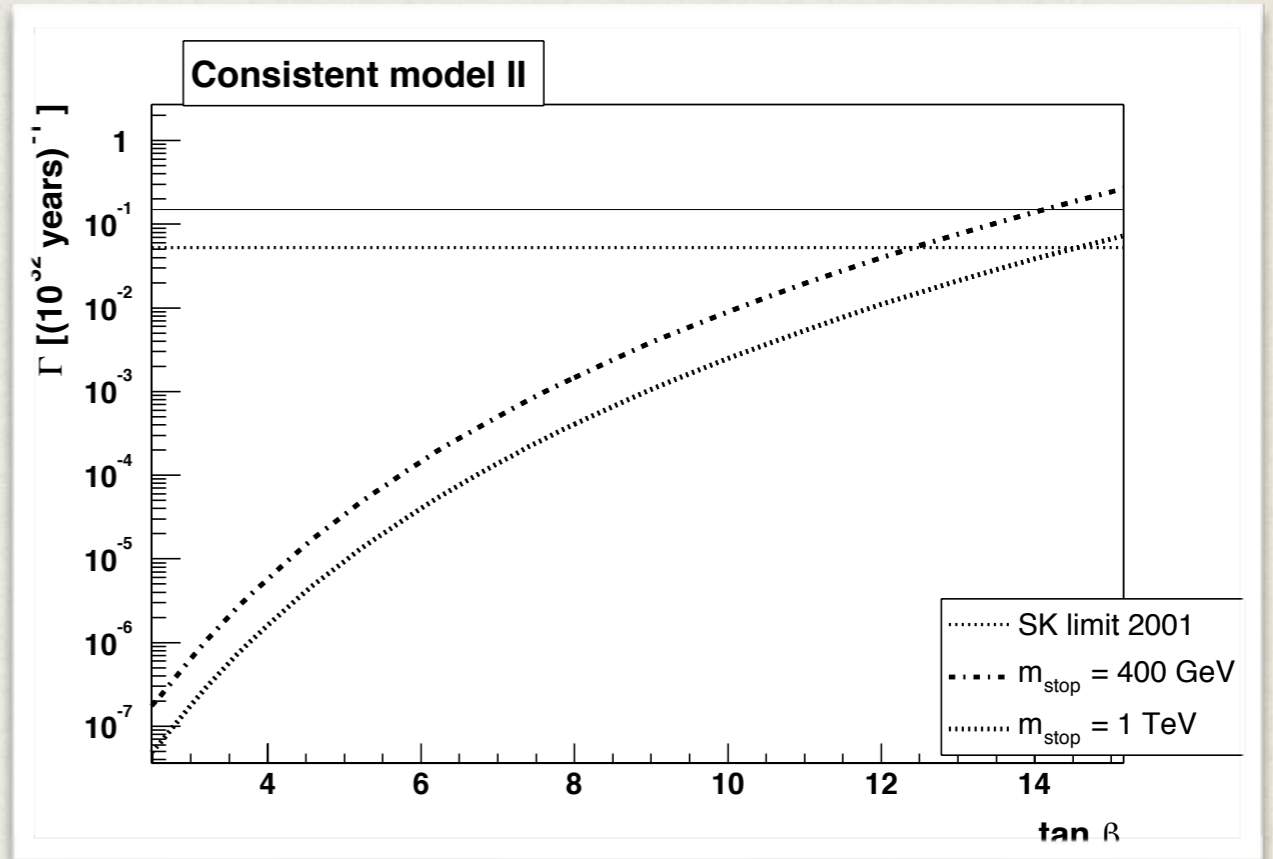
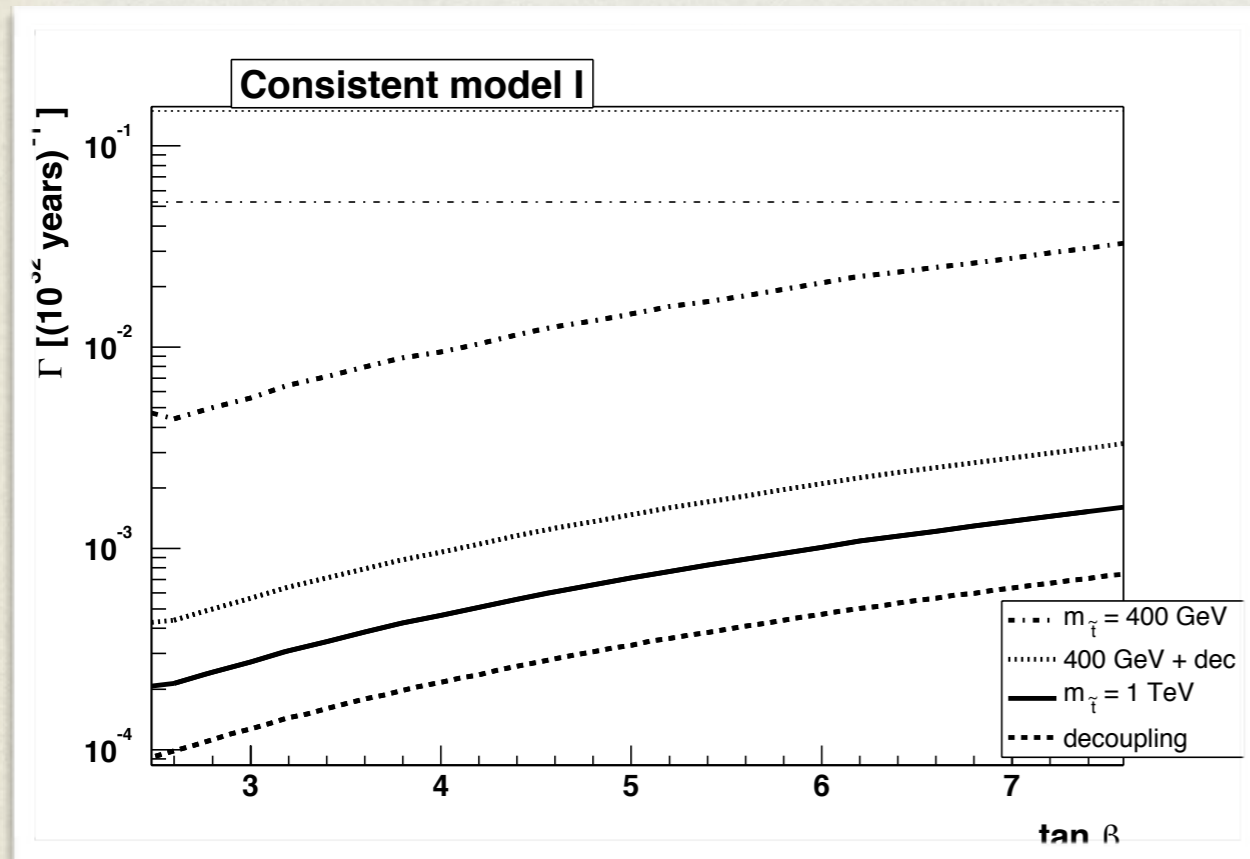


