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One-loop Adjoint Masses for Non-Supersymmetric Intersecting Branes

Pascal Anastasopoulos

Based on: 1105.0591 [hep-th]
with I. Antoniadis, K. Benakli, M. Goodsell, A. Vichi

Corfu - 12/09/2011

Plan of the talk

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- ✦ Motivation

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- ❖ Radiative masses for adjoint scalars at:

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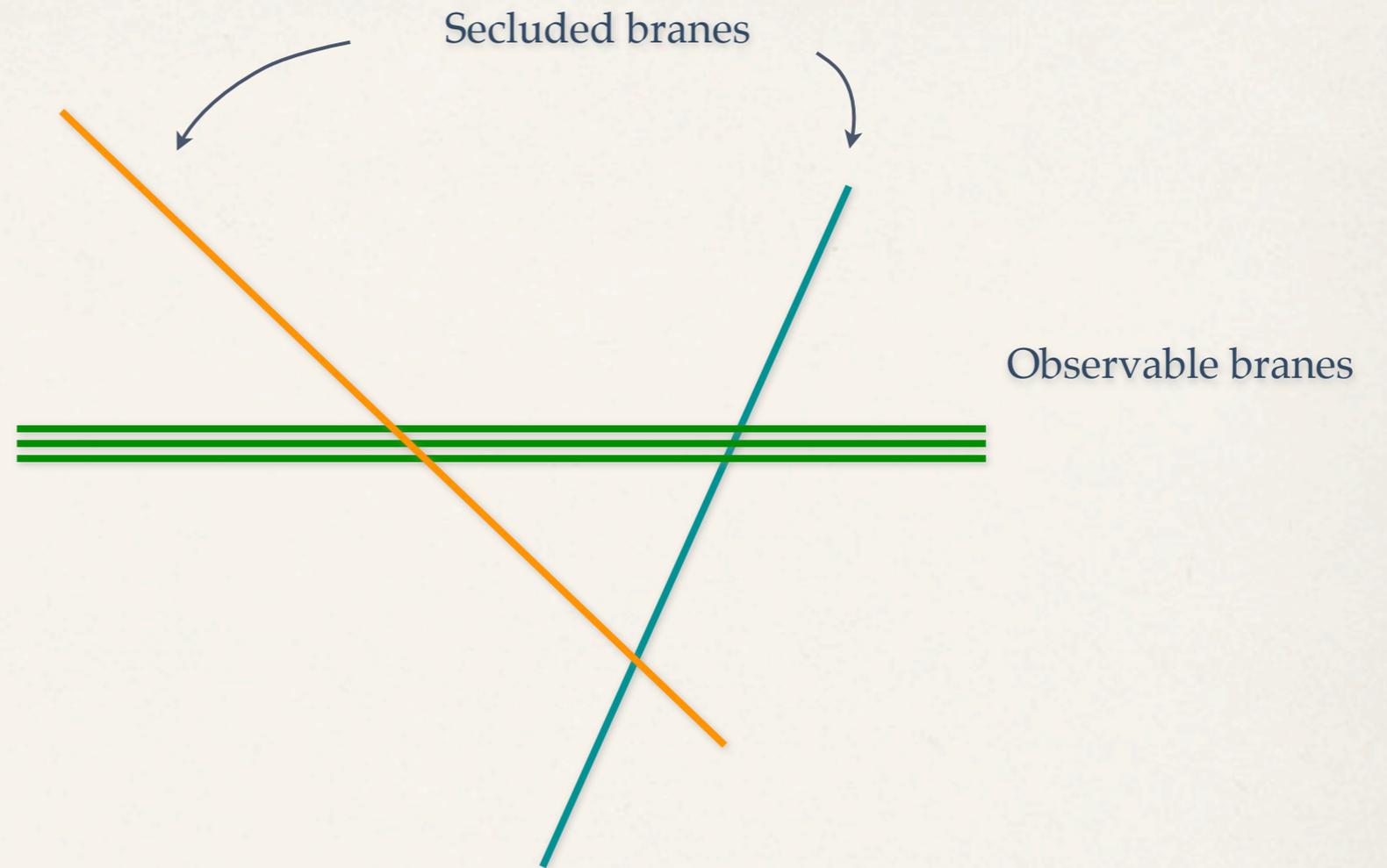
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Introduction and motivation

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- * The **same splitting** can be mapped upon T-duality into **branes intersecting at angles**.

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- * A **supersymmetric vacuum** can be obtained through a **specific choice of intersection angles** between D-branes.

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- ❖ However, some **adjoint scalars** become **tachyonic** in the **effective field theory**.

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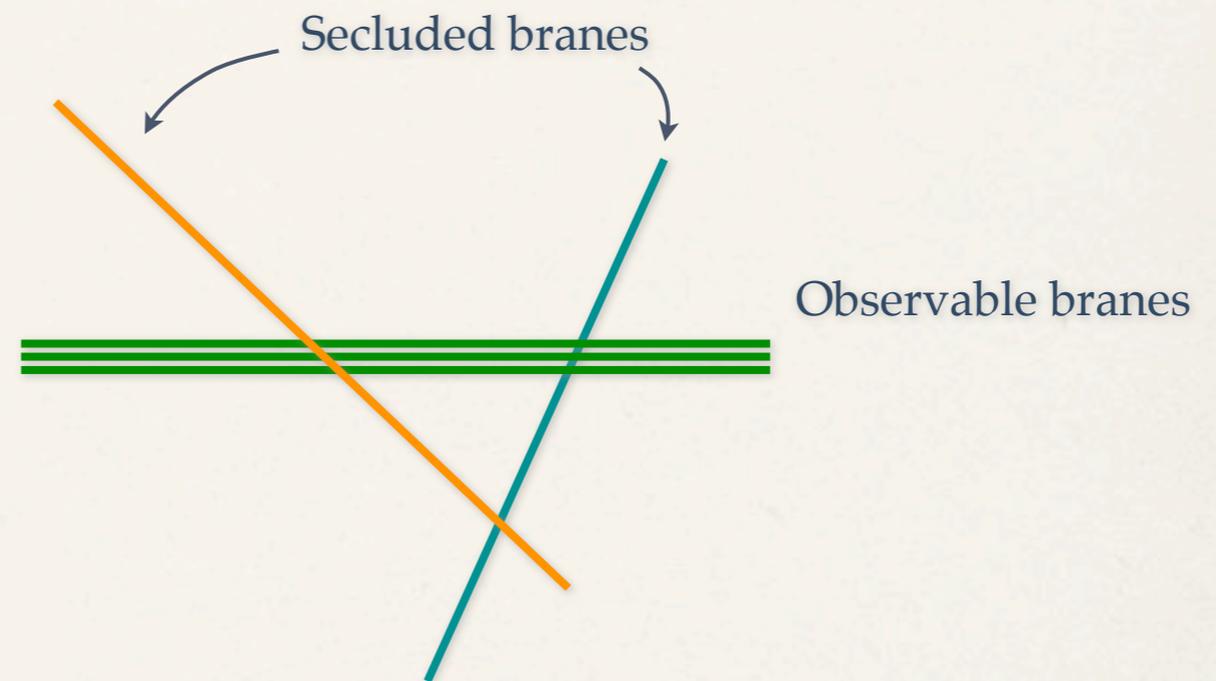
Observable branes



- * Our aim is to built models with:
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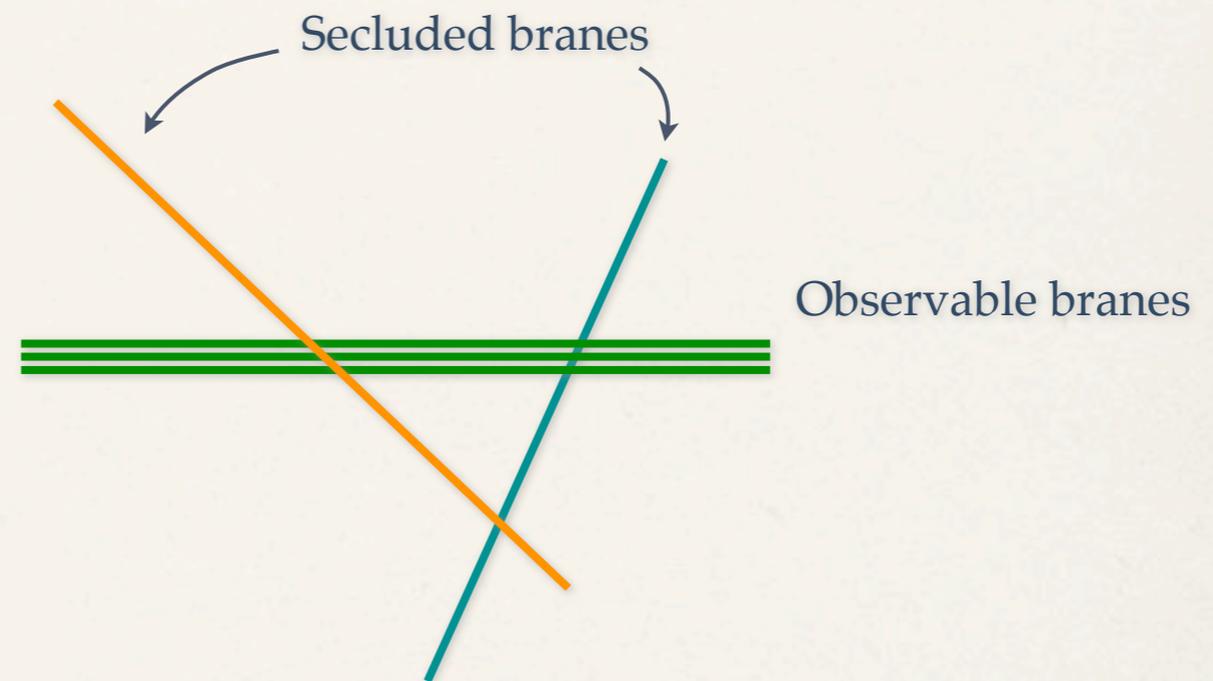
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- ✦ **Supersymmetry breaking** will be **communicated** to OS via **messengers** aka strings at the intersections.

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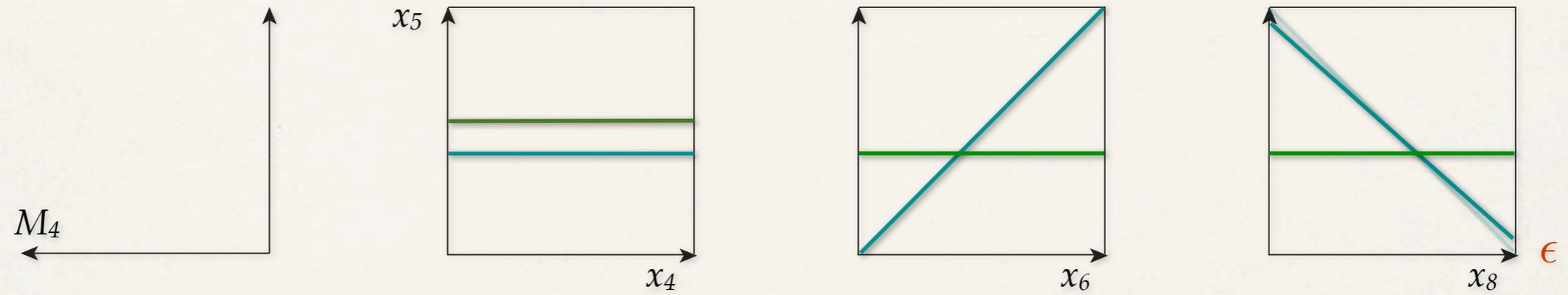
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- ❖ For the $\mathcal{N} \approx 2$ and $\mathcal{N} \approx 4$ cases, one can derive the **one-loop effective potential** and **read** from there the masses of the **adjoint representations**.



D-brane setup

Brane configuration

Brane configuration

- * Consider two **D₆-branes** a, b in: $\mathcal{M}_4 \times \mathcal{T}_1^2 \times \mathcal{T}_3^2 \times \mathcal{T}_3^2$.

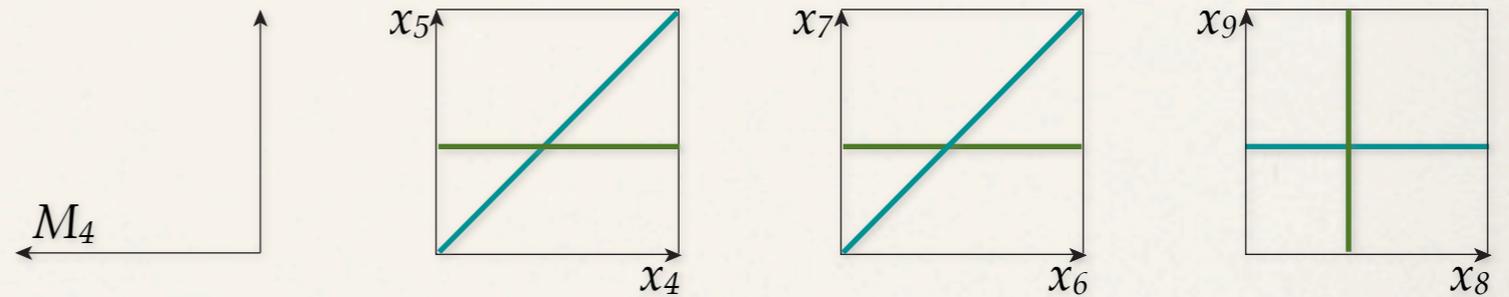
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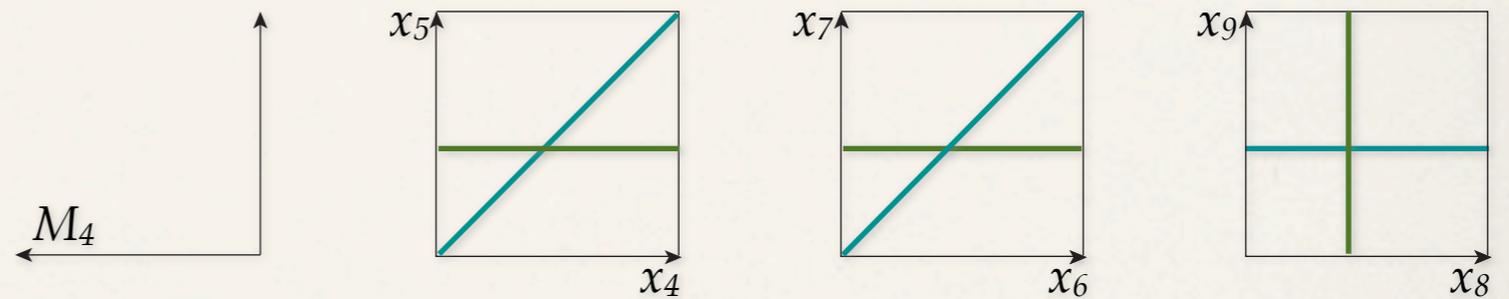
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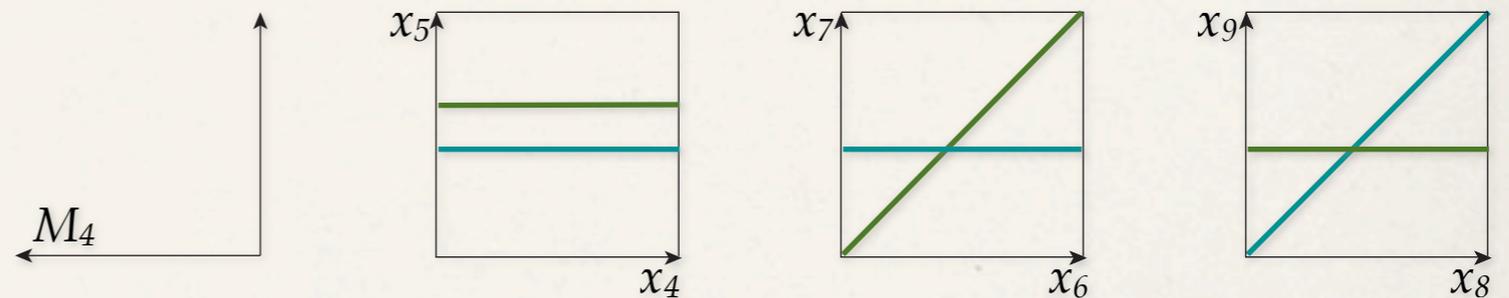
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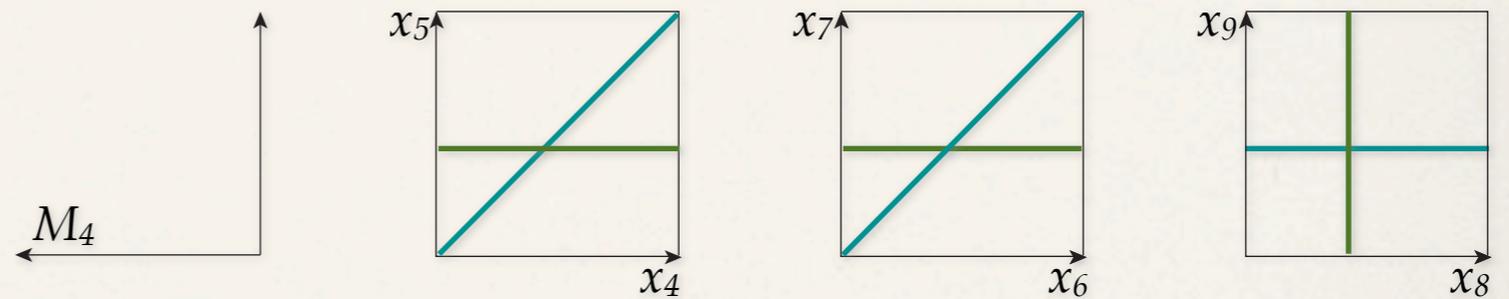
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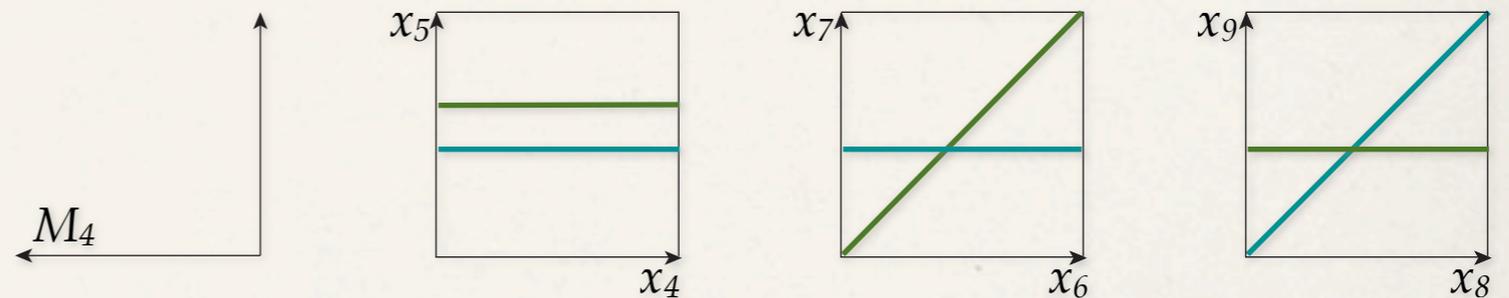
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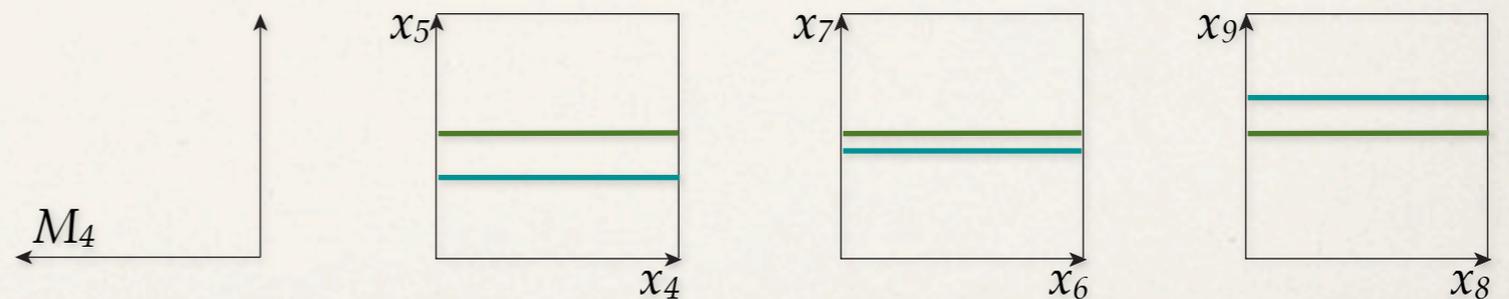
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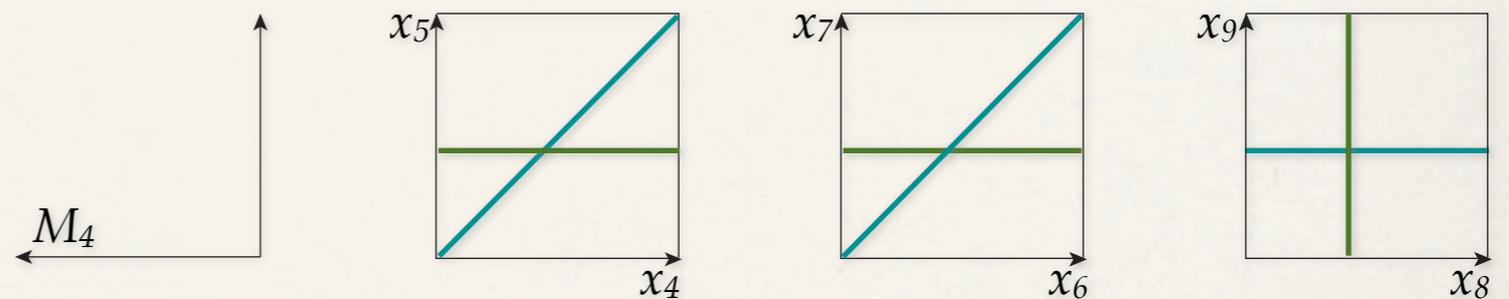
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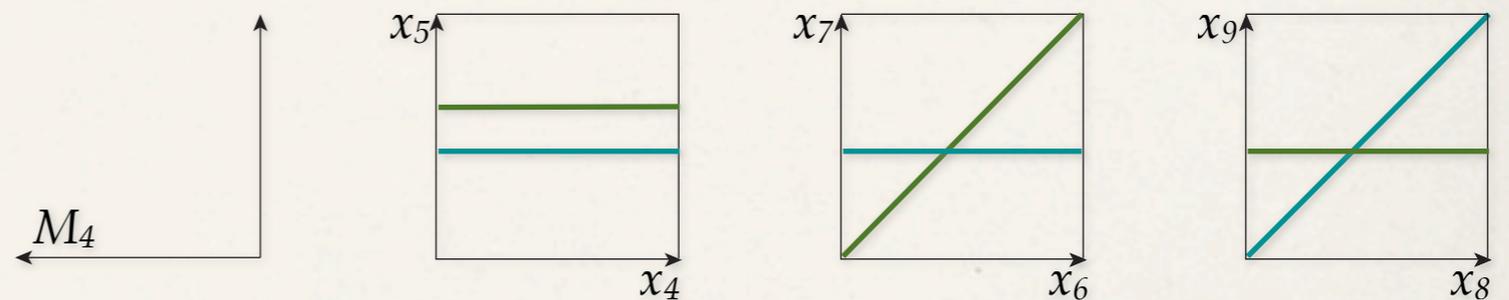
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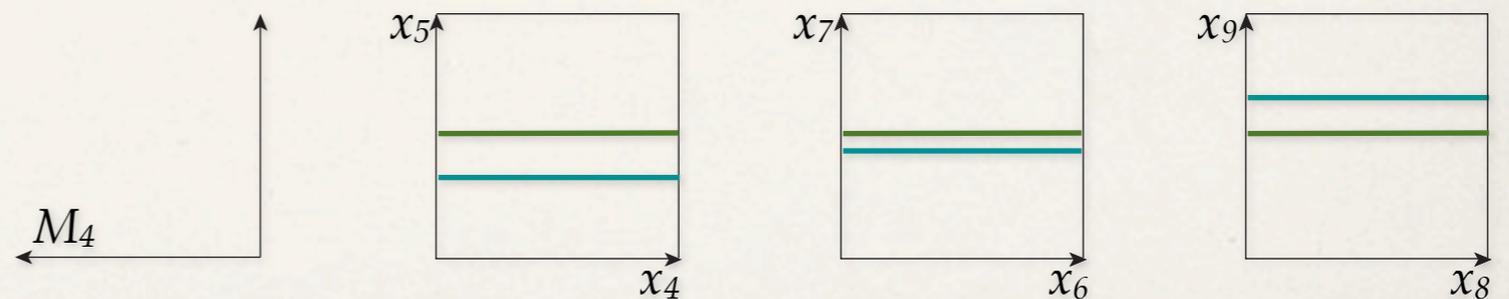
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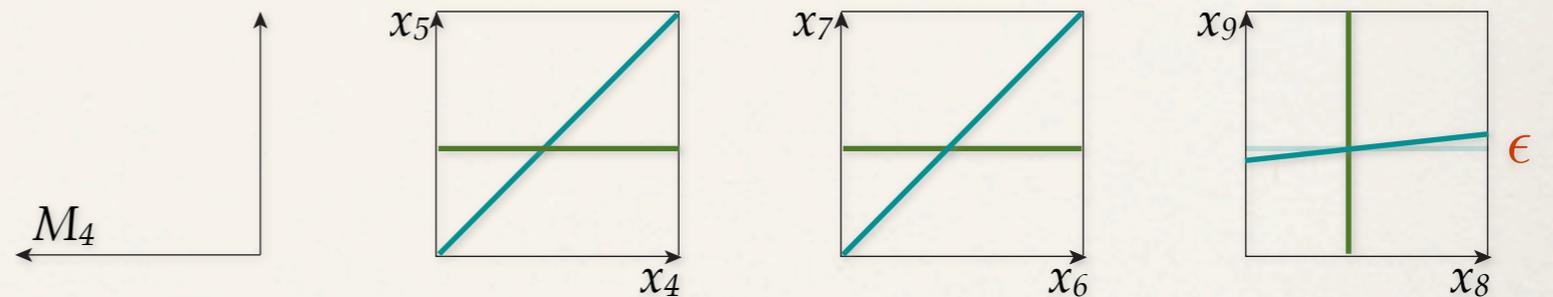


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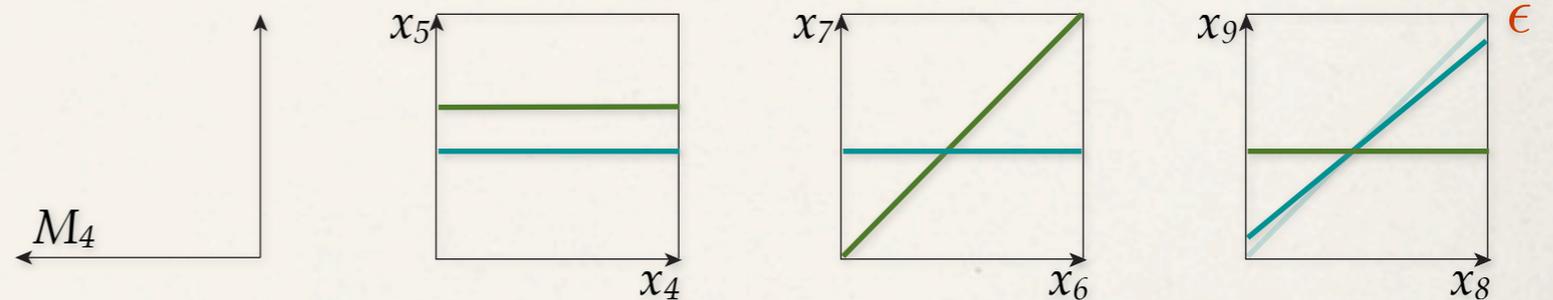
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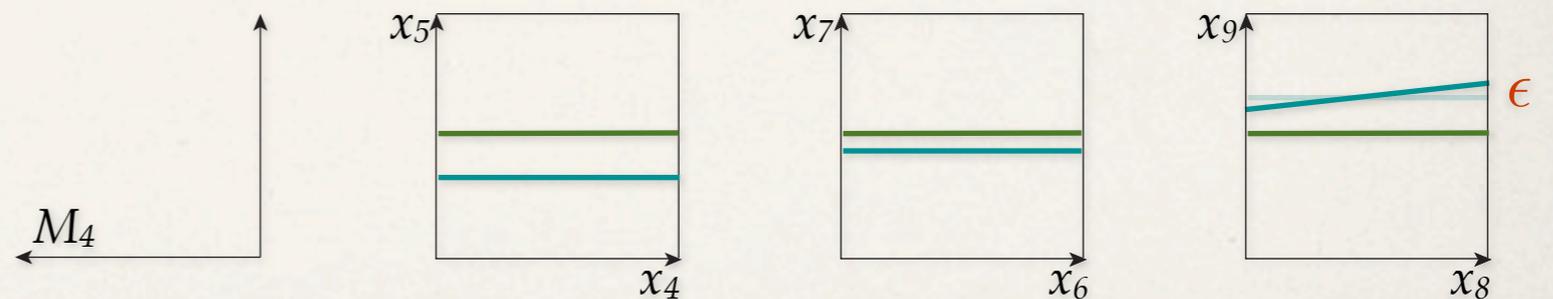
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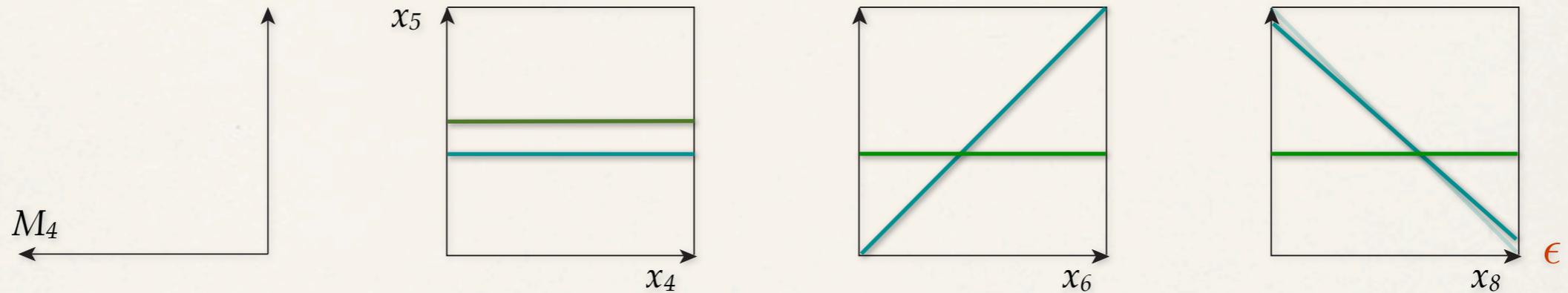