- If we make the other choice:

$$Y_d = Y_e^{\text{exp.}}$$



• Consistent (non-renormalisable) model examples



• Proton decay rate to kaons in the final state

Model I

$$Y_{qq} = Y_{ue} = \text{diag}(0, 0, y_t)$$

$$Y_{ud} = \text{diag}(0, y_s - y_\mu, y_b - y_\tau)$$

$$Y_{ql} = \text{diag}(y_e - y_d, 0, 0)$$

Model II

$$Y_{qq} = Y_{ue} = \text{diag}(0, 0, y_t)$$

$$Y_{ud} = \text{diag}(y_d - y_e, y_s - y_\mu, y_b)$$

$$Y_{ql} = \text{diag}(0, 0, y_\tau)$$

OTHER STRATEGY

[D.E.C, P. Carrilho]

$$H_c \longrightarrow M_{Pl}$$

$$C_{5R}^{i1kl} < 4.8 \quad C_{5L}^{ijkl} < 8 \times 10^{-7} \quad C_{5R}^{i2kl} < 0.023 \quad C_{5R}^{i3kl} < 1.4 \times 10^{-3}$$

Point 1

$$C_{5R}^{i1kl} < 0.6 \quad C_{5L}^{ijkl} < 2 \times 10^{-7} \quad C_{5R}^{i2kl} < 3 \times 10^{-3} \quad C_{5R}^{i3kl} < 1.7 \times 10^{-4}$$

Point 2

$$C_{5R}^{i1kl} < 34 \quad C_{5L}^{ijkl} < 9.5 \times 10^{-6} \quad C_{5R}^{i2kl} < 0.16 \quad C_{5R}^{i3kl} < 9.7 \times 10^{-3}$$

Point 3

$$C_{5R}^{i1kl} < 267 \quad C_{5L}^{ijkl} < 5.9 \times 10^{-5} \quad C_{5R}^{i2kl} < 1.3 \quad C_{5R}^{i3kl} < 0.077$$