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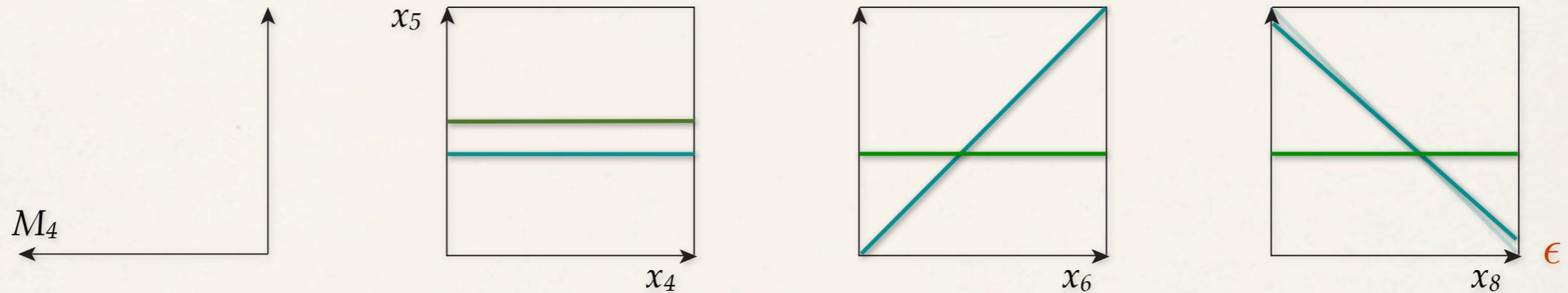
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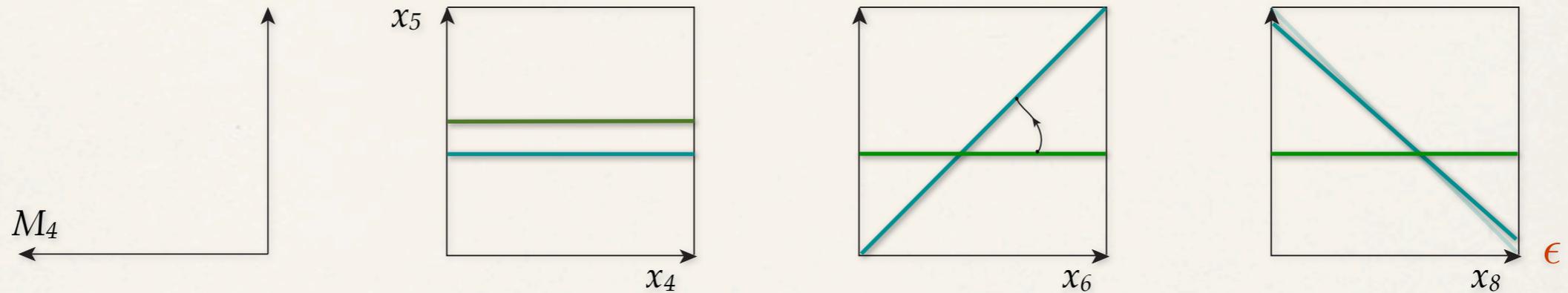
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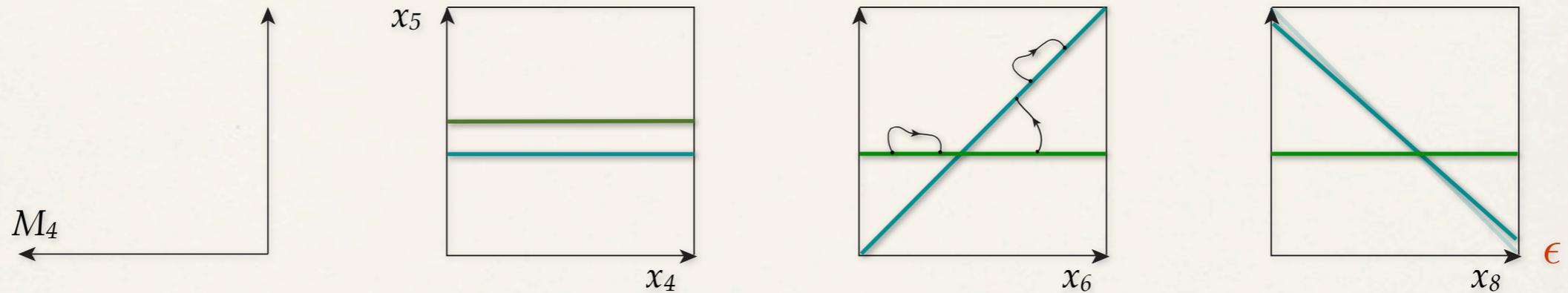
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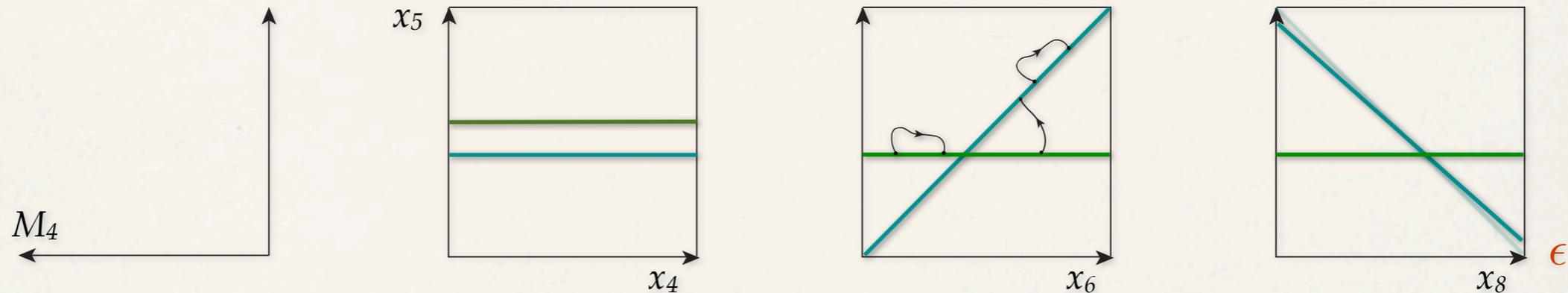
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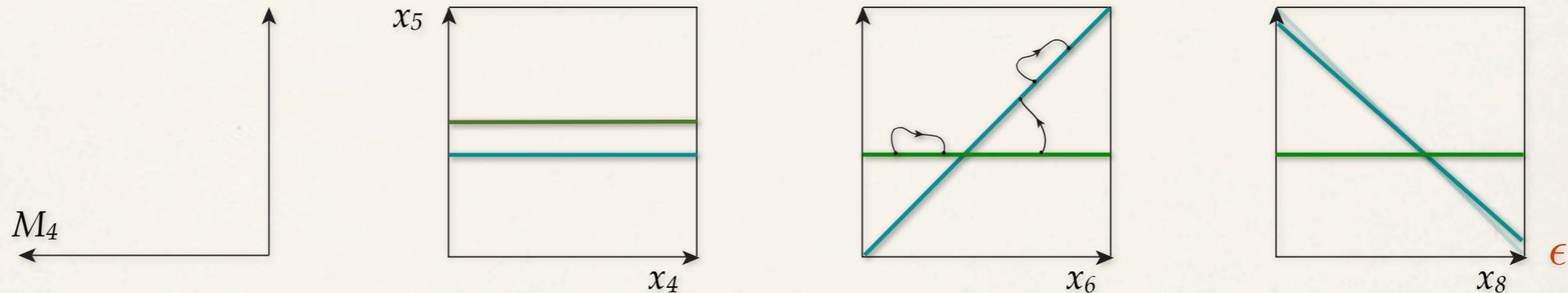
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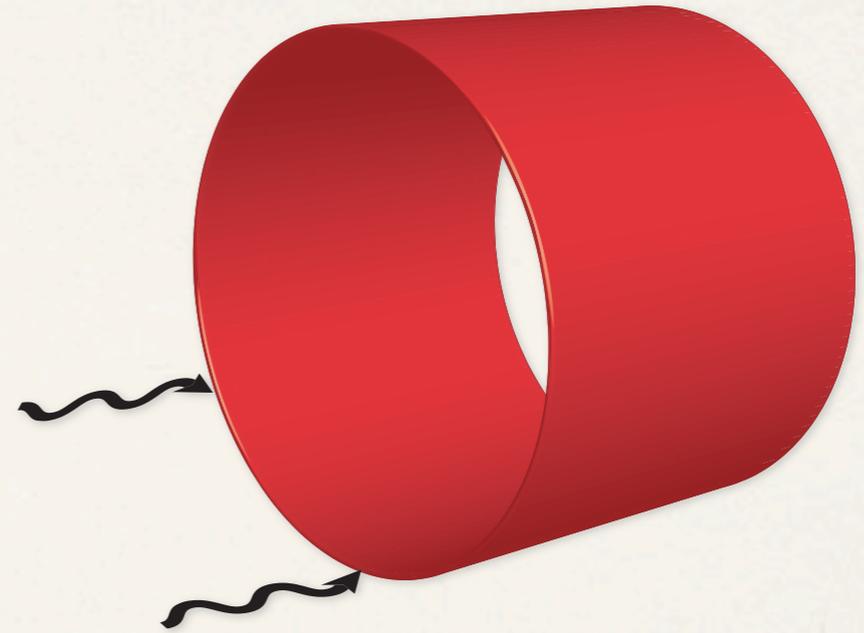
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- ❖ The later will obtain **masses at 1-loop** due to couplings with the bi-fundamentals.



Amplitudes

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Poppitz, Bain Berg

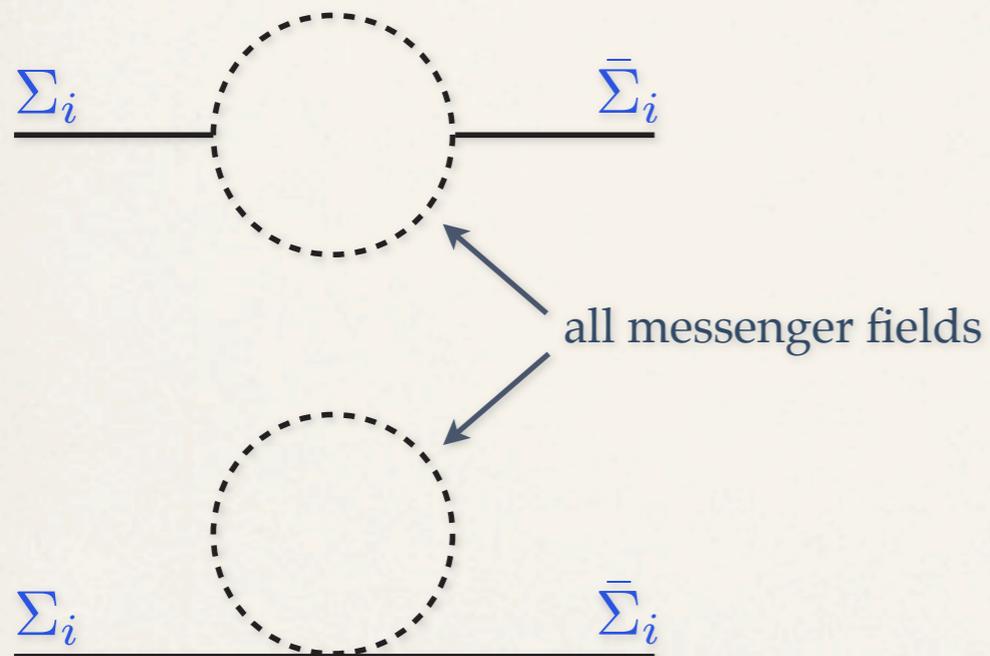
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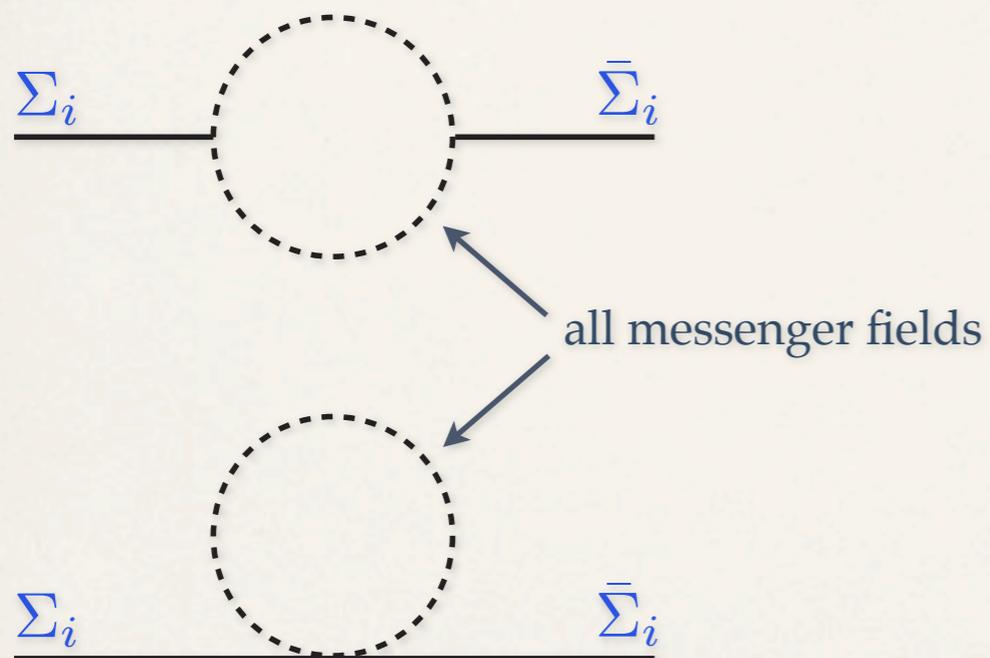
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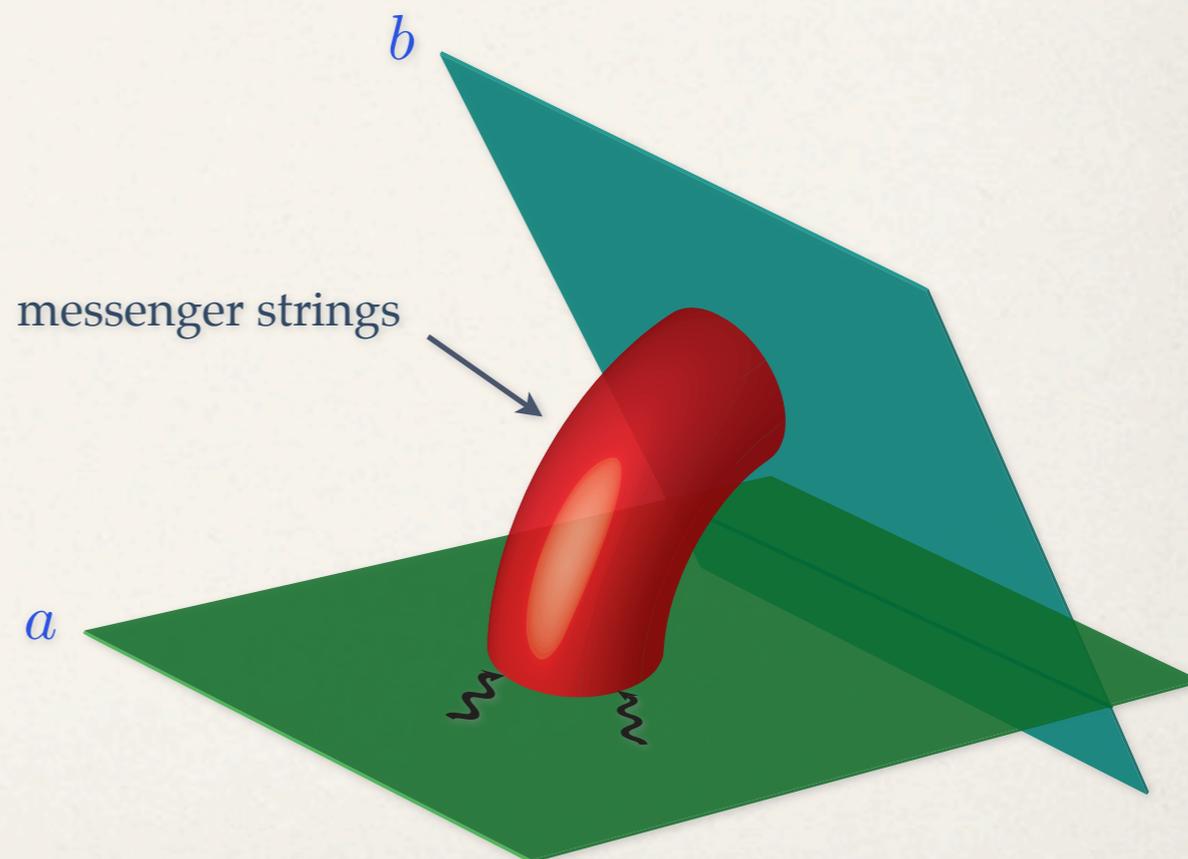
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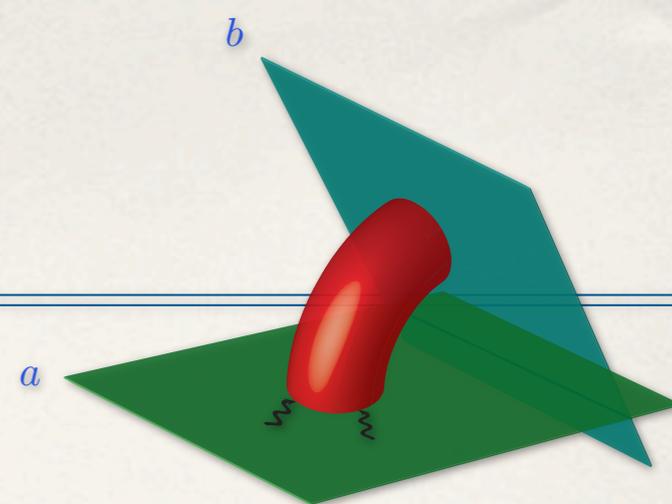


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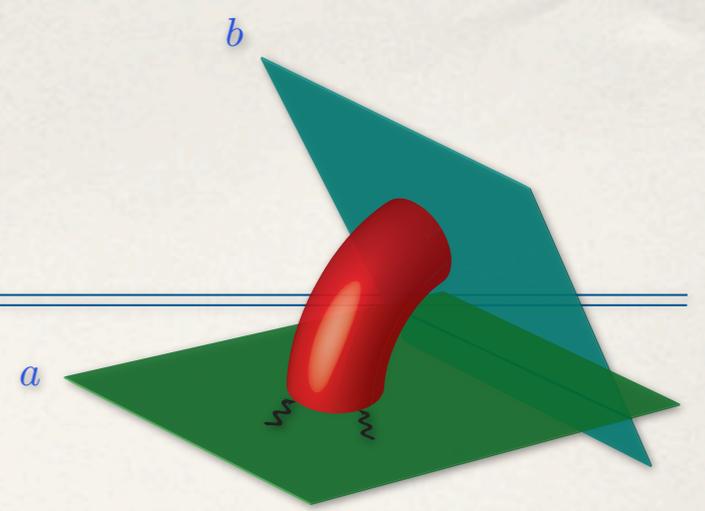
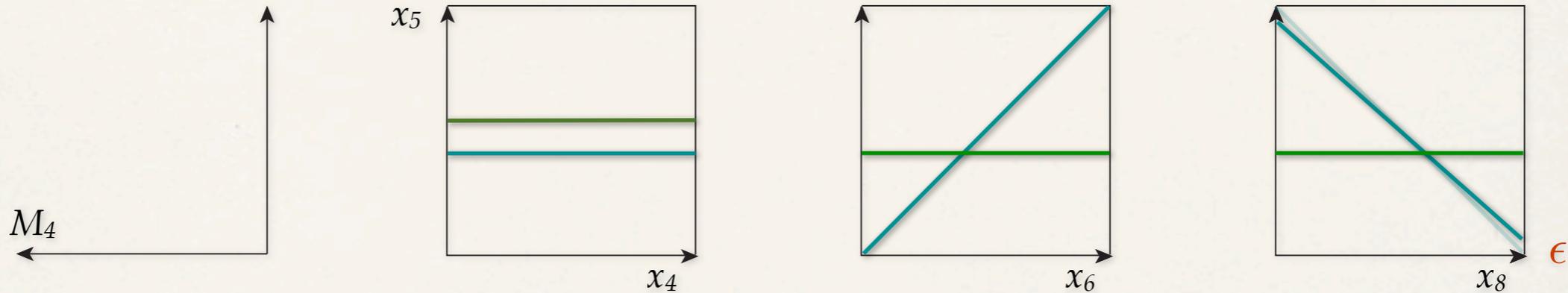
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The computational techniques



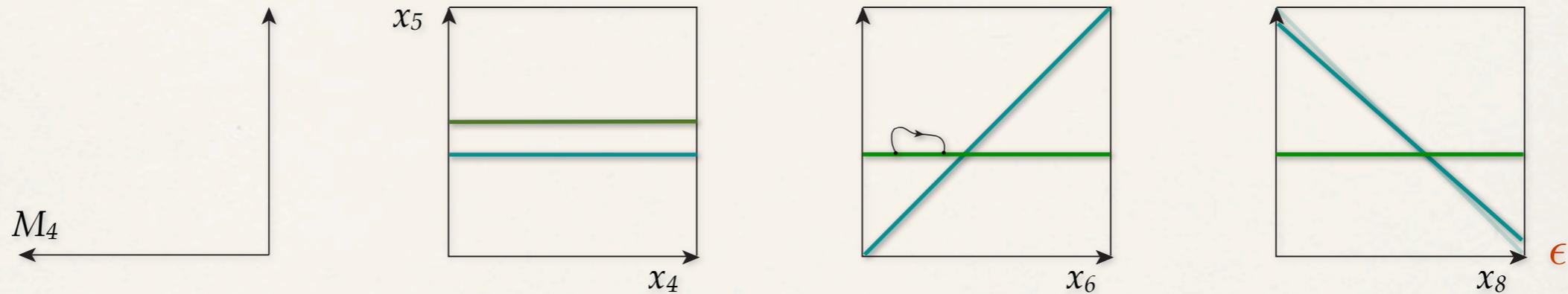
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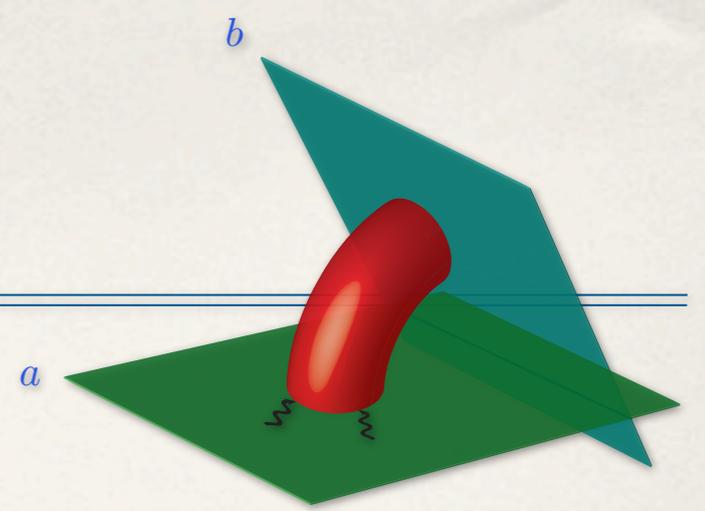


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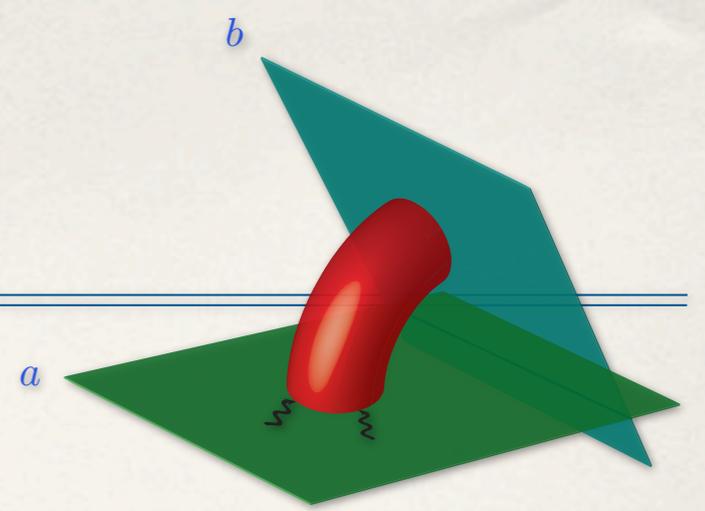
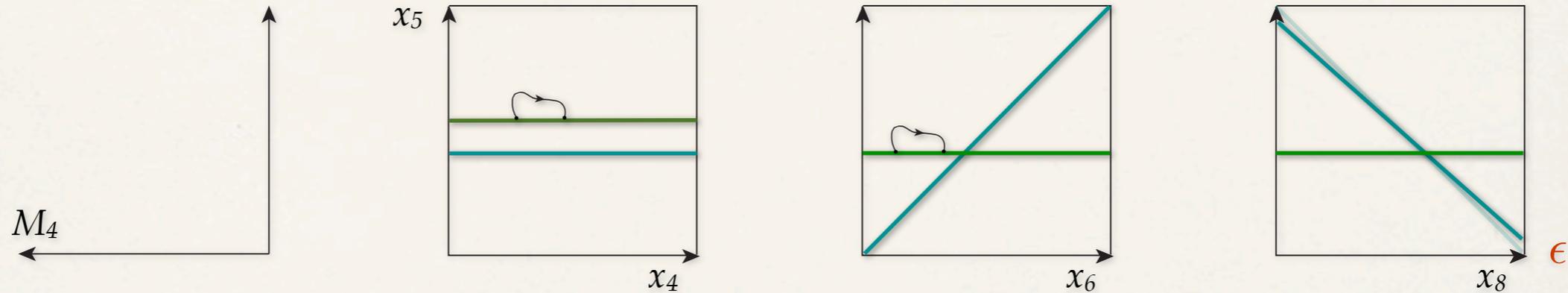


- Adjoint scalars in **non-parallel** directions.



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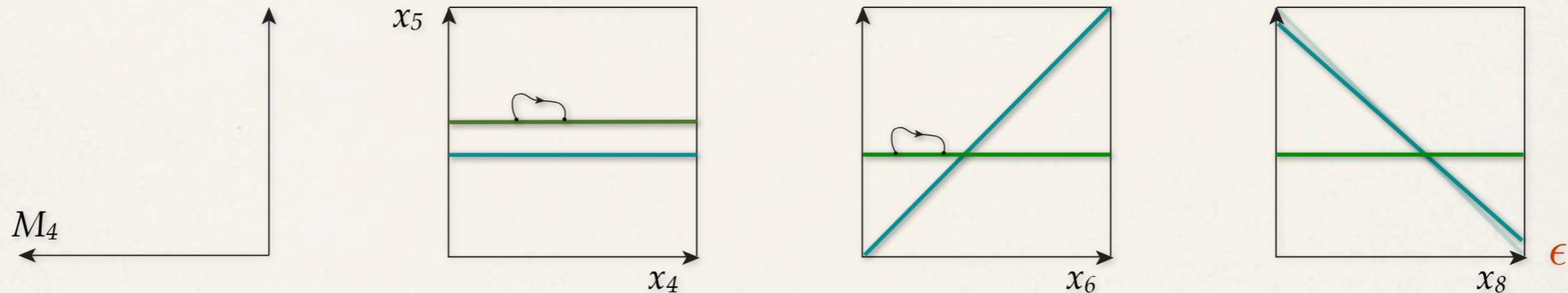
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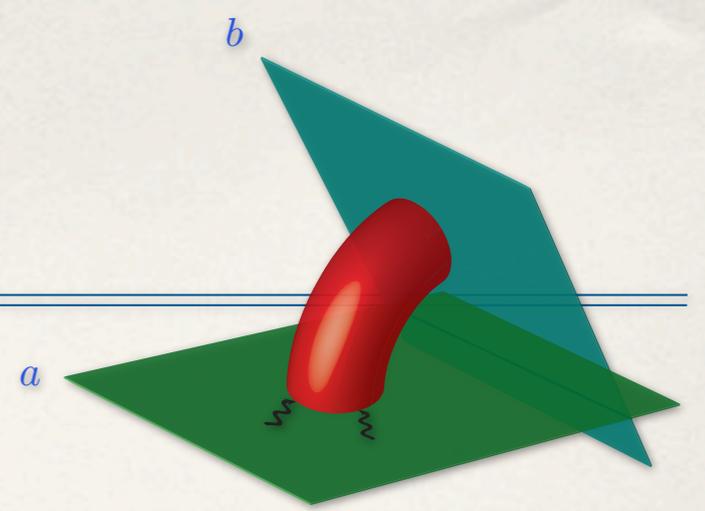
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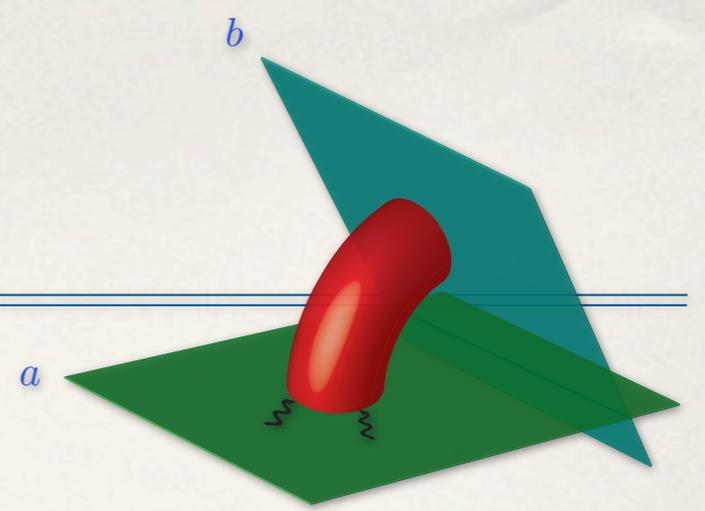
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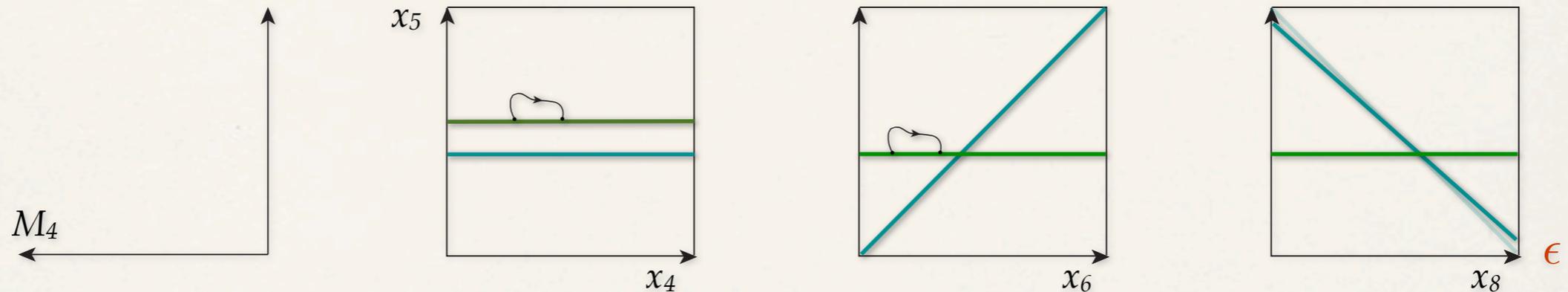
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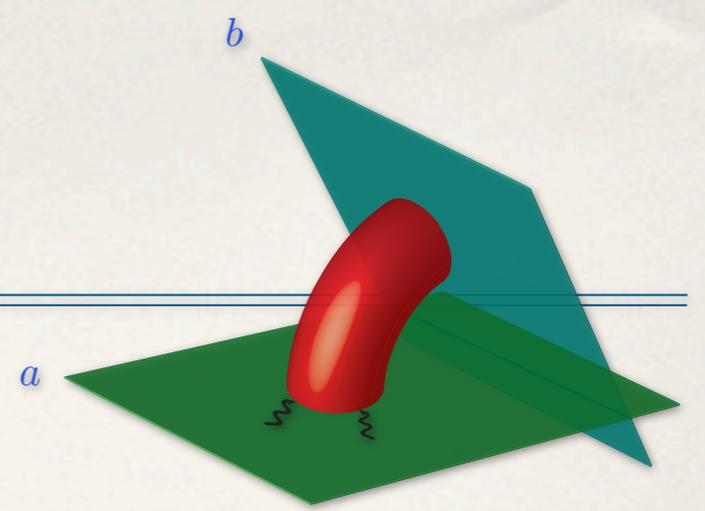