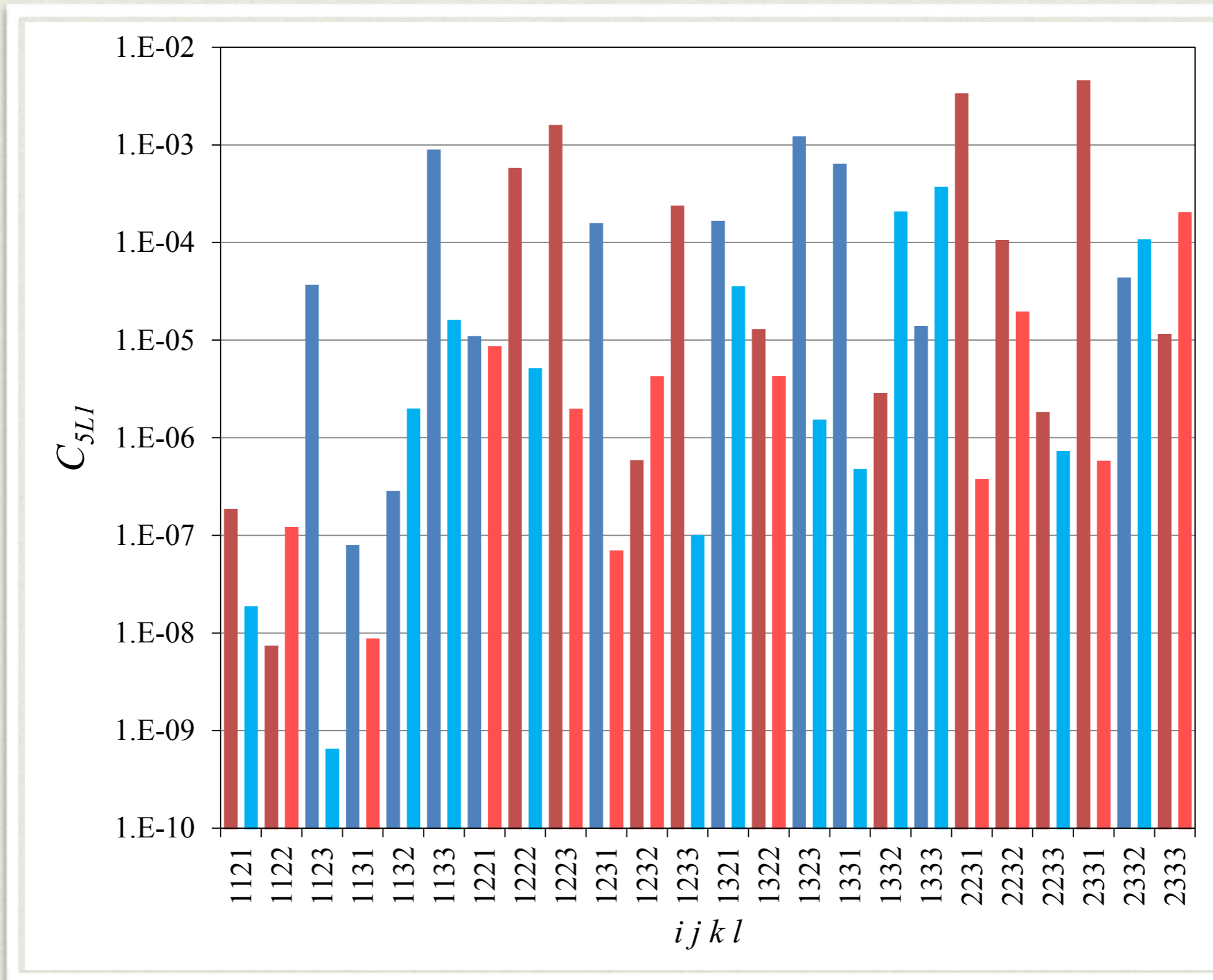
Point 5

$$C_{5R}^{i1kl} < 190 \quad C_{5L}^{ijkl} < 1.6 \times 10^{-5} \quad C_{5R}^{i2kl} < 0.92 \quad C_{5R}^{i3kl} < 0.055$$