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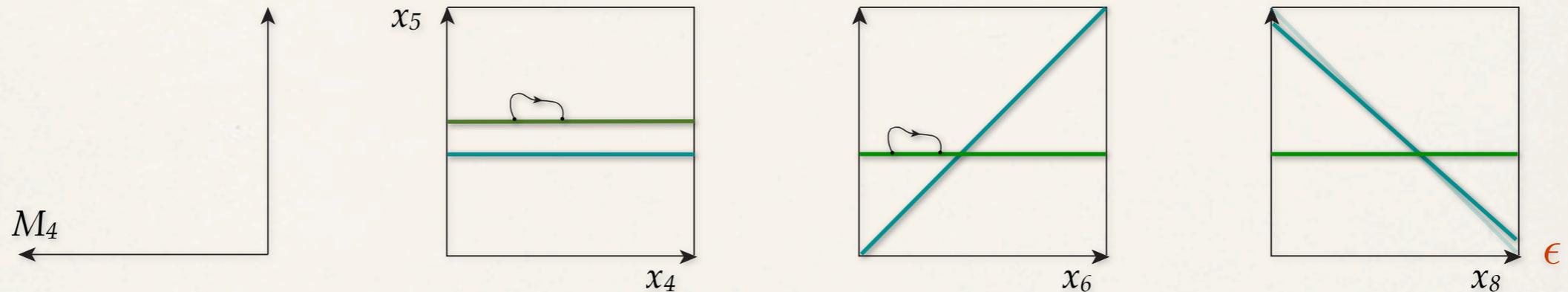


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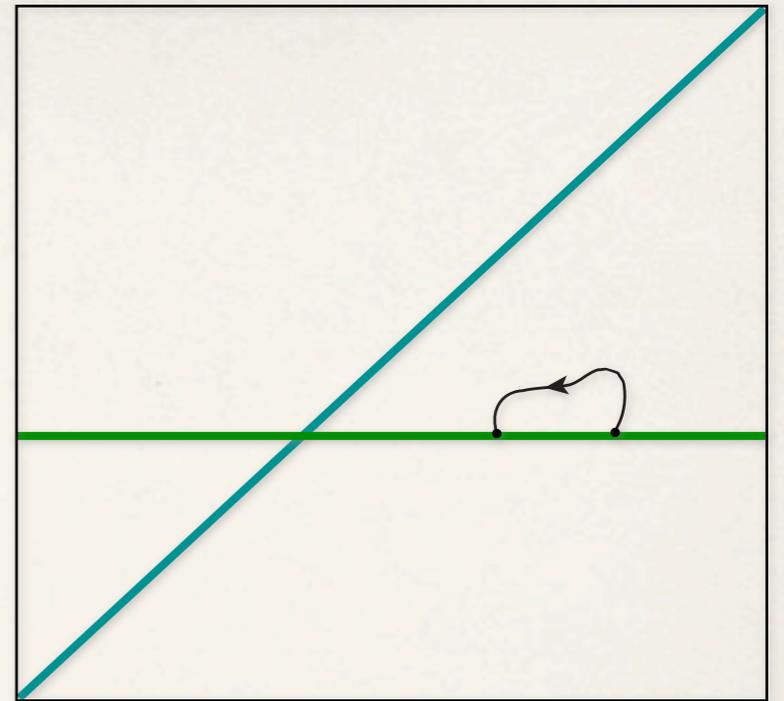
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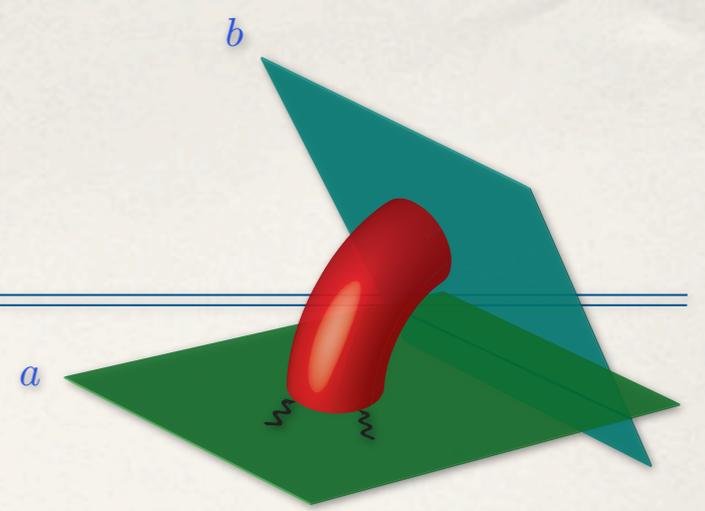


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 - Computing the **partition function** in the presence of **brane-displacements** etc...



Adjoint masses for non-parallel dimensions

The amplitude method

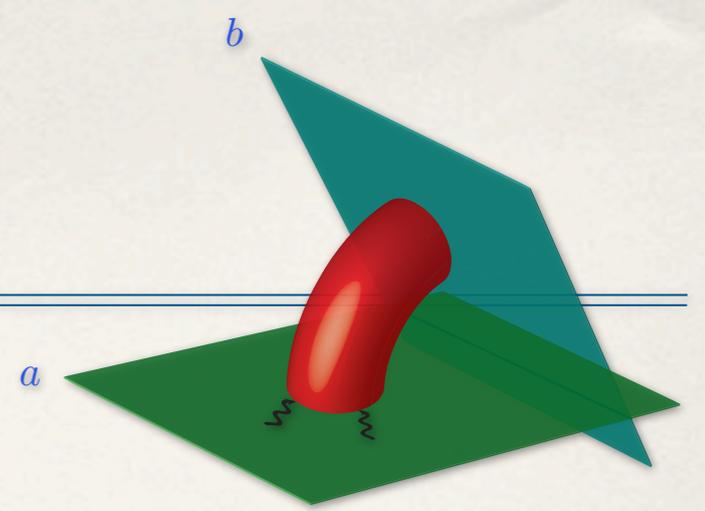


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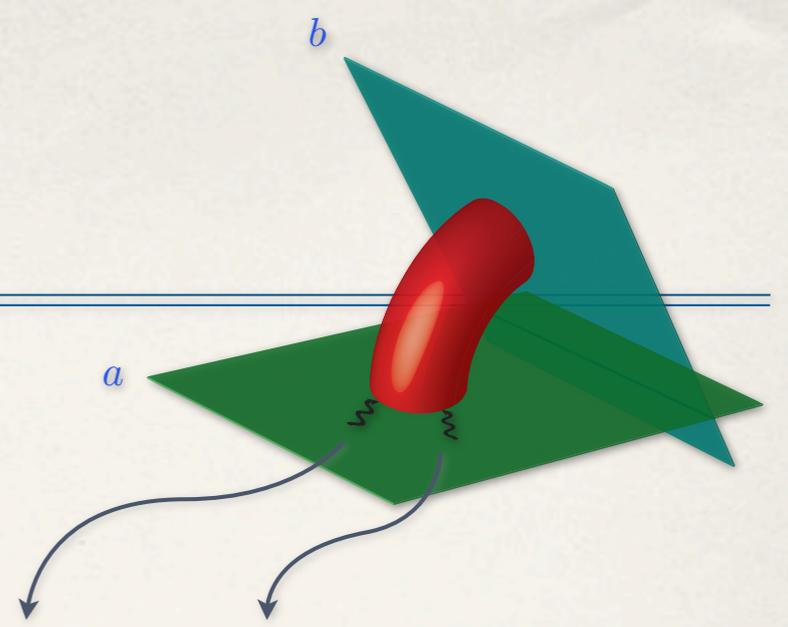


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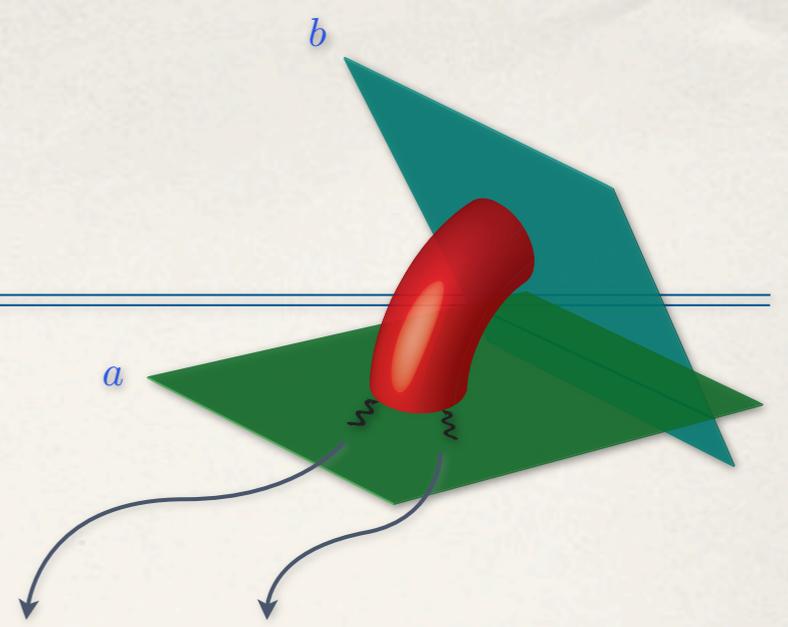
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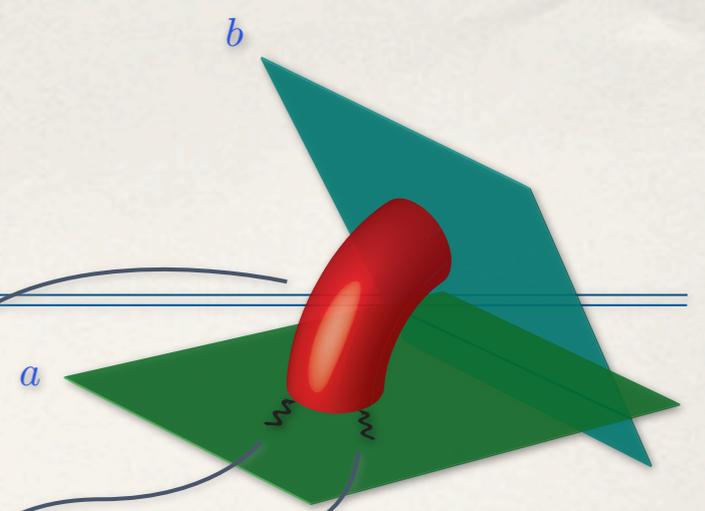
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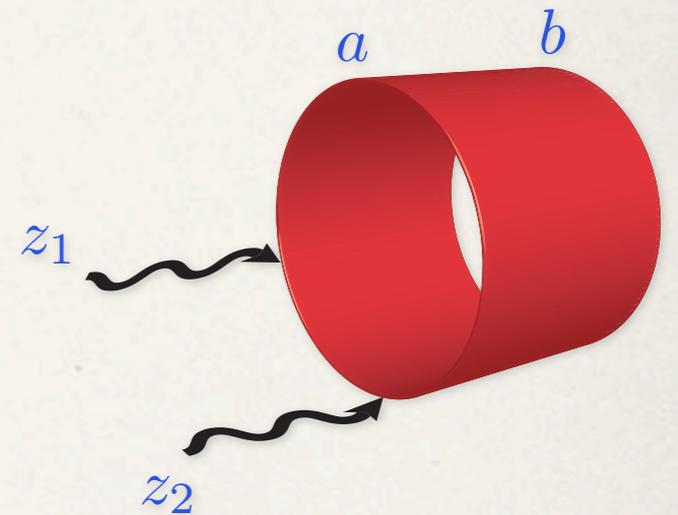
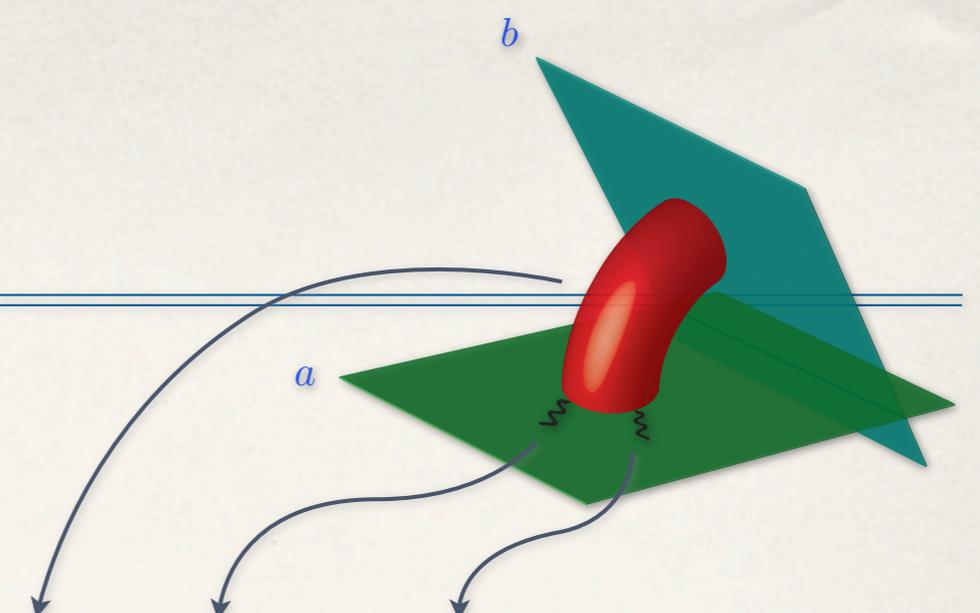
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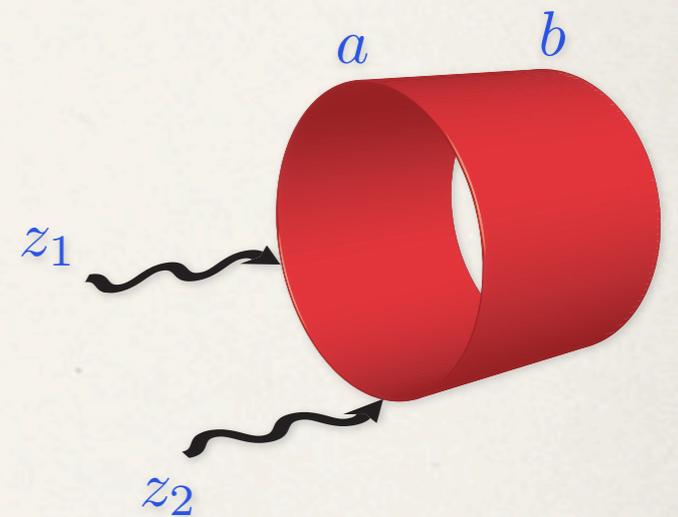
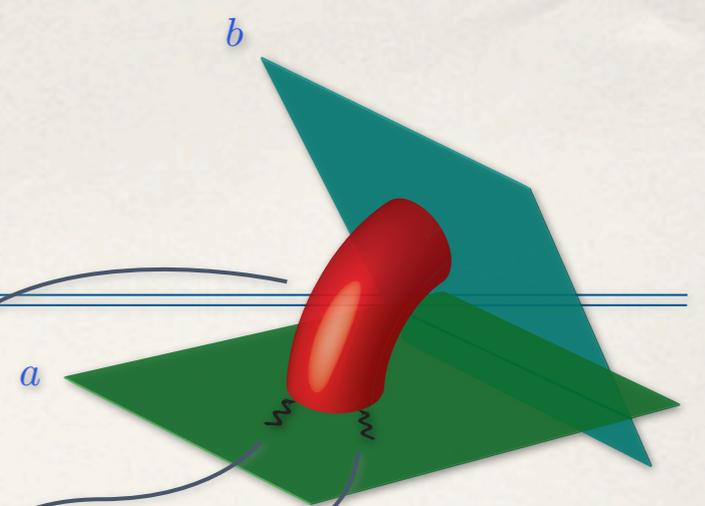
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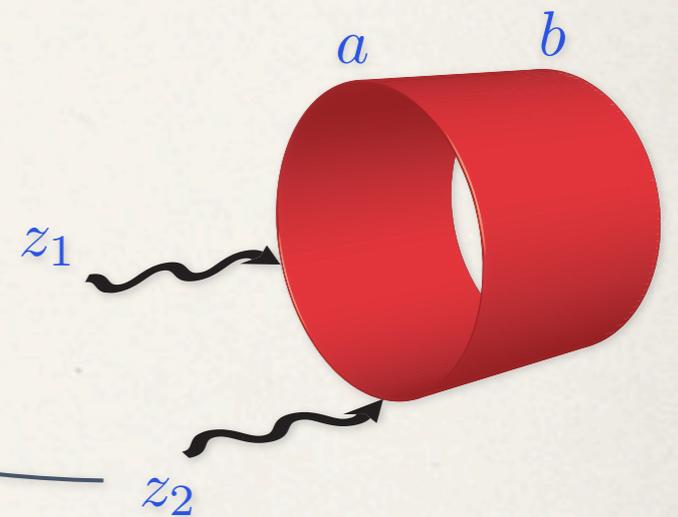
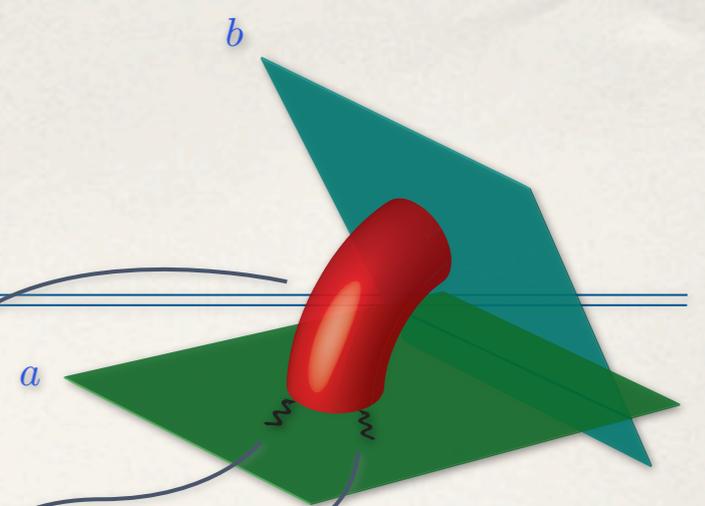
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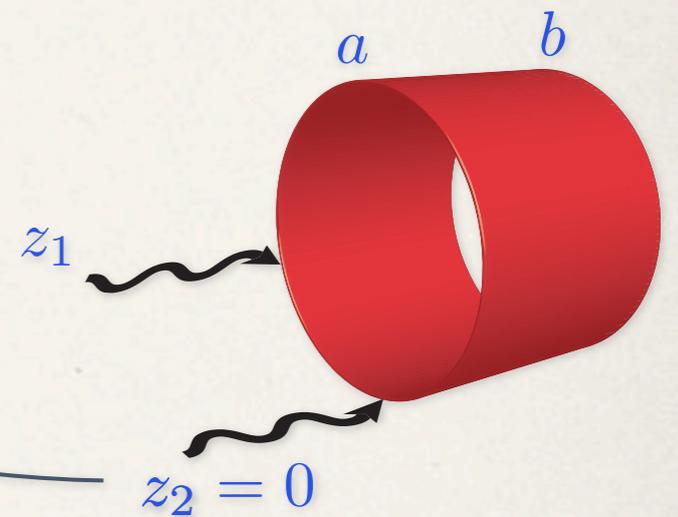
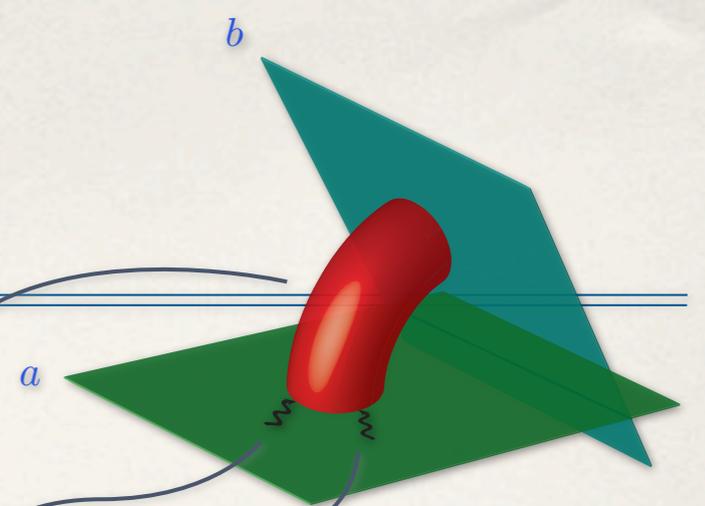
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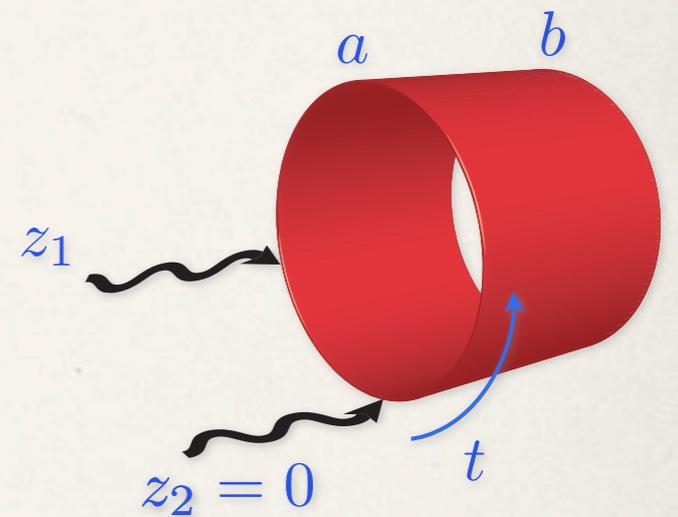
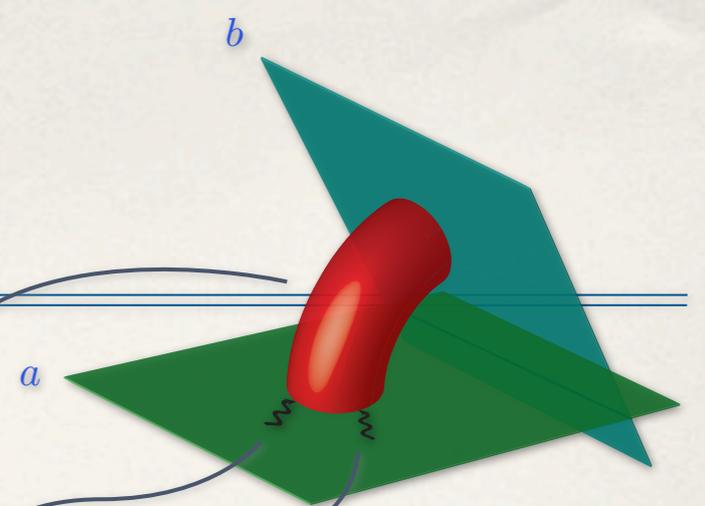
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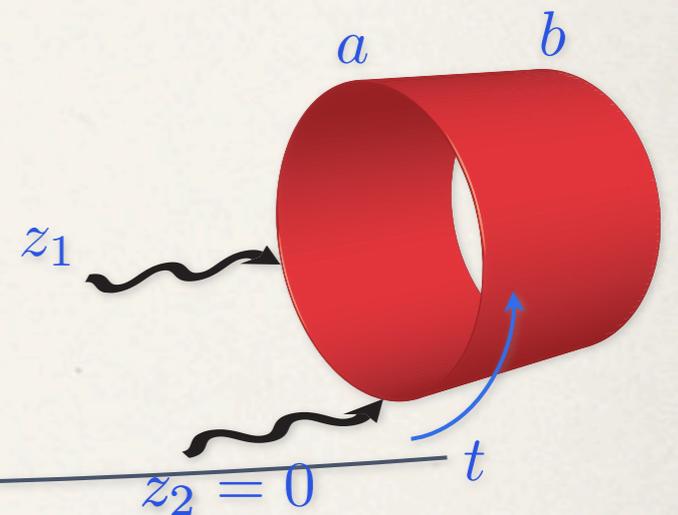
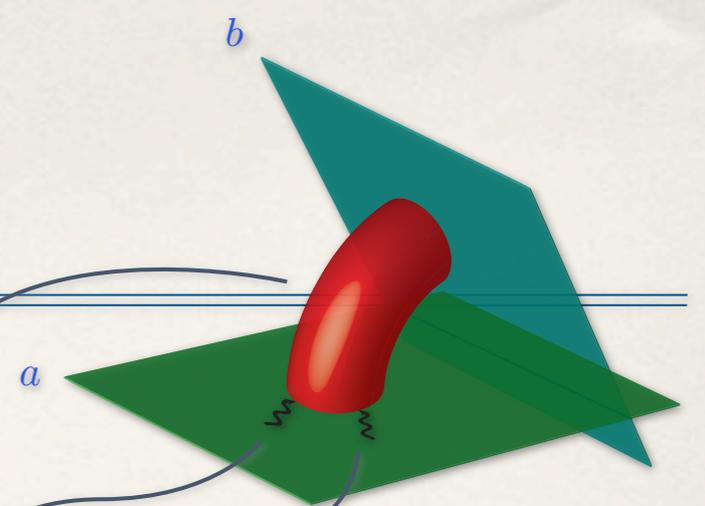
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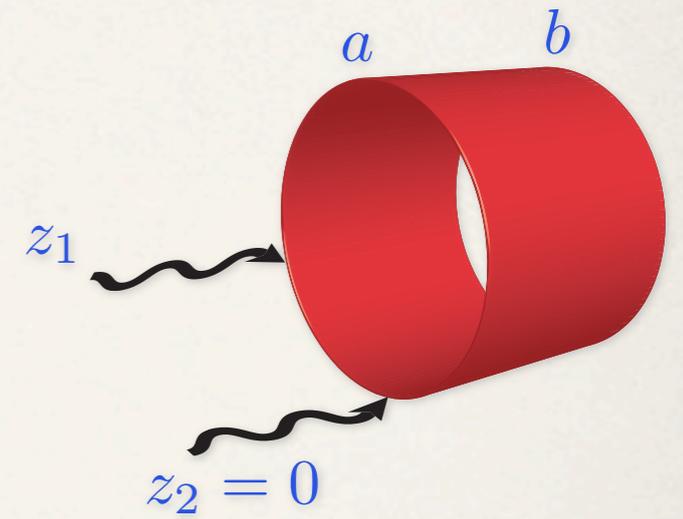
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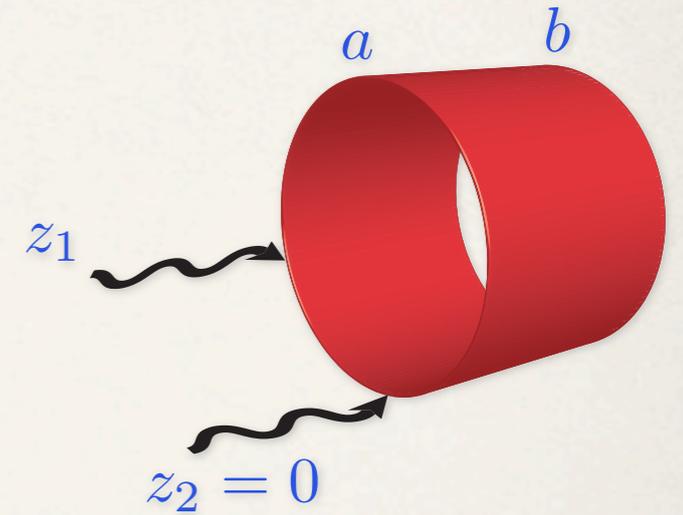