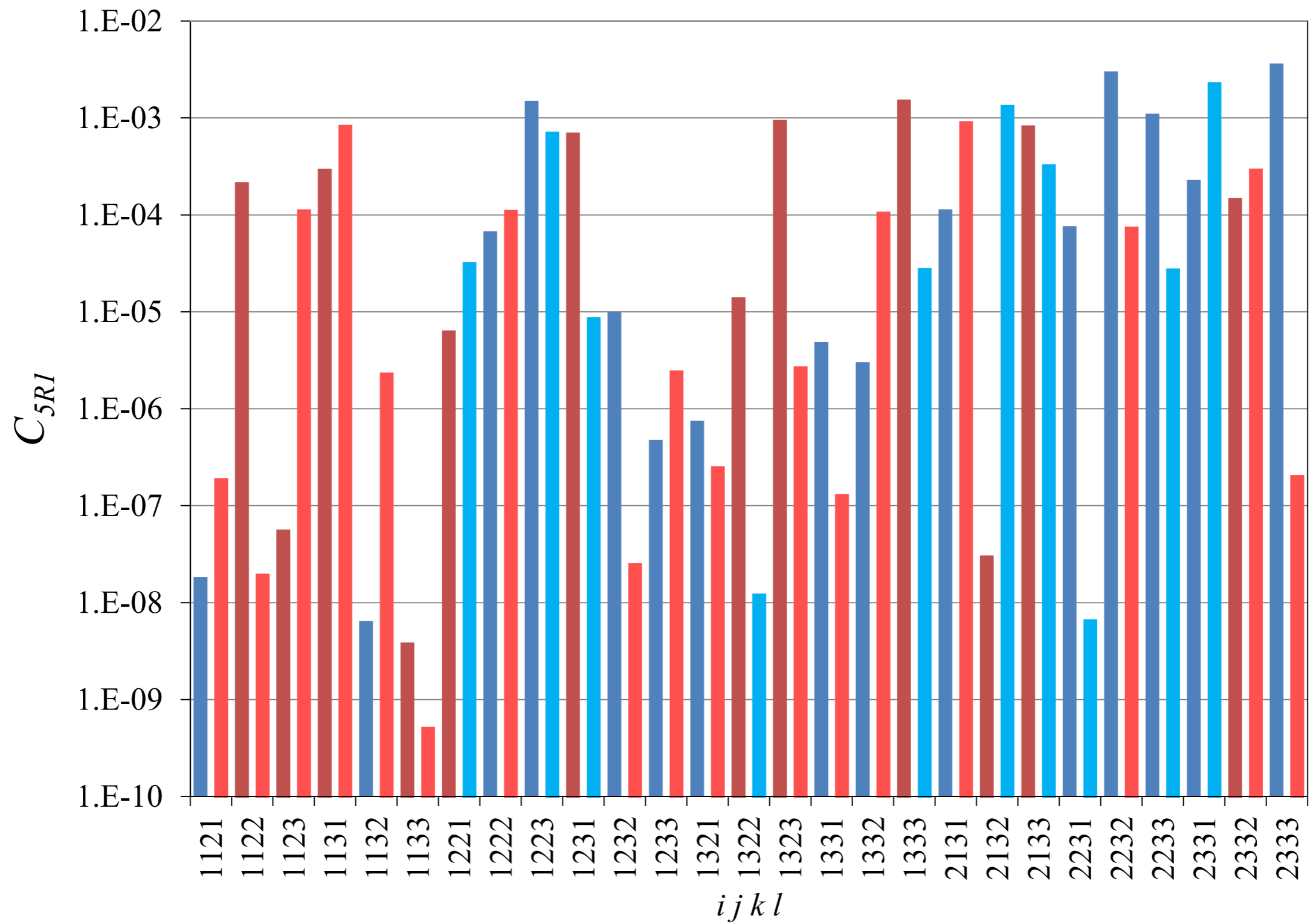
Point 4

$$C_{5R}^{i1kl} < 435 \quad C_{5L}^{ijkl} < 3.2 \times 10^{-4} \quad C_{5R}^{i2kl} < 2.1 \quad C_{5R}^{i3kl} < 0.13$$

Point 6



• Constraining the 24 independent Wilson coefficients



CONCLUSIONS

- **Grand Unified Theories make the bridge between Proton decay and Fermion masses and mixing**
- **Proton decay was not yet discovered and therefore puts constraints on GUT models**
- **Minimal SUSY/ NON-SUSY SU(5) is ruled out by the fermion spectrum**
- **The renormalisable Adjoint model solves unification and proton decay**
- **Dangerous D=5 operators can be a good discriminator among different Models Beyond SM**

A proton once said,



«I'll fulfill

My long-term belief in free will.

Though theorists (may) say

That I ought to decay

I'm damned if I think that I will».

-David Halliday