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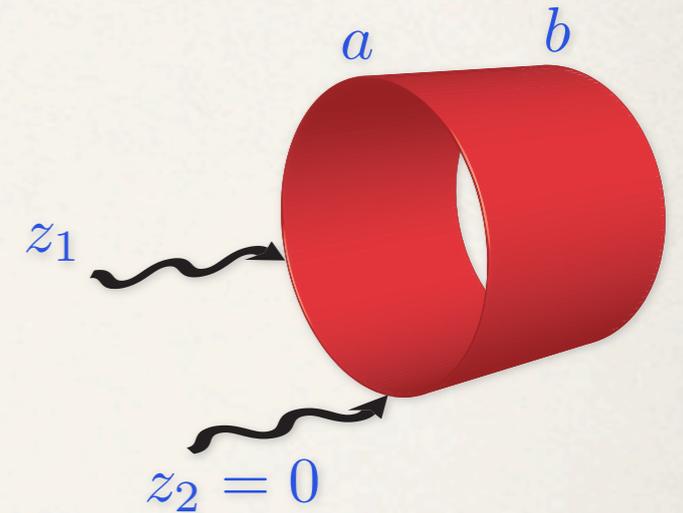
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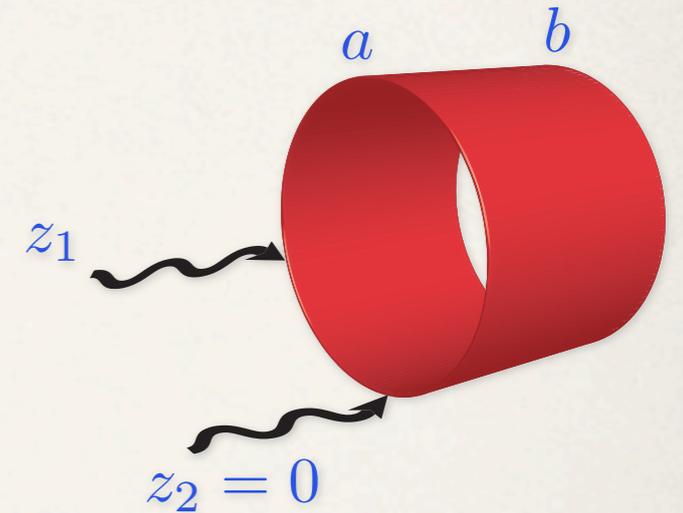


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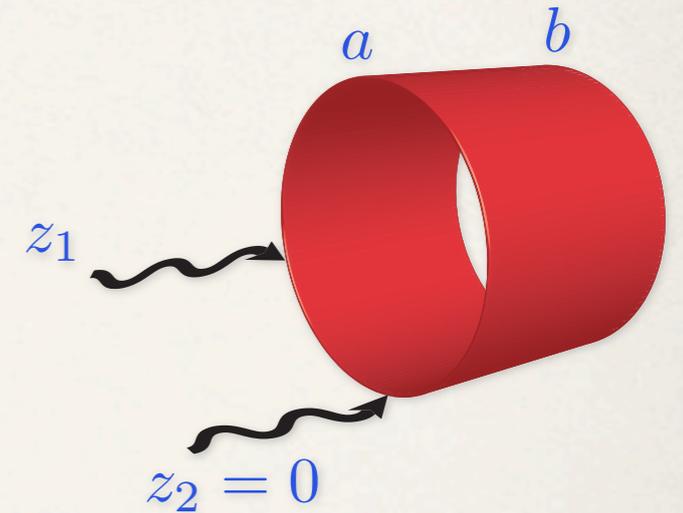


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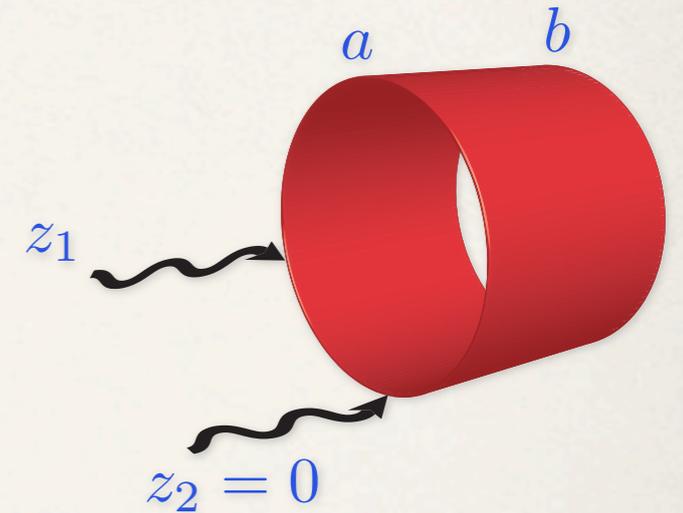


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- ❖ After **several steps** we get an expression only of well known $\vartheta_1(z, it/2)$'s.



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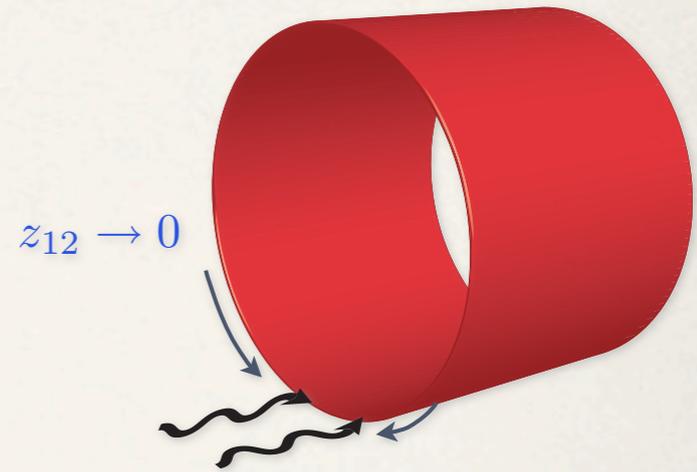
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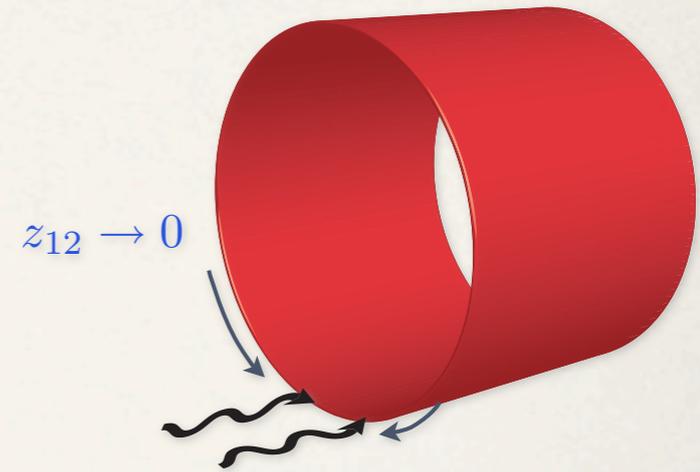


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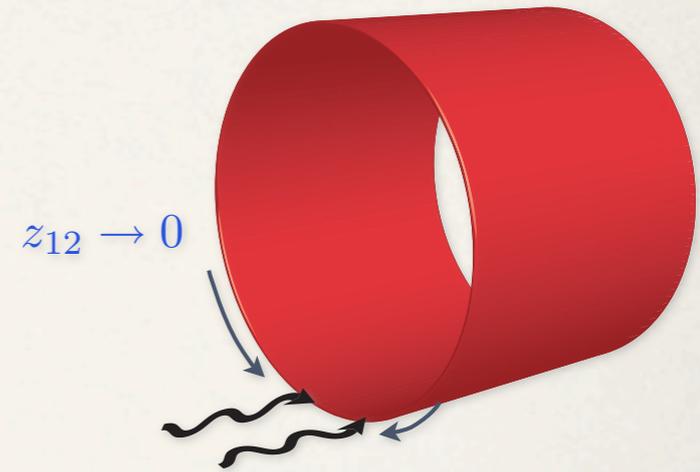
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Uncommon but might appear due to massless open string in the loop

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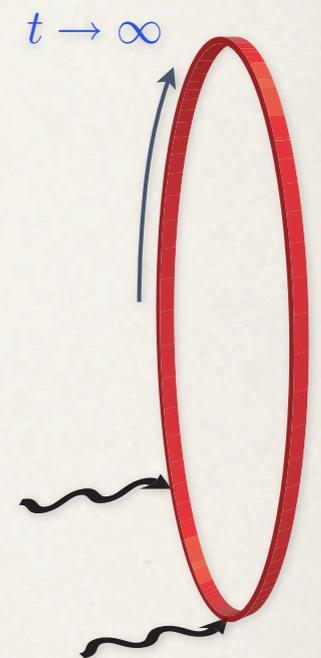
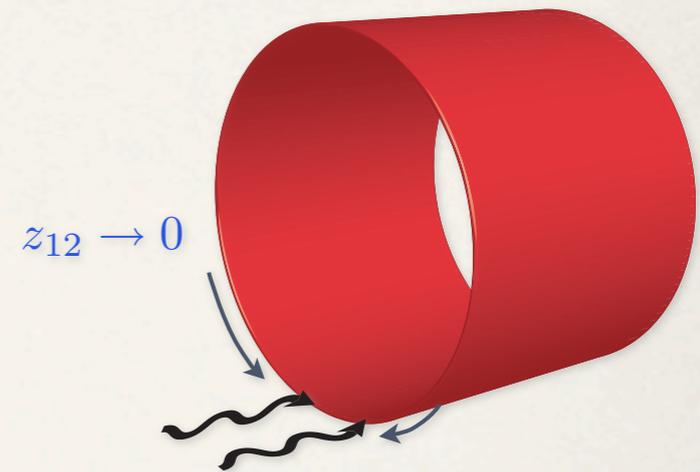
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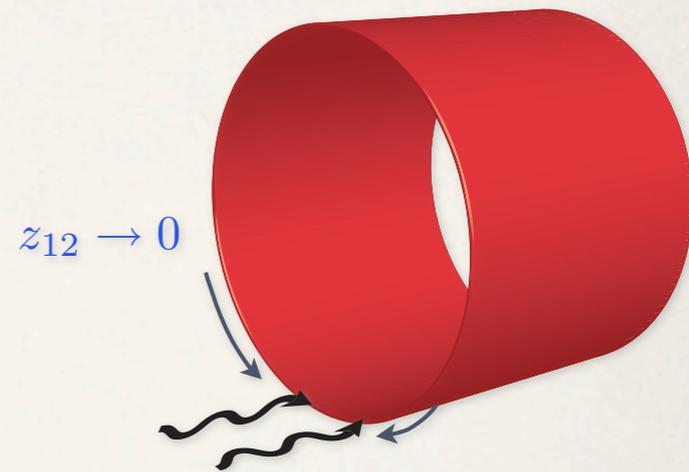


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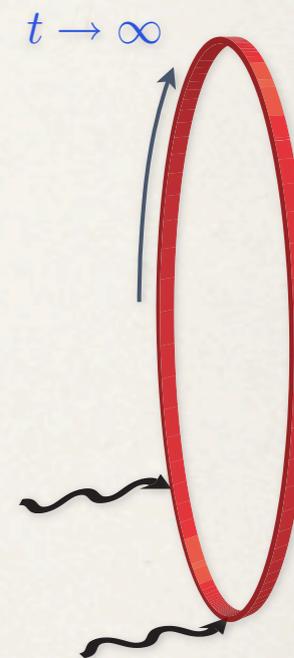
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▸ At the closed string IR (**long tube limit** $t \rightarrow 0$):

$$\mathcal{A} \sim k^2 \int dl e^{-k^2 \langle XX \rangle(z_1)} \begin{cases} \text{opposite boundary} & k^2 \int_a^\infty dl e^{-\pi\alpha'k^2 l} \longrightarrow \frac{1}{\pi\alpha'} \\ \text{same boundary} & k^2 \int_a^\infty dl (2 \sin \pi x)^{-2\alpha'k^2} \longrightarrow \text{tadpole} \end{cases}$$

Antoniadis Kiritsis Rizos, Anastasopoulos



Adjoint scalar masses

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- * In our case,
 - There are **no world-sheet poles**. They cancel since our amplitude is even.
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 - There is **long tube contribution** (open string UV).

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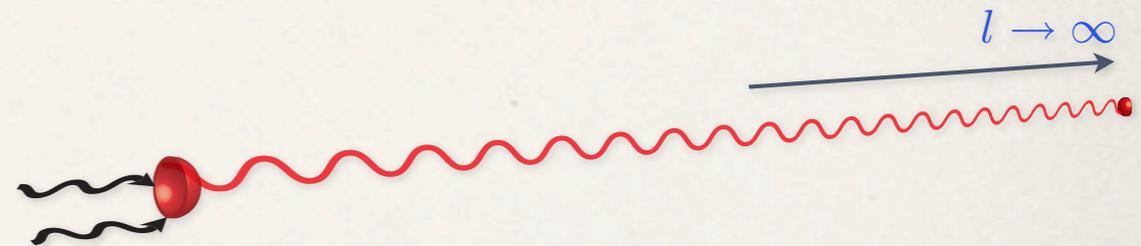


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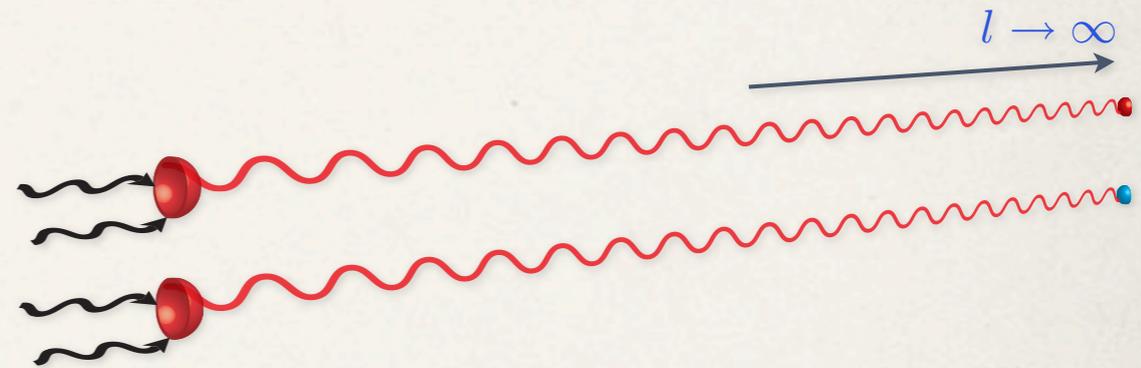


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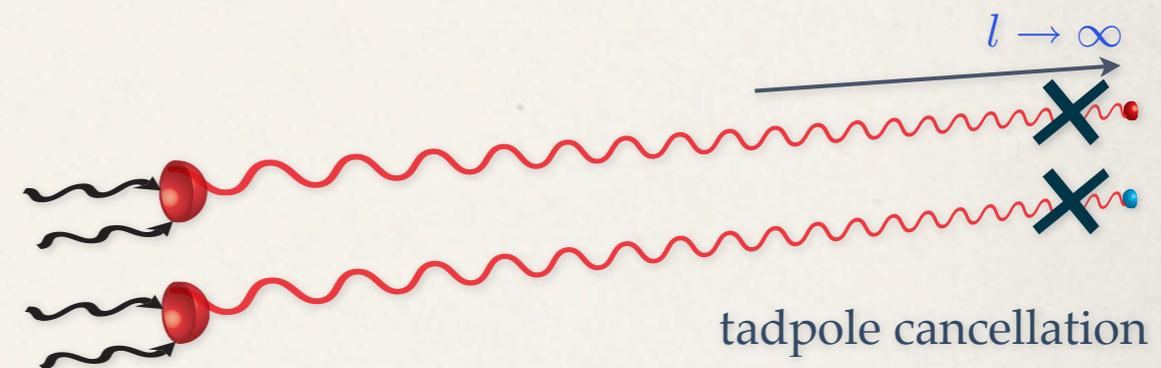


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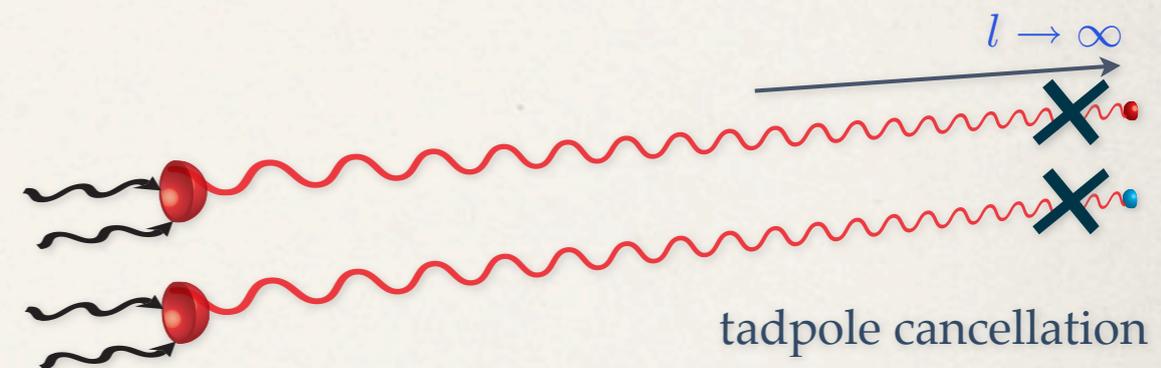
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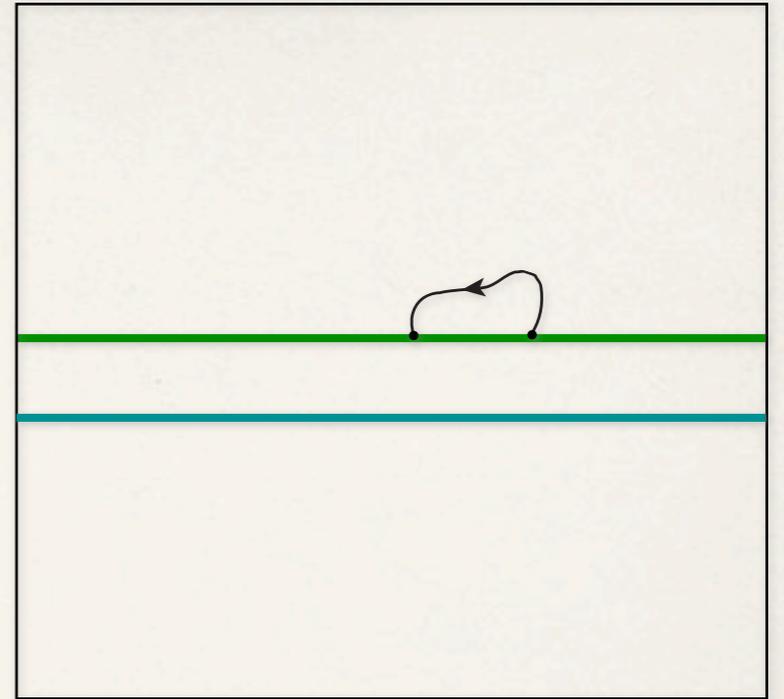
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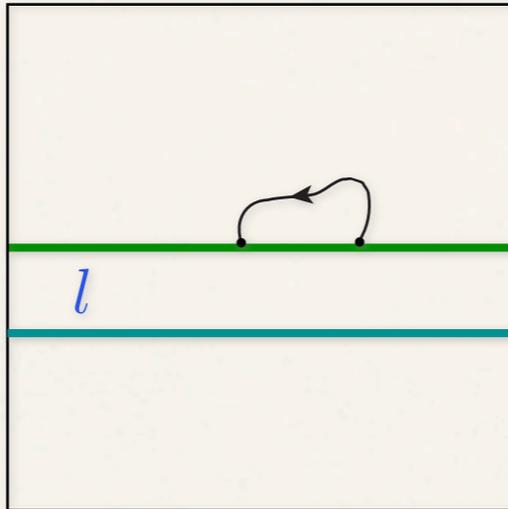


Adjoint masses for parallel dimensions

Effective potential

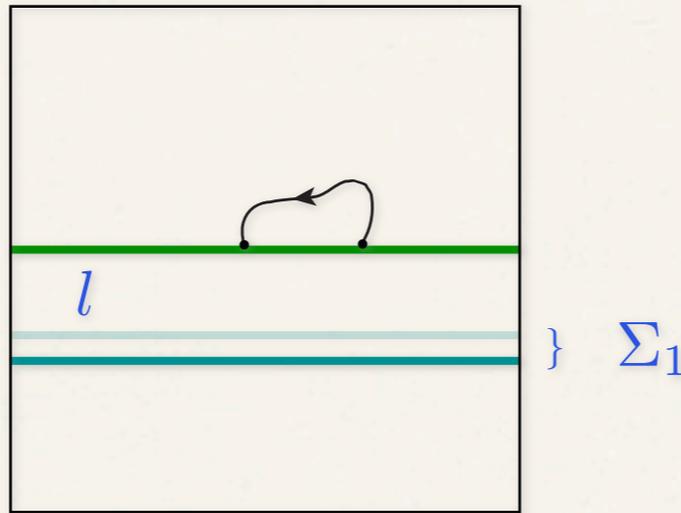
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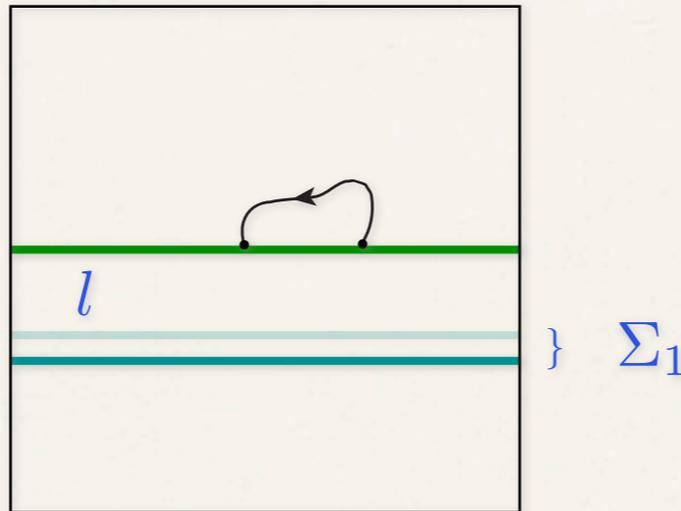
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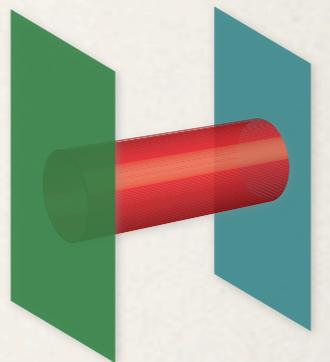
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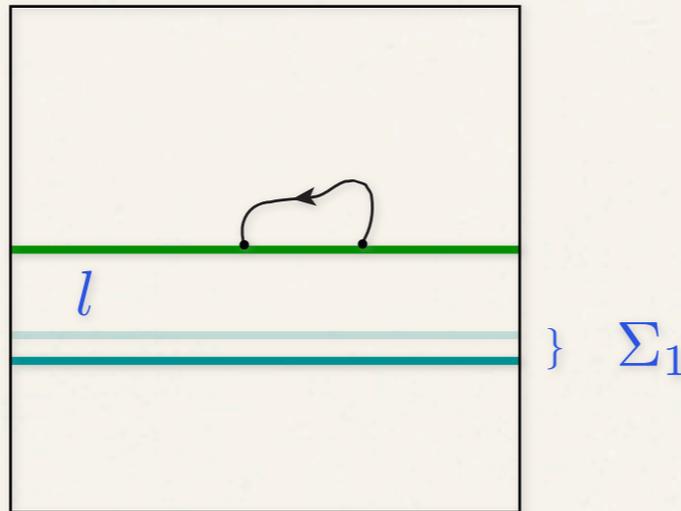


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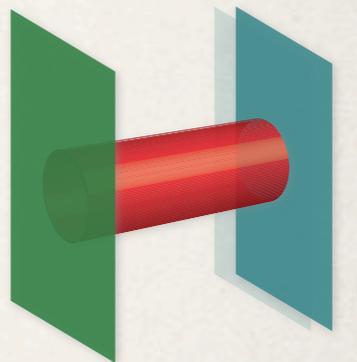


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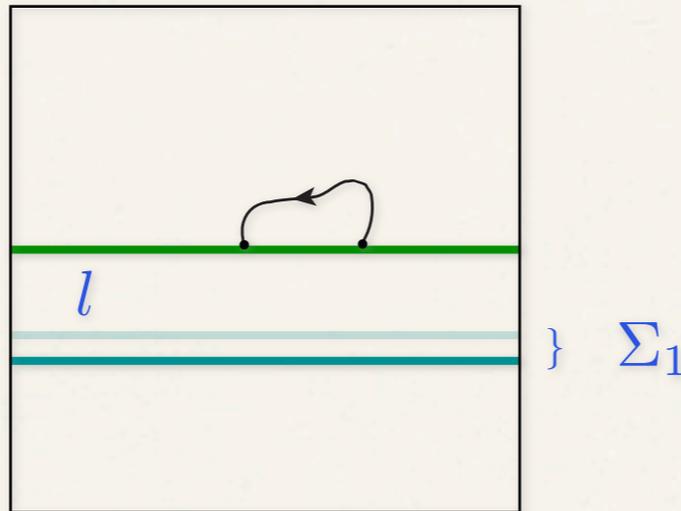


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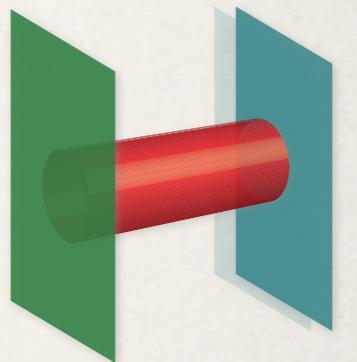


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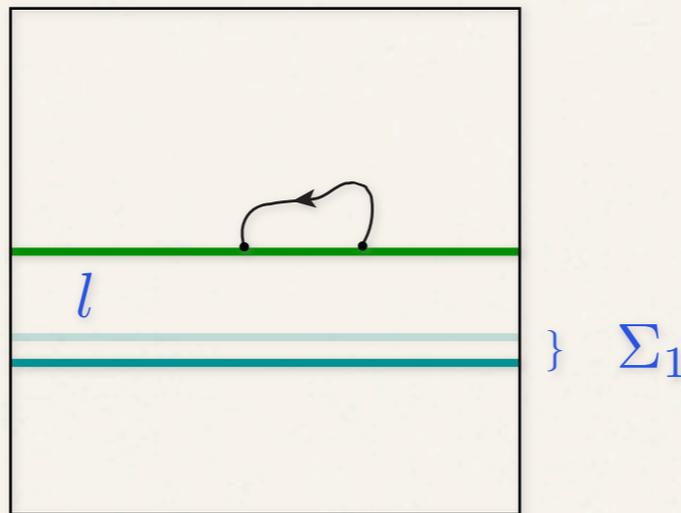


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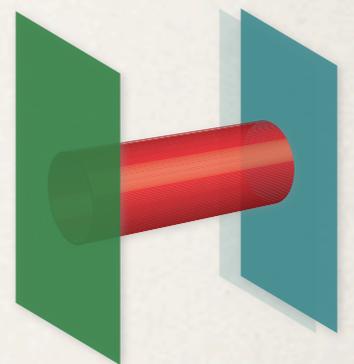


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- ❖ The second derivatives will give the **masses** of **windings** and **Wilson lines**.
- ❖ That method is **much simpler**, but **can only be performed** for the $\mathcal{N} \approx 2, 4$.



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- * The potential for the $\mathcal{N} \approx 2$ case is:

$$V(\Sigma_1, \Sigma_2) = -64\pi^2 \varepsilon^2 \sum_{m,n} \int \frac{dt}{t} e^{-2\pi t ((\Sigma_1 + mR_{1,1})^2 + (\Sigma_2 + l + nR_{2,1})^2)}$$

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from where we can compute the **tadpoles**:

$$V^{(0,1)} \sim -32\pi^2 \varepsilon^2 \sum_{m,n} \frac{l + nR_{2,1}}{(mR_{1,1})^2 + (l + nR_{2,1})^2} \neq 0$$

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$$V^{(2,0)} \sim 32\pi^2 \varepsilon^2 \sum_{m,n} \frac{(mR_{1,1})^2 + (l + nR_{2,1})^2}{\left[(mR_{1,1})^2 + (l + nR_{2,1})^2 \right]^2} \leq 0$$
$$V^{(0,2)} \sim -32\pi^2 \varepsilon^2 \sum_{m,n} \frac{(mR_{1,1})^2 - (l + nR_{2,1})^2}{\left[(mR_{1,1})^2 + (l + nR_{2,1})^2 \right]^2} \geq 0$$
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} tachyon

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- * The potential for the $\mathcal{N} \approx 4$ case is:

$$V(\Sigma_{1,i}, \Sigma_{2,i}) \sim -4\pi^2 \varepsilon^3 \left(\sum_{i=1,2} ((\Sigma_{1,i} + \tilde{n}_i R_{1,i})^2 + (\Sigma_{2,i} + l_i + n_i R_{2,i})^2) \right)^{-1}$$

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- * The **tadpoles** in this case:

$$V^{(1,0,0,0)} \sim 8\pi^2 \varepsilon^3 \sum_{\tilde{n}, n} \frac{\tilde{n}_1 R_{1,1}}{(\sum_i ((\tilde{n}_i R_{1,i})^2 + (l_i + n_i R_{2,i})^2))^2} \rightarrow 0$$

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which can be **cancelled** by properly choosing image branes.

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* The **adjoints masses**:

$$\begin{aligned}
 V^{(2,0,0,0)}|_{a_{i,j} \rightarrow 0} &\sim 16i\pi^2 \varepsilon^3 \sum_{\tilde{n},n} \frac{-4(\tilde{n}_1 R_{1,1})^2 + S[\tilde{n},n]}{S[\tilde{n},n]^3} && \neq 0 \\
 V^{(1,1,0,0)}|_{a_{i,j} \rightarrow 0} &\sim 16i\pi^2 \varepsilon^3 \sum_{\tilde{n},n} \frac{4(\tilde{n}_1 R_{1,1})(l_1 + n_1 R_{2,1})}{S[\tilde{n},n]^3} && \rightarrow 0 \\
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 V^{(0,0,0,2)}|_{a_{i,j} \rightarrow 0} &\sim 16i\pi^2 \varepsilon^3 \sum_{\tilde{n},n} \frac{-4(l_2 + n_2 R_{2,2})^2 + S[\tilde{n},n]}{S[\tilde{n},n]^3} && \neq 0
 \end{aligned}$$

where: $S[\tilde{n},n] = (\tilde{n}_1 R_{1,1})^2 + (l_1 + n_1 R_{2,1})^2 + (\tilde{n}_2 R_{1,2})^2 + (l_2 + n_2 R_{2,2})^2$.

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- * Therefore, there is at least one **tachyonic** state.

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- ❖ **Tachyons** might be cancelled in models with **Scherk-Schwarz** deformations...

work in progress